

The latest on proton charge radius

**Nuclear Physics Seminar
University of Virginia, Nov 8, 2011**

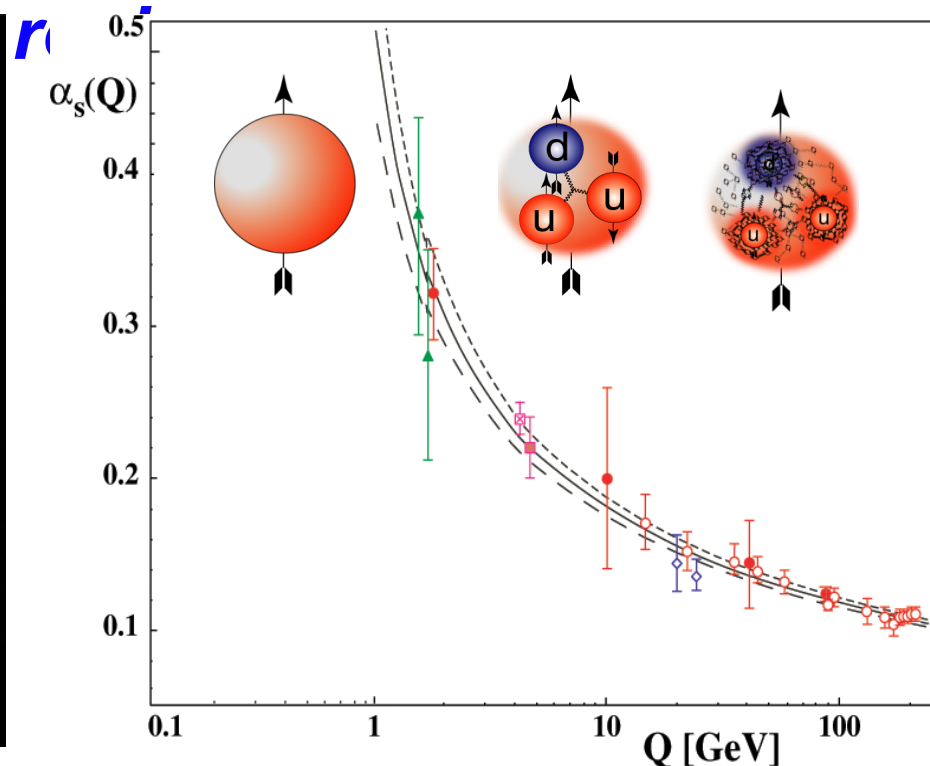
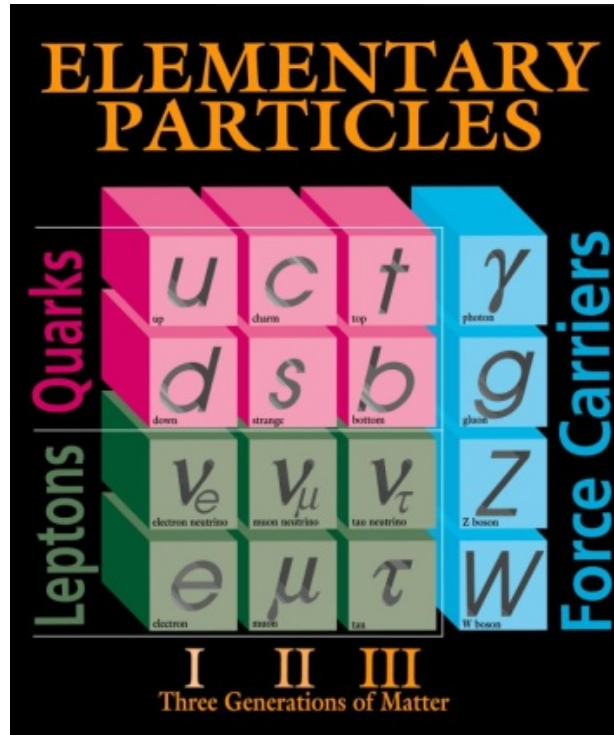
***Haiyan Gao
Duke University and TUNL***



Outline

- Introduction
- Proton EM form factors and charge radius
- Proton charge radius from H Lamb shift
- A new experiment on proton charge radius
- Summary

QCD: still unsolved in non-perturbative



Gauge bosons: gluons (8)

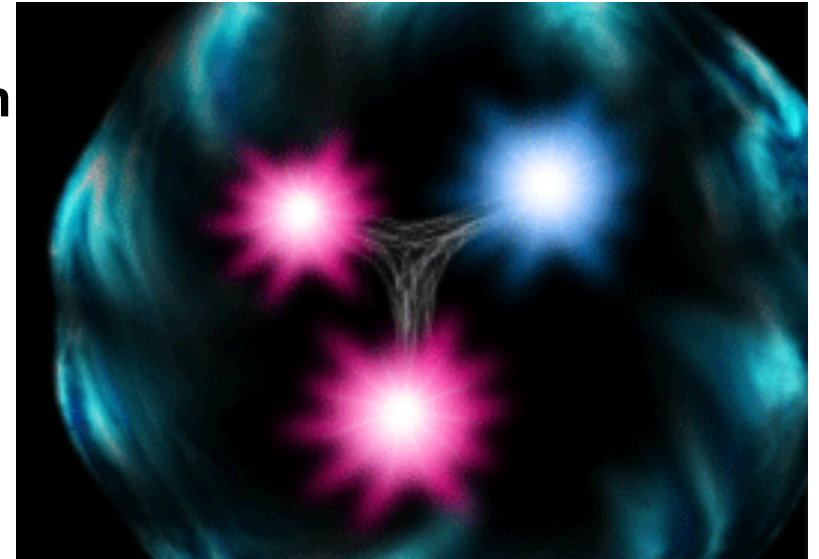
- 2004 Nobel prize for “asymptotic freedom”
- *non-perturbative regime QCD ?????*
- One of the top 10 challenges for physics!
- QCD: Important for discovering new physics beyond SM
- *Nucleon structure is one of the most active areas*

QCD



Nucleon Structure

- Strong interaction, running coupling ~ 1
 - QCD: the theory of strong interaction
 - asymptotic freedom (2004 Nobel)
perturbation calculation works at high energy
 - interaction significant at intermediate energy
quark-gluon correlations
 - confinement
interaction strong at low energy
coherent hadron
 - Chiral symmetry
 - theoretical tools:
pQCD, OPE, Lattice QCD, ChPT

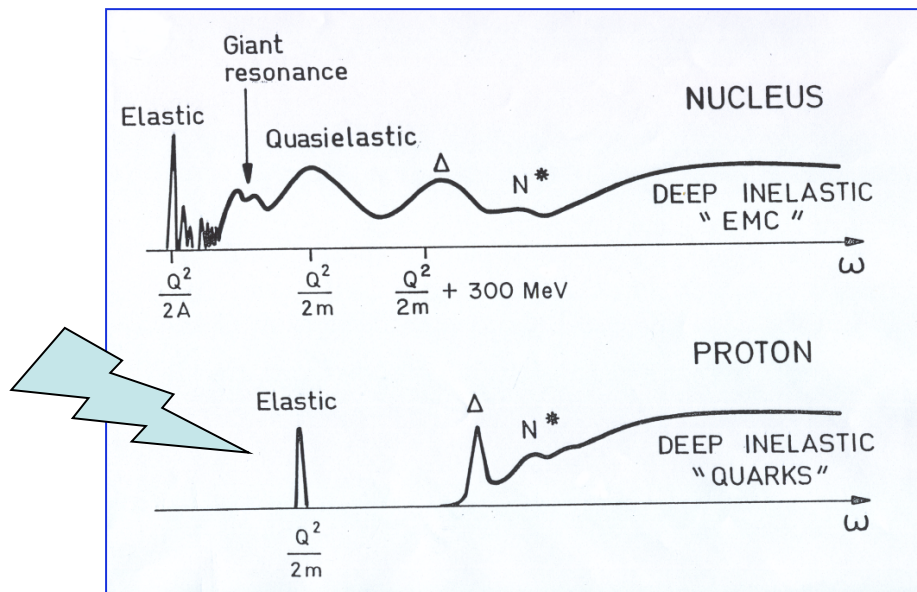


- Charge and magnetism (current E) distribution
 - Nucleon: Electric G_E and magnetic G_M form factor
- Spin distribution
- Quark momentum and flavor distribution
- Polarizabilities
- Strangeness content
-

This talk focuses on proton charge radius

Lepton scattering: powerful microscope!

- Clean probe of hadron structure
- Electron (lepton) vertex is well-known from QED
- One-photon exchange dominates, *higher-order exchange diagrams are suppressed*
- *One can vary the wave-length of the probe to view deeper inside the hadron*



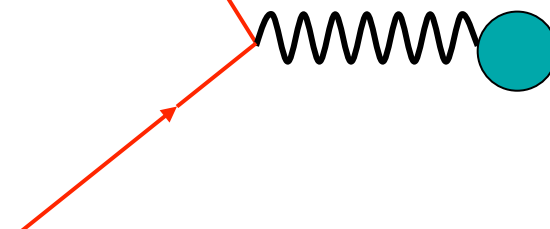
Virtual photon 4-momentum

$$q = k - k' = (\vec{q}, \omega)$$

$$Q^2 = -q^2$$

$$\alpha = \frac{1}{137}$$

k

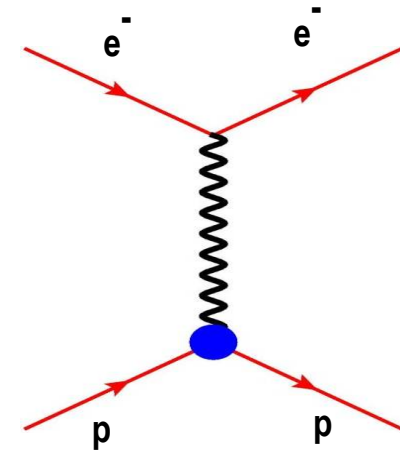


The Proton Charge Radius

- In the limit of first Born approximation the elastic ep scattering (one photon exchange):

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left(\frac{E'}{E} \right) \frac{1}{1+\tau} \left(G_E^p{}^2(Q^2) + \frac{\tau}{\varepsilon} G_M^p{}^2(Q^2) \right)$$

$$Q^2 = 4EE' \sin^2 \frac{\theta}{2} \quad \tau = \frac{Q^2}{4M_p^2} \quad \varepsilon = \left[1 + 2(1+\tau) \tan^2 \frac{\theta}{2} \right]^{-1}$$



- Structure less "proton":

$$\left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} = \frac{\alpha^2 [1 - \beta^2 \sin^2 \frac{\theta}{2}]}{4k^2 \sin^4 \frac{\theta}{2}}$$

- At very low Q^2 , cross section dominated by G_E^p : →

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left(\frac{E'}{E} \right) \frac{1}{1+\tau} G_E^p{}^2(Q^2)$$

$$G_E^p(Q^2) = 1 - \frac{Q^2}{6} \langle r^2 \rangle + \frac{Q^4}{120} \langle r^4 \rangle + \dots$$

- r.m.s. charge radius given by the slope:

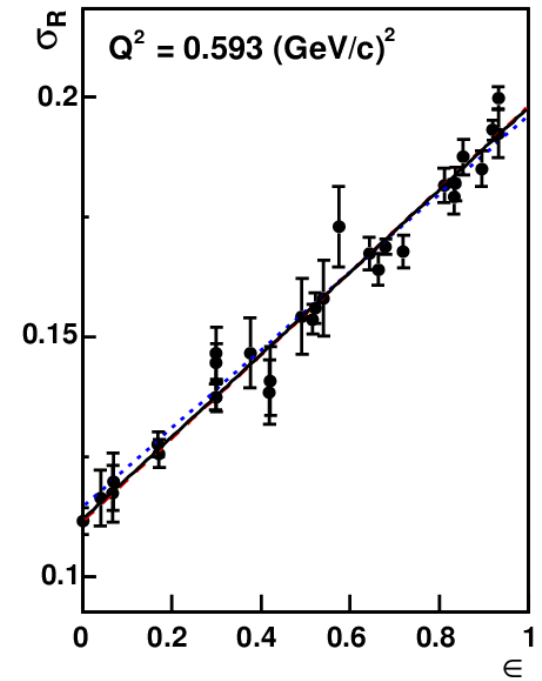
$$\langle r^2 \rangle = -6 \left. \frac{dG_E^p(Q^2)}{dQ^2} \right|_{Q^2=0}$$

Size of the proton: unpolarized electron-nucleon scattering (Rosenbluth Separation)

- Elastic e-p cross section

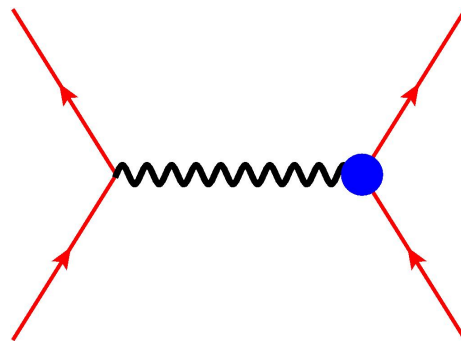
$$\begin{aligned}\frac{d\sigma}{d\Omega} &= \frac{\alpha^2 \cos^2 \frac{\theta}{2}}{4E^2 \sin^4 \frac{\theta}{2}} \frac{E'}{E} \left(\frac{G_E^p{}^2 + \tau G_M^p{}^2}{1 + \tau} + 2\tau G_M^p{}^2 \tan^2 \frac{\theta}{2} \right) \\ &= \sigma_M f_{rec}^{-1} \left(A + B \tan^2 \frac{\theta}{2} \right)\end{aligned}$$

- At fixed Q^2 , fit $d\sigma/d\Omega$ vs. $\tan^2(\theta/2)$
 - Measurement of absolute cross section
 - Dominated by either G_E or G_M
 - Low Q^2 by G_E
 - High Q^2 by G_M



$$\sigma_R = \tau G_M^2 + \epsilon G_E^2$$

$$\begin{aligned}\tau &= \frac{Q^2}{4M^2} \\ \epsilon &= (1 + 2(1 + \tau) \tan^2 \frac{\theta}{2})^{-1}\end{aligned}$$

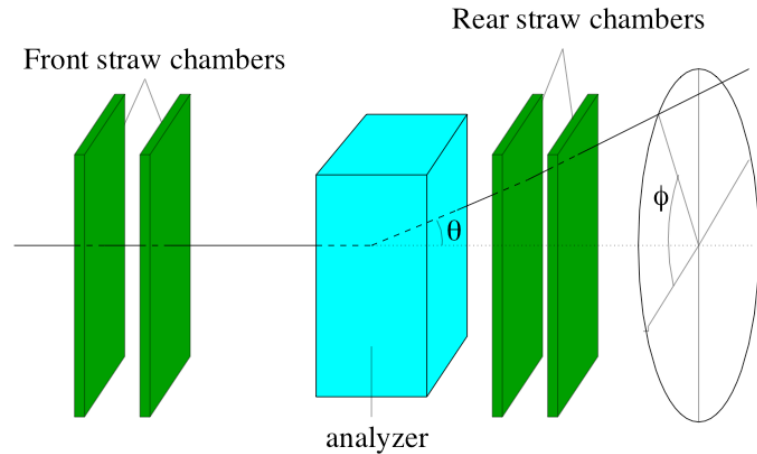


Electron-proton elastic scattering with longitudinally polarized electron beam and recoil proton polarization

Polarization Transfer



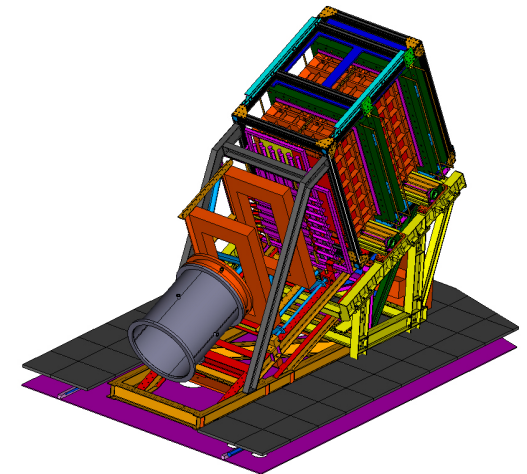
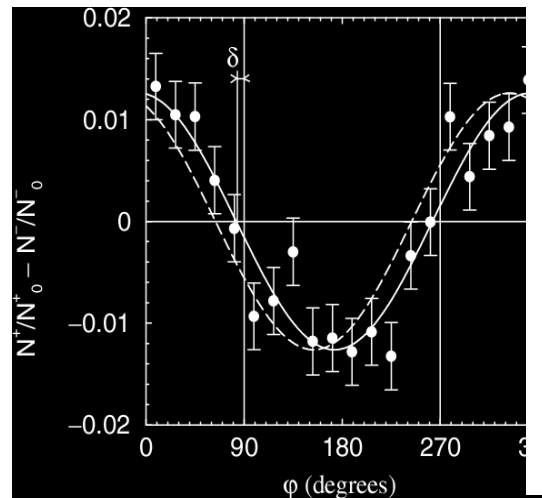
$$\frac{G_E^p}{G_M^p}$$



- Recoil proton polarization

$$\frac{G_E^p}{G_M^p} = -\frac{P_t}{P_l} \frac{E + E'}{2M} \tan \frac{\theta}{2}$$

- Focal Plane Polarimeter
 - recoil proton scatters off secondary carbon target
 - P_t , P_l measured from φ distribution
 - P_b , and analyzing power cancel out in ratio



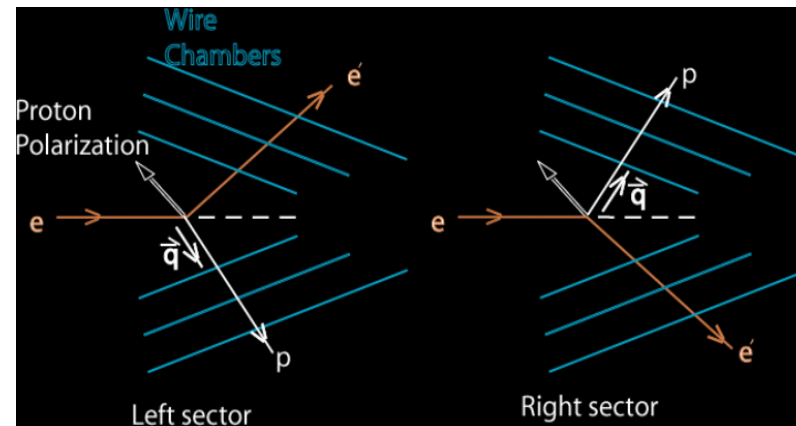
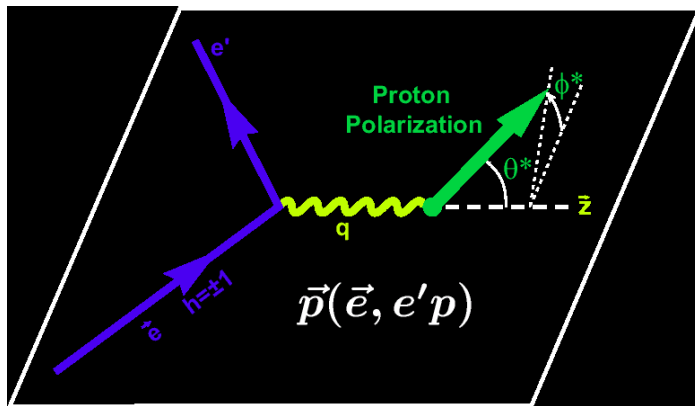
Focal-plane polarimeter

Asymmetry Super-ratio Method

Polarized electron-polarized proton elastic scattering

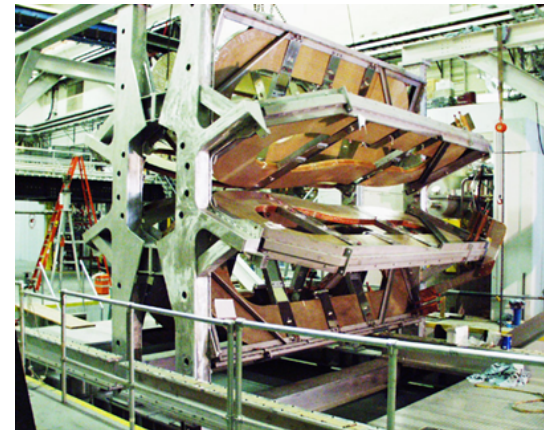
- Polarized beam-target asymmetry

$$A_{exp} = P_b P_t \frac{-2\tau v_{T'} \cos \theta^* G_M^p{}^2 + 2\sqrt{2\tau(1+\tau)} v_{TL'} \sin \theta^* \cos \phi^* G_M^p G_E^p}{(1+\tau) v_L G_E^p{}^2 + 2\tau v_T G_M^p{}^2}$$

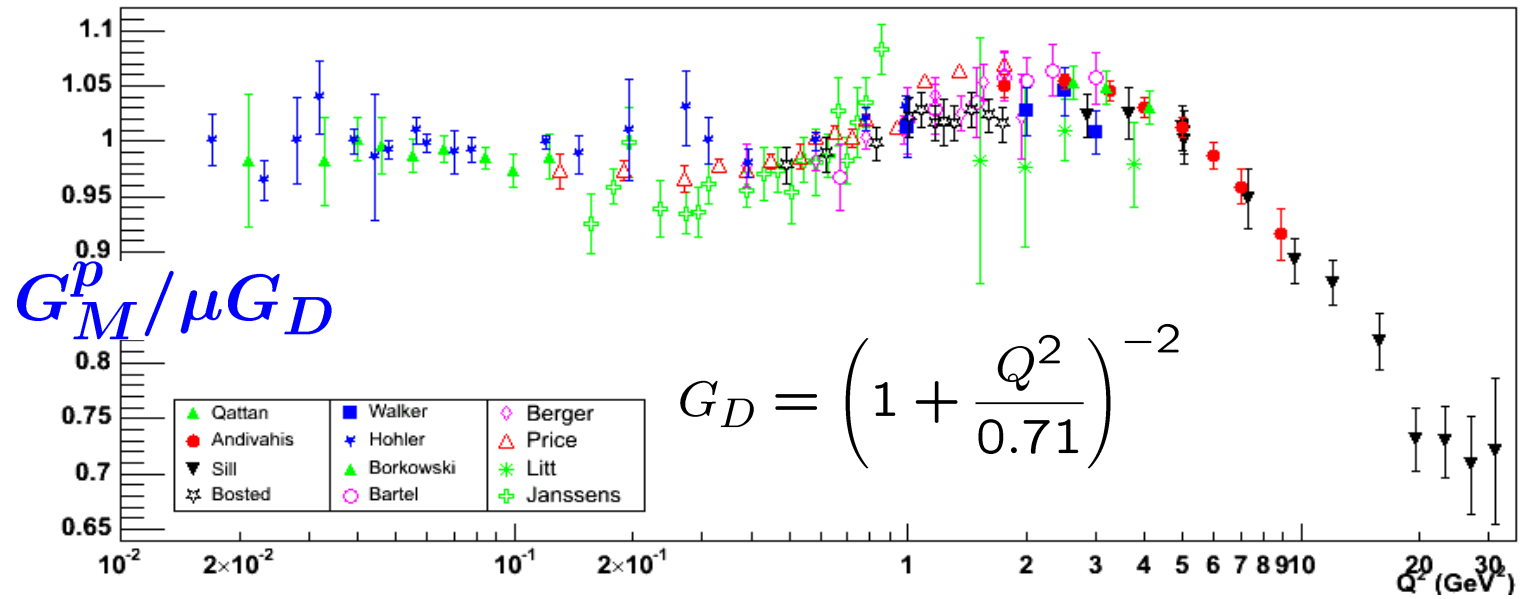
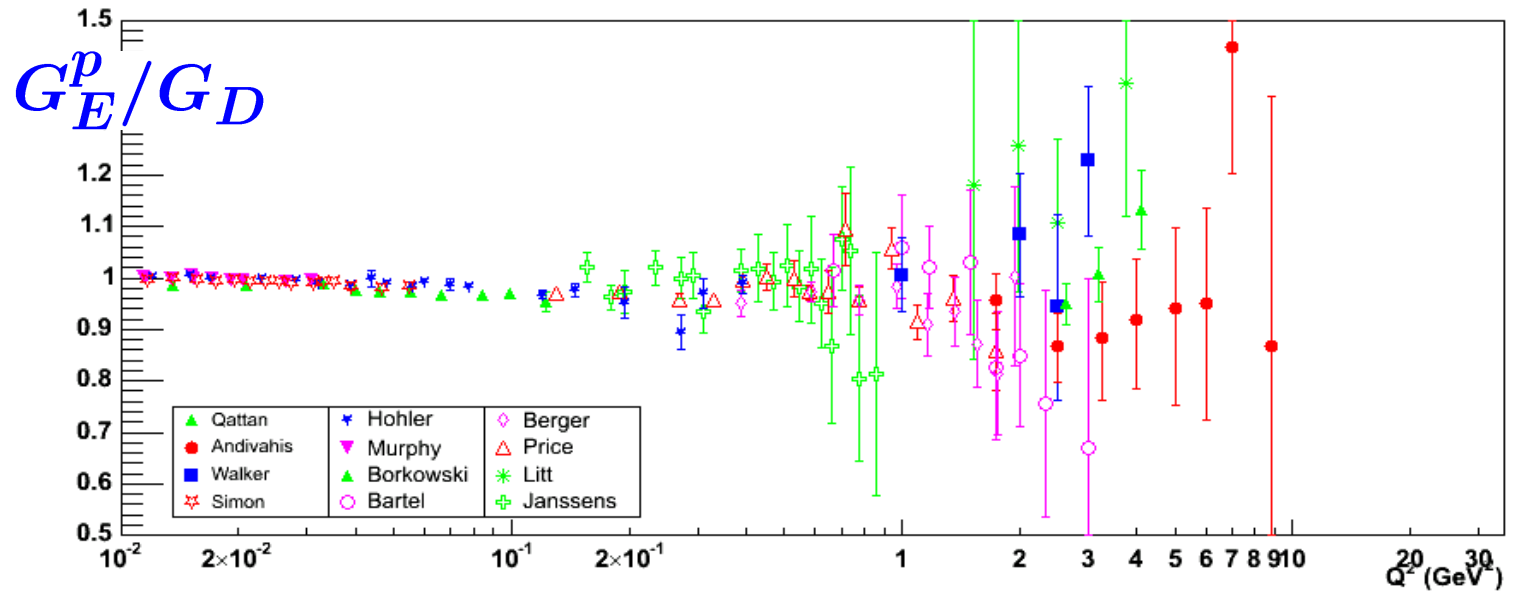


$$R_A = \frac{A_1}{A_2} = \frac{a_1 - b_1 \cdot G_E^p / G_M^p}{a_2 - b_2 \cdot G_E^p / G_M^p}$$

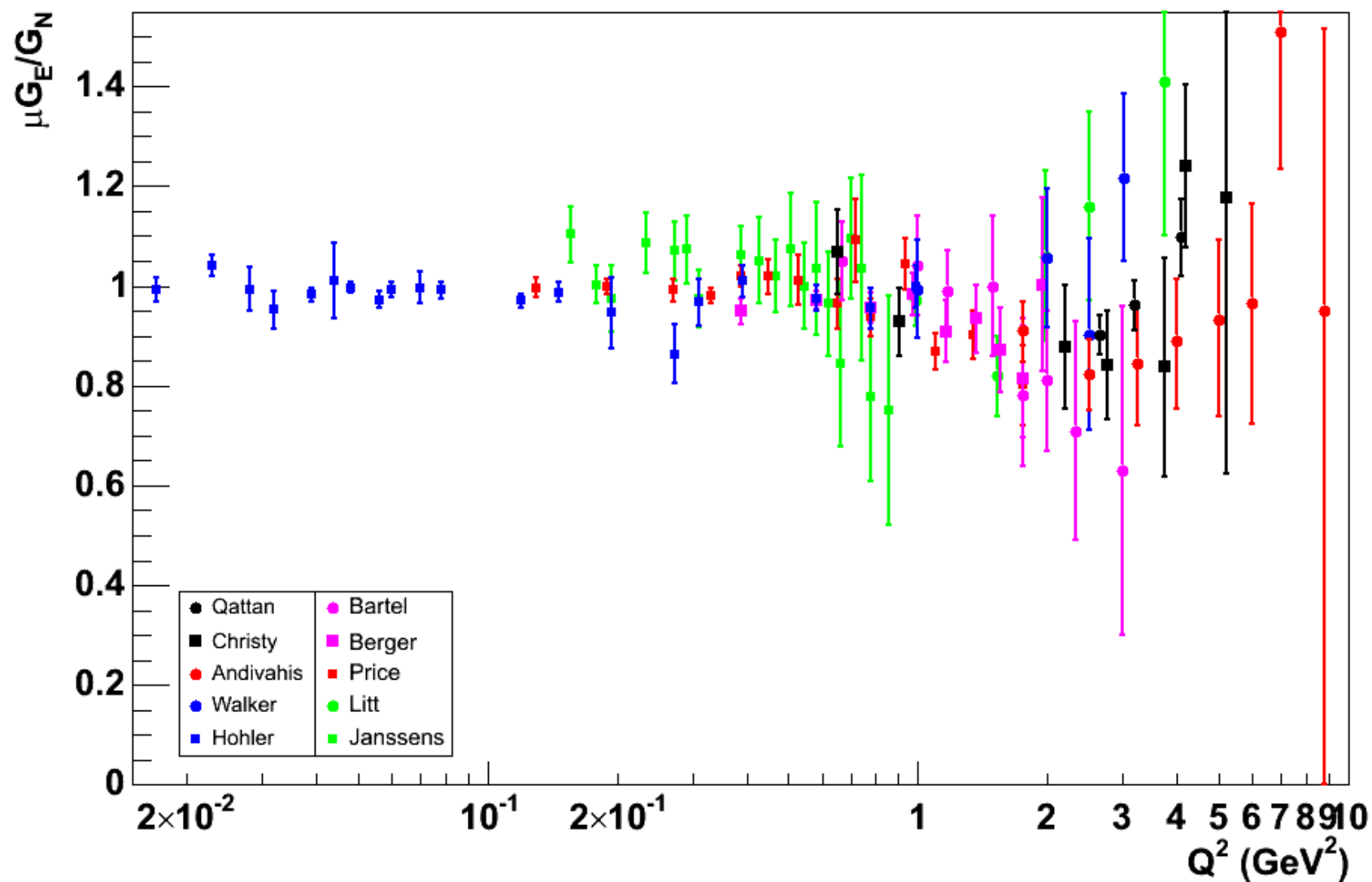
BLAST pioneered the technique, will be used in upcoming Jlab Hall A experiment



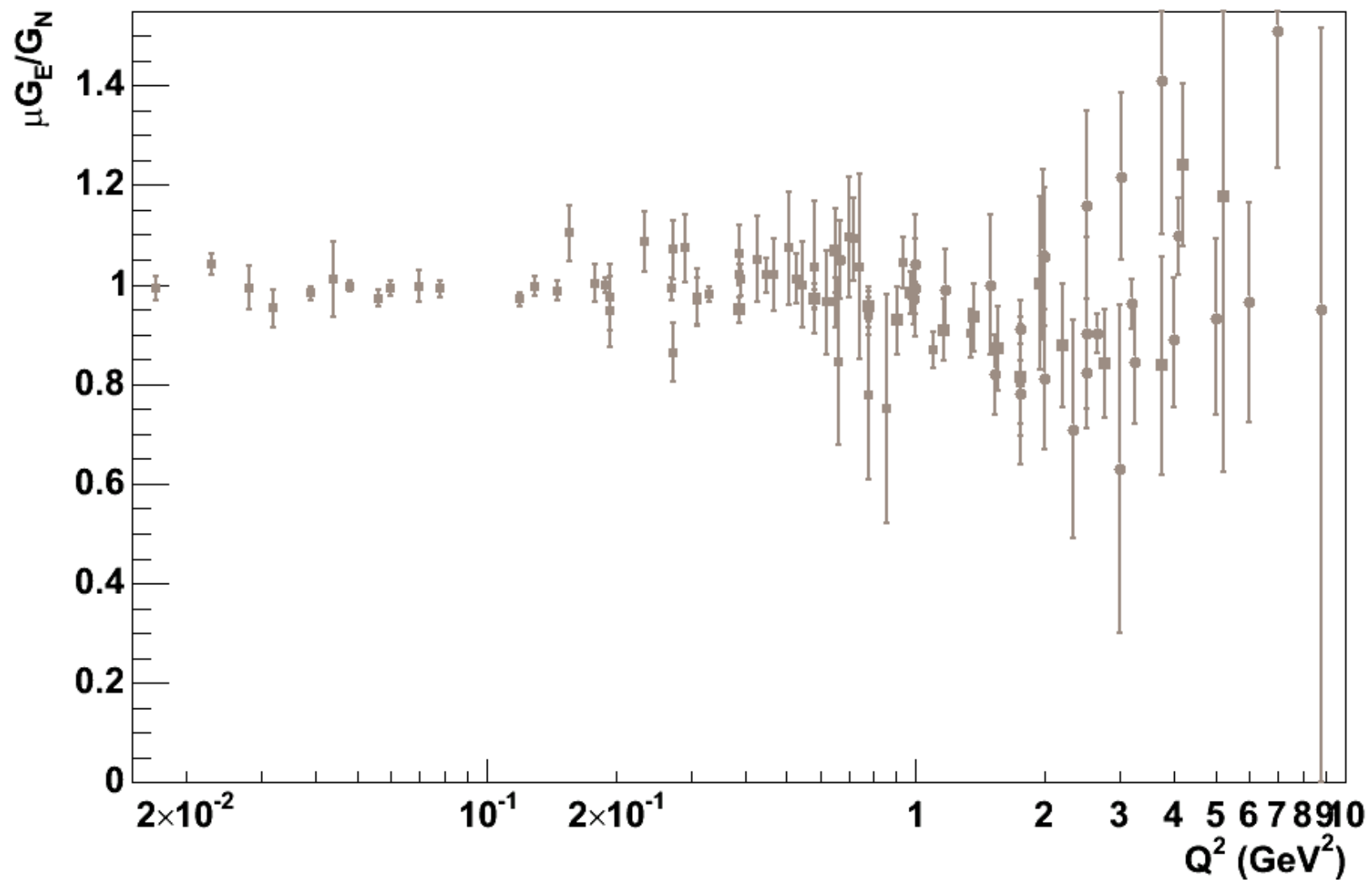
World Unpolarized Data



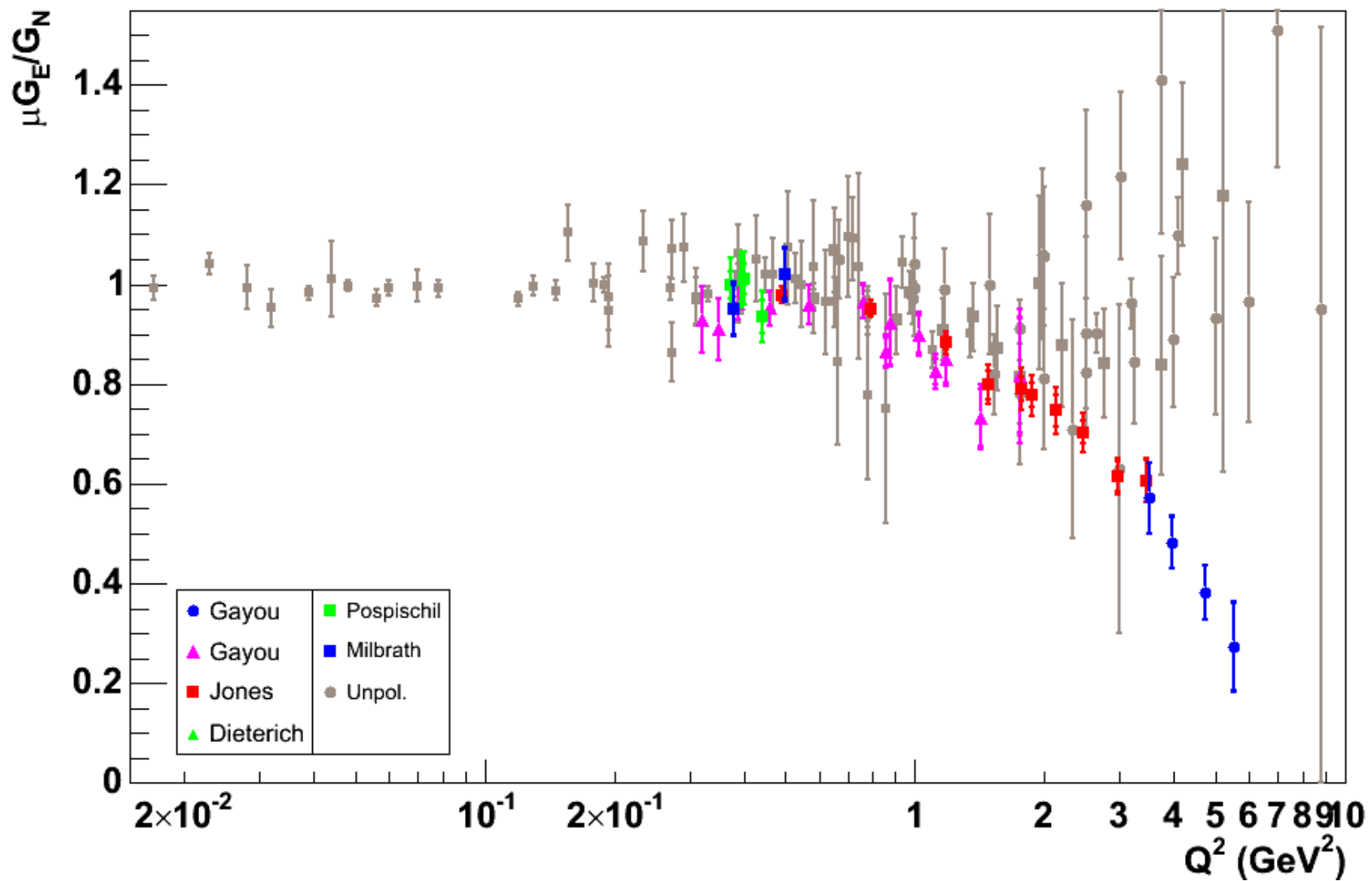
$\mu G_E/G_M$ — World Data



$\mu G_E/G_M$ — World Data



$\mu G_E/G_M$ — World Data



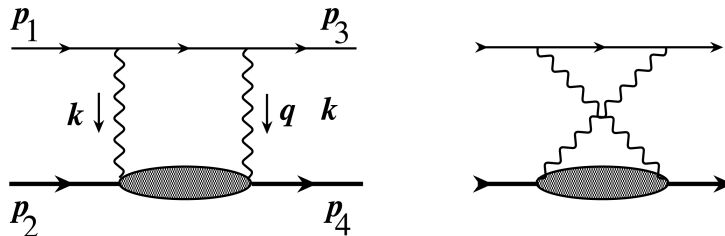
Two - Photon Exchange (TPE)

- Proton form factor measurements

- Comparison of precise Rosenbluth and Polarization measurements of G_E^p/G_M^p show **clear discrepancy** at high Q^2

P.A.M. Guichon and M. Vanderhaeghen, PRL 91, 142303 (2003)

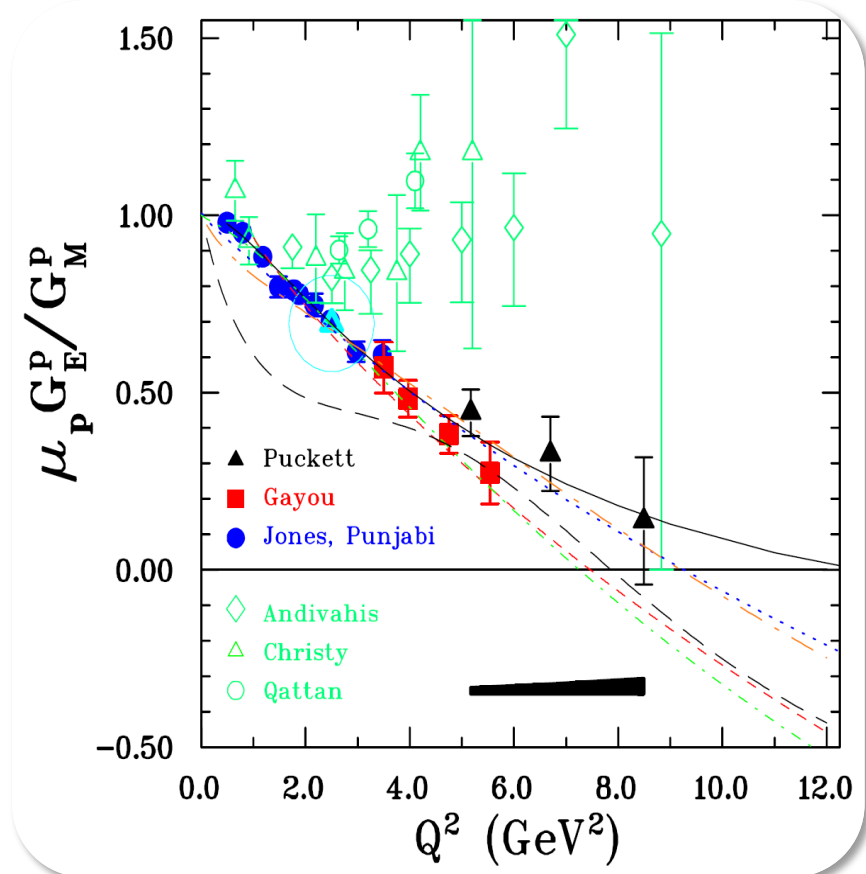
- Two-photon exchange** corrections believed to explain (part of) the discrepancy



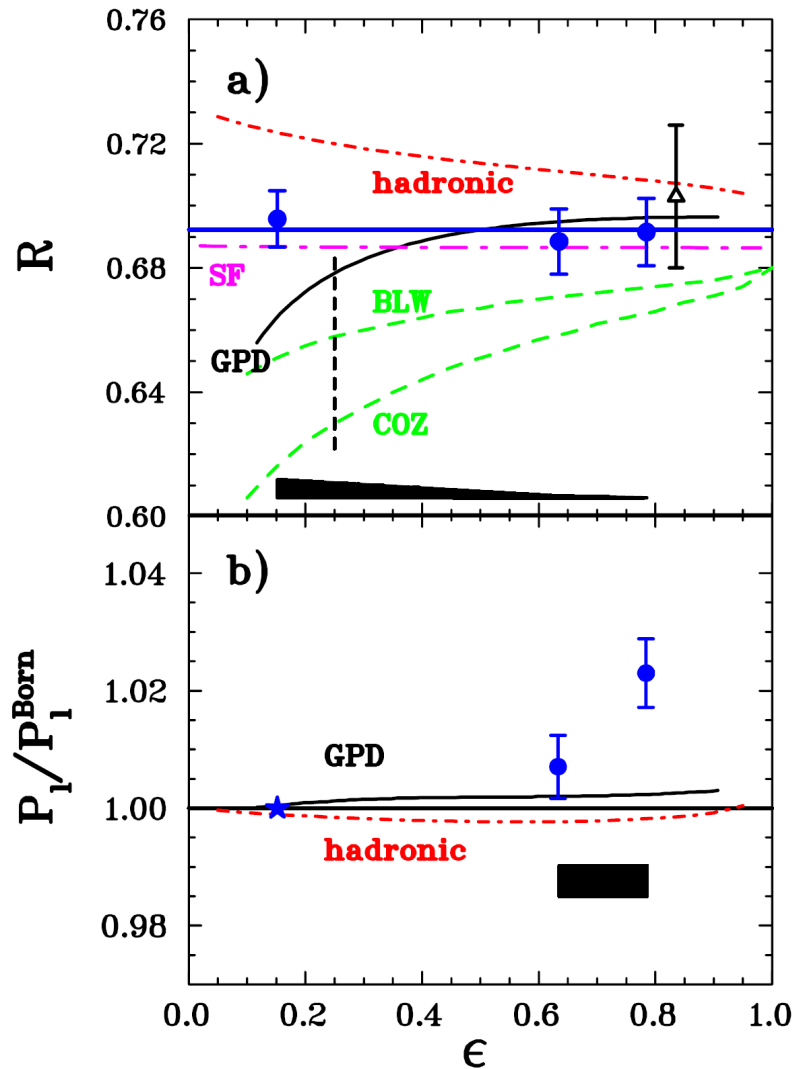
■ Have only limited direct evidence of effect on cross section

— Active experimental, theoretical program to fully understand TPE effects

Blunden et al (05); Afanasev et al (05);
Arrington et al (07);
Carlson and Vanderhaeghen (07) ,.....



Two-Photon Exchange

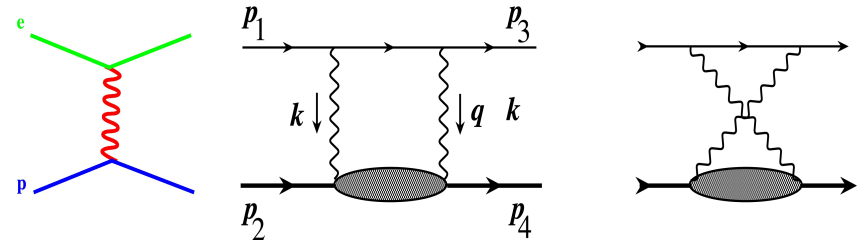


$$R = \mu_p G_E / G_M, Q^2 = 2.5 \text{ GeV}^2$$

ϵ , virtual photon polarization

15
M. Mehdi *et al*, PRL 106, 132501 (2011)

Golden mode: positron-proton vs. electron-proton elastic scattering



$$\frac{\sigma_{e^+}}{\sigma_{e^-}} = \frac{(A_{1\gamma} + A_{2\gamma})^2}{(A_{1\gamma} - A_{2\gamma})^2} \approx 1 + 4 \text{Re} A_{2\gamma} A_{1\gamma}$$

Three new e^+/e^- experiments:

- BINP Novosibirsk – internal target
- JLab Hall B – LH2 target, CLAS (2012)
- DESY (OLYMPUS) - internal target

OLYMPUS Projected Results

Former BLAST experiment

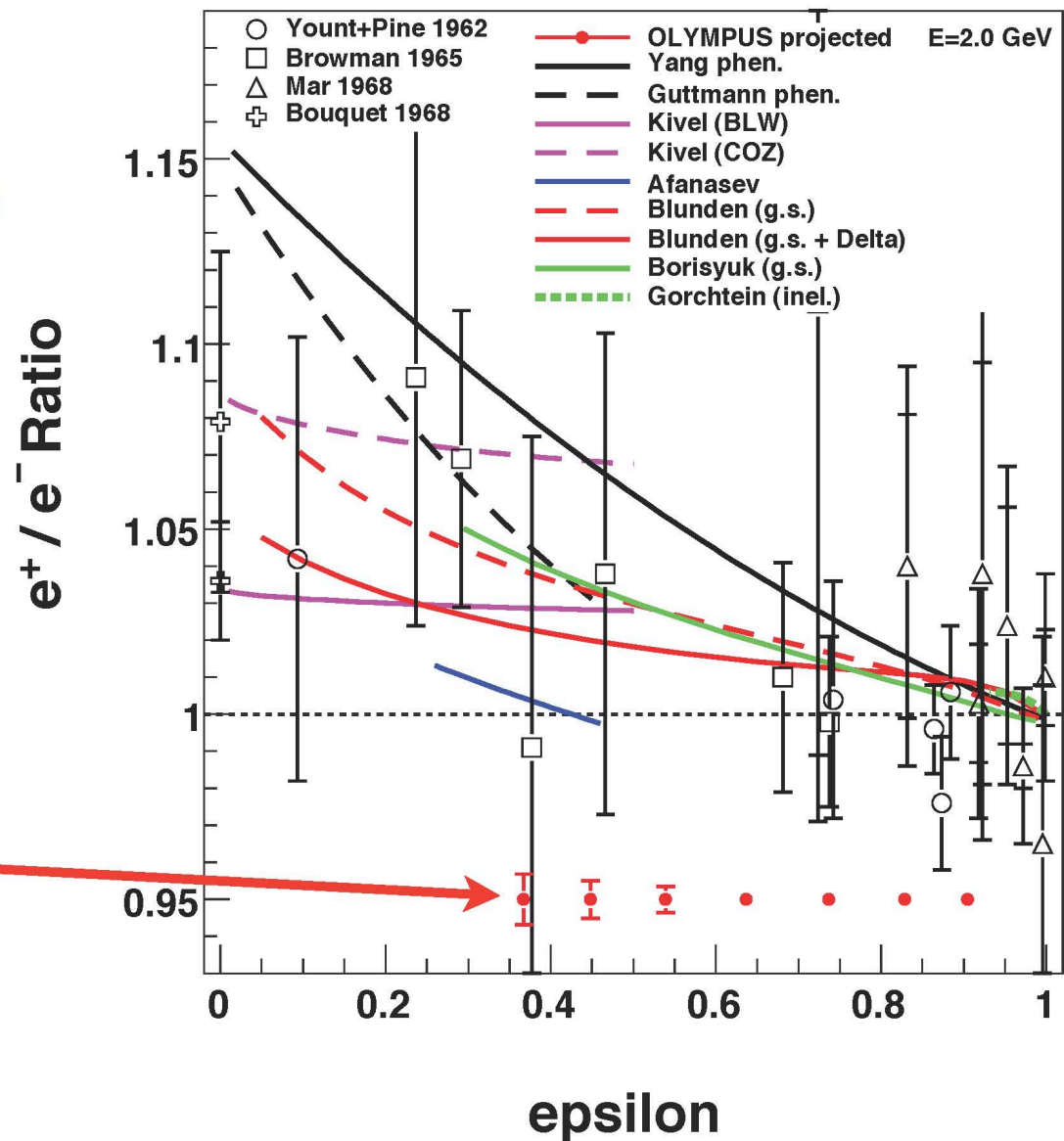
- windowless, internal gas target of pure hydrogen
- large acceptance
- left / right symmetric
- reversible magnetic field
- 1% luminosity measure

DORIS storage ring

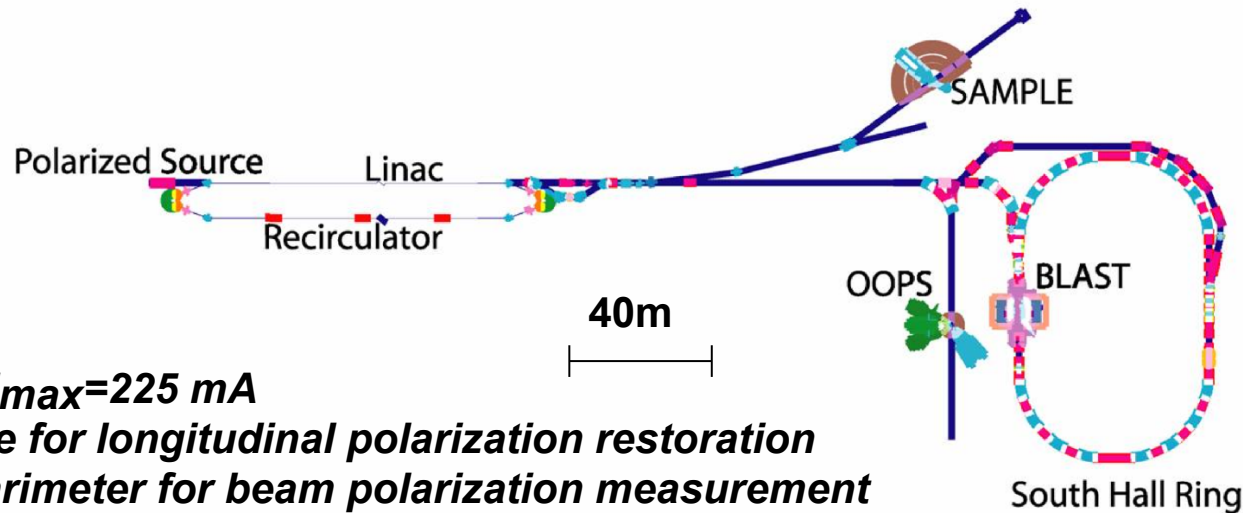
- switch e^- / e^+ frequently
- 2 GeV beam energy

Expected precision

- $2 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$
- 500 hours with e^+ and e^-



The *BLAST* Experiment



$E_0 = 850 \text{ MeV}$ $I_{\text{max}} = 225 \text{ mA}$

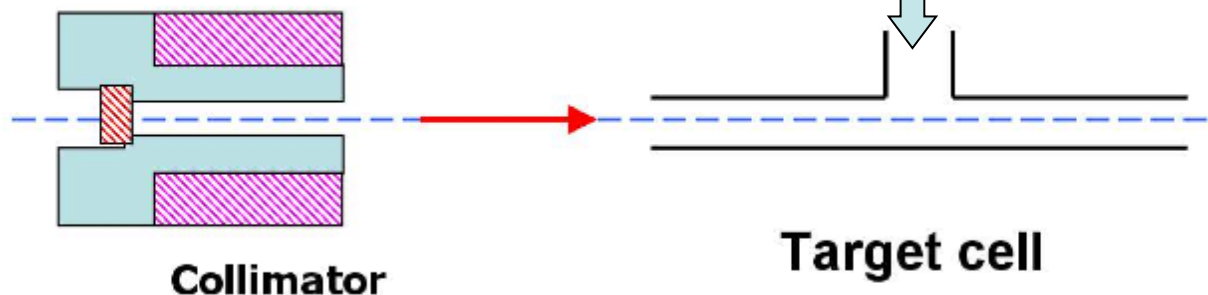
Siberian snake for longitudinal polarization restoration

Compton polarimeter for beam polarization measurement

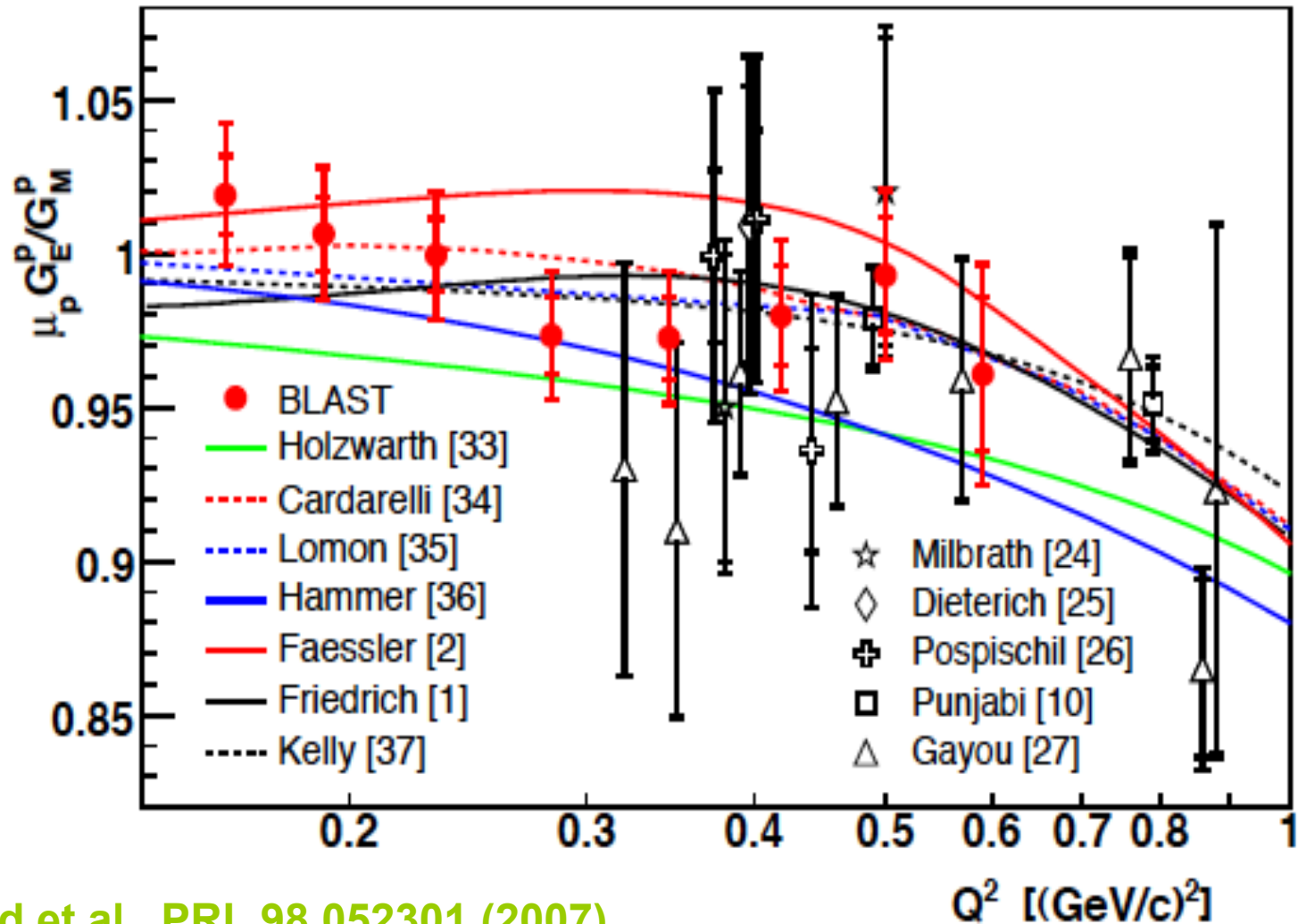
- **BLAST: internal target physics program**

- **Nucleon electromagnetic structure** This talk
- Spin structure of few nucleon system,

- Thin, pure, highly polarized species, low magnetic field, open-ended thin cell



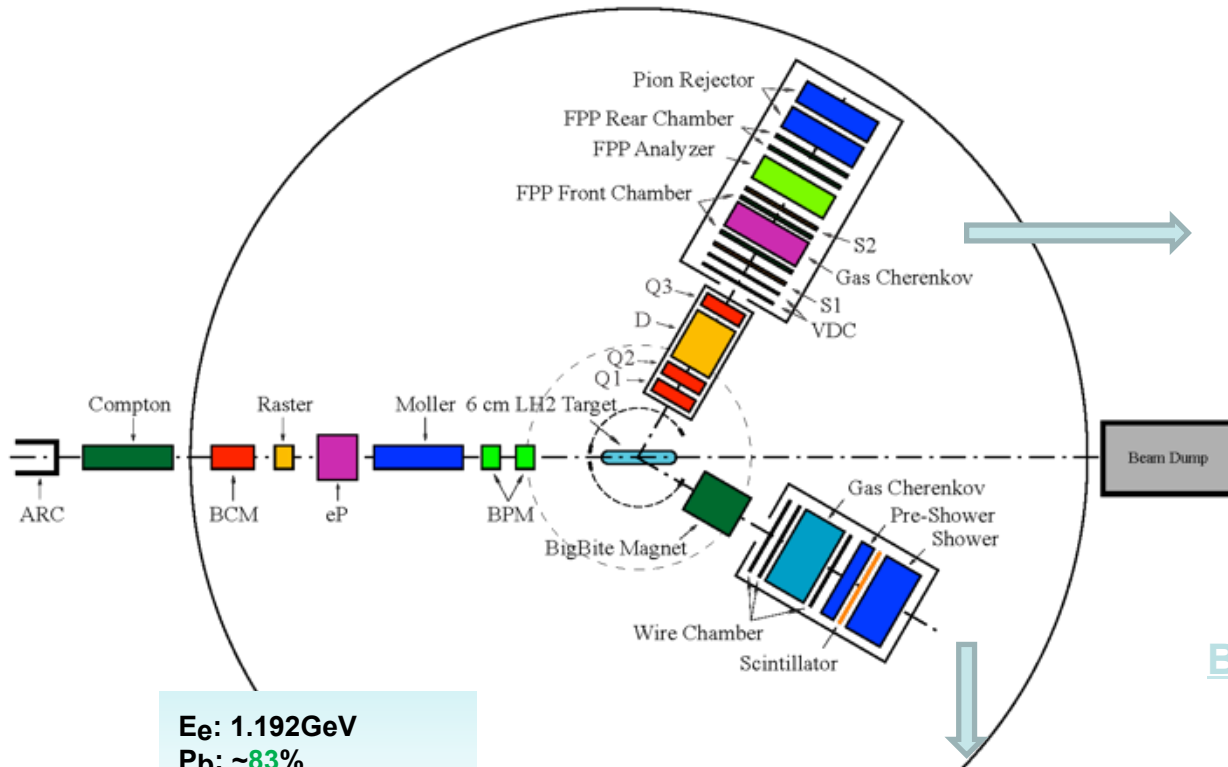
Results – G_E^p / G_M^p



C. Crawford et al., PRL 98 052301 (2007)

Experimental Setup

LHRS



$E_e: 1.192\text{GeV}$
 $P_b: \sim 83\%$

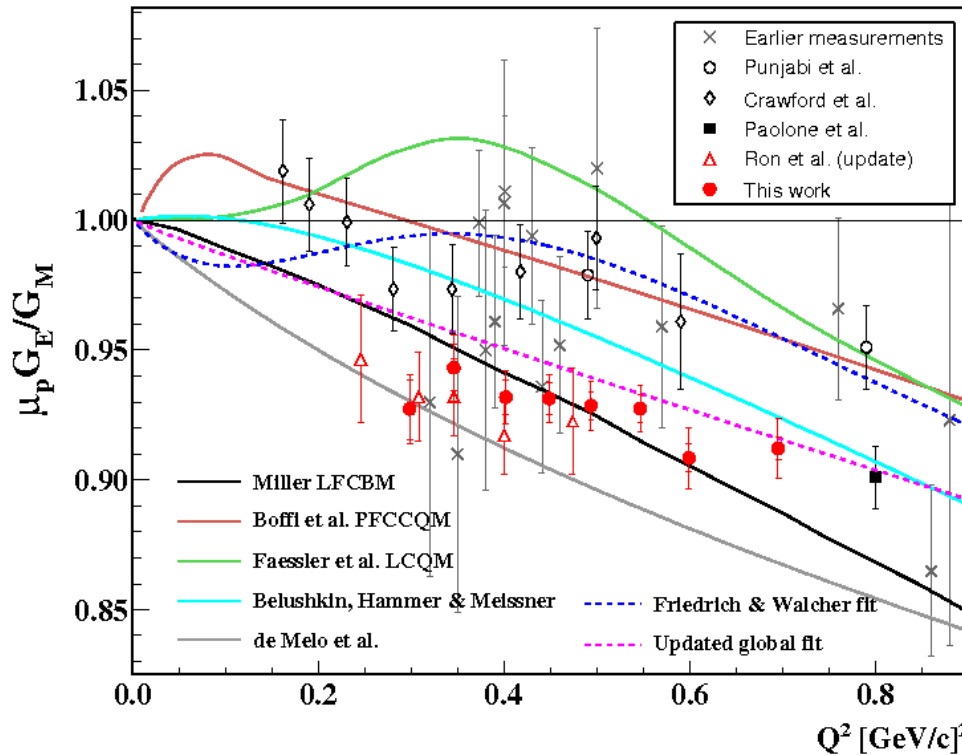
- $\Delta p/p_0: \pm 4.5\%$,
- out-of-plane: ± 60 mrad
- in-plane: ± 30 mrad
- $\Delta\Omega: 6.7\text{msr}$
- QQDQ
- Dipole bending angle 45°
- **VDC+FPP**
- $P_p: 0.55 \sim 0.93 \text{ GeV/c}$

BigBite

- Non-focusing Dipole
- Big acceptance.
 - $\Delta p: 200\text{-}900\text{MeV}$
 - $\Delta\Omega: 96\text{msr}$
- PS + Scint. + **SH**



Electromagnetic form factor of nucleons at low Q^2

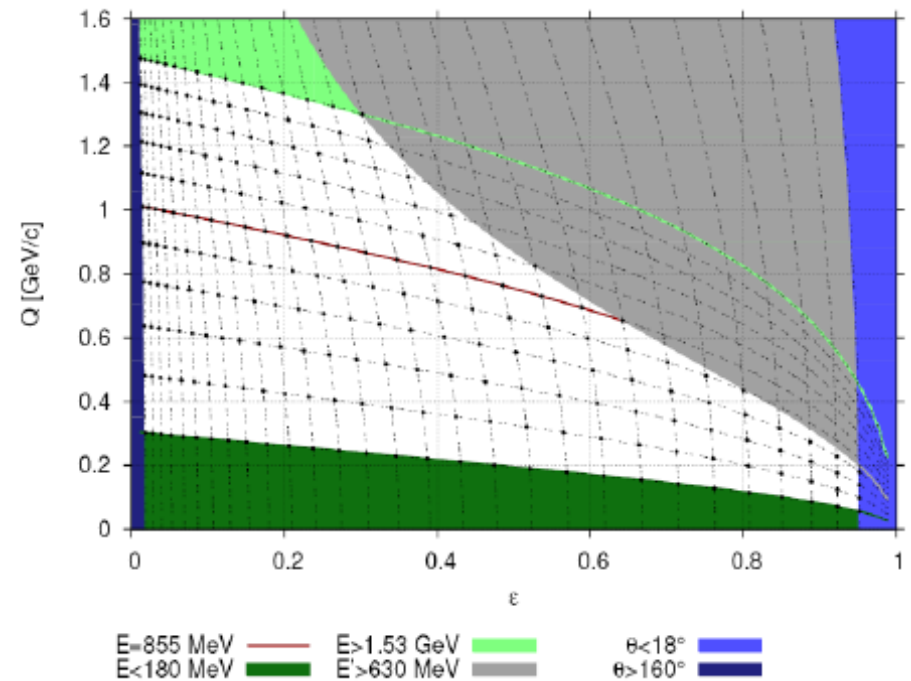


In the limit of Q^2 goes to zero, the slope of the electric form factor determines the charge radius of the nucleon

Crucial for proton charge radius

$$r_p \propto \frac{d}{dQ^2} G_E(Q^2) \Big|_{Q^2=0}$$

X. Zhan et al. (recoil polarization)
arXiv:1102.0318)
C. Crawford et al. (pol. Target)
PRL98, 052301 (2007)



high precision unpolarized XS measurement at Mainz

($Q^2 \sim 0.004 - 1 \text{ GeV}^2$)

J.C. Bernauer et al. PRL105, 242001 (2010)

Charge radius from atomic physics

$$\langle p(p_f) | \sum_q e_q \bar{q} \gamma^\mu q | p(p_i) \rangle = \bar{u}(p_f) \left[\gamma_\mu F_1^p(q^2) + \frac{i\sigma_{\mu\nu}}{2m} F_2^p(q^2) q_\nu \right] u(p_i)$$

- For a point particle amplitude for $p + \ell \rightarrow p + \ell$

$$\mathcal{M} \propto \frac{1}{q^2} \Rightarrow U(r) = -\frac{Z\alpha}{r}$$

- Including q^2 corrections from proton structure

$$\mathcal{M} \propto \frac{1}{q^2} q^2 = 1 \Rightarrow U(r) = \frac{4\pi Z\alpha}{6} \delta^3(r) (r_E^p)^2$$

- Proton structure corrections $\left(m_r = m_\ell m_p / (m_\ell + m_p) \approx m_\ell \right)$

$$\Delta E_{r_E^p} = \frac{2(Z\alpha)^4}{3n^3} m_r^3 (r_E^p)^2 \delta_{\ell 0}$$

- **Muonic hydrogen can give the best measurement of r_E^p !**

Motivation for precise information on proton radius

- A fundamental static property of the nucleon
 - Important for understanding how QCD works
- An important physics input to the bound state QED calculations, affects muonic H Lamb shift ($2S_{1/2} - 2P_{1/2}$) by as much as 2%
- Lamb Shift ($2S_{1/2} - 2P_{1/2}$) measurements are becoming more and more precise
- High precision tests of QED?
- Turning things around one can determine proton radius using QED and Lamb shift measurements

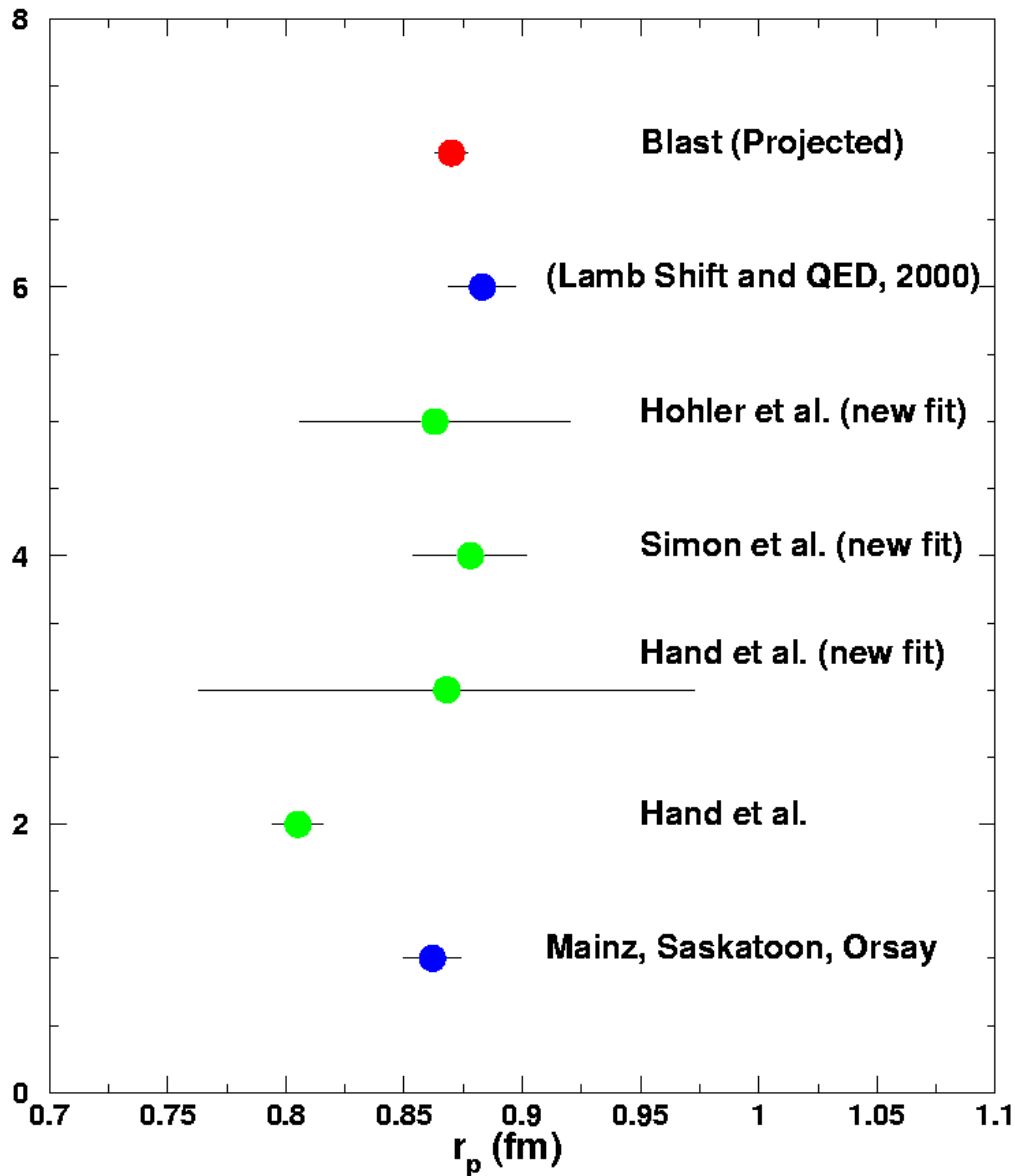
Methods for measuring proton charge radius

- Electron-proton elastic scattering to determine electric form factor

$$r_{rms} = \sqrt{\langle r^2 \rangle} = -6 \frac{\partial G_E(Q^2)}{\partial(Q^2)} \Big|_{Q^2=0}$$

- Hydrogen spectroscopy (CODATA) (Lamb shift)
- Muonic Hydrogen (spectroscopy) (Lamb shift)

Personal story of proton charge radius before 2000



- *Motivated by discrepancy between Hand et al and Mainz, Saskatoon, Orsay results*
- *Discrepancy is a problem for H Lamb shift experiments*
- *Proposed a new experiment using BLAST and laser-driven polarized hydrogen target with sub percent precision*
- *Experiment did not happen – beam turned off*
- *No problem, PSI muonic hydrogen Lamb experiment will resolve everything*

Find out what happened ten years later soon

Muonic Hydrogen

- The **muon** is about 200 times heavier than the electron.
- Therefore, the atomic Bohr radius of muonic hydrogen is smaller than in ordinary hydrogen.
- This increases sensitivity of muonic hydrogen Lamb shift to the **finite size** of the proton.

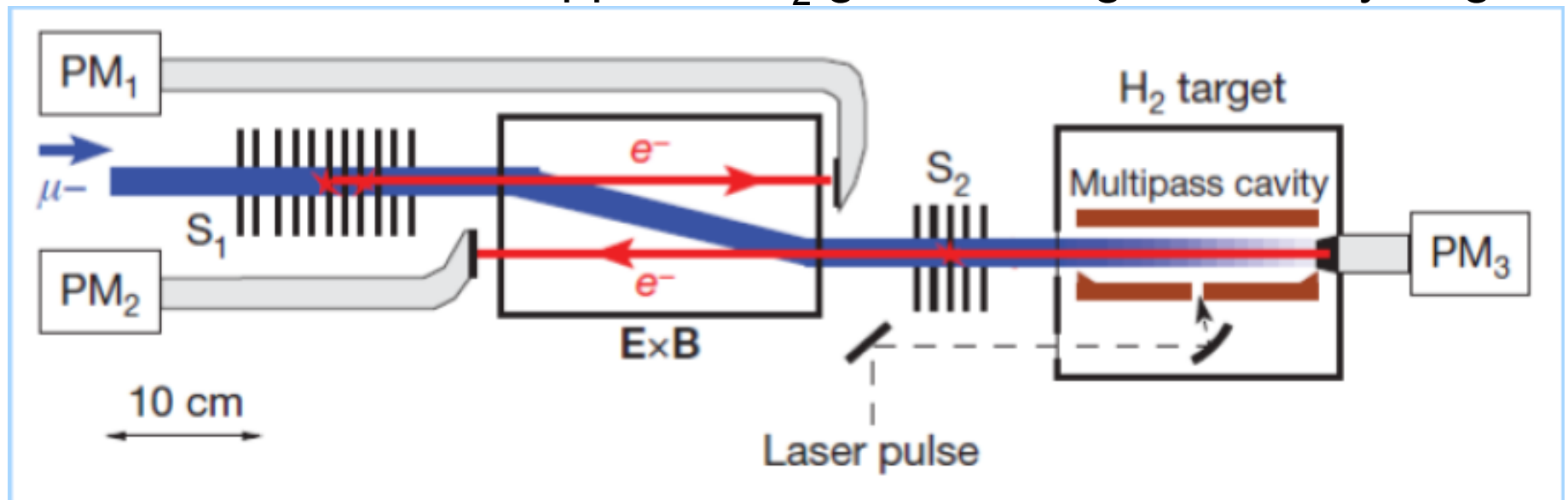
PSI Experiment

- Generation of muonic hydrogen
- X-ray time spectra
- Results
- Theoretical calculation

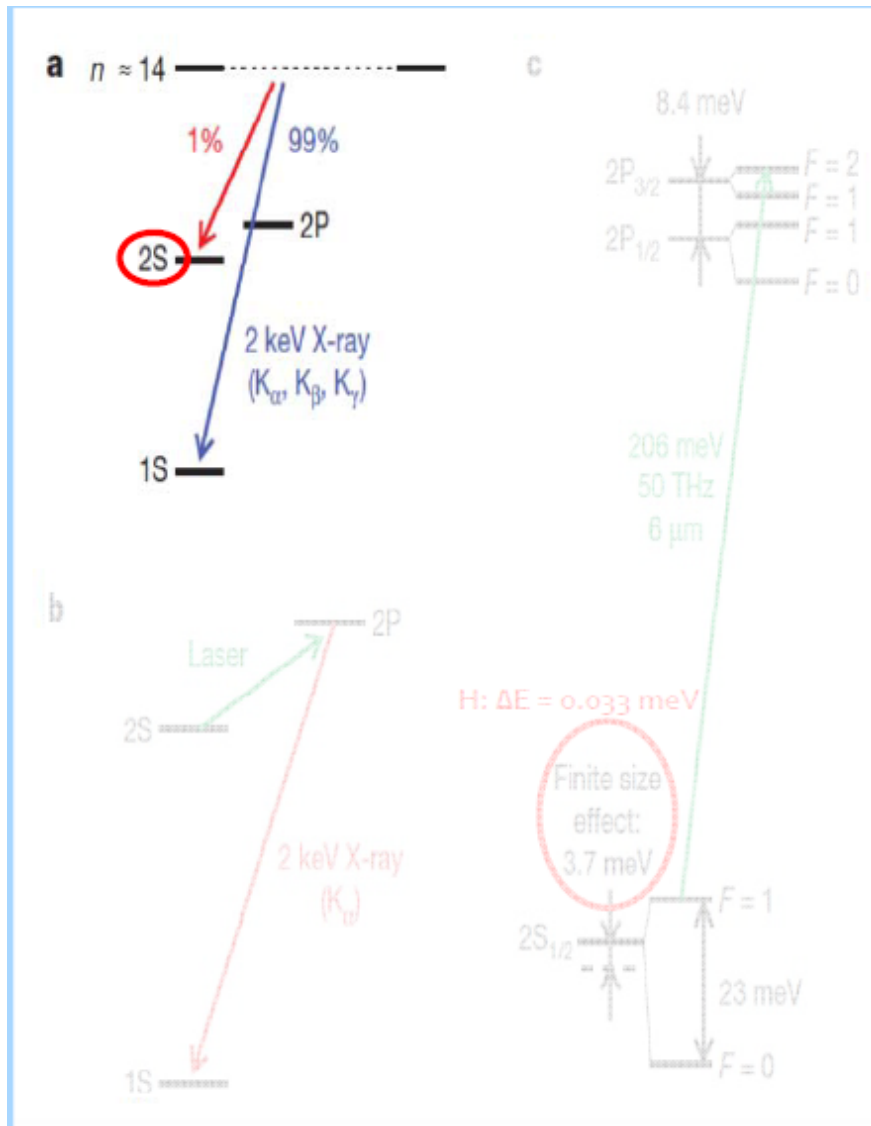
slides from Rebcca Boll

Generation of muonic hydrogen

- Slow **muons** pass two stacks of ultra-thin carbon foils (S_1 , S_2)
- The secondary electrons are detected in scintillators and read out by photomultipliers, acting as a trigger for the laser
- The muons are stopped in H_2 gas, forming muonic hydrogen

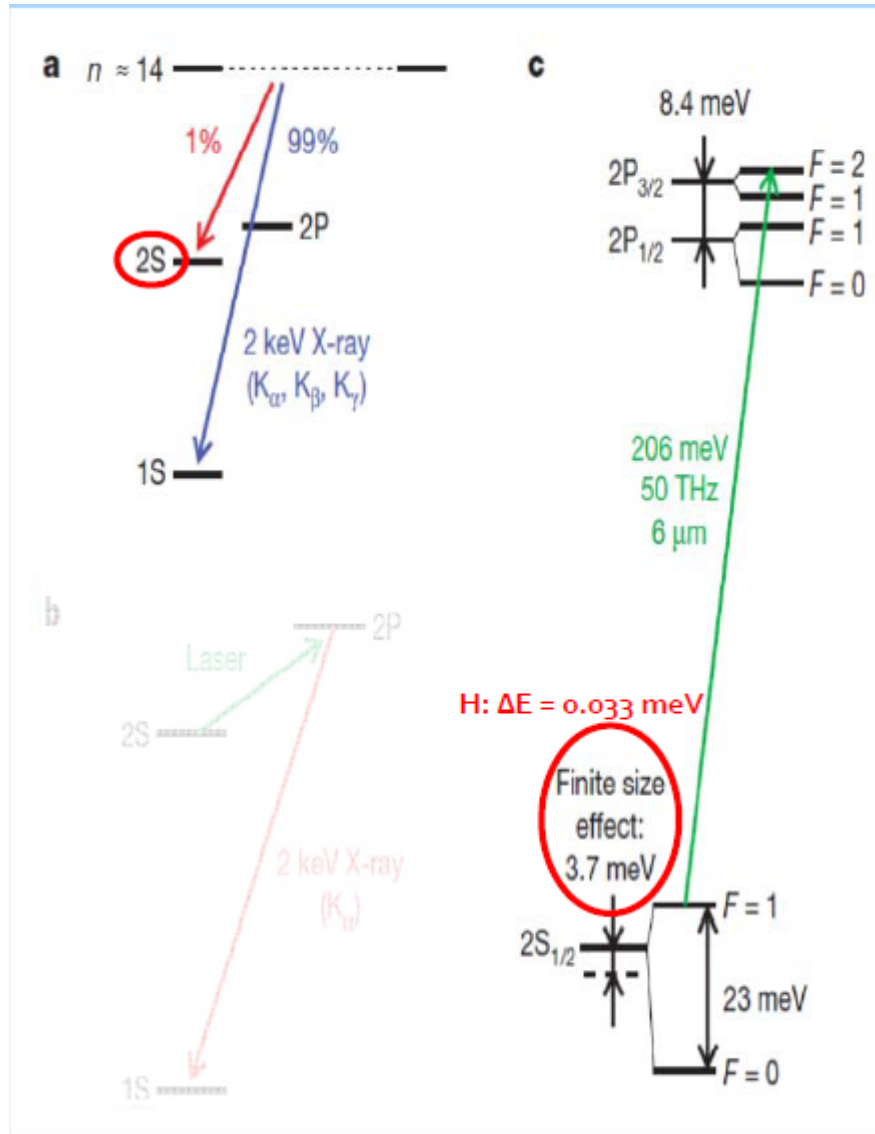


Energy levels and transitions



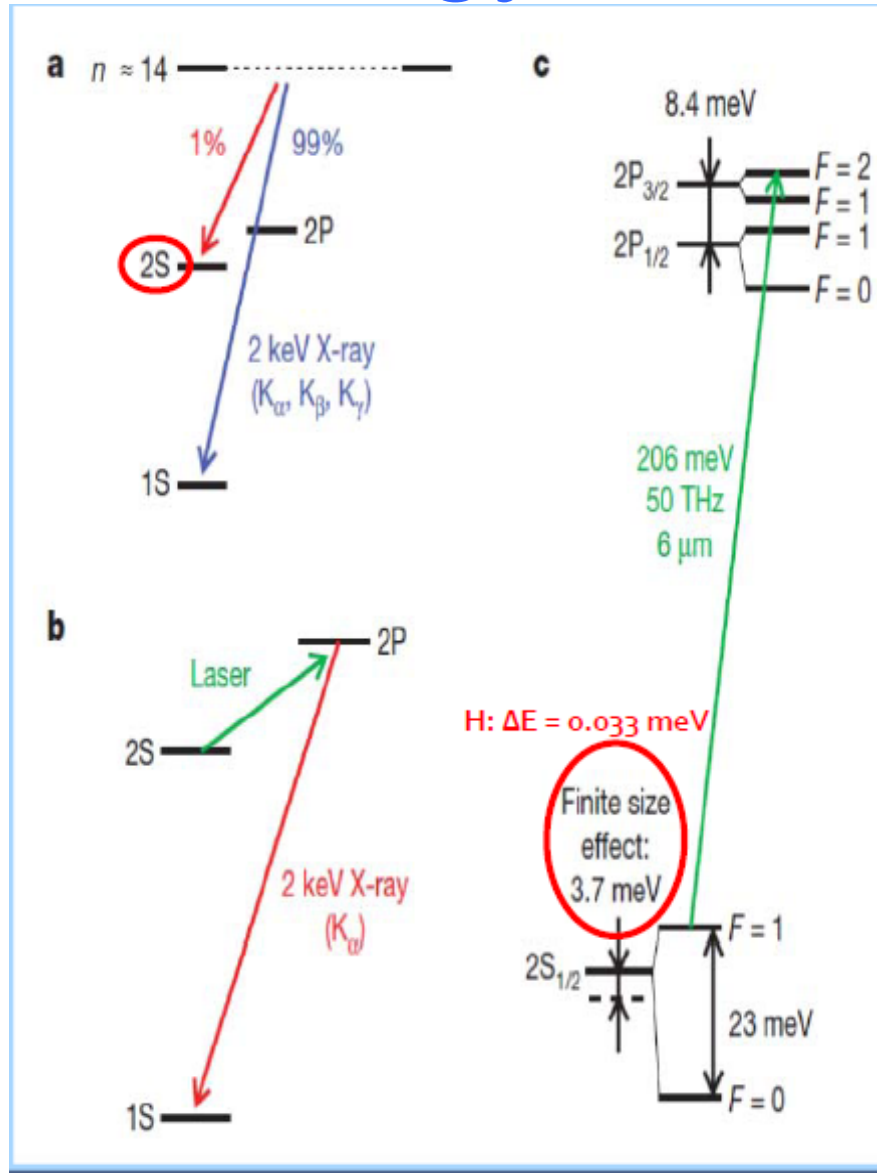
- The muonic hydrogen is **highly excited** when generated ($n \approx 14$)
- Most of the atoms de-excite quickly to $1S$, but about 1% reach the **long-lived 2S-state** (lifetime about $1\mu\text{s}$)

Energy levels and transitions



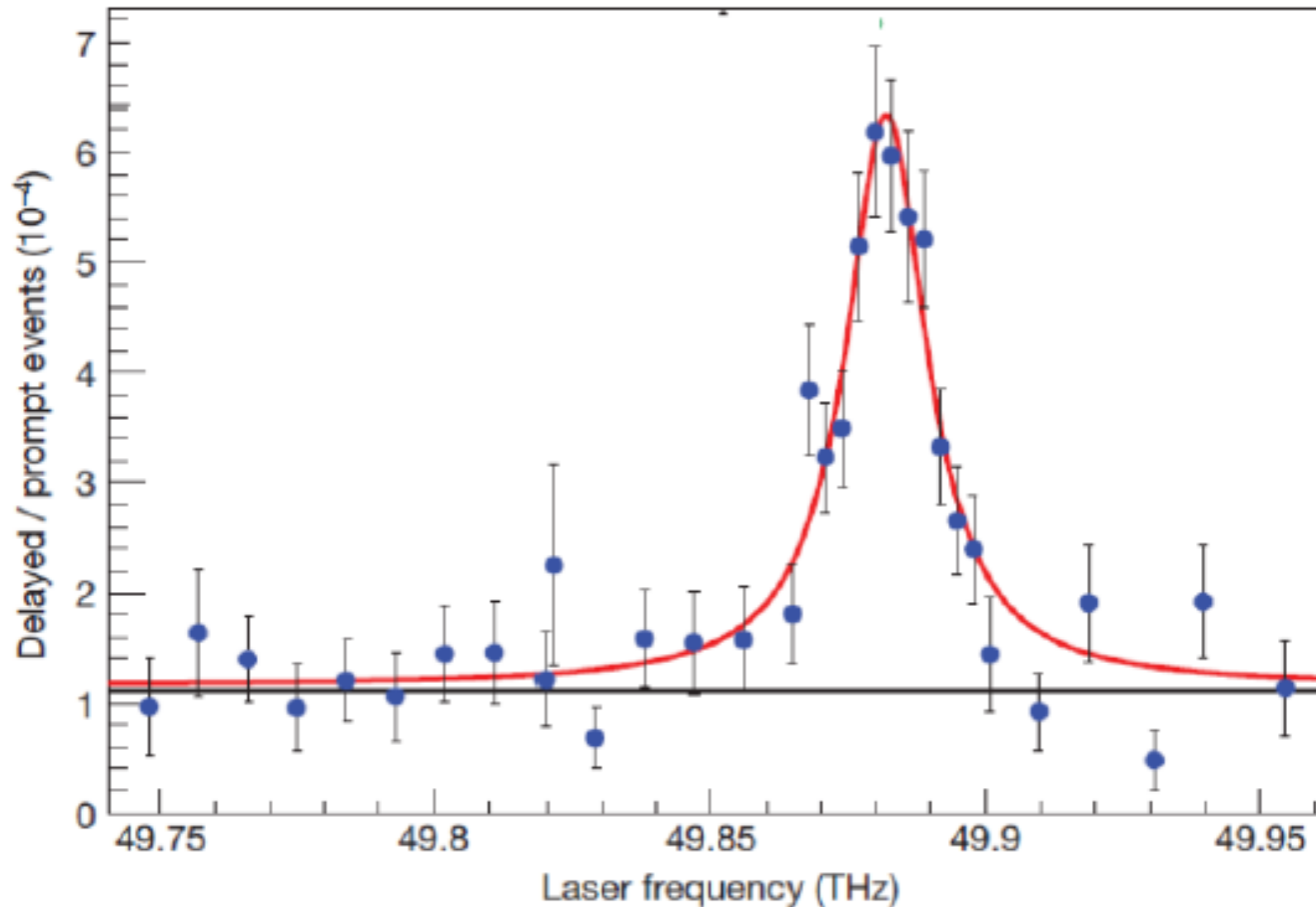
- For the $2S_{1/2} - 2P_{3/2}$ transition, **finite size effects** are two orders of magnitude higher than for ordinary H
- A **pulsed laser beam** ($\lambda = 6\mu\text{m}$) induces the excitation from $2S_{1/2}$ to $2P_{3/2}$ (gives the largest signal of all possible optical transitions)

Energy levels and transitions



- This is then followed by a de-excitation from $2P_{3/2}$ to $1S_{1/2}$ via **emission of an X-ray**

X-ray timing and $2S_{1/2} - 2P_{3/2}$ transition spectra



Result

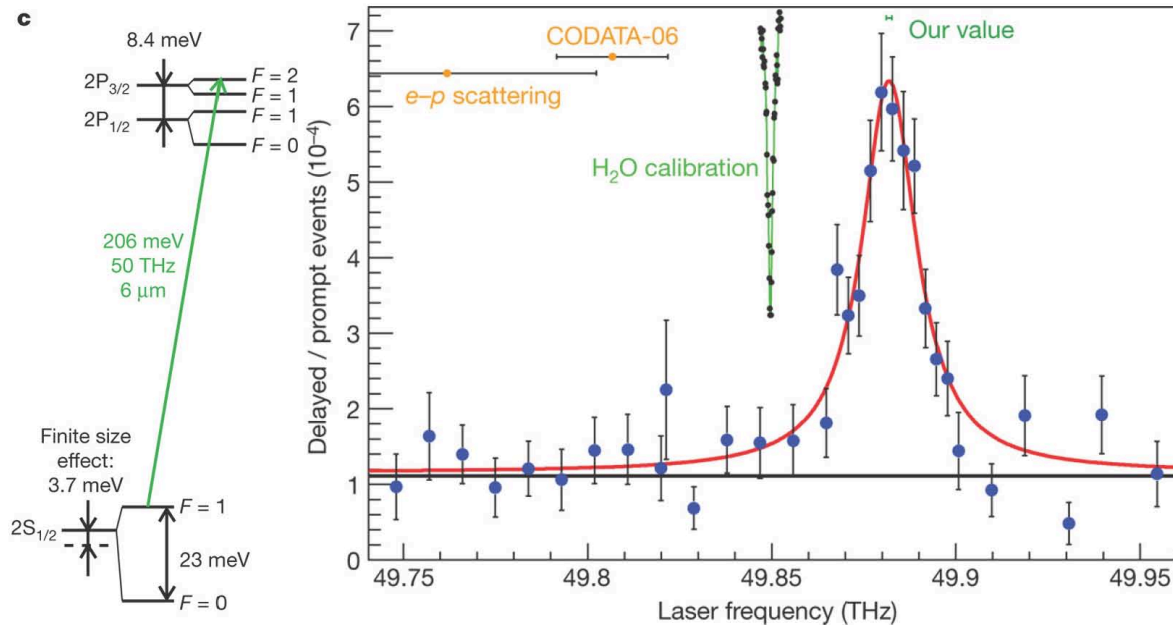
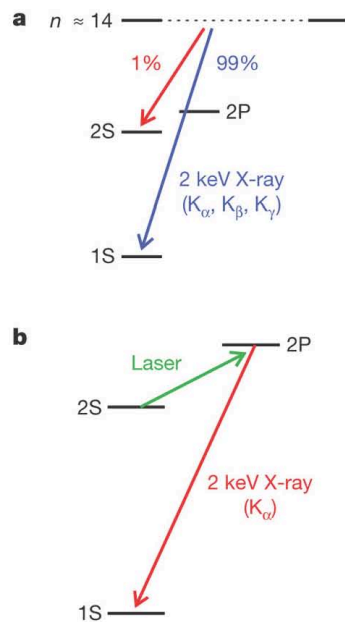
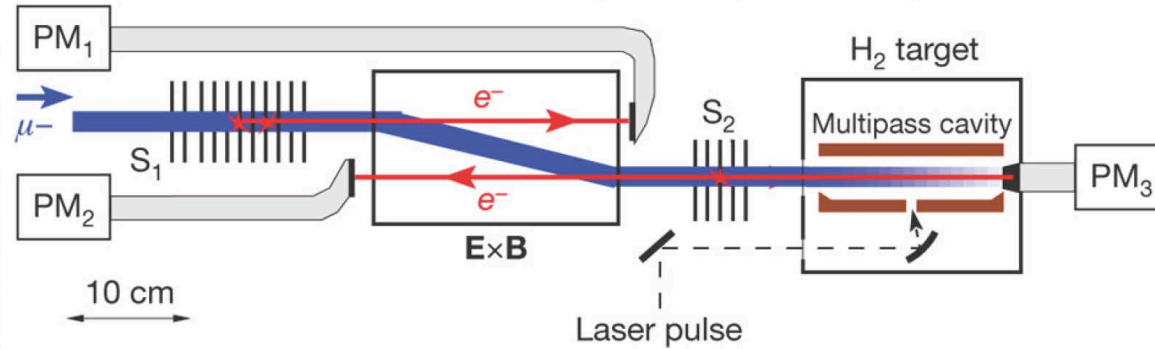
- The transition frequency between $2P_{3/2}$ and $2S_{1/2}$ is obtained to be $\Delta\nu = 49881.88(77) \text{ GHz}$, corresponding to an energy difference of $\Delta E = 206.2949(32) \text{ meV}$.
- **Theory** predicts a value of
$$\Delta E = 209.9779(49) - 5.2262 r_p^2 + 0.0347 r_p^3 \text{ meV}$$
- This results in a proton radius of $r_p = 0.84184(67) \text{ fm}$.

2005: Re-analysis electron-proton scattering $r_p = 0.897(18) \text{ fm}$
2008: Hydrogen spectroscopy (CODATA) $r_p = 0.8768(69) \text{ fm}$
2010: The new value is $r_p = 0.84184(67) \text{ fm}$

Muonic hydrogen Lamb shift experiment at PSI



Nature **466**, 213-216 (8 July 2010)



2010: new value is
 $r_p = 0.84184(67) \text{ fm}$

unprecedented precision, great! But different from everybody else's value; Not quite!
 M.A. Belushkin et al. (2007); T. Friedmann(2009)

Calculations

Contribution	Value [meV]	Uncertainty [10 ⁻⁴ meV]
Uehling	205.0282	
Källen-Sabry	1.5081	
VP iteration	0.151	
Mixed $\mu - e$ VP	0.00007	
Hadronic VP [21,23]	0.011	20
Sixth order VP [24]	0.00761	
Whichmann-Kroll	-0.00103	
Virtual Delbrück	0.00135	
Light-by-light	-	10
Muon self-energy and muonic VP (2 nd order)	-0.66788	
Fourth order electron loops	-0.00169	
VP insertion in self energy [17]	-0.0055	10
Proton self-energy [18]	-0.0099	
Recoil [17,43]	0.0575	
Recoil correction to VP (one-photon)	-0.0041	
Recoil (two-photon) [19]	-0.04497	
Recoil higher order [19]	-0.0096	
Recoil finite size [32]	0.013	10
Finite size of order $(Z\alpha)^4$ [32]	$-5.1975(1) r_p^2$	(620)
Finite size of order $(Z\alpha)^5$	$0.0347(30) r_p^3$	(20)
Finite size of order $(Z\alpha)^6$	-0.0005	
Correction to VP	$-0.0109 r_p^2$	
Additional size for VP [19]	$-0.0164 r_p^3$	
Proton polarizability [18,33]	0.015	40
Fine structure $\Delta E(2P_{3/2} - 2P_{1/2})$	8.352	10
$2P_{3/2}^{F=2}$ hyperfine splitting	1.2724	
$2S_{1/2}^{F=1}$ hyperfine splitting [42], $(-22.8148/4)$	-5.7037	20

An additional term 0.31 meV
to match CODATA value

Recent evaluation by Jentschura,
Annals Phys. 326, 500 (2011)

Proton Polarizability contribution is 0.015(4) meV

Summary

2005: Re-analysis e-p scattering $r_p = 0.897(18)$ fm (Sick 2003)

2008: Hydrogen spectroscopy (CODATA) $r_p = 0.8768(69)$ fm (Mohr 2008)

2010: The new value is $r_p = 0.84184(67)$ fm (muonic Lamb Shift)

2010: Mainz ep cross section $r_p = 0.879(5)_{\text{stat}}(4)_{\text{sys}}(2)_{\text{mod}}(4)_{\text{group}}$

Magnetic radius: $r_p = 0.777(13)_{\text{stat}}(9)_{\text{sys}}(5)_{\text{mod}}(2)_{\text{group}}$

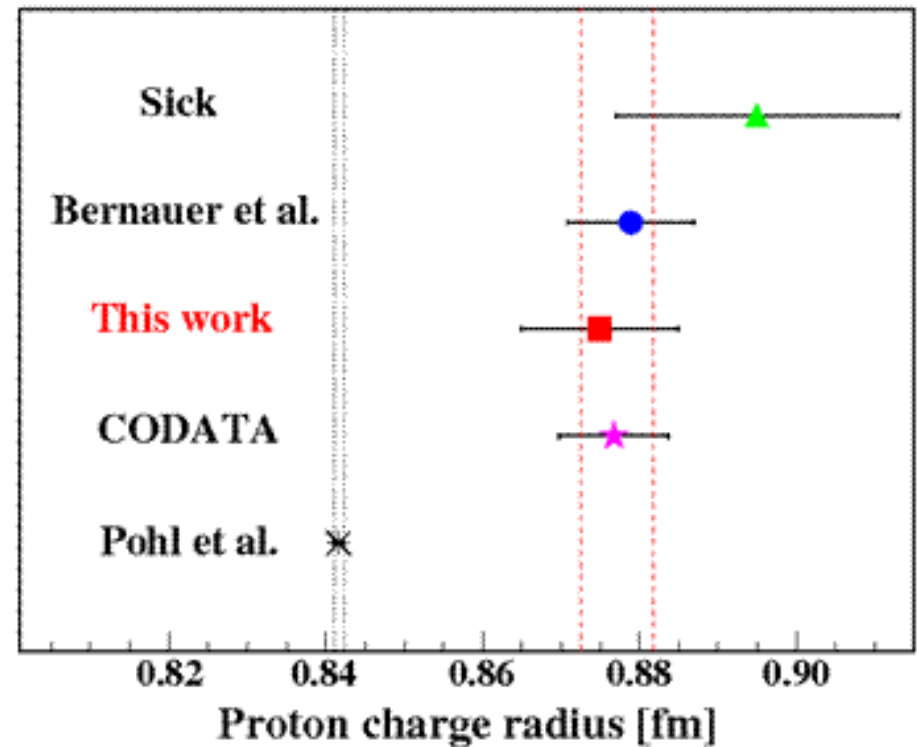
2010: Model independent analysis Paz and Richard,
PRD82,113005 (2010)

$$r_E^p = 0.877^{+0.031}_{-0.049} \pm 0.011 \text{ fm}$$

2011: JLab $r_p = 0.875(10)$,

$r_p = 0.867(20)$ (magnetic)

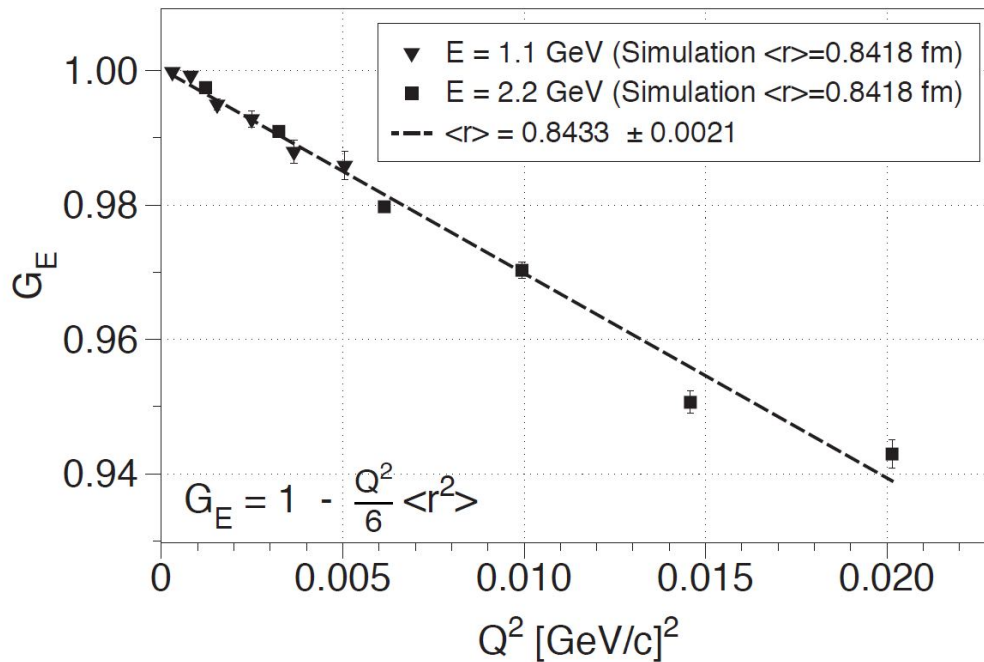
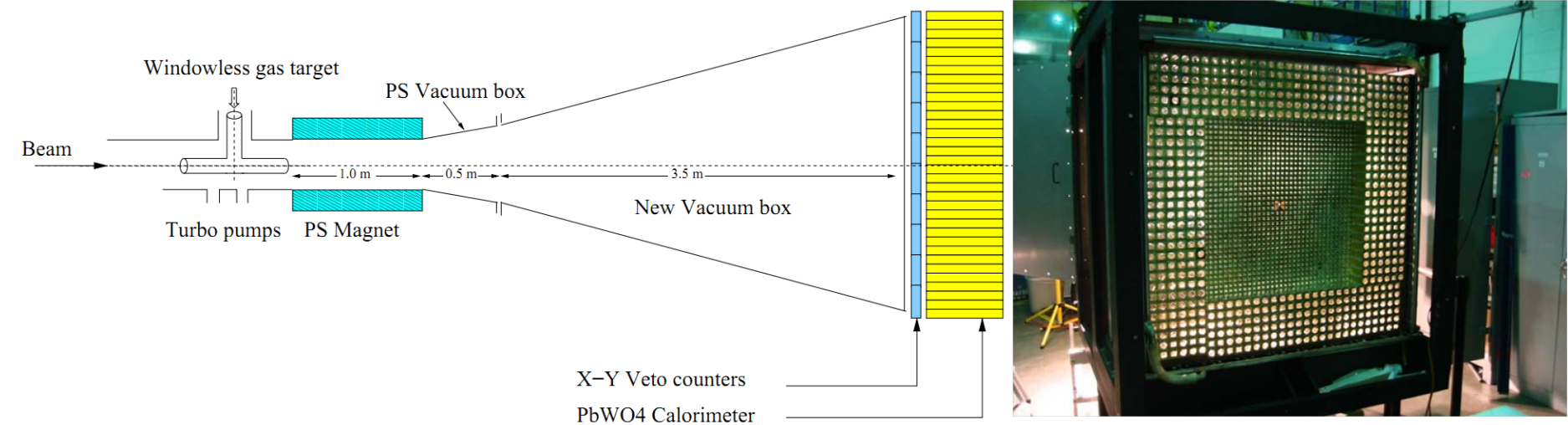
Zhan et al. arXiv:1102.0318



Partial summary

- **Exotic particles**, e.g. Barger et al. PRL106,153001 (2011) and references
- **New PV muonic force**, Batell et al. PRL 107 (011803) 2011
- **Contributions to the muonic H Lamb shift**: Carlson and Vanderhaeghen, arXiv:1101.5965, Jentschura, Annals Phys. 326, 500 (2011), Borie, arXiv: 1103:1772, Carroll et al, arXiv:1108.5785,....
- **Higher moments of the charge distribution and Zemach radii**, Distler, Bernauer and Walcher, PLB696, 343(2011),..
- **New experiments: Mainz, Jlab, PSI, ...**

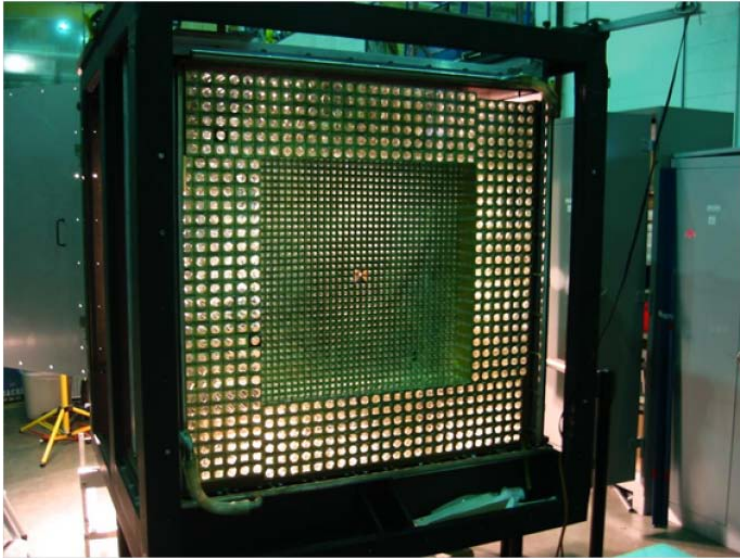
A new ep experiment on charge radius



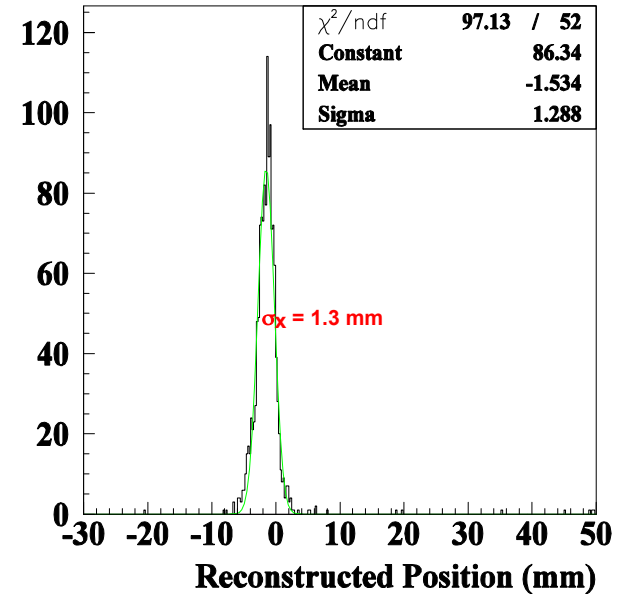
- EM calorimeter
- Windowless target, Low background
- QED moller process as normalization by ep and ee at the same time
- extremely low Q^2 : 10^{-2} - 10^{-4} GeV^2
- Sub % overall precision

Gasparian, Khandaker, Gao, Dutta to JLab PAC38 (conditionally approved)

Electromagnetic HyCal calorimeter

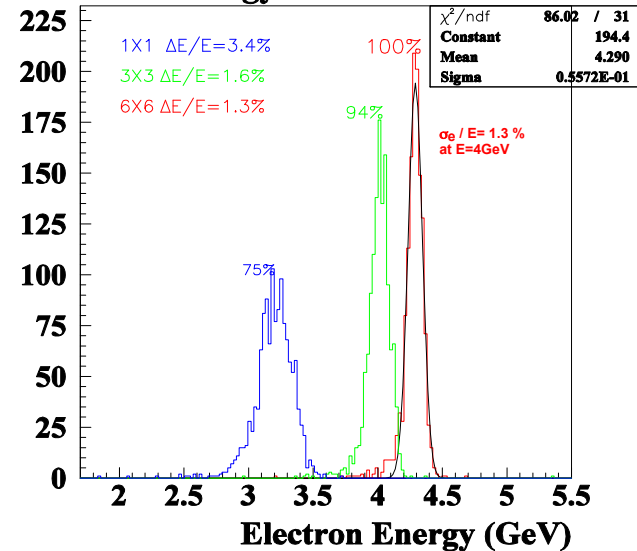


Position Resolution

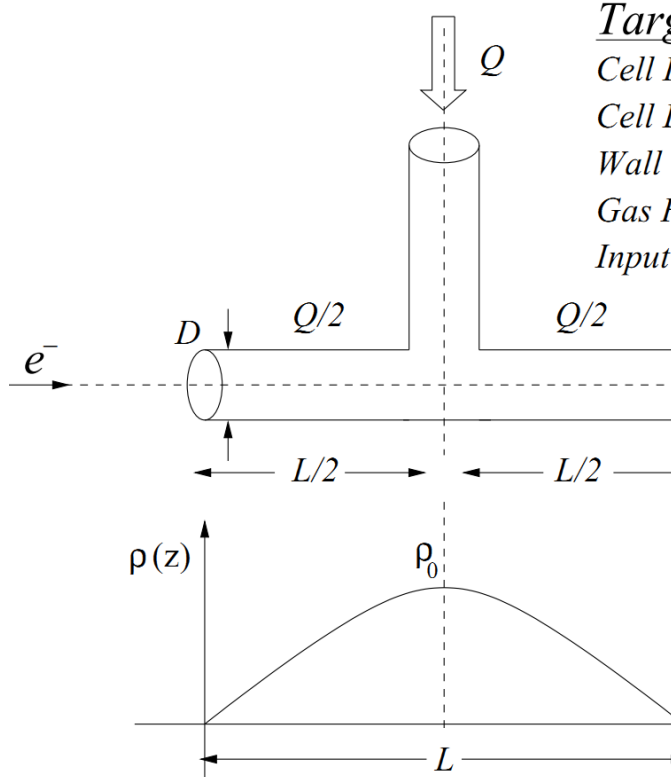


- High resolution, large acceptance
HyCal calorimeter (**PbWO₄** part only)
- Windowless H₂ gas flow target
- XY – veto counters
- Vacuum box, one thin window at HyCal only
- Harp scanner for beam profile

Energy Resolution

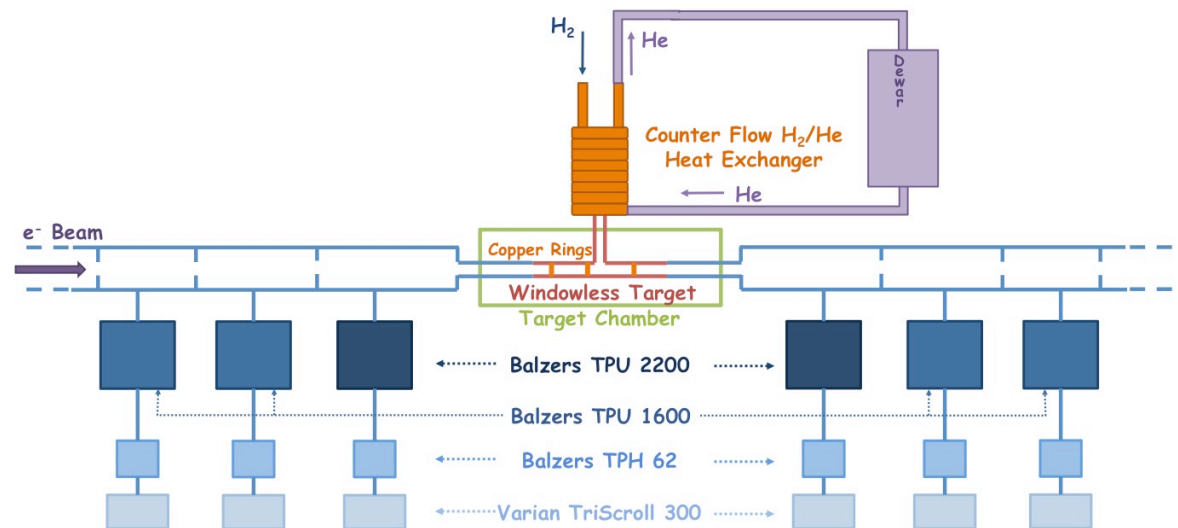


Windowless Gas Flow H₂ Target



Target Parameters:

Cell Diameter = 4 mm
 Cell Length = 4 cm
 Wall Thickness = 30 μm Kapton
 Gas Flow rate = 6 Torr-l/s
 Input Gas Temp = 25 K



- Major background for typical magnetic spectrometer experiments is from target window material.
- This proposed experiment is essentially a background-free measurement.
- Similar targets in OLYMPUS and HERMES at DESY.

Control of Systematic Errors

- Major improvements over past experiments:

1) Simultaneous detection of two processes

❖ $ep \rightarrow ep$

❖ $ee \rightarrow ee$ Moller scattering



Tight control of systematic errors



Low beam background

2) Windowless H₂ gas target

3) Very low Q² range: [2x10⁻⁴ – 2x10⁻²] (GeV/c)²



Model independent r_p extraction

- Extracted diff. cross sections for $ep \rightarrow$

ep

$$\left(\frac{d\sigma}{d\Omega} \right)_{ep} (Q_i^2) = \frac{N_{\text{exp}}^{\text{yield}} (ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{beam}}^{e^-} \cdot N_{\text{tgt}}^{\text{H}} \cdot \epsilon_{\text{geom}}^{ep} (\theta_i \pm \Delta\theta) \cdot \epsilon_{\text{det}}^{ep}}$$

- ... and for $ee \rightarrow ee$, Moller

$$\left(\frac{d\sigma}{d\Omega} \right)_{e^-e^-} = \frac{N_{\text{exp}}^{\text{yield}} (e^-e^- \rightarrow e^-e^-)}{N_{\text{beam}}^{e^-} \cdot N_{\text{tgt}}^{\text{H}} \cdot \epsilon_{\text{geom}}^{e^-e^-} \cdot \epsilon_{\text{det}}^{e^-e^-}}$$

- Then ep cross section is related to Moller:

$$\left(\frac{d\sigma}{d\Omega} \right)_{ep} (Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}} (ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}} (e^-e^- \rightarrow e^-e^-)} \cdot \frac{\epsilon_{\text{geom}}^{e^-e^-}}{\epsilon_{\text{geom}}^{ep}} \cdot \frac{\epsilon_{\text{det}}^{e^-e^-}}{\epsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega} \right)_{e^-e^-}$$

- Two major sources of systematic errors, N_e and N_{tgt} , typical for all previous experiments, are canceling out.

Control of Systematic Errors (cont'd)

(Moller event selection)

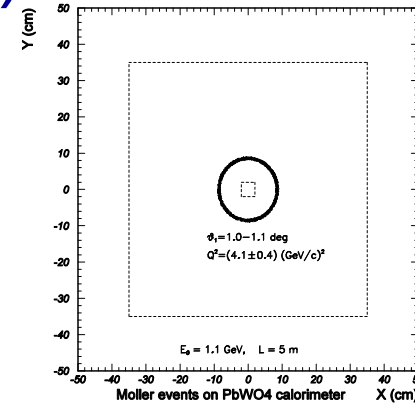
Will analyze Moller events in 3 different ways:

1) Single-arm method: one Moller e^- is in the same Q^2 range

ϵ_{det} will be measured for [0.5 – 2.0] GeV range

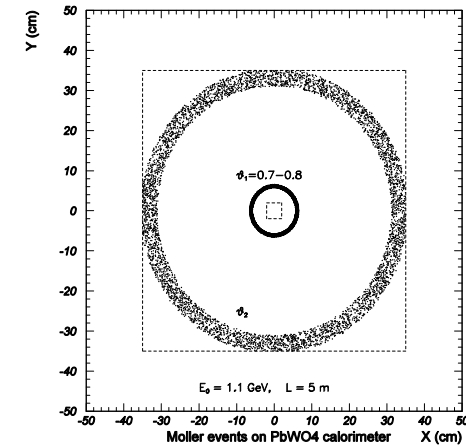
Relative ϵ_{det} are needed for this experiment

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-)} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$



2) Coincident Method

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-)} \cdot \frac{\epsilon_{\text{geom}}^{e^-e^-}}{\epsilon_{\text{geom}}^{ep}} \cdot \frac{\epsilon_{\text{det}}^{e^-e^-}}{\epsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$



3) Integrated over HyCal acceptance

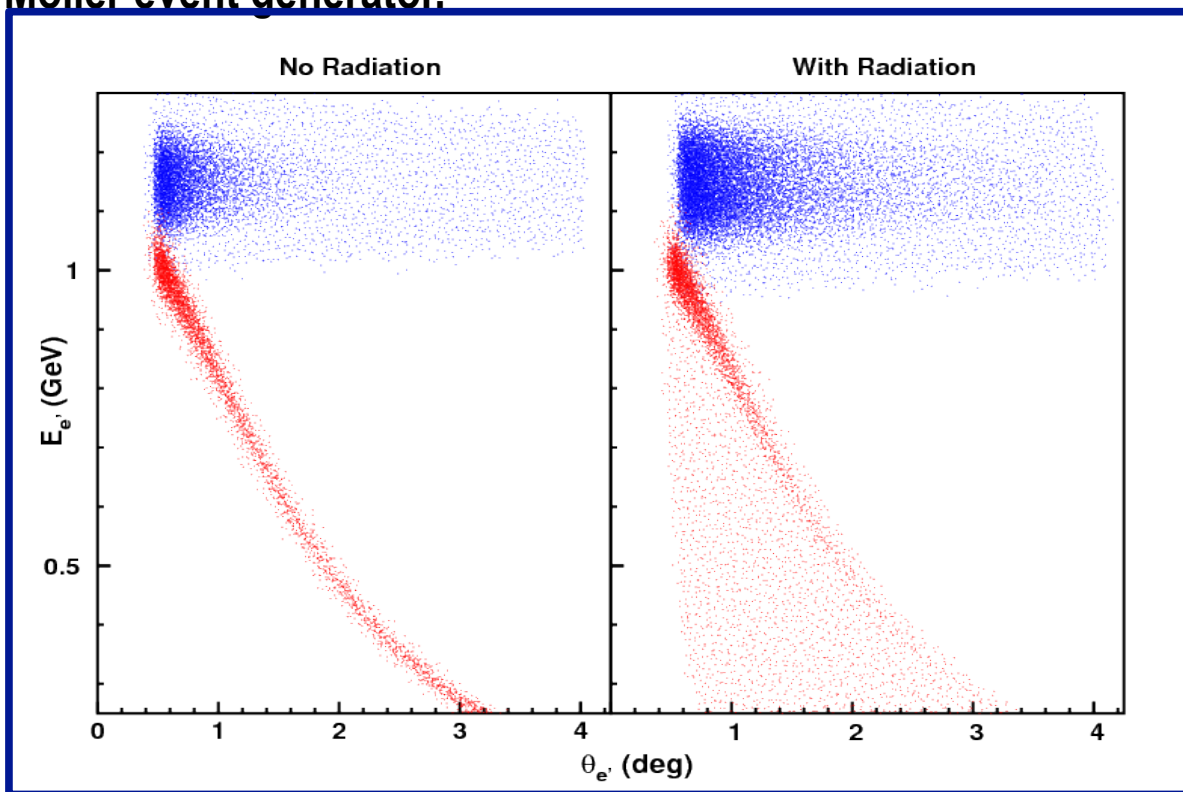
$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep, \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^-, \text{ on PWO})} \right] \frac{\epsilon_{\text{geom}}^{e^-e^-}(\text{all PWO})}{\epsilon_{\text{geom}}^{ep}(\theta_i \pm \Delta\theta)} \frac{\epsilon_{\text{det}}^{e^-e^-}(\text{all PWO})}{\epsilon_{\text{det}}^{ep}(\theta_i \pm \Delta\theta)} \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

Relative ϵ_{det} will be measured with high precision.

Contribution of ϵ_{det} and ϵ_{geom} in cross sections will be on second order only.

Event Selection and Radiative Corrections

- **ep elastic** radiative corrections were simulated using ELRADGEN¹ within an ep elastic event generator (in consultation with I. Akushevich)²
- Moller radiative corrections were simulated using MERADGEN within a Moller event generator.

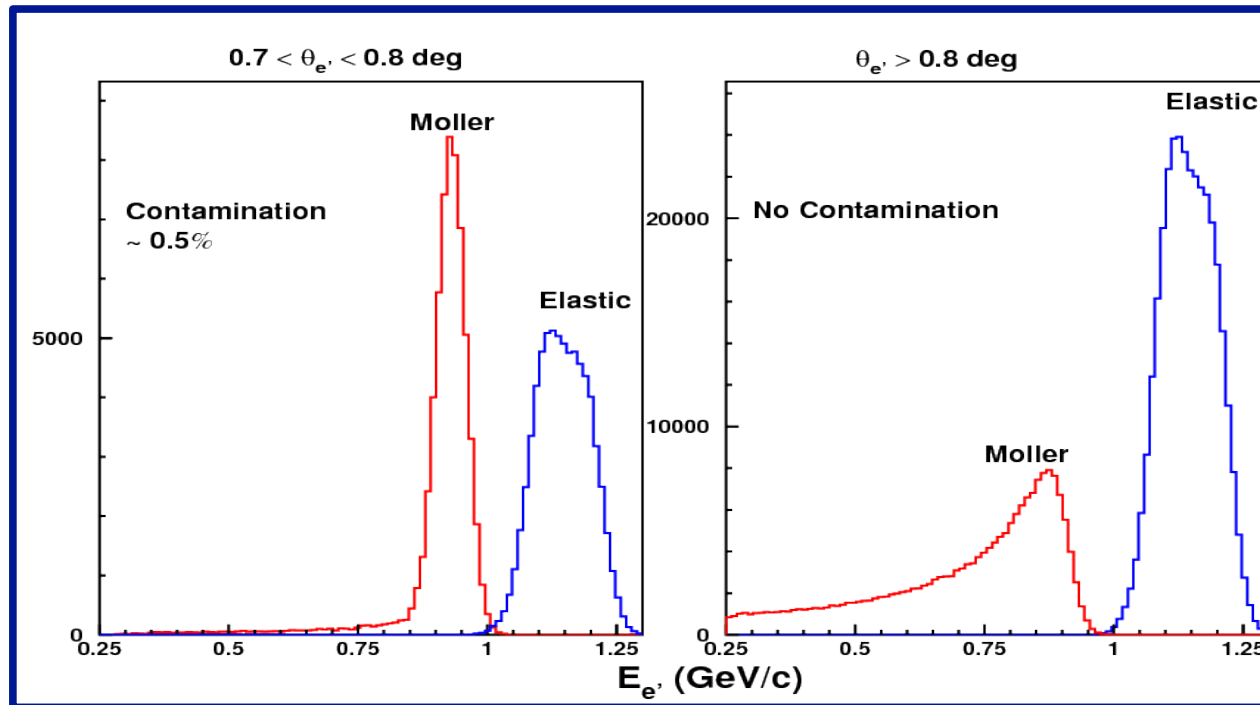


¹ I. Akushevich, O. Filoti, A. Ilyichev, and N. Shumeiko, arXiv:hep-ph/1104.0039v1, (2011).

² A. Afanasev, E. Chudakov, V. A. Zukunov and A. N. Ilyichev, Comp. Phy. Comm, 176, 218 (2007)

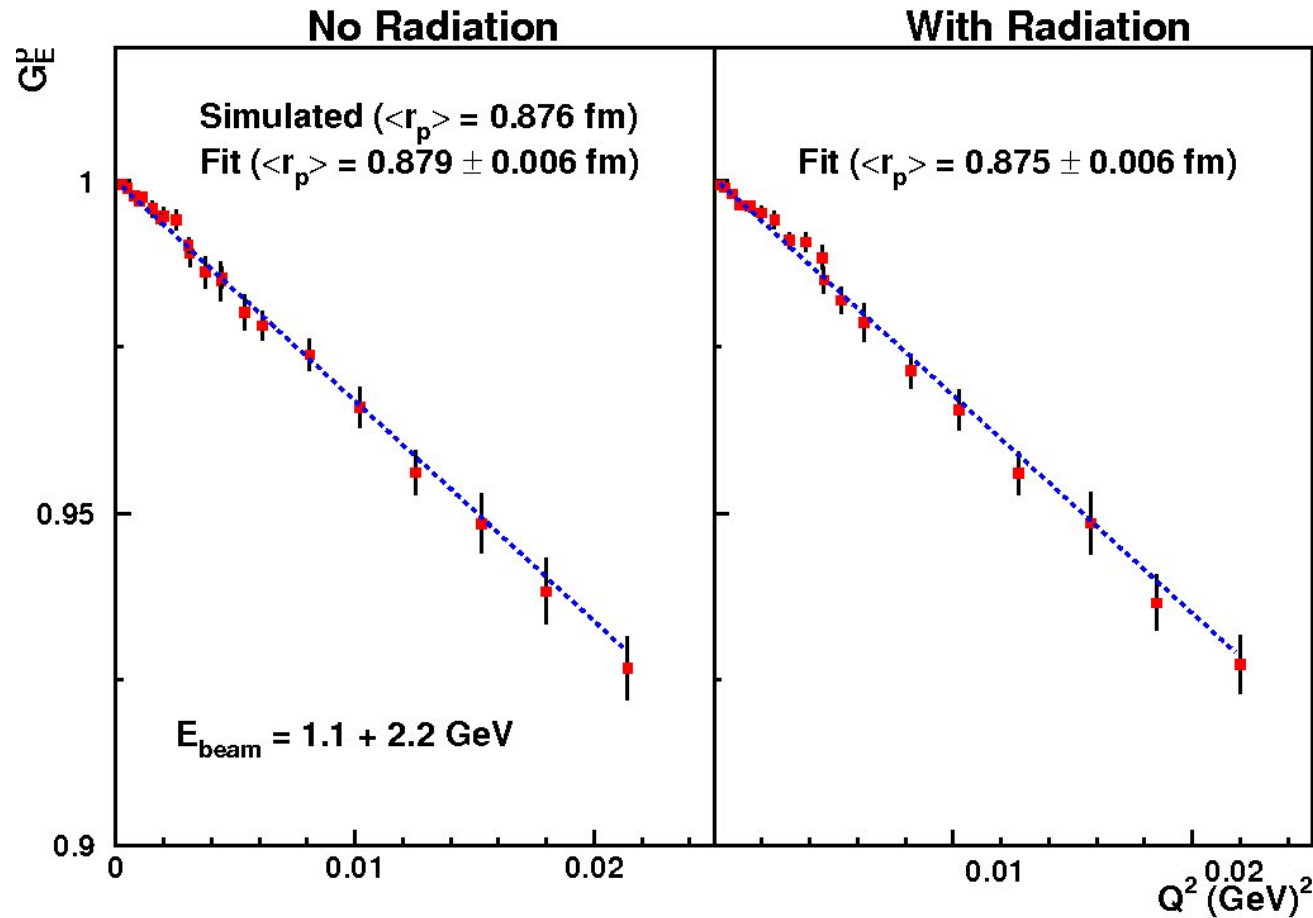
Elastic/Moller Overlap

- Overlap of $E_{e'}$ spectra of radiated events $\sim 0.5\%$ contamination from Moller events (for $0.7 < \theta_{e'} < 0.8$ deg)



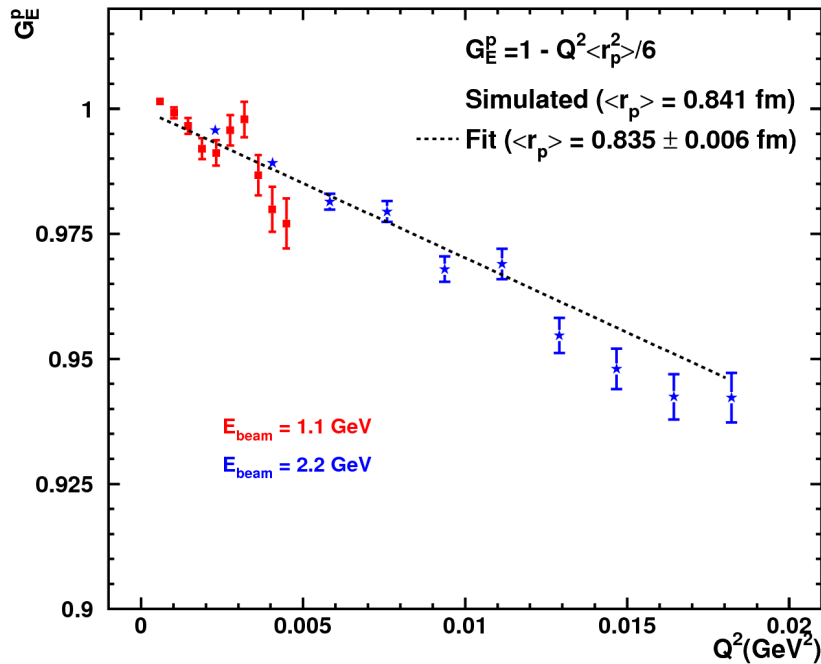
- Addresses TAC's concerns about possible overlap of Moller and Elastic events at the smallest angles.

Radiative Corrections

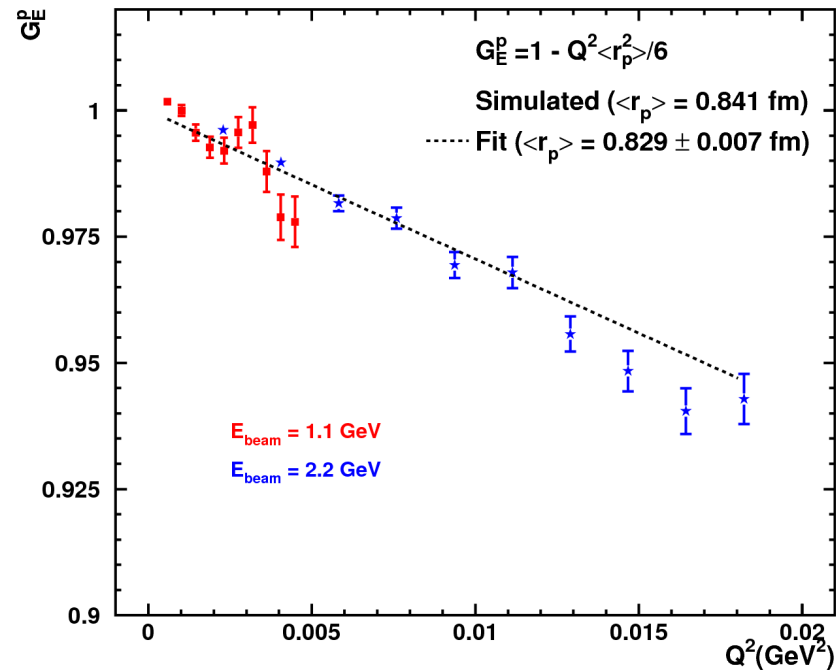


- Extracting r_p from simulations with and without radiation we have estimated the systematic uncertainty from **radiative corrections** to be **< 0.3%**

Control of Systematic Errors (Calorimeter Misalignment)



0 mm shift $r_p = 0.835 \pm 0.006$ fm



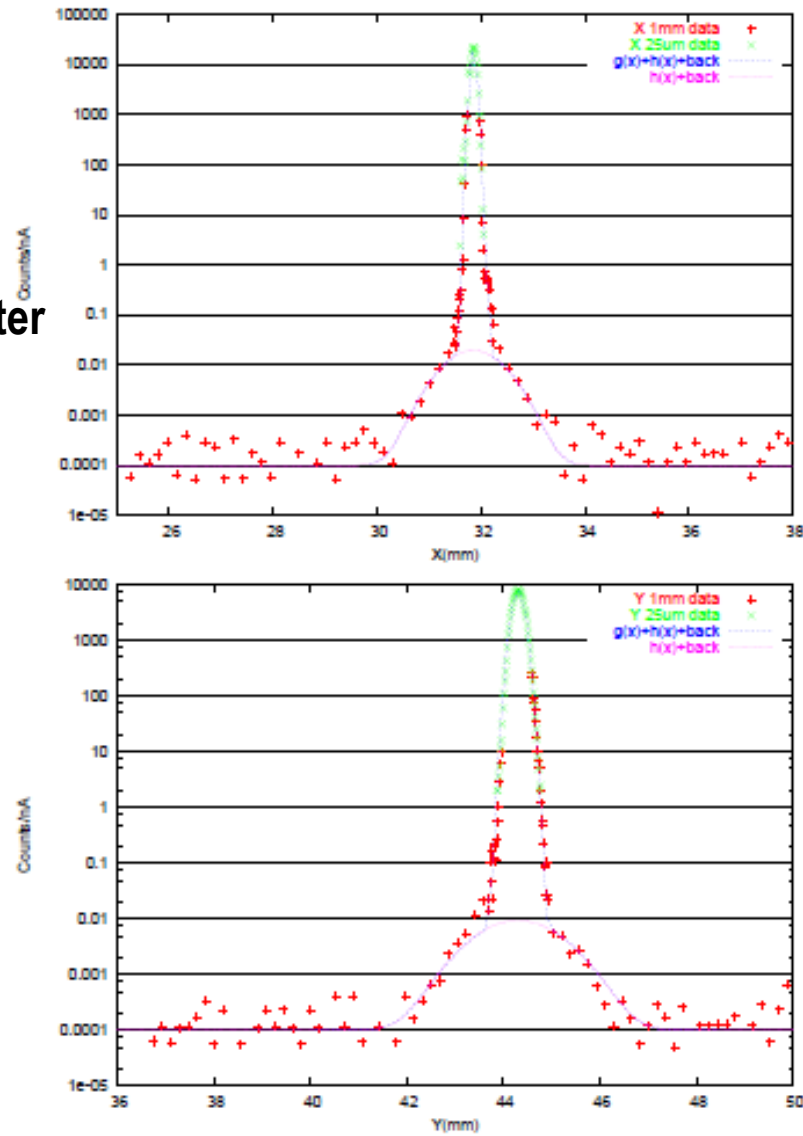
1mm shift $r_p = 0.829 \pm 0.007$ fm

- accuracy of engineering survey: **0.7 mm**
- Off-line check with co-planarity of Moller events (done in PrimEx experiments with Compton)

➤ HyCal misalignment is not a problem for r_p extraction

HPS Quality Electron Beam Test

- Signal/Noise $\approx 10^8$ level reached starting from ± 2 mm from beam center
- Electron beam size $\approx 25 \mu\text{m}$



Beam Time Request and Estimated Error Budget

■ Beam time

	Time (days)
Setup checkout, calibration	3.5
H ₂ gas target commission	5
Statistics at 1.1 GeV	2
Energy change	0.5
Statistics at 2.2 GeV	2
Empty target runs	2
Total	15

■ Estimated error budget (added quadratically)

Contributions	Estimated Error (%)
Statistical error	0.2
Acceptance (including Q ² determination)	0.4
Detection efficiency	0.1
Radiative corrections	0.3
Background and PID	0.1
Fitting error	0.2
Total Systematics	0.6%

Summary and outlook

- Two frontiers for discovering new physics
 - High energy such as LHC
 - Low energy high precision (intensity) frontier
- Surprise on proton charge radius from muonic hydrogen atom Lamb shift measurement due to high precision
- New precision measurement using different experimental technique from electron scattering is **a MUST**
- New experiment using EM calorimeter and windowless gas target will reach unprecedented low Q^2 region
- New physics or not will dependent on new precision results from electron scattering, and new Lamb shift measurements on H, D and He

Thanks to, D. Dutta, A. Gasparian, M. Khandaker, G. Paz, X.H. Zhan

Supported by U.S. Department of Energy under contract number DE-FG02-03ER41231