

# Does the Gluon Carry Proton's Spin?

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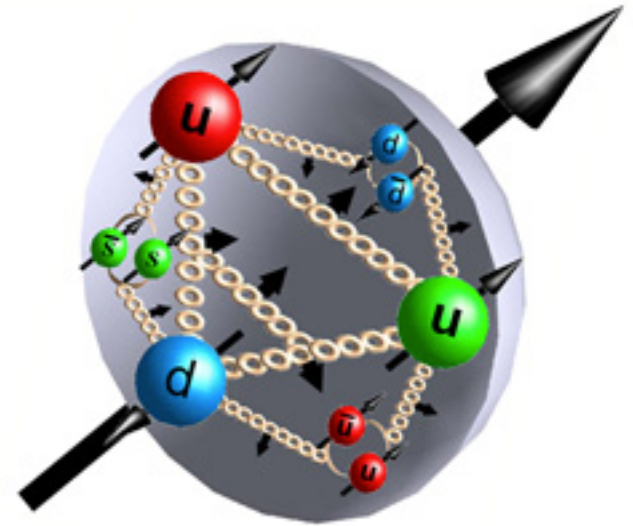


# Motivation

To understand the spin structure of the proton

Proton is composite particle:

- ❖ Two up and one down valence quarks
- ❖ Bound together by gluons
- ❖ Sea quarks (produced in pairs)



**How do the properties of the proton arise from these constituents?**

# The Inner Life of Protons

❖ Charge:  $+1 = \underset{u}{\frac{2}{3}} + \underset{u}{\frac{2}{3}} - \underset{d}{\frac{1}{3}}$

- ❖ Mass: Up and down quarks are almost massless ( $m_u + m_u + m_d \approx 9 \text{ MeV}/c^2$ , total mass of proton  $m_p \approx 938 \text{ MeV}/c^2$ )
- Remaining mass is due to the kinetic energy of the quarks and **the energy of the gluon fields that binds the quarks together.**

# Terminology Used



- ❖ **Helicity:** Projection of spin vector onto momentum
- ❖ **Bjorken  $x$ :** Momentum fraction carried by parton (quark or gluon) of hadron.
- ❖ **Fragmentation function:** Probability that a parton at a short distance fragments into a hadron with fraction  $z$  of the parent momentum  $x$ .
- ❖ **Partonic cross section:** Likelihood of interaction between particles.
- ❖ **Spin dependent parton distribution function:** The probability density for finding a particle with a certain longitudinal momentum fraction  $x$  at momentum transfer  $Q^2$ .



# Momentum

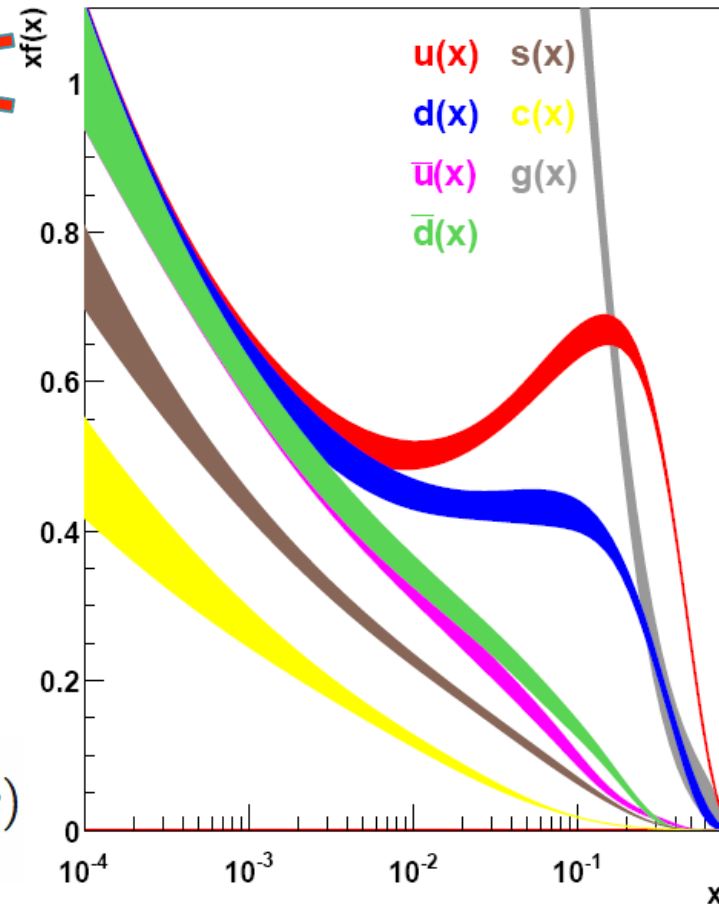
Initial thought:

❖ Momentum:  ~~$1 = 1/3 + 1/3 + 1/3$~~

❖ The total momentum is not only contributed by the quarks but is smeared out due to continuously interchanging gluons

❖ Gluons themselves carry some momentum!

$$1 = \sum_q \int_0^1 x dx [q(x) + \bar{q}(x)] + \int_0^1 x dx g(x)$$



**What about SPIN?**

# Spin Composition of the Proton

Initial thought:

- ❖ Spin is contributed only by quarks

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2} - \frac{1}{2}$$

- ❖ EMC results show only small fraction of spin is contributed by quarks ~ 30%<sup>1</sup>

## PROTON SPIN CRISIS BEGIN

### ❖ What else could contribute?

- ❖ Need to consider spin of sea quarks, gluon and orbital angular momentum

$$\frac{1}{2} = \frac{1}{2} \left( \underbrace{\Delta u_v + \Delta d_v + \Delta q_s}_{\Delta \Sigma} \right) + L_q + \Delta G + L_g$$

<sup>1</sup>S. D. Bass, Rev. Mod. Phys. 77, 1257 (2005)

# Hunting $\Delta G$

## ❖ Via Double Helicity Asymmetry

$$A_{LL} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = \frac{\sum_{a,b,c=q,\bar{q},g} \Delta f_a \otimes \Delta f_b \otimes \Delta \hat{\sigma} \otimes D_{\pi/c}}{\sum_{a,b,c=q,\bar{q},g} f_a \otimes f_b \otimes \hat{\sigma} \otimes D_{\pi/c}}$$

++ = Same helicity =  + 

+ - = Opposite helicity =  + 

- ❖  $\Delta f(a/b) \approx \Delta g$ : Spin dependent parton distribution function (Our Focus).
- ❖  $\Delta \sigma$ : Hard scattering cross section.
- ❖  $D_{\pi/c}$ : Fragmentation function (Cross section is used to get fragmentation function).

# Taking a Look inside an Atom

- ❖ Rutherford's scattering experiment:

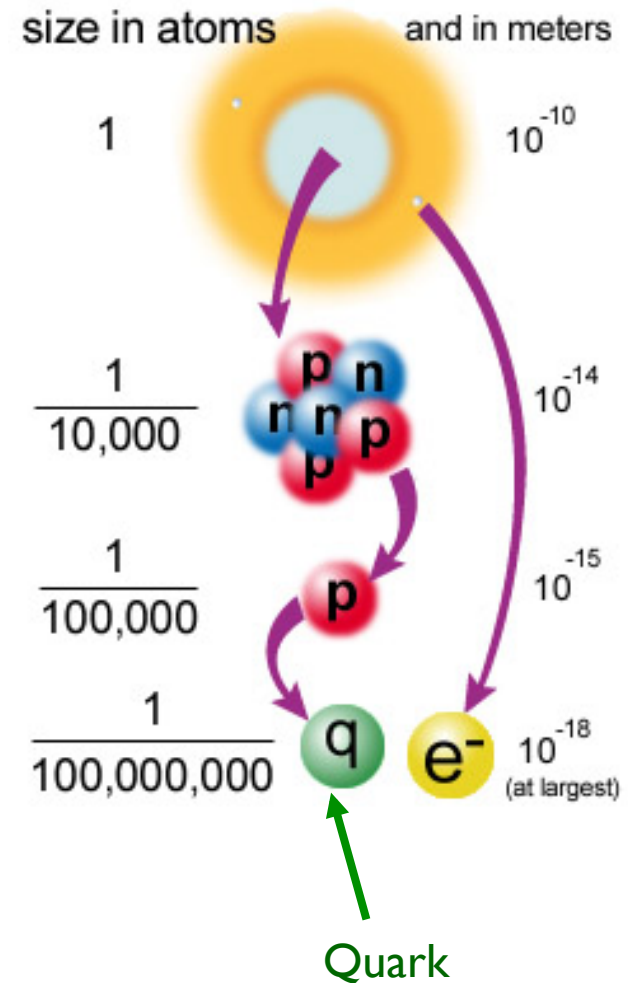
- ❖ structure of atom
- ❖ Energy is less to probe inside nucleus  
(Energy: 5.5 MeV)

- ❖ Similarly, scattering of electrons with protons at large angles (SLAC):

- ❖ “hard” subcomponents in the proton
- ❖ Little knowledge on nucleon  
(Energy: 1 – 10 GeV)

- ❖ Proton-proton scattering (RHIC):

- ❖ deeper inside proton
- ❖ reveals the structure of proton  
(Energy: up to 255 GeV)

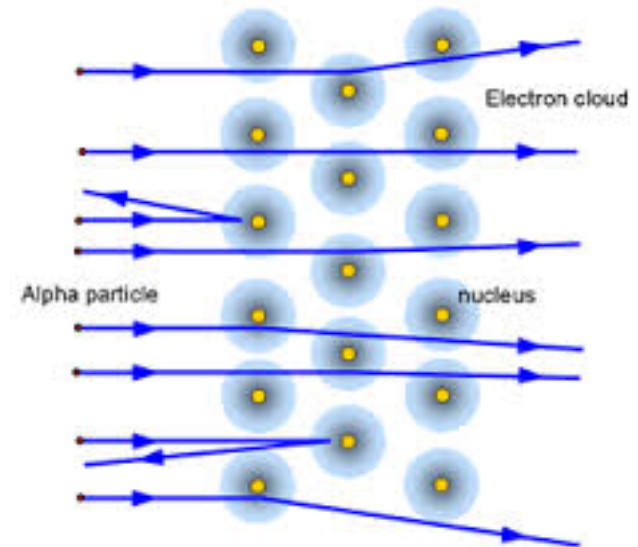




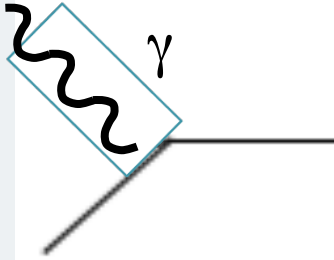
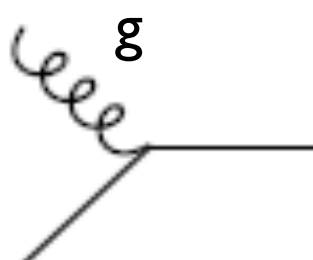
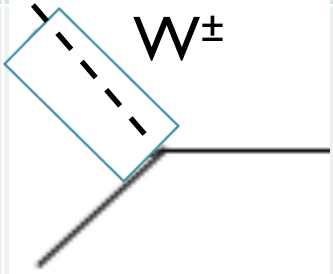
# TOOLBOX

# How can we study the proton?

- ❖ Can't use a microscope
  - ❖ Quantum Mechanics tells us that observation changes the system
- ❖ Instead, use some kind of probe to interact with what is inside
  - ❖ Basic technique is scattering
    - Example: Rutherford scattering experiment with alpha particles
      - ❖ → Structure of Atom
  - ❖ Try the same thing, using electrons and protons (quarks and gluons)
- ❖ **But what kind of probes can we use?**

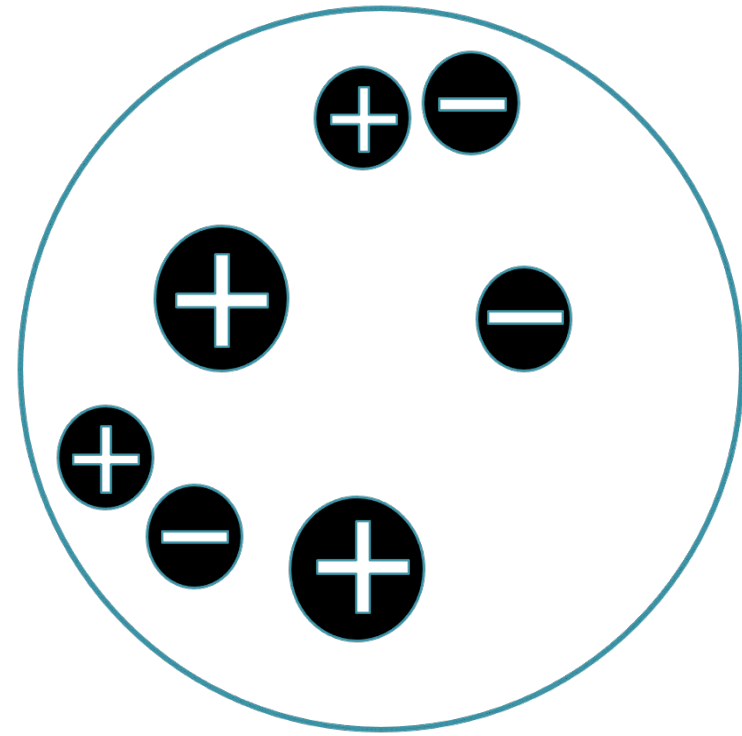


# 3 Forces → 3 Probes

Force	Electromag.	Strong Nuc.	Weak Nuc.
Carrier	photon	gluon	$W^+, W^-$ (& Z) boson
Charge	+, -	color: r, g, b and anticolor	weak charge: flavor
Relative Strength	1	100	$10^{-11}$
Standard (Feynman) symbol			

# Electromagnetic: The Photon

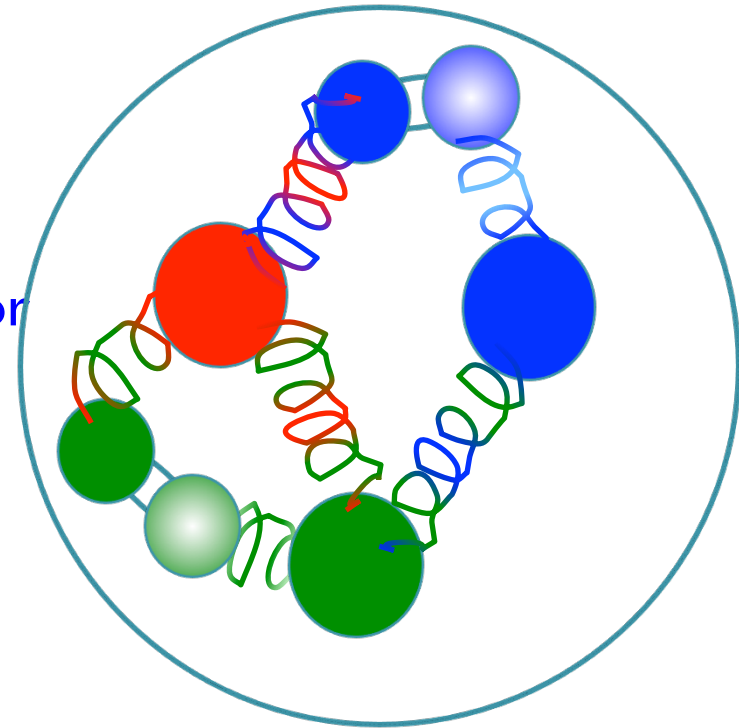
- ❖ Only interact with charged particles, i.e. quarks
  - Limited direct information on gluons
- ❖ Very similar to X-ray scattering to study structure of crystals and other materials:
- ❖ In the case of protons, photon of (much high) energy  $Q^2$  scatters off a quark with momentum  $xP$ , and we have a distribution of quarks  $f(x, Q^2)$ .





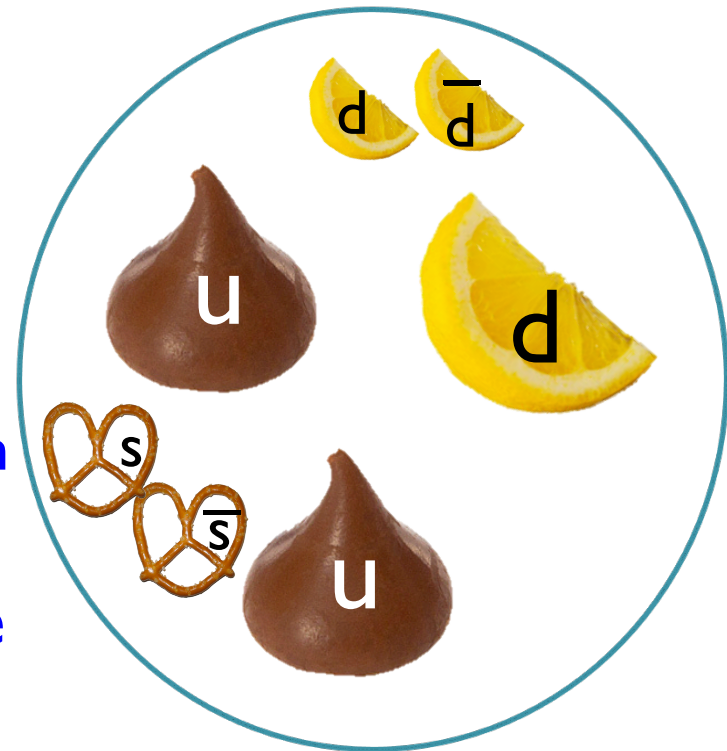
# Strong Nuclear: The Gluon

- ❖ Gluons interact via “color” force.
- ❖ Both quarks and gluons carry color charge, so can study both
- ❖ Gluons are self interacting, unlike photons
- ❖ Can directly access gluons

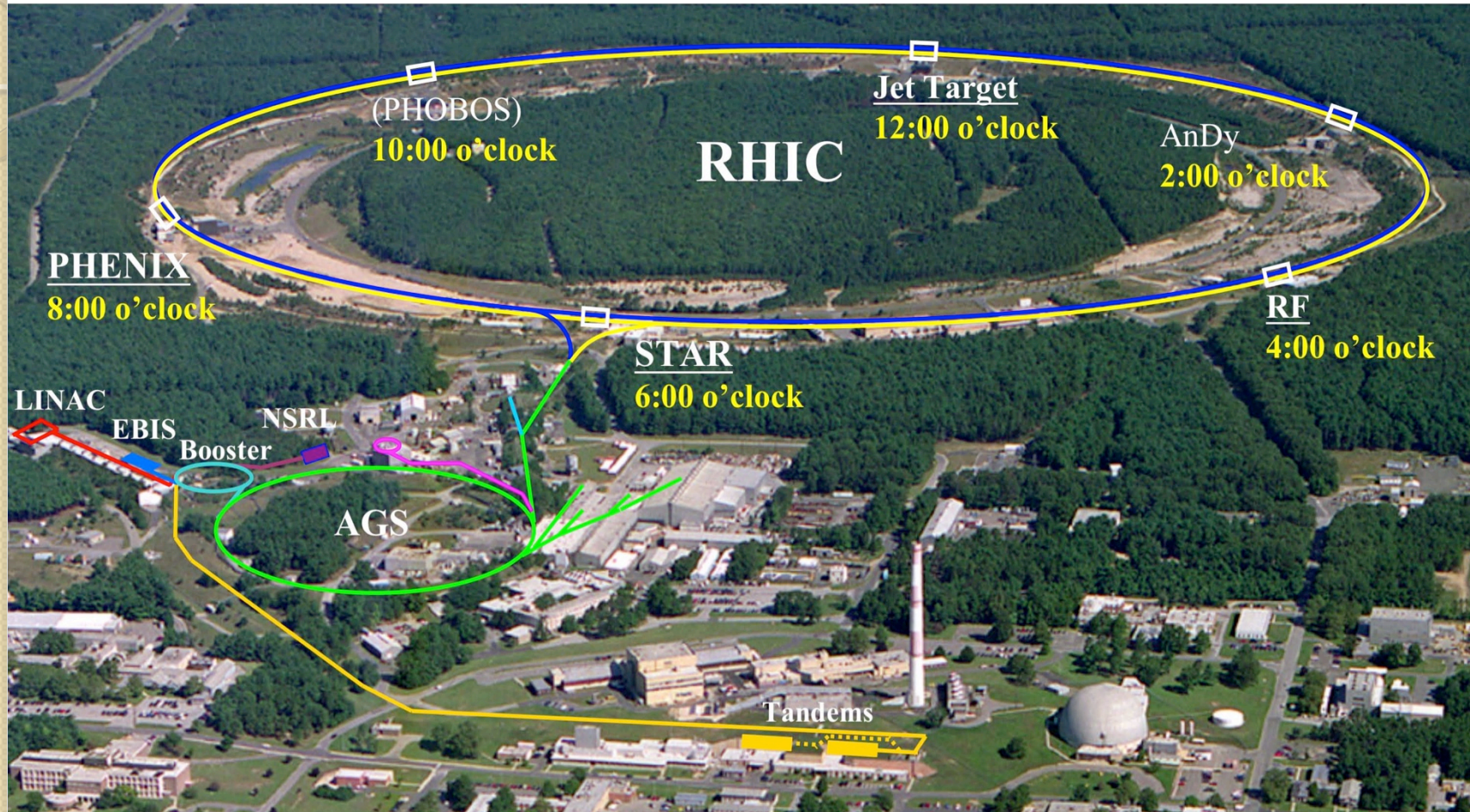


# Weak Nuclear: The W & Z Bosons

- ❖ Weak force is sensitive to quark flavor
  - ❖ Explains neutron decay to proton
    - ❖  $d \rightarrow u + W \rightarrow u + e + \nu_e$
- ❖ How can we get W's?
  - ❖ Can use neutrinos to study
    - ❖ Requires a lot of materials as neutrinos don't interact much
  - ❖ Also can annihilate quarks and anti-quarks to produce W's
    - ❖ What we do at RHIC



# Studying Proton Structure in Lab: RHIC



Relativistic Heavy Ion Collider (RHIC) can collide several species including the polarized protons



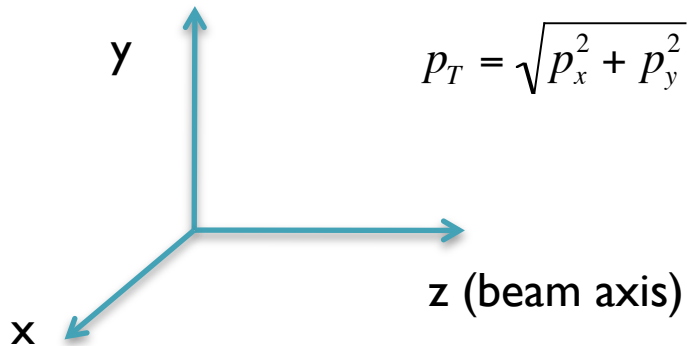
- Up to  $\sqrt{s}=510$  GeV
- $P \sim 55\%$  @  $\sqrt{s}=510$  GeV,  $P \sim 60\%$  @  $\sqrt{s}=200$  GeV
- Transverse or longitudinal polarization



# Kinematic Variables



Transverse Momentum

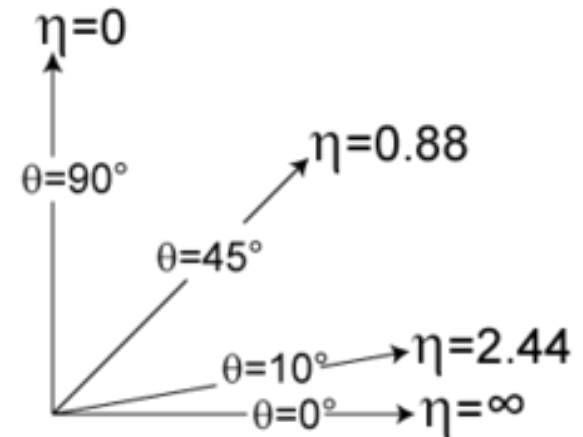


Invariant Mass

$$m_{\gamma\gamma} = \sqrt{E_1 E_2 - \vec{p}_1 \cdot \vec{p}_2}$$

Rapidity

$$y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$
$$\approx \eta = -\ln[\tan(\theta/2)]$$



# PHENIX Experiment:

Special Interest for spin:

$$\pi^0 \rightarrow \gamma\gamma$$

Detectors Used:

## 1. Photon Identification:

Electromagnetic Calorimeter (EMCal):

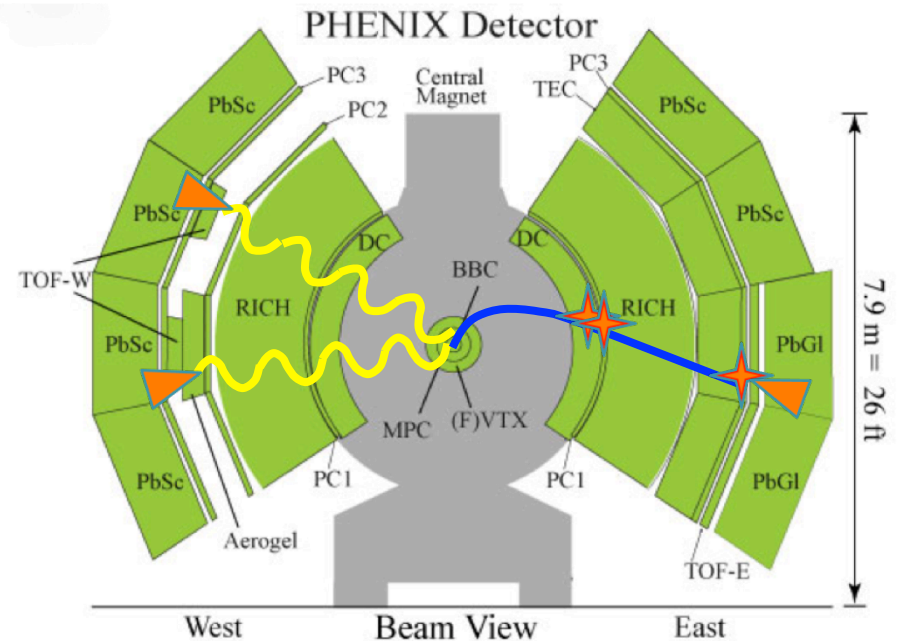
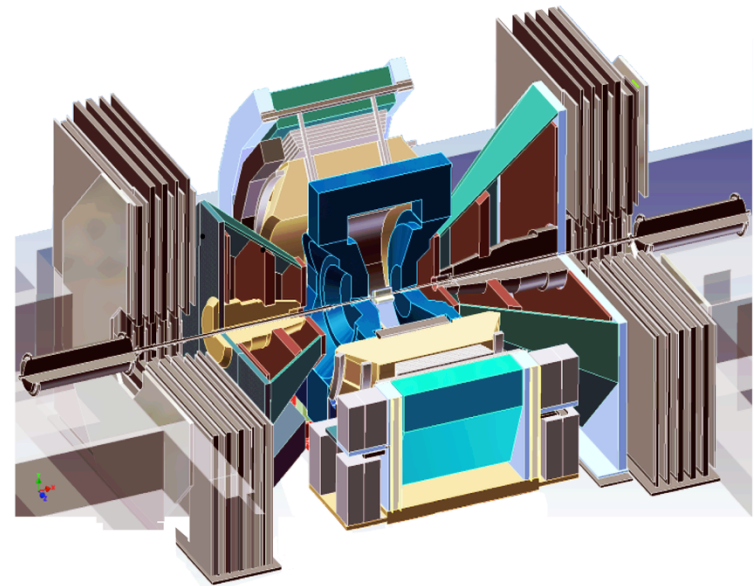
- ❖ 6 sectors PbSc with 64 layers of Pb and scintillator
- ❖ 2 sectors PbGl
- ❖  $|\Delta\eta| < 0.35$
- ❖  $\Delta\phi = \pi$  (2 arms  $\times \pi/2$ )

## 2. Hadron Identification:

Pad Chambers in front of EMCal.

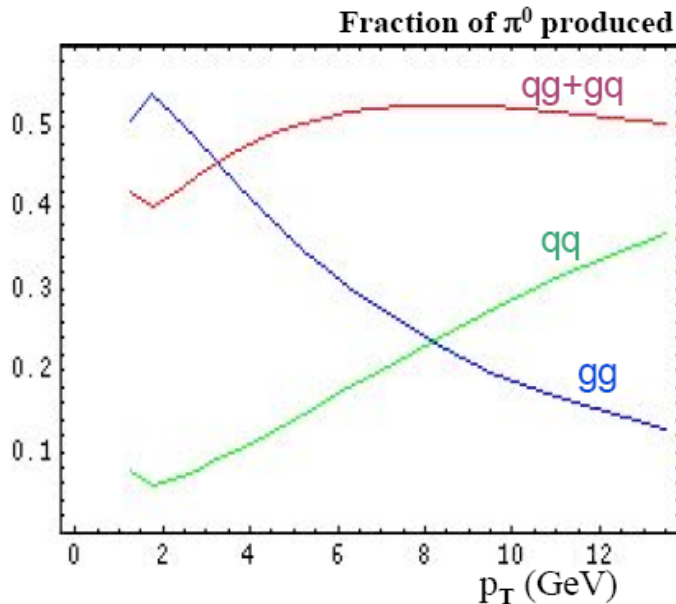
## 3. Relative Luminosity:

- ❖ Beam Beam Counter(BBC).
- ❖ Zero Degree Calorimeter(ZDC)

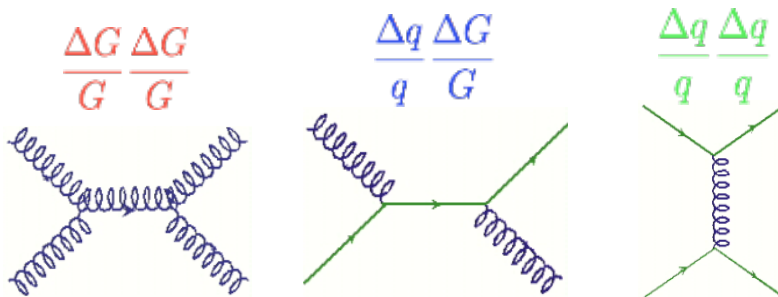


# $\pi^0$ as a Probe for $\Delta G$ :

## Why $\pi^0$ ?

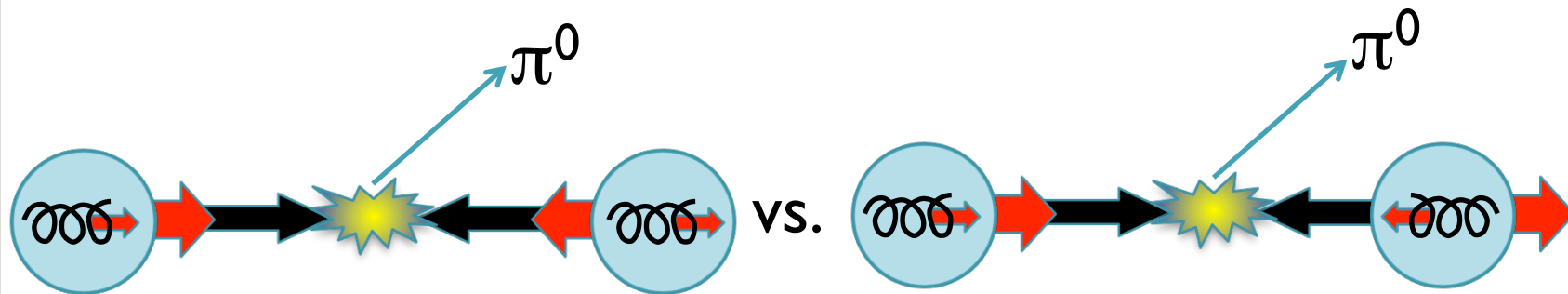


- ❖  $\pi^0$  is most dominantly produced particle observed in PHENIX detector
- ❖ processes that involve gluons are dominant in accessed kinematic range



# What Exactly is Measured in this Experiment?

- ❖ We want to know how aligned the gluon spin is to the proton:



$$A_{LL} = \frac{\text{Diagram 1} - \text{Diagram 2}}{\text{Diagram 3} + \text{Diagram 4}}$$

The diagrams in the equation represent different spin configurations of the colliding protons. Each diagram shows two blue circles (protons) with internal wavy lines and red arrows. A yellow starburst in the center represents the production of a  $\pi^0$  particle, indicated by a blue arrow labeled  $\pi^0$ .

Mom. 

Spin 

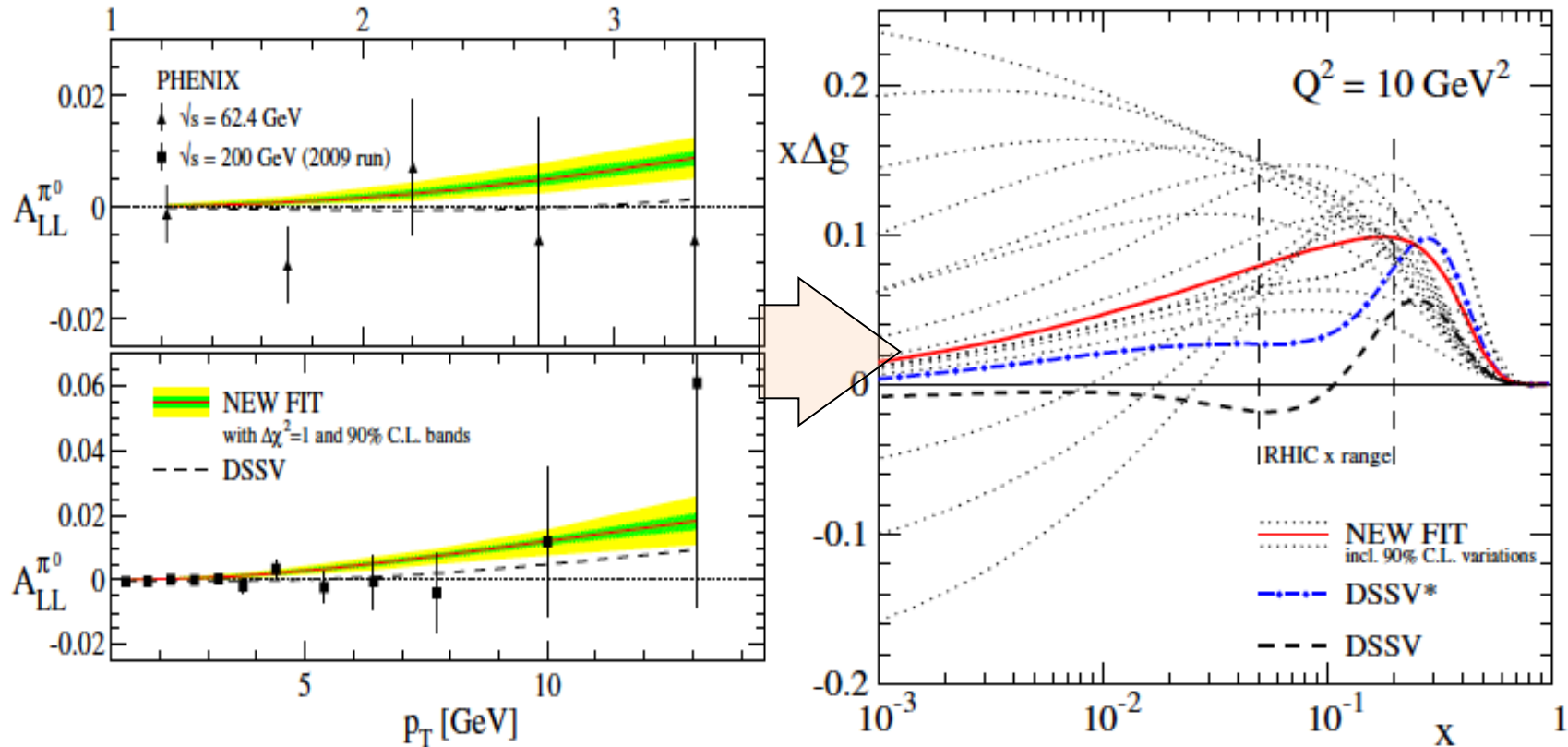


# Necessary Ingredients for $A_{LL}$

$$A_{LL} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = \frac{1}{P_b P_y} \frac{N_{++} - RN_{+-}}{N_{++} + RN_{+-}}$$

- ❖ Helicity dependent particle yields (N)
  - $\pi^0$ ,  $\pi^+$ ,  $\pi^-$ ,  $\eta$  etc
- ❖ Beam polarization (P)
- ❖ Relative luminosity (R)

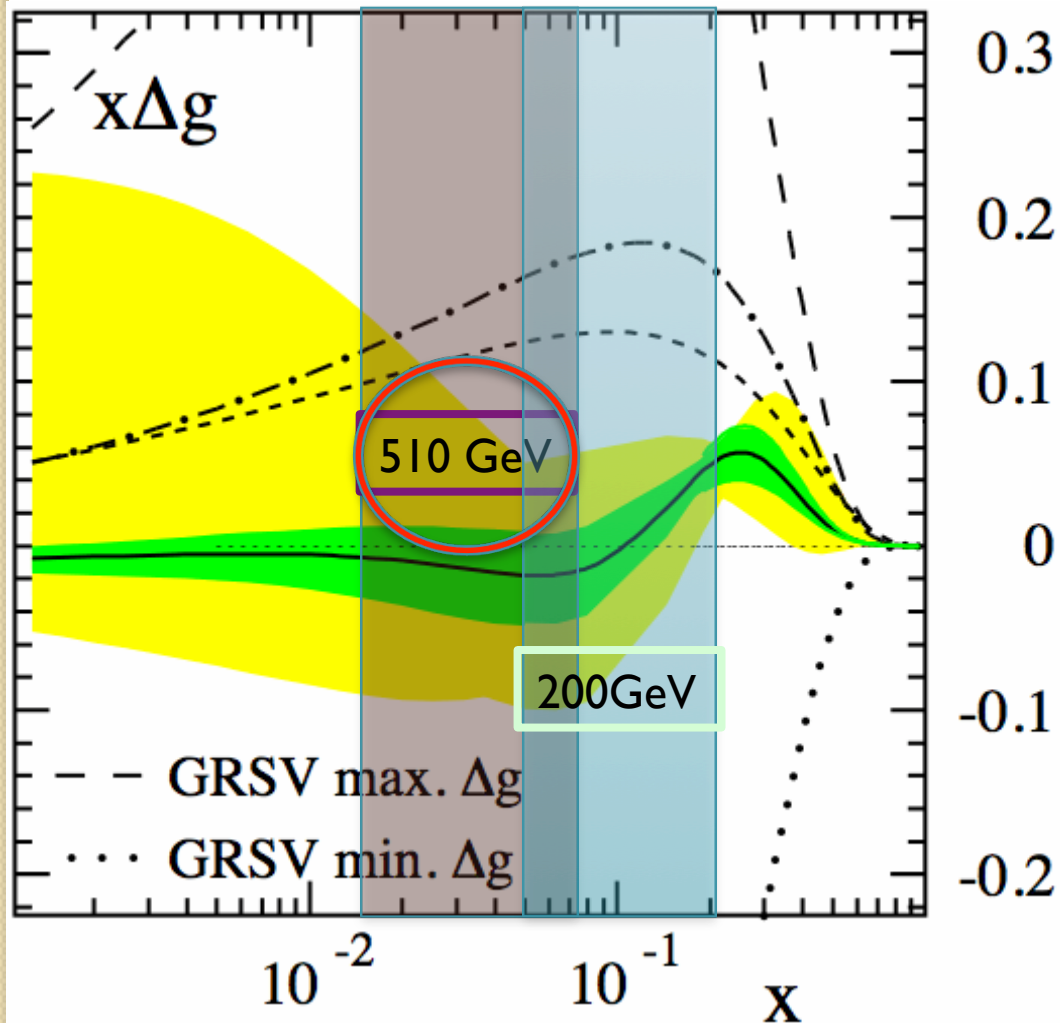
# Current Status on: $\Delta G$



PHENIX  $\sqrt{s} = 62.4$  GeV (upper panel)  
and 200 GeV (lower panel) data

PRL 113, 012001 (2014)

## What is new in this analysis?

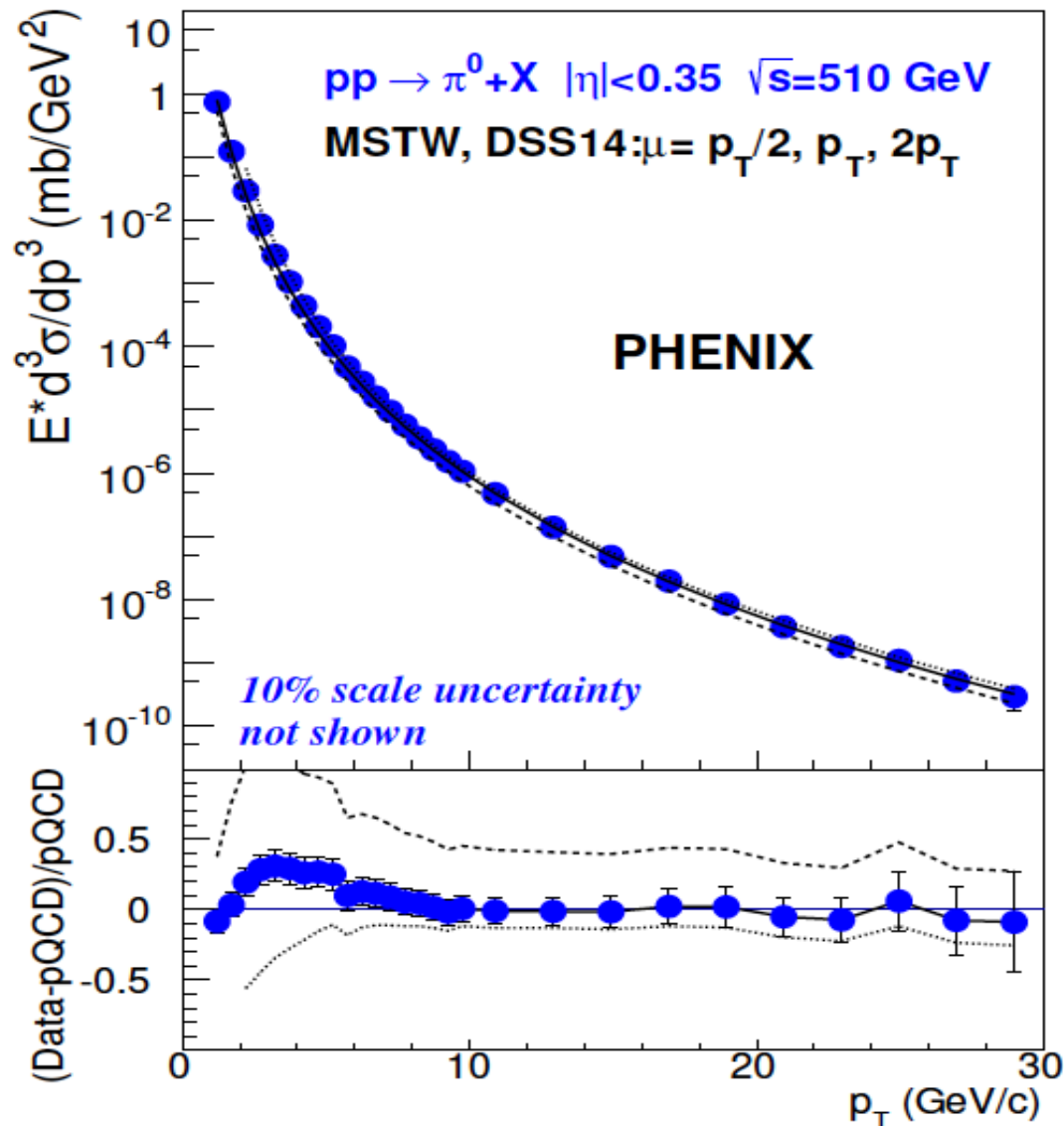


$\Delta g$  has larger uncertainty at small  $x$  region. Large lower region is still unexplored.

# Data Selection

- ❖ Data was recorded in 2012 and 2013 (>312 hours) with the PHENIX central arm detectors
- ❖ Average polarization:
  - ❖ Blue:  $0.55 \pm 0.02$
  - ❖ Yellow:  $0.56 \pm 0.02$
- ❖ An extensive QA analysis was performed
- ❖ Additional cuts were applied to improve the quality of the data
  - ❖ Total Luminosity (p + p collisions):  $155 \text{ pb}^{-1}$
  - ❖ Luminosity (good data):  $108 \text{ pb}^{-1}$  (Run 13),  $20 \text{ pb}^{-1}$  (Run 12)

# Cross-Section Results from 2013



- ❖ Comparison is made with theoretical calculation (pQCD)
- ❖ Theory agrees well with data

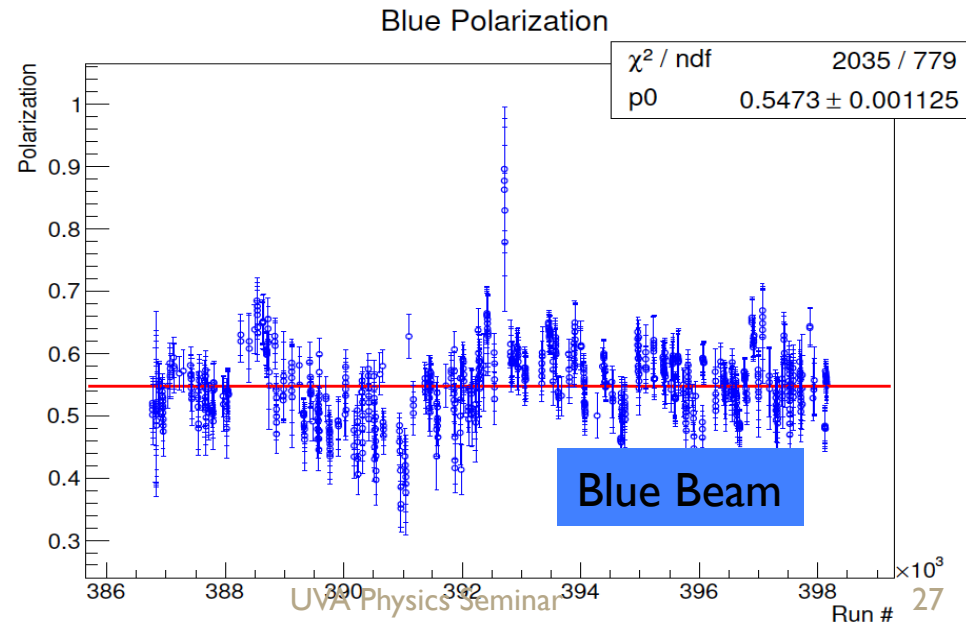
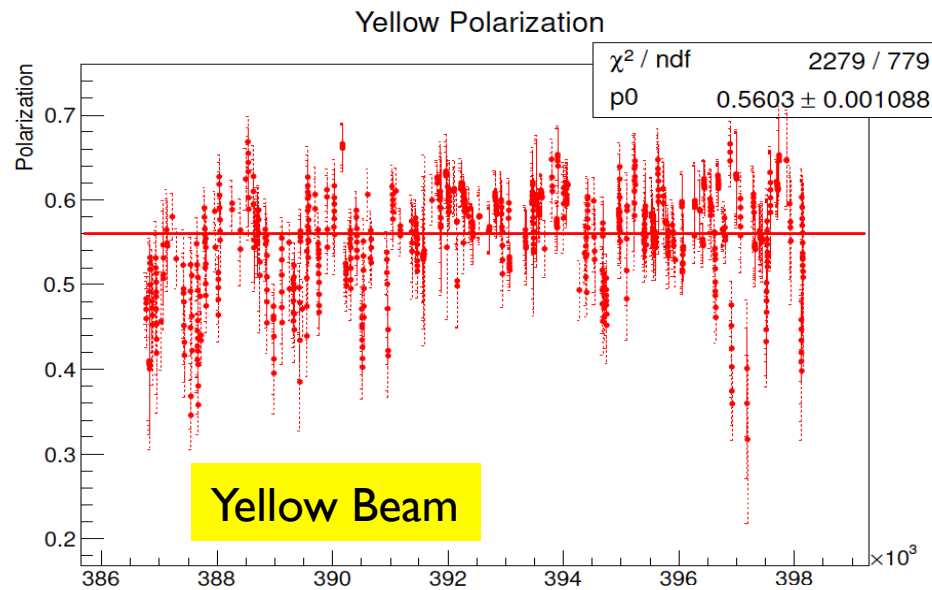
# Basic Ingredients for $A_{LL}$

Recap

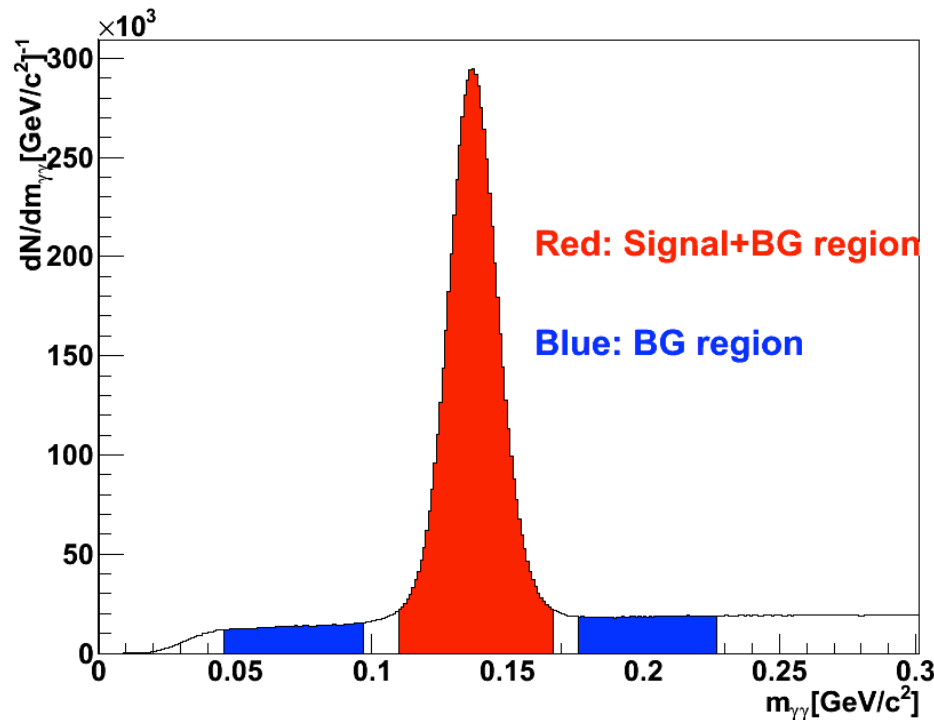
$$A_{LL} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} = \frac{1}{P_b P_y} \frac{N_{++} - RN_{+-}}{N_{++} + RN_{+-}}$$

- ① Polarization information
- ② Yield from  $\pi^0$  and
- ③ Relative luminosity

# Polarization Results



# $\pi^0$ Yield



- ❖ Invariant mass spectrum of  $\pi^0$  reconstructed from associated di-photons in the detector in each event

$$m_{\pi^0} = \sqrt{E_1 E_2 - \vec{p}_1 \cdot \vec{p}_2}$$

- ❖ Red: signal + background region
- ❖ Blue: background regions



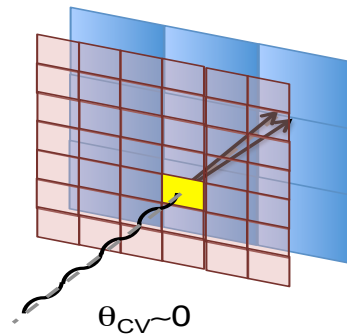
# Major Sources of Background

- ❖ Charged hadrons
- ❖ Uncorrelated background



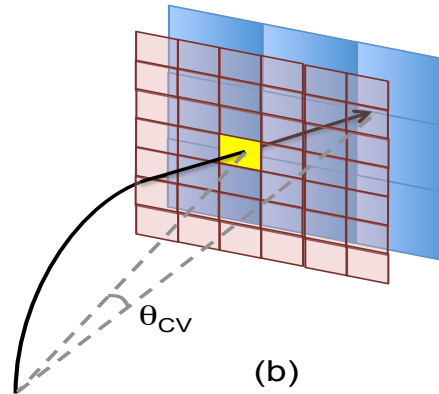
## CHARGEVETO CUT (REMOVING CHARGED HADRONS)

# Veto Cut to Remove Charged Hadron



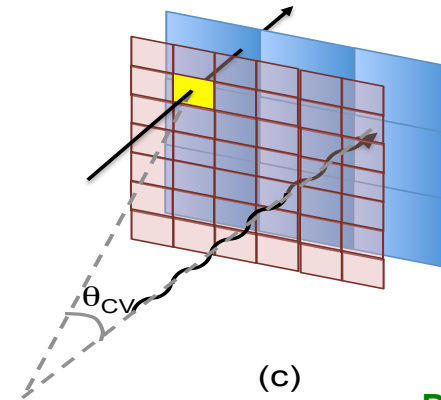
(a)

Conversion  
like



(b)

Hadron like



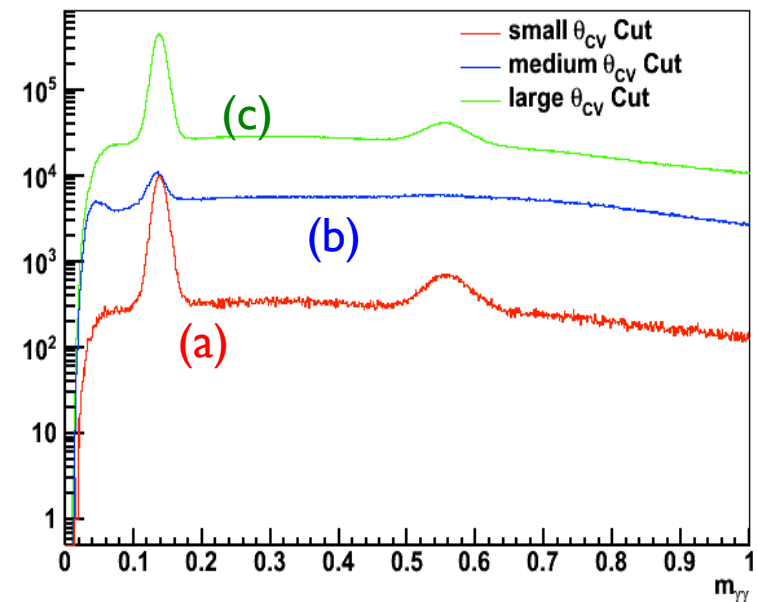
(c)

Photon like

$5.0 < p_T < 6.0$

## Charge Veto:

- ❖ Use pad chamber in front of EMCAL to tag charged hadrons
- ❖ Based on angle ( $\theta_{cv}$ ) between EMCAL and Pad hit:
  - ❖ Exclude **hadrons** with moderate  $\theta_{cv}$
  - ❖ Retain **conversion electrons** with near zero  $\theta_{cv}$

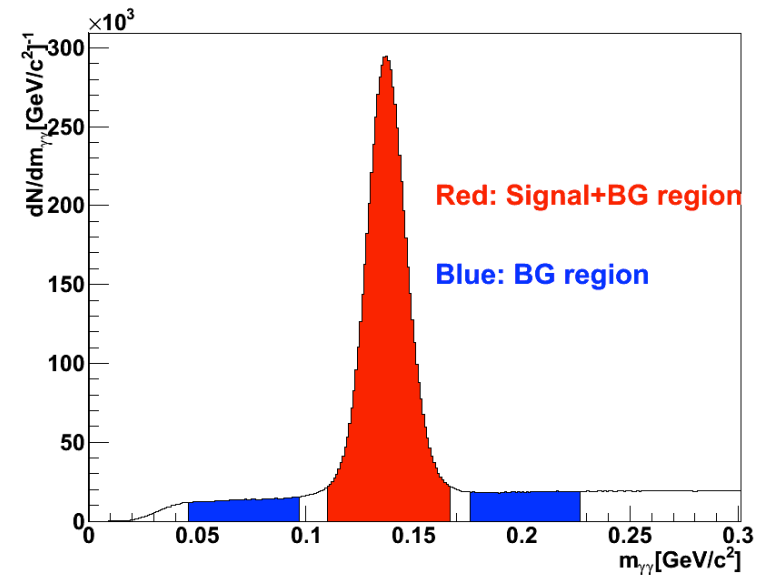


# Uncorrelated background

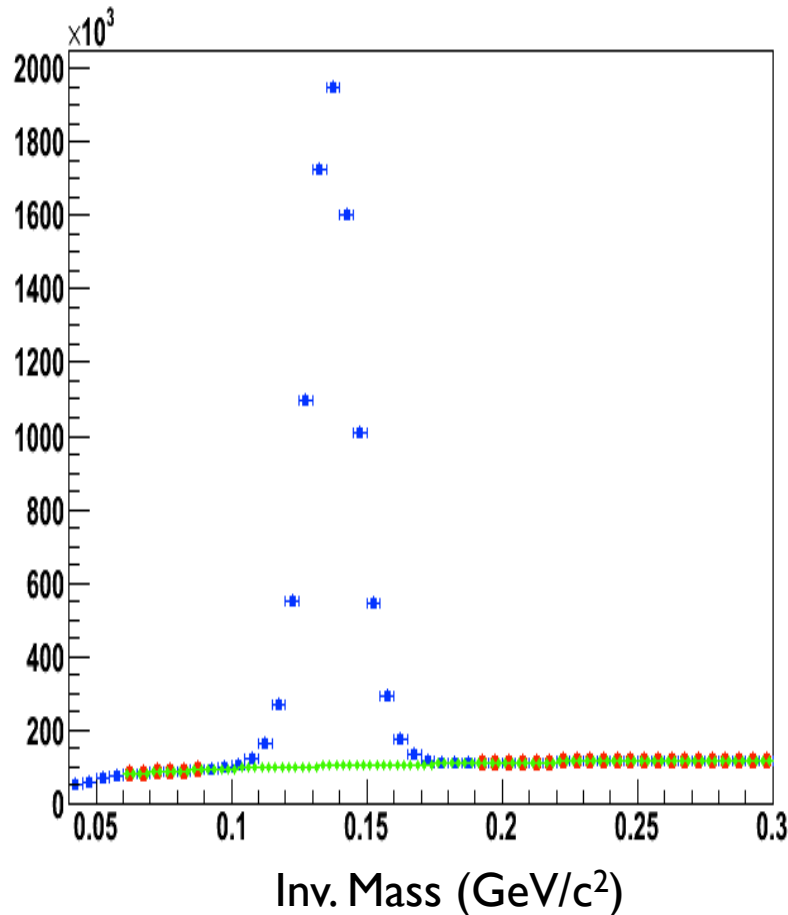
- ❖ Random pair matching
- ❖ Their effect can't be reduced but can be estimated by calculating the background fraction

# Background Fraction Calculation

- ❖ Ratio of number of counts in background region (**blue area**) and  $\pi^0$ s in signal region (**red area**)
- ❖ The  $\pi^0$  in background region is calculated by using Gaussian Process Regression (GPR) method
- ❖ The  $\pi^0$  in signal region is calculated by simply counting the yields from histograms



# GPR Method for Estimation of Background Fraction

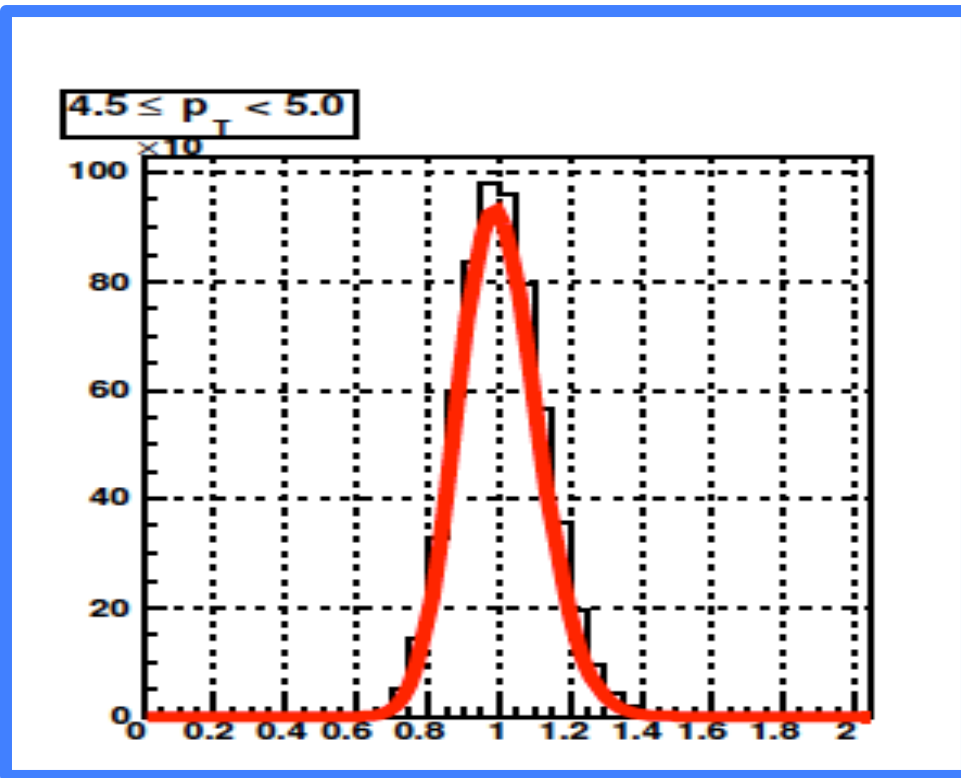


- ❖ Gaussian Process Regression(GPR) method is used to find the  $\pi^0$  in the background region.
- ❖ Here, blue is our data, red is the fit by GPR and green is extrapolated values



# **SYSTEMATIC UNCERTAINTY STUDIES**

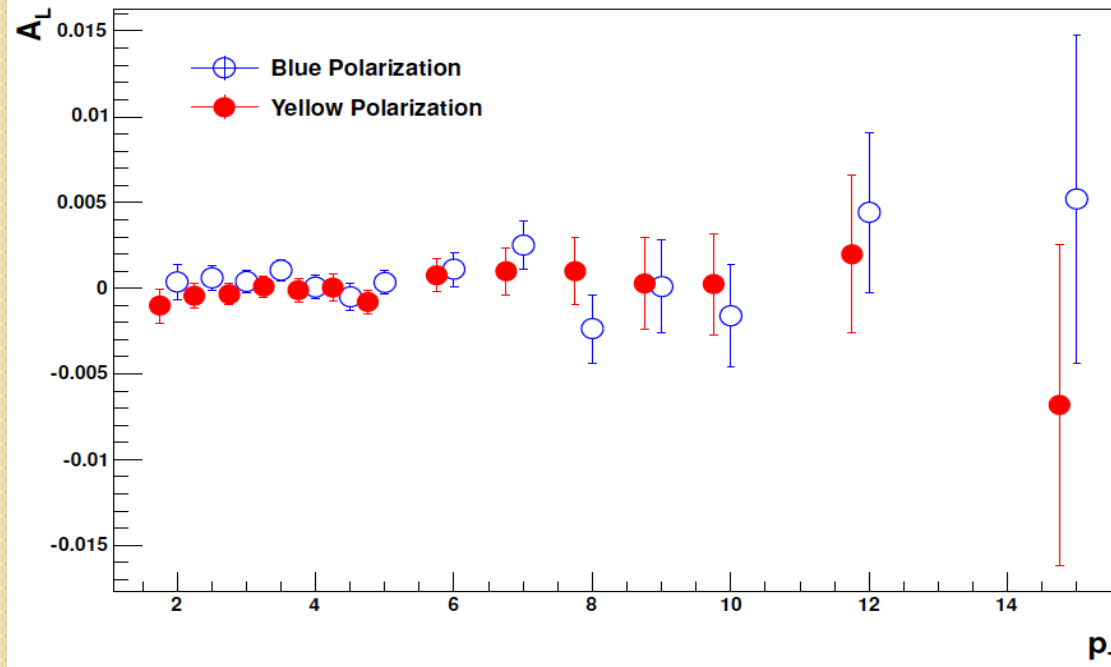
# Bunch Shuffling (representative plots)



- ❖ Method to test if there is any systematic effect due to different bunches
- ❖ Randomly assign helicity for all bunches.
- ❖ Get  $A_{LL}$  for all fills in each  $p_T$  bin.
- ❖ Find  $\chi^2/\text{NDF}$  for each sample.



# Single Spin Asymmetry



- ❖ Parity violating property
- ❖ Strong interaction preserve the parity
- ❖ Small value of SSA is expected  
(Strong interactions conserve parity)



# RESULTS

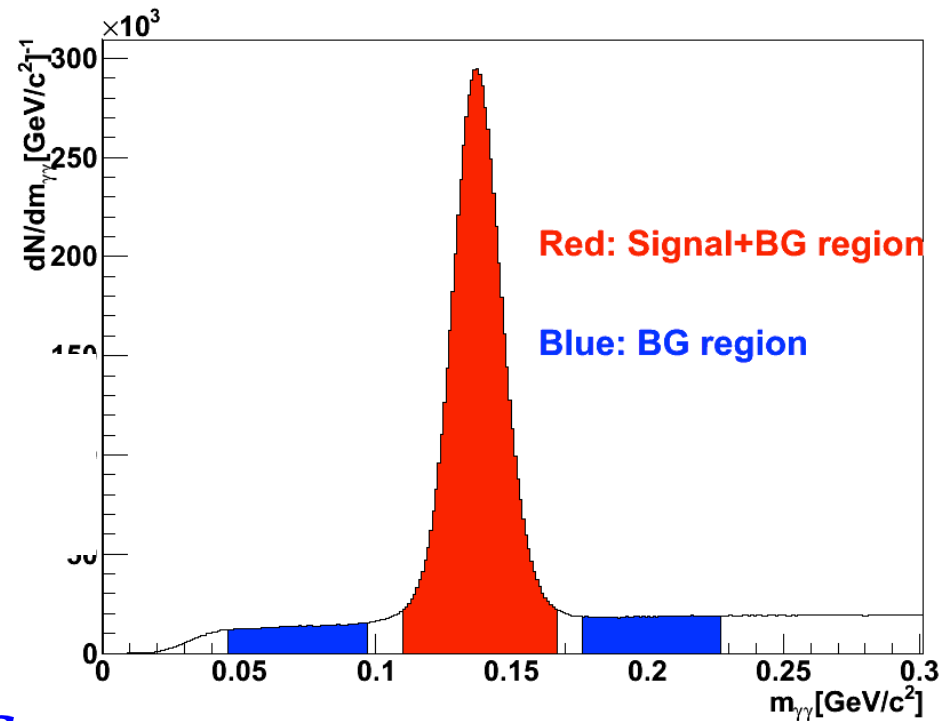
# Double Helicity Asymmetry: $A_{LL}$

- ❖ Double helicity asymmetry for signal region (red region) and background region (blue) is calculated
- ❖ The background subtracted asymmetry is given by:

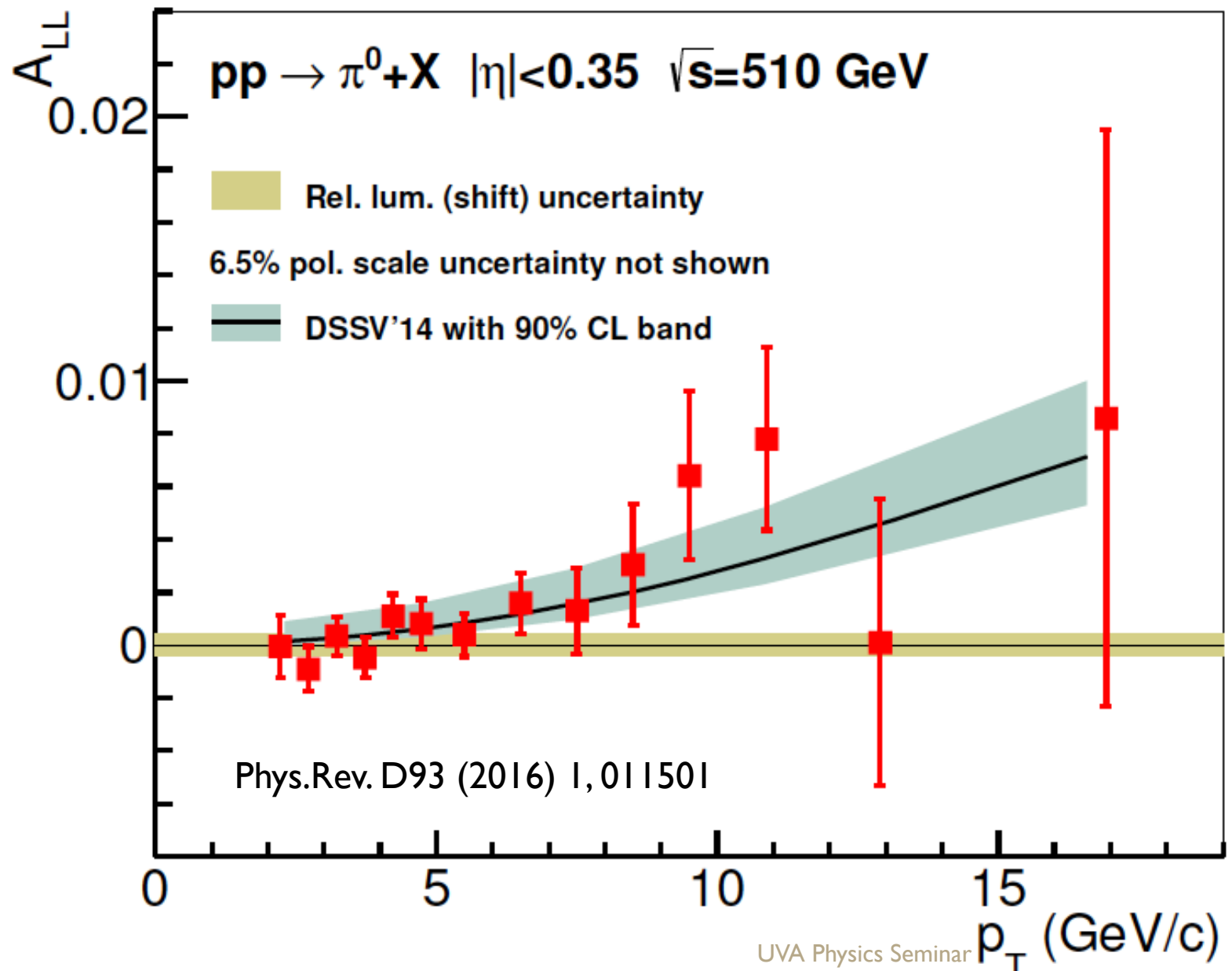
$$A_{LL} = \frac{A_{LL}^{\pi^0+BG} - r A_{LL}^{BG}}{1-r}$$

- ❖  $r$  is given by:

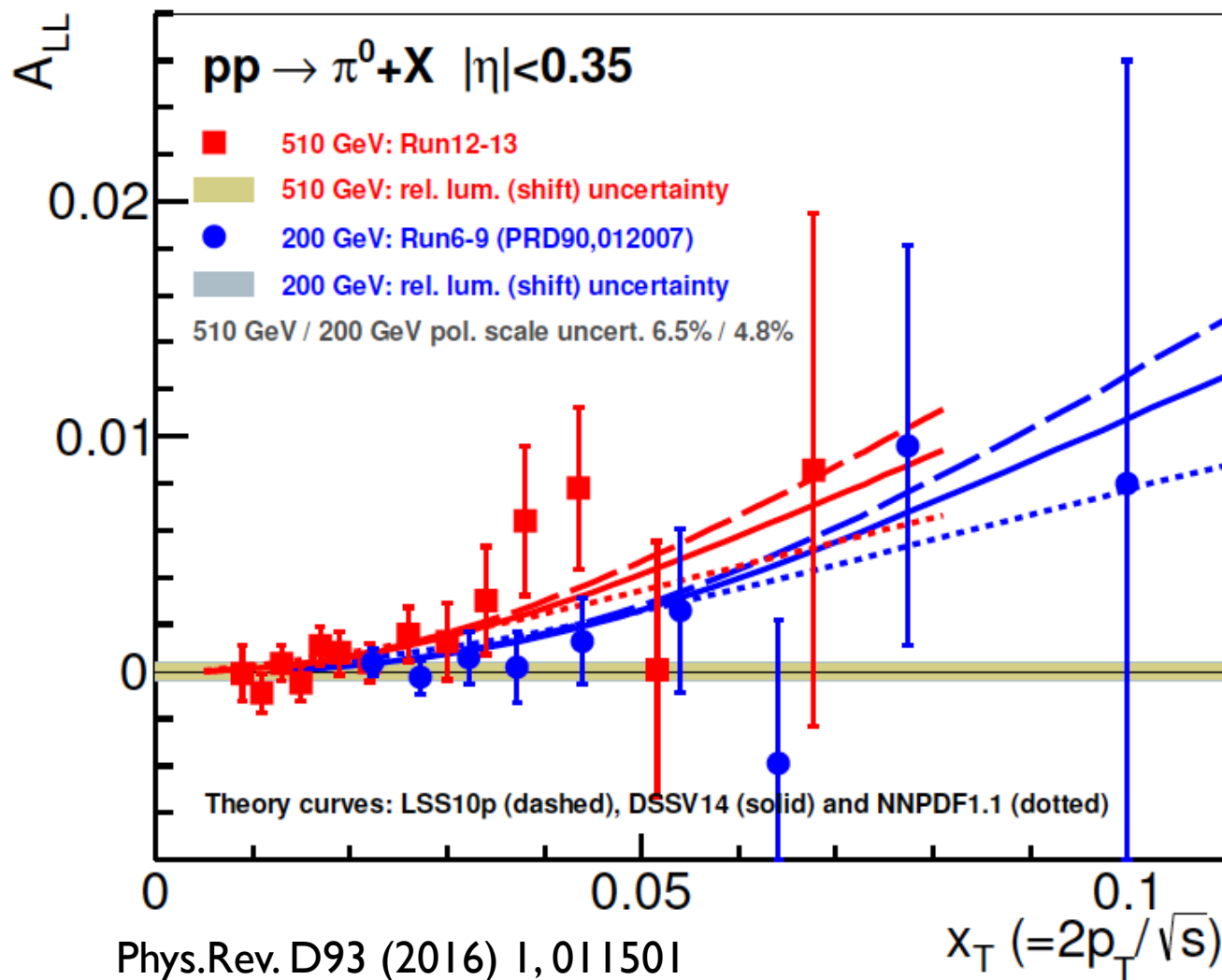
$$r = \frac{N^{BG}}{N^{BG} + \pi^0}$$



# Double Helicity Asymmetry From 510 GeV Data



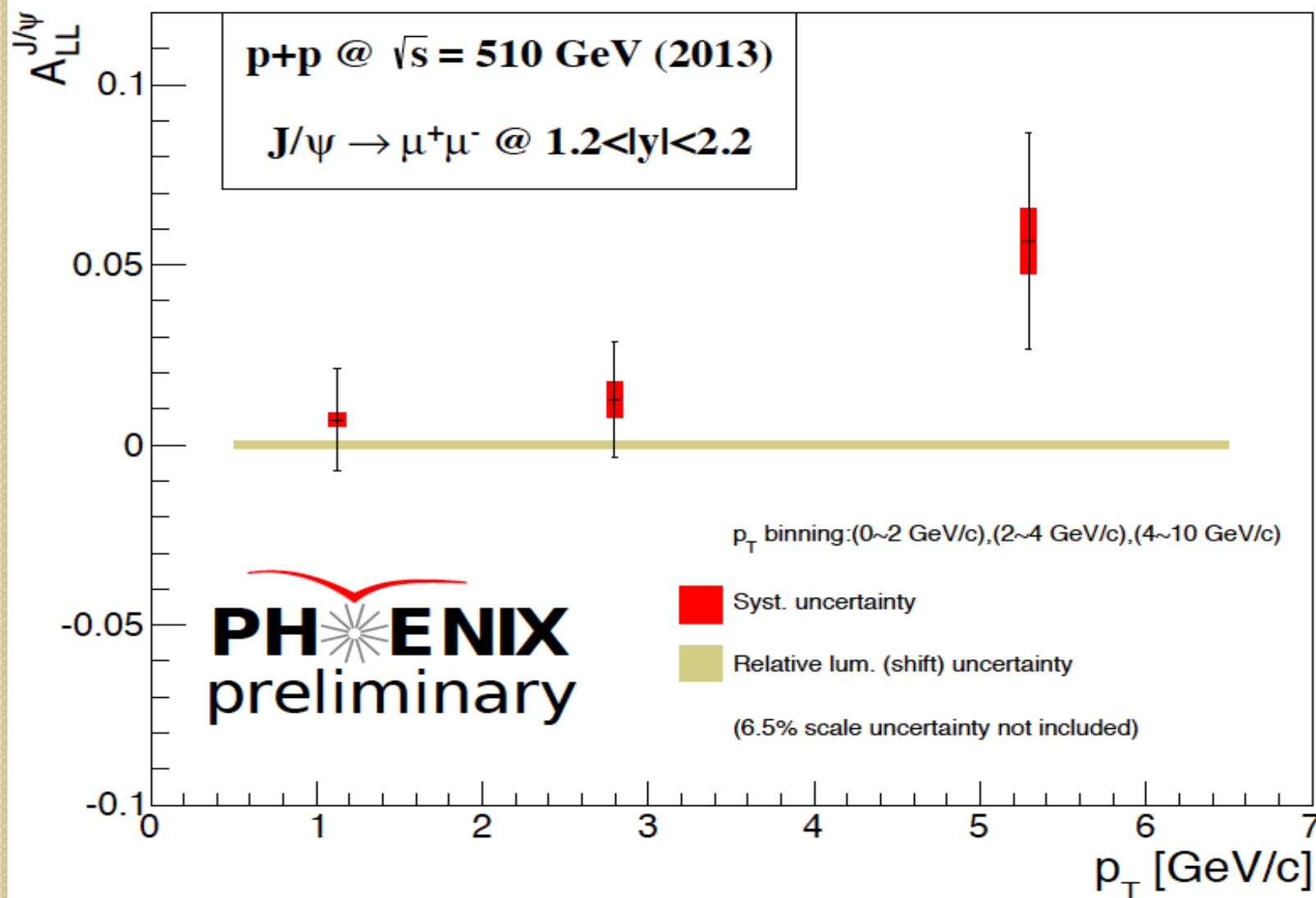
# Comparison of Double Helicity Asymmetry at different center of mass energies



Phys.Rev. D93 (2016) 1, 011501

Preprint: arXiv:1510.02317

# Double Helicity Asymmetry Results from $J/\psi$



# Summary & Conclusion



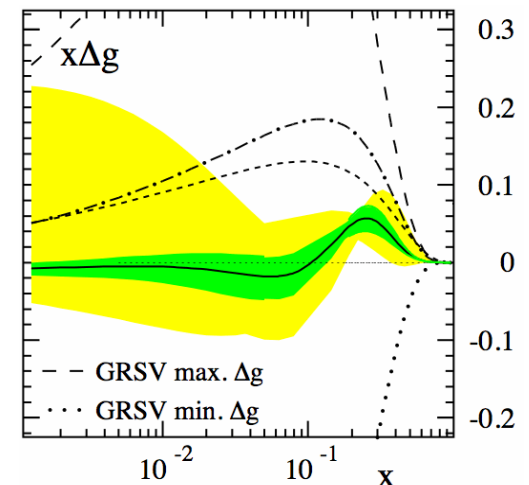
- ❖ Cross-section and double helicity asymmetry from  $\pi^0$  production at center of mass energy of 510 GeV is measured
  - ❖ **For the first time in PHENIX, non-zero asymmetry is observed in  $\pi^0$  production (Published in Phys.Rev. D93 (2016) 1, 011501)**
  - ❖ Theory agrees very well with the measured cross-section
- ⇒ allows using the theory to interpret  $A_{LL}$  results

# Future Prospects

- ❖ PHENIX has measured  $A_{LL}$  of  $\pi^0$  production in several data sets ( $\sqrt{s} = 62.4, 200$  and  $510$  GeV).  $\pi^0$  data was included in global analysis. DSSV ++ indicates non-zero  $\Delta G$

$$\int_{0.05}^{1.0} \Delta g(x) dx = 0.2^{+0.06}_{-0.07}$$

- ❖ New data to be used in global fit
- ❖ Still large uncertainty at low Bjorken  $x$  region:  
Need to extend coverage to lower- $x$  region



- ❖ Electron Ion Collider (EIC) is the ultimate solution for the complete understanding of gluon polarization as well as orbital angular momentum (OAM) of quarks and gluons





Finally, Answer to my Initial Question:

Does the Gluon Carry Proton's Spin?

**Yes, indeed!!!**

# Understanding the Nucleon is like: (Elephant and 6 Blind People)





Asymmetry Results from Fit

# APPENDIX

# Cross-Section of $\pi^0$ Meson

$$E \frac{d^3\sigma}{d^3p} = \frac{1}{2\pi p_T} \frac{1}{BR} \frac{1}{L} \frac{1}{A \epsilon_{trig} \epsilon_{rec}} \frac{N(\Delta p_T, \Delta y)}{\Delta p_T \Delta y}$$


















- BR is the branching ratio ~99%,
- L is the integrated luminosity  $\sim N^{MB} / \sigma^{BBC}$   
( $\sigma^{BBC} = 32.5$  mb),
- A is the acceptance calculated from simulation,
- $\epsilon_{trig}$  is the trigger efficiency,
- $\epsilon_{rec}$  is the reconstruction efficiency.
- N is the number of reconstructed  $\pi^0$  mesons.



# **POLARIZATION MEASUREMENTS**

# Understanding the Spin Structure of Nucleon

## What is a nucleon???

QUARKS	mass → $\approx 2.3 \text{ MeV}/c^2$ charge → $2/3$ spin → $1/2$  up	mass → $\approx 1.275 \text{ GeV}/c^2$ charge → $2/3$ spin → $1/2$  charm	mass → $\approx 173.07 \text{ GeV}/c^2$ charge → $2/3$ spin → $1/2$  top	mass → 0 charge → 0 spin → 1  gluon	mass → $\approx 126 \text{ GeV}/c^2$ charge → 0 spin → 0  Higgs boson
	mass → $\approx 4.8 \text{ MeV}/c^2$ charge → $-1/3$ spin → $1/2$  down	mass → $\approx 95 \text{ MeV}/c^2$ charge → $-1/3$ spin → $1/2$  strange	mass → $\approx 4.18 \text{ GeV}/c^2$ charge → $-1/3$ spin → $1/2$  bottom	mass → 0 charge → 0 spin → 1  photon	
	mass → $0.511 \text{ MeV}/c^2$ charge → -1 spin → $1/2$  electron	mass → $105.7 \text{ MeV}/c^2$ charge → -1 spin → $1/2$  muon	mass → $1.777 \text{ GeV}/c^2$ charge → -1 spin → $1/2$  tau	mass → $91.2 \text{ GeV}/c^2$ charge → 0 spin → 1  Z boson	
LEPTONS	mass → $< 2.2 \text{ eV}/c^2$ charge → 0 spin → $1/2$  electron neutrino	mass → $< 0.17 \text{ MeV}/c^2$ charge → 0 spin → $1/2$  muon neutrino	mass → $< 15.5 \text{ MeV}/c^2$ charge → 0 spin → $1/2$  tau neutrino	mass → $80.4 \text{ GeV}/c^2$ charge → $\pm 1$ spin → 1  W boson	GAUGE BOSON

To understand nucleons, we need to understand the Standard model.

# Quest from last 30 Years

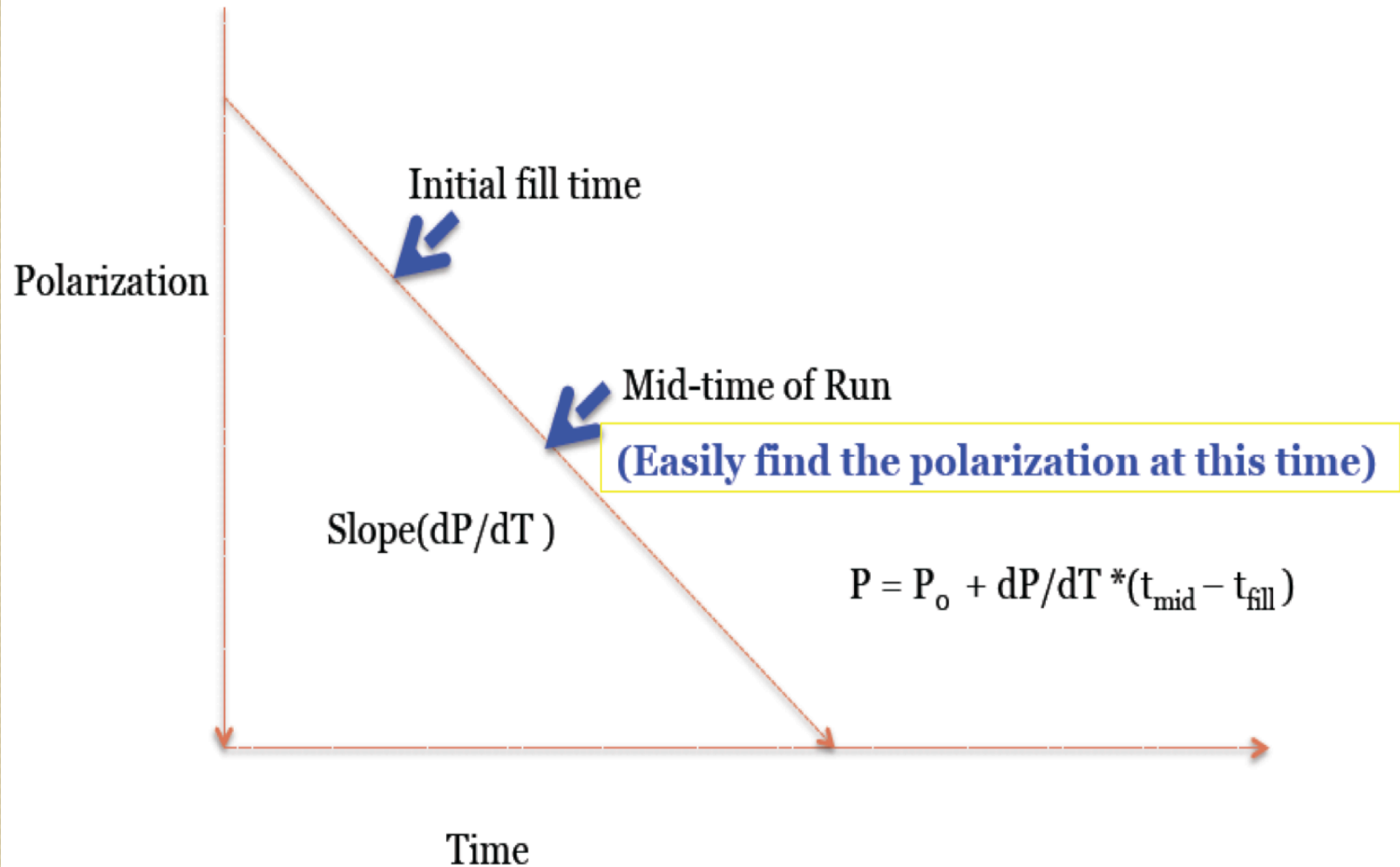


# Polarization Measurements

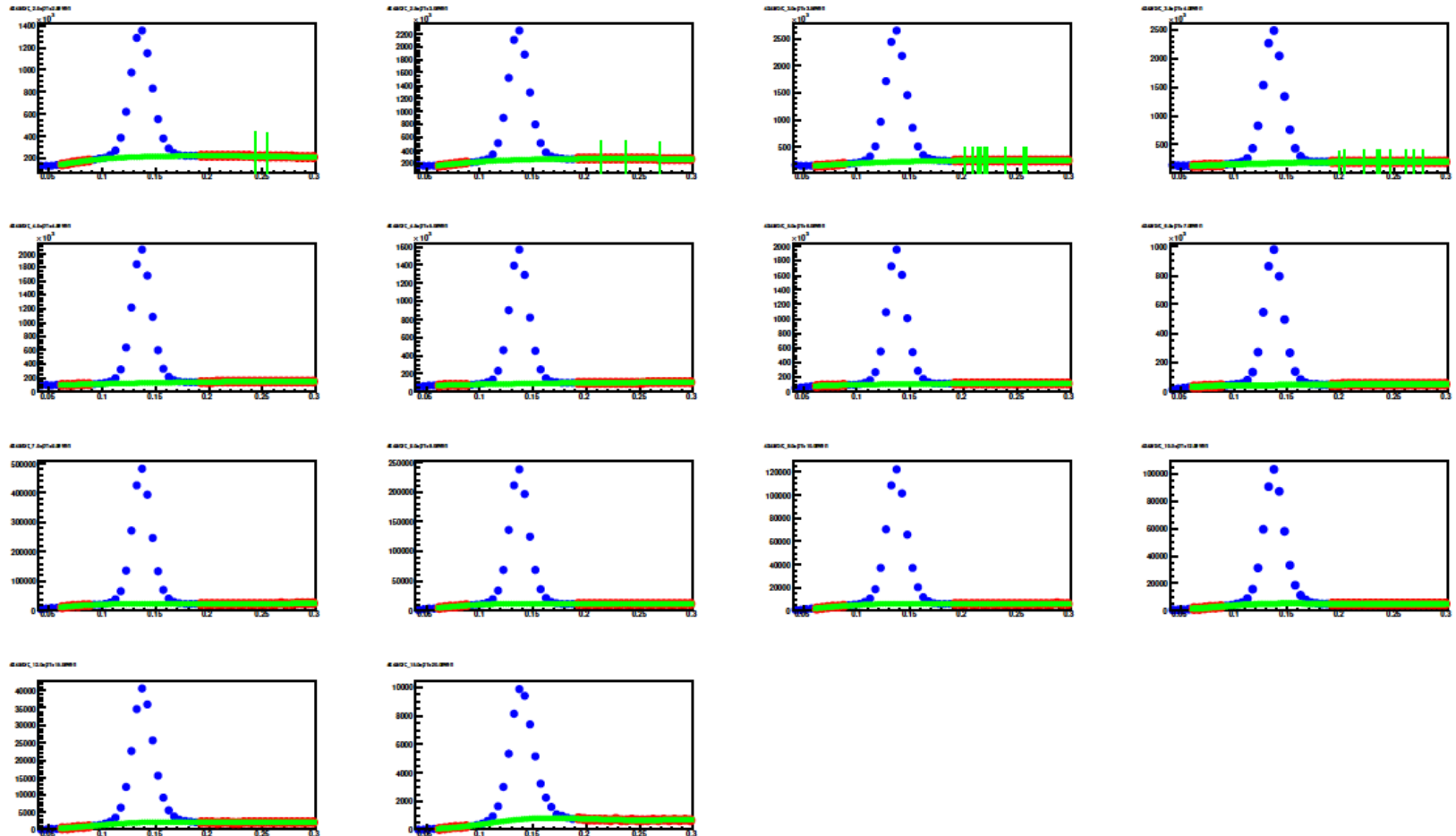
- ❖ Fill-by-fill polarization values provided by the CNI group
- ❖ Change it to run-by-run values
  - ◆ Polarization values at beginning of each fill is known
  - ◆ Time stamp of each run is known
  - ◆ We find the mid-value of time
  - ◆ Calculate the polarization value at that particular time



# Polarization Calculations

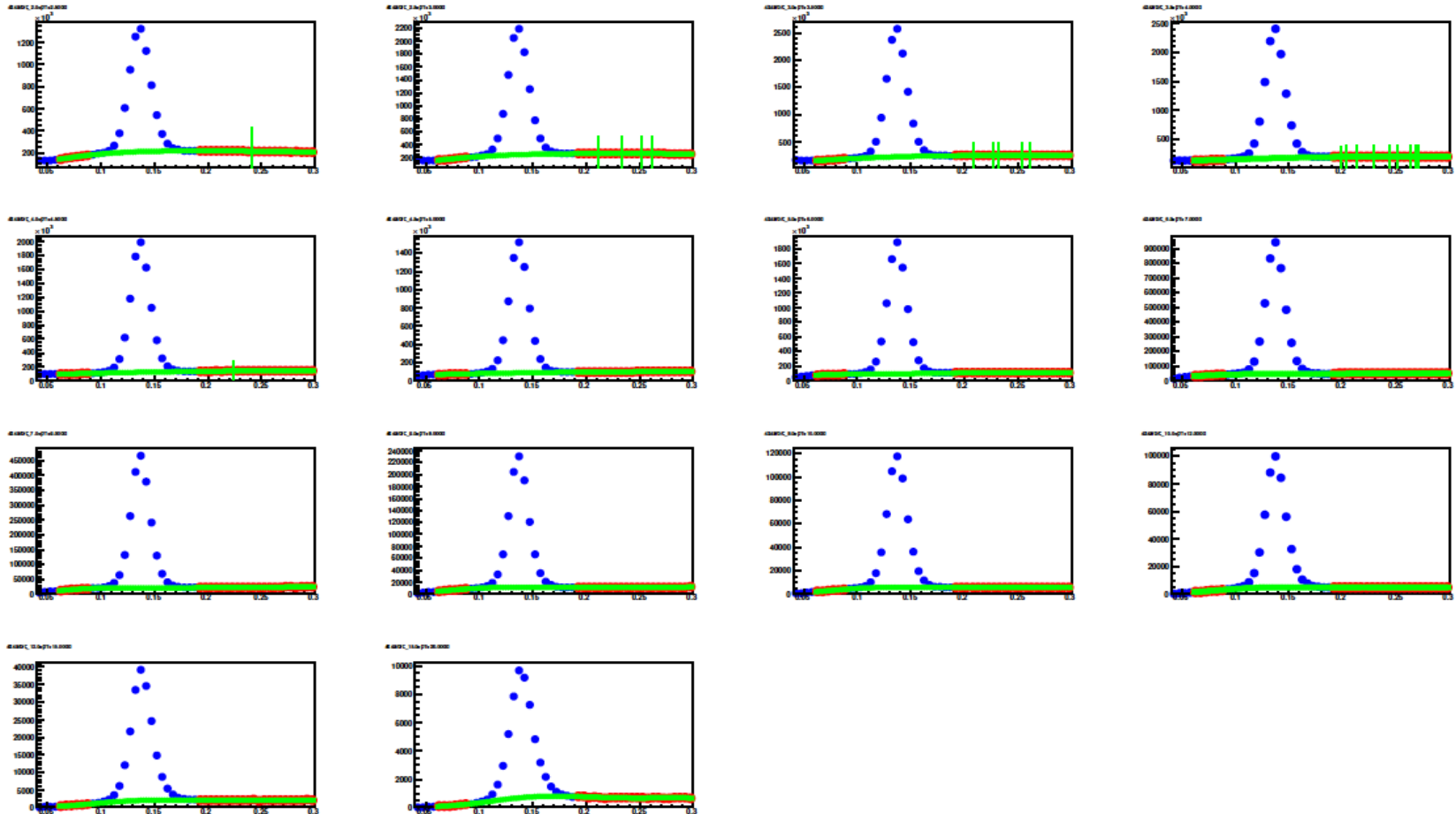


# Background Fraction Calculation (GPR method) Even Crossing



# Background Fraction Calculation (GPR method)

## Odd Crossing



# Bunch Shuffling: Procedure

- ❖ Generate 600000 random bunches
- ❖ Apply same set of cuts as was applied in the data analysis.
- ❖ Calculate  $A_{LL}$  fill by fill and find the mean from fit.
- ❖ Calculate the Chi Square per NDF and draw this distribution.

# Bunch Shuffling

- ❖ Technique to ensure any systematic uncertainty from bunch to bunch or fill to fill is less than our statistical uncertainty.

Procedure:

- ❖ Randomly assign helicity for all bunches.
- ❖ Get  $A_{LL}$  for all fills in each pT bin.
- ❖ Find  $\chi^2/\text{NDF}$  for each sample.

# Getting Veto Parameters

- ❖ Upper edge: Large veto angle  $\rightarrow$  Due to uncorrelated hits  $\rightarrow$  Need to keep
- ❖ Middle part: Medium veto angle  $\rightarrow$  Due to charged hadron  $\rightarrow$  Need to throw
- ❖ Lower edge: Small veto angle  $\rightarrow$  Due to photon conversion  $\rightarrow$  Need to keep

