

Brout-Englert-Higgs Mechanism and Beyond

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- ▶ The framework that combines principles of the Quantum Mechanics and the Special Relativity is the Quantum Field Theory (QFT)
- ▶ Lagrangian (\mathcal{L}) is used instead of Hamiltonian (\mathcal{H})
- ▶ Physicists knew the Quantum Electrodynamics (QED) and tried to build a theory to explain the β -decay based on similar ideas
- ▶ This theory agreed with experiments AT LOW ENERGY, but had BAD HIGH ENERGY BEHAVIOR



A quick revision (continued..)

- ▶ To solve this a theory of 'weak interactions' was put forward adding W^\pm bosons as the force carriers of the weak force



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- ▶ To cancel certain 'badly behaving interactions' a third neutral W^0 boson was added
- ▶ Three matrices ($T^{1,2,3}$) were required for this cancellation with a condition

$$[T^a, T^b] = T^a T^b - T^b T^a = i \sum_c \epsilon^{abc} T^c$$

$\Rightarrow SU(2)$ group symmetry !



A quick revision (continued..)

- ▶ Construct Lagrangian of (Weak + QED) \rightarrow ELECTROWEAK THEORY ($SU(2) \times U(1)$ symmetry)

W^μ and A^μ combine to give W^\pm , Z^0 and photon γ



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- ▶ Meaning of having a symmetry: If the 'Fields' associated with all particles undergo transformation under the symmetry group (something like multiplication by $Exp(i \sum_a T^a \alpha^a)$), the Lagrangian of the theory remains invariant



A quick revision (continued..)

- ▶ If we want a freedom of performing such transformations at a point in space-time without affecting fields at other space-time points (LOCAL SYMMETRY: $\alpha \rightarrow \alpha(x)$),



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- ▶ Same for mass terms like $m_f \bar{\Psi}_f \Psi_f$ of fermions (electron, neutrinos, muon etc.)
- ▶ Because these particles MUST be massive some other mechanism is needed to give these particles their masses



BROUT-ENGLERT-HIGGS MECHANISM

In 1964 by 3 groups: Robert Brout and François Englert; by Peter Higgs; and by Gerald Guralnik, C. R. Hagen, and Tom Kibble

Incorporated in the Standard Model by Steven Weinberg (1967) and Abdus Salam (1968)



Introduction to the Standard Model

Three generations of matter (fermions)

	I	II	III		
mass →	2.4 MeV/c ²	1.27 GeV/c ²	171.2 GeV/c ²	0	7 GeV/c ²
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
name →	u up	c charm	t top	γ photon	H Higgs boson
Quarks	4.8 MeV/c ²	104 MeV/c ²	4.2 GeV/c ²	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	d down	s strange	b bottom	g gluon	
Leptons	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	91.2 GeV/c ²	
	0	0	0	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ Z boson	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	80.4 GeV/c ²	
	-1	-1	-1	± 1	
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Gauge bosons



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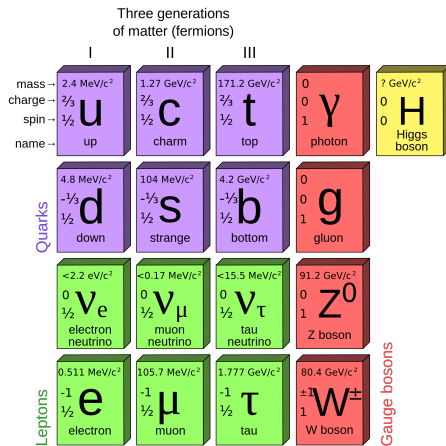
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 - ▶ $SU(3) \times SU(2) \times U(1)$
- LOCAL GAUGE SYMMETRY

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- Accounts for *almost* everything about Electroweak and Strong interactions of the fundamental particles in Nature (not gravitational)
- $SU(3) \times SU(2) \times U(1)$ LOCAL GAUGE SYMMETRY
- It is important to understand how all these elementary particles get their masses or massless-ness



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- ▶ This means that in the stable state of the universe that we are in, $SU(2) \times U(1)$ is broken
- ▶ Thus, $SU(2) \times U(1)$ symmetry must have existed right after the Big Bang and soon after that
THE SYMMETRY WAS BROKEN *SPONTANEOUSLY*



SOME CONCEPTS



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the fields need to have small values i.e.
average value zero + quantum fluctuations



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- ▶ Hereafter, we'll use the covariant derivative in the kinetic terms



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- ▶ Lagrangian: $\mathcal{L} = (D_\rho \phi)^\dagger (D^\rho \phi) - \frac{1}{4} F_{\rho\sigma} F^{\rho\sigma} - V(\phi)$

$$\text{with potential } V(\phi) = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$



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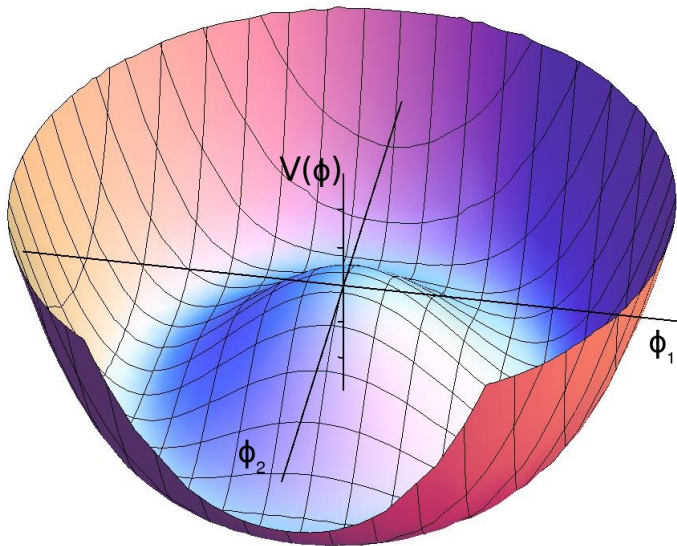
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- ▶ No higher orders of ϕ to ensure that all infinite interactions/diagrams can be cancelled (*Renormalizability!*)

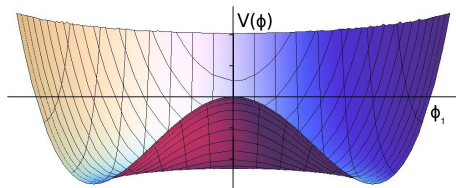
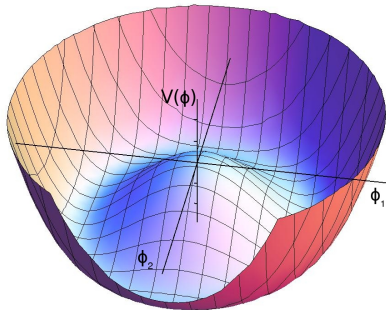


Only case of interest: $\mu^2 > 0$

($\mu^2 < 0$ does not have the 'valley')



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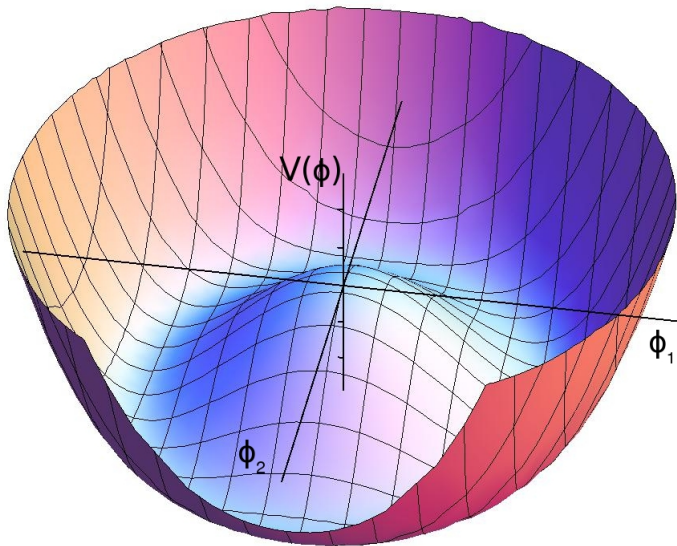
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- ▶ This is the state that all the 'Expectation (like average) values' (e.g. $\langle \phi \rangle$) are seen to be in



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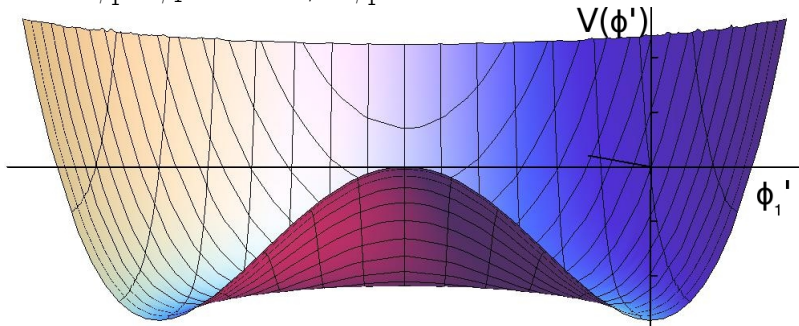
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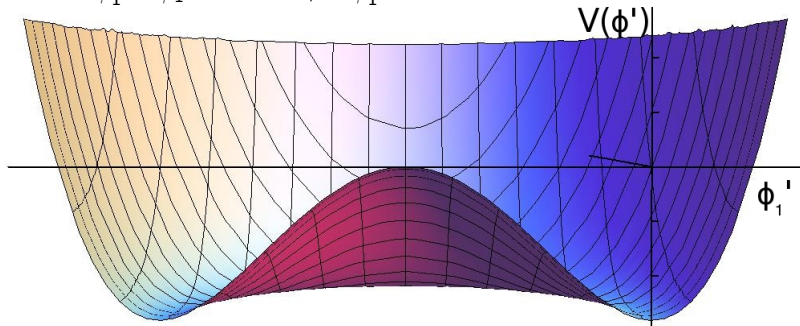
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- ▶ One problem in working with these fields: We want to use perturbation theory
And perturbation theory requires smallness of the terms in the expansion (much like Taylor expansion)
- ▶ So the fields must have average value zero in the ground state



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- The symmetry OF THE GROUND STATE is broken SPONTANEOUSLY



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$$\begin{aligned}(D_\rho \phi)^\dagger (D^\rho \phi) &= (\text{some 'ok' terms}) + \frac{g^2 v^2}{2} A_\rho A^\rho \text{ (hurray!)} \\ &\quad - g v A_\rho (\partial^\rho \phi_2 + g A^\rho \phi'_1) \text{ (problem again!!)}\end{aligned}$$



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- ▶ Try polar coordinates:

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- ▶ $\phi(x) \approx \frac{1}{\sqrt{2}} (v + \eta(x) + i \theta(x))$ and
- $$= \frac{1}{\sqrt{2}} (v + \phi'_1(x) + i \phi_2(x))$$



- ▶ Use symmetry and transform:

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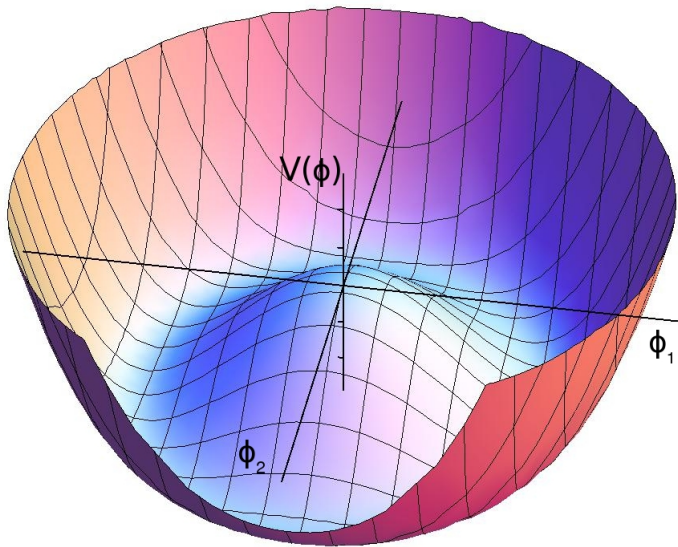
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- ▶ AND a scalar particle associated with ϕ'_1 has appeared having mass ($\sqrt{2} \mu$)
 \rightarrow BROUT-ENGLERT-HIGGS BOSON :-)





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- ▶ Higgs field interacts with the fermions through Yukawa interaction

$$\sim g_f \phi \bar{\psi}_f \psi_f = \frac{g_f v}{\sqrt{2}} \bar{\psi}_f \psi_f + (\text{interaction with } \phi')$$
 → masses of fermions (Neutrinos are still massless)



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- ▶ Many Grand Unified Theories (GUT) postulate right-handed neutrinos at mass $\sim 10^{16-17}$ GeV!!
Cannot be detected at LHC or near future colliders



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ACCESSIBLE TO LHC



Is it possible to have mass of the right-handed neutrino in the mass range
ACCESSIBLE TO LHC
WITH NO NEW FUNDAMENTAL FORCES
added to the Standard Model ?



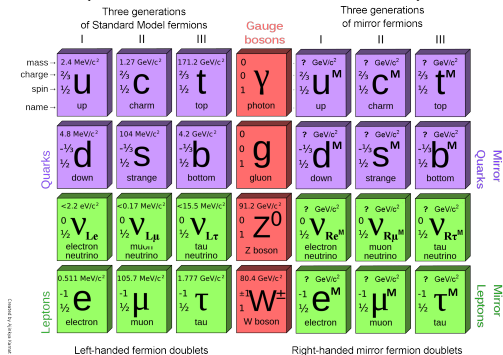
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Three generations
of mirror fermions.



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Three generations of Standard Model fermions						Three generations of mirror fermions		
	I	II	III	Gauge bosons	I	II	III	
mass →	2.4 MeV/c ²	1.27 GeV/c ²	171.2 GeV/c ²	0	? GeV/c ²	? GeV/c ²	? GeV/c ²	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	
name →	u up	c charm	t top	Y photon	u ^M up	c ^M charm	t ^M top	
Quarks								Mirror Quarks
	4.8 MeV/c ²	104 MeV/c ²	4.2 GeV/c ²	0	? GeV/c ²	? GeV/c ²	? GeV/c ²	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	
	d down	s strange	b bottom	g gluon	d ^M down	s ^M strange	b ^M bottom	
Leptons								Mirror Leptons
	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	91.2 GeV/c ²	? GeV/c ²	? GeV/c ²	? GeV/c ²	
	0	0	0	0	0	0	0	
	ν_{Le} electron neutrino	$\nu_{L\mu}$ muon neutrino	$\nu_{L\tau}$ tau neutrino	Z ⁰ Z boson	ν_{Re}^M electron neutrino	$\nu_{R\mu}^M$ muon neutrino	$\nu_{R\tau}^M$ tau neutrino	
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	80.4 GeV/c ²	? GeV/c ²	? GeV/c ²	? GeV/c ²	
	-1	-1	-1	±1	-1	-1	-1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	
	e electron	μ muon	τ tau	W [±] W boson	e ^M electron	μ ^M muon	τ ^M tau	

Left-handed fermion doublets

Right-handed mirror fermion doublets

? GeV/c ² ±2 0 H ₅ ^{±±} Higgs boson	? GeV/c ² ±1 0 H ₅ [±] Higgs boson	? GeV/c ² 0 0 H ₅ ⁰ Higgs boson	? GeV/c ² 0 0 H ₁ ^{0'} Higgs boson	? GeV/c ² 0 0 H ₁ ^{0,R} Higgs boson
? GeV/c ² ±1 0 H _{3,1} [±] Higgs boson	? GeV/c ² 0 0 H _{3,1} ⁰ Higgs boson	? GeV/c ² ±1 0 H _{3,2} [±] Higgs boson	? GeV/c ² 0 0 H _{3,2} ⁰ Higgs boson	? GeV/c ² 0 0 H ₁ ^{0,L} Higgs boson
				?? eV/c ² 0 0 φ _S Higgs boson

- Interacts only with mirror fermions
- Interacts with Standard Model and mirror fermions
- Interacts with Standard Model fermions

Created by Ajinkya Kamat



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- ▶ Many exciting possibilities in this model as well as others.
Stay tuned!



Thank You :-)

