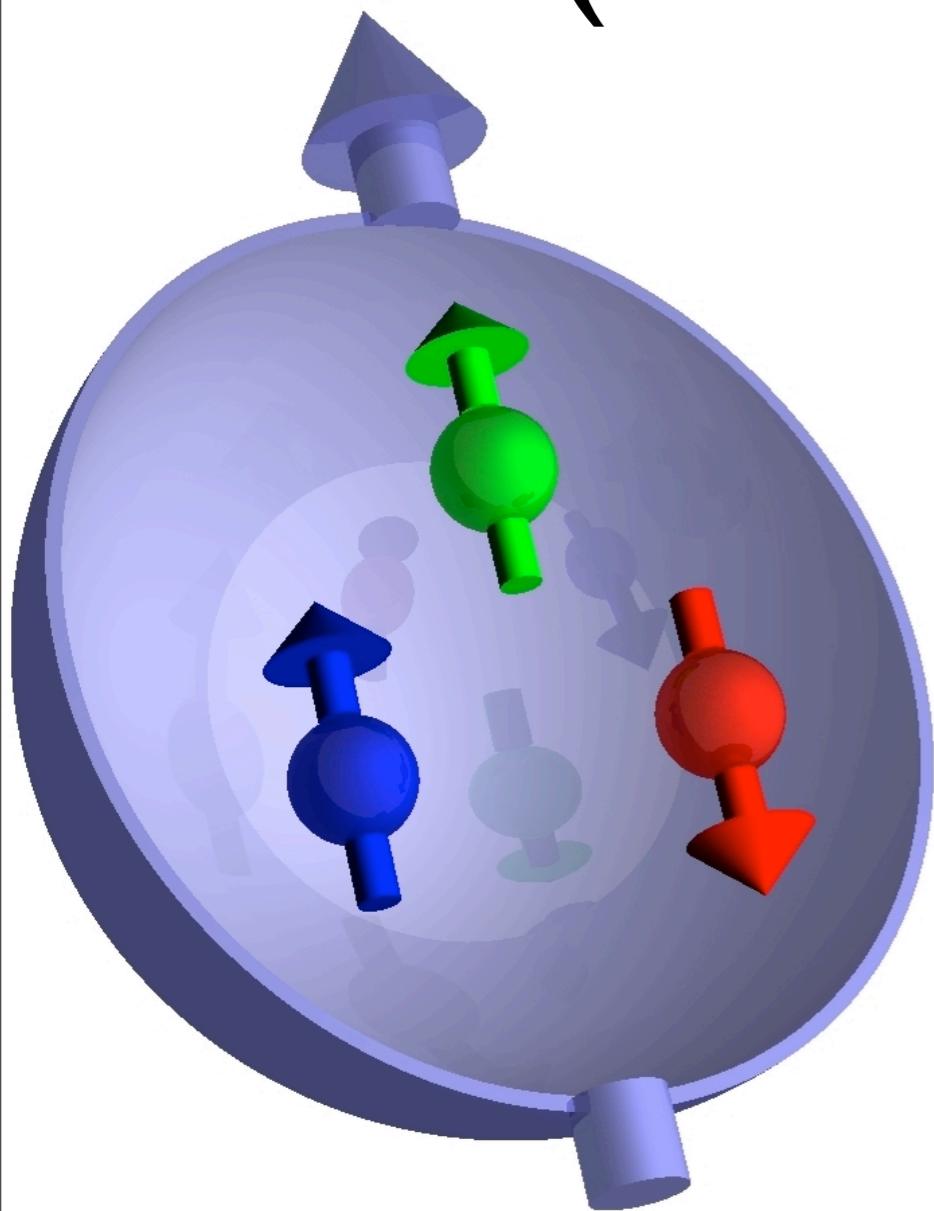


The Structure of the Nucleon (with a HERMES bias)



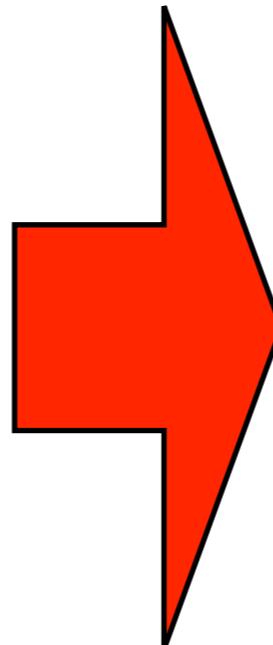
Morgan J Murray, University of Glasgow



University
of Glasgow

Overview

- History of the Field
- Notable Results
- Future Highlights



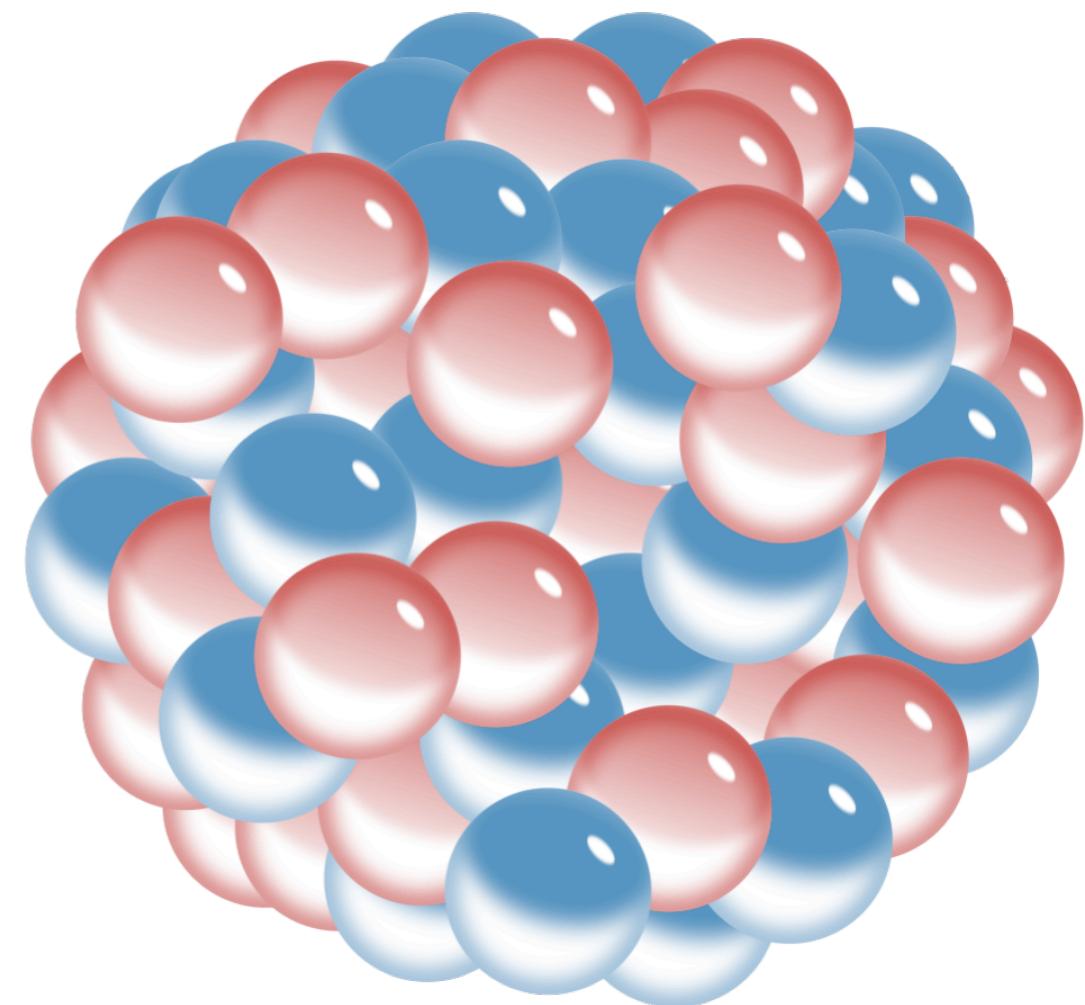
Where were we?

Where are we?

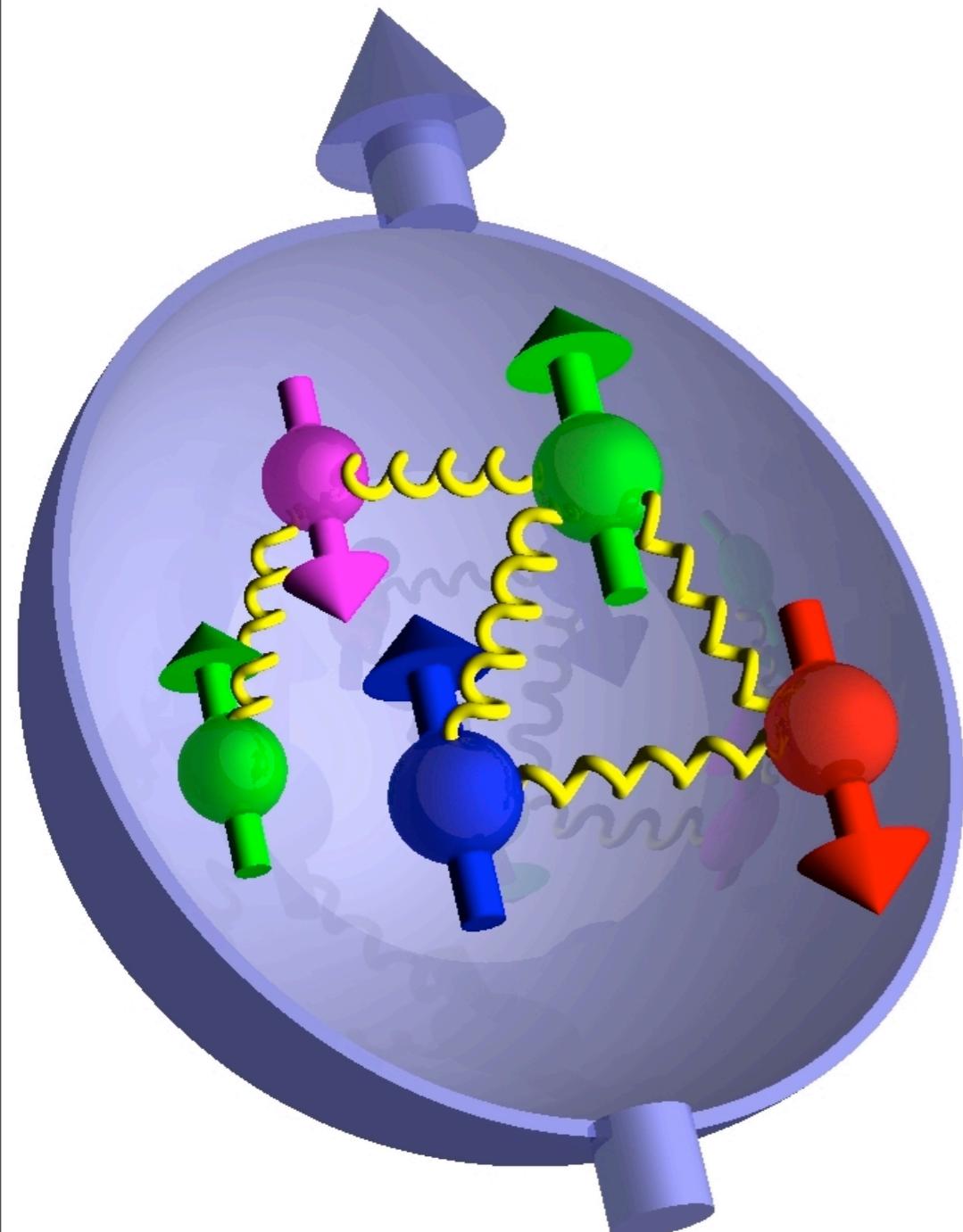
Where are we going?

Nucleons

- All matter made of atoms;
subatomic structure is **nucleons**
- Protons and Neutrons
- Look at **form factors** to
determine **electric and magnetic**
distribution inside the nucleon

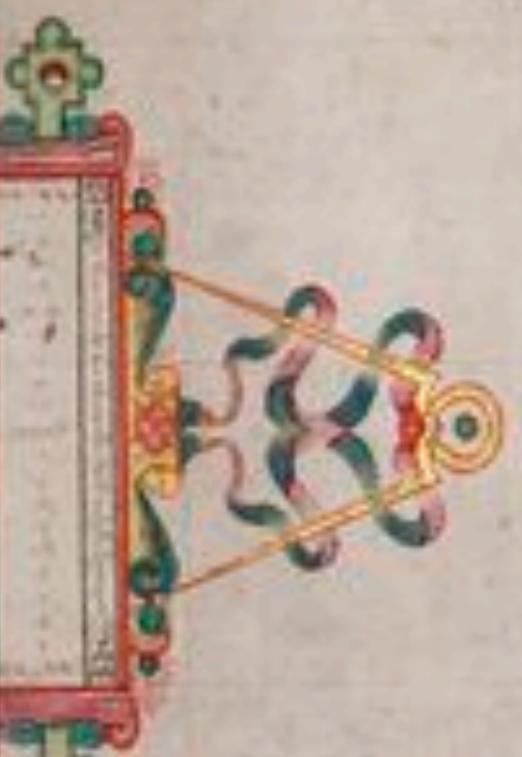


Quarks and Gluons



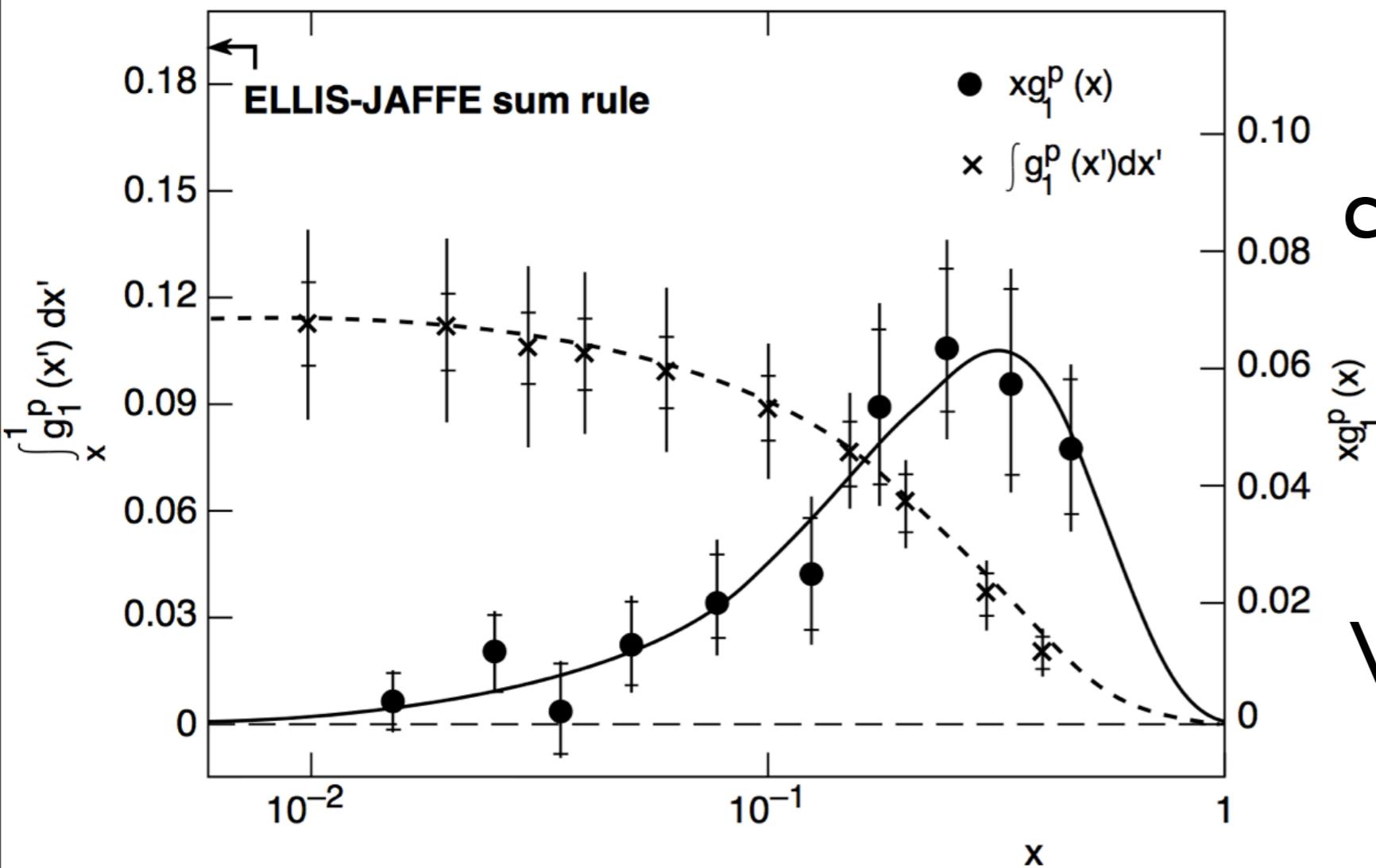
- Division between **quarks** and **gluons**
- Division between **sea** and **valence quarks**
- Concerned only with **up, down** and **strange**

THE SOUTH PART OF VIRGINIA



Exploration

The Motivation



Expected that the nucleon's spin is carried by the quarks:

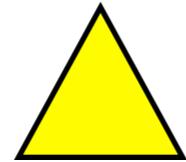
$$\frac{1}{2} + \frac{1}{2} - \frac{1}{2} = \frac{1}{2}$$

Via the Ellis-Jaffe sum rule, EMC said NO!

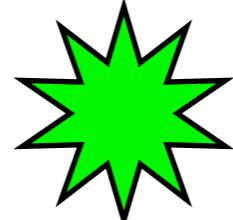
Spin Crisis!!!

How do we explain
the EMC result?

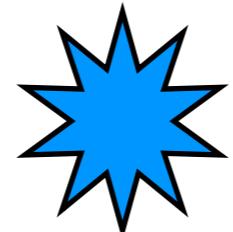
Quark spin



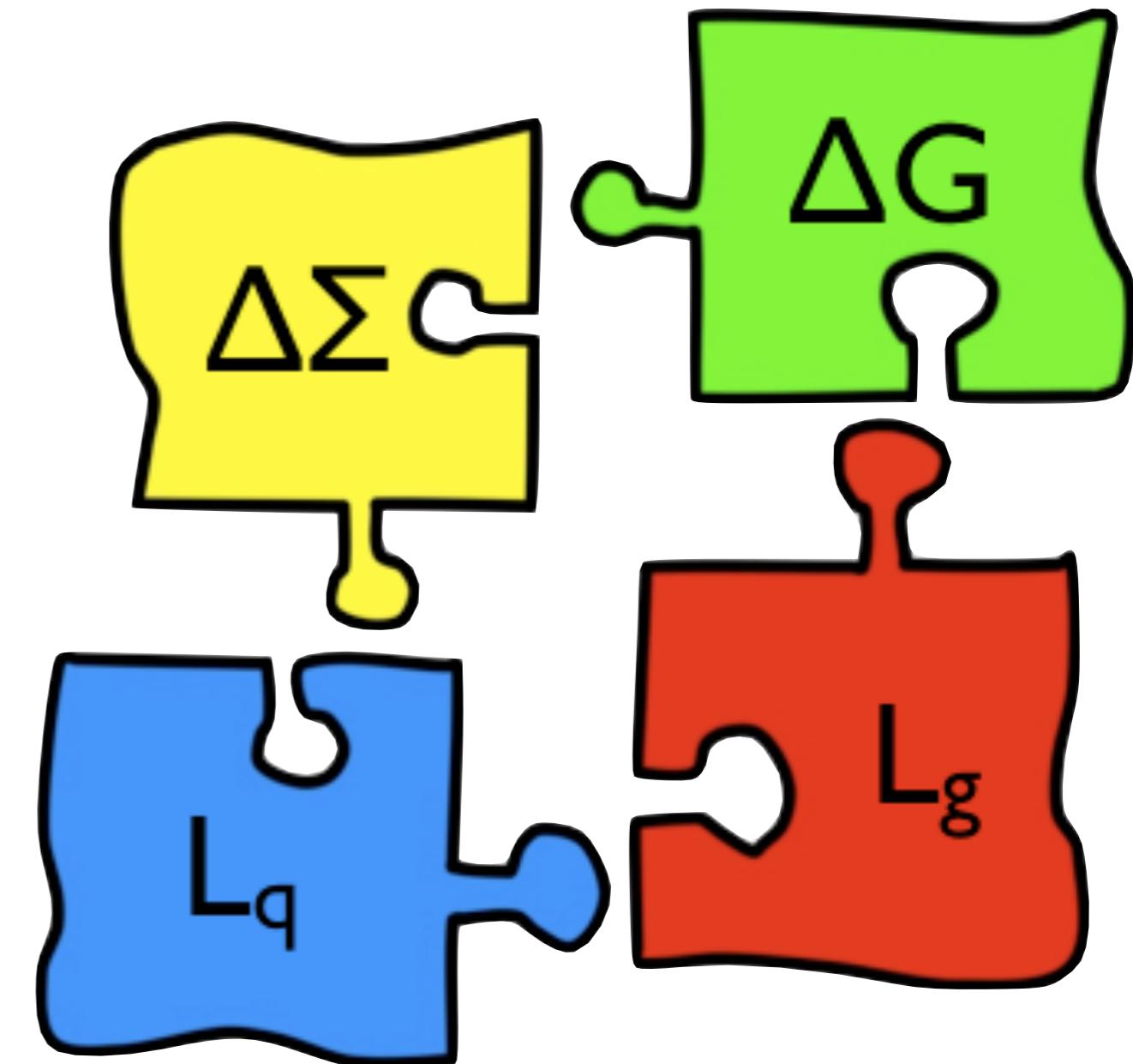
Gluon spin



Quark Orbital
Angular Momentum



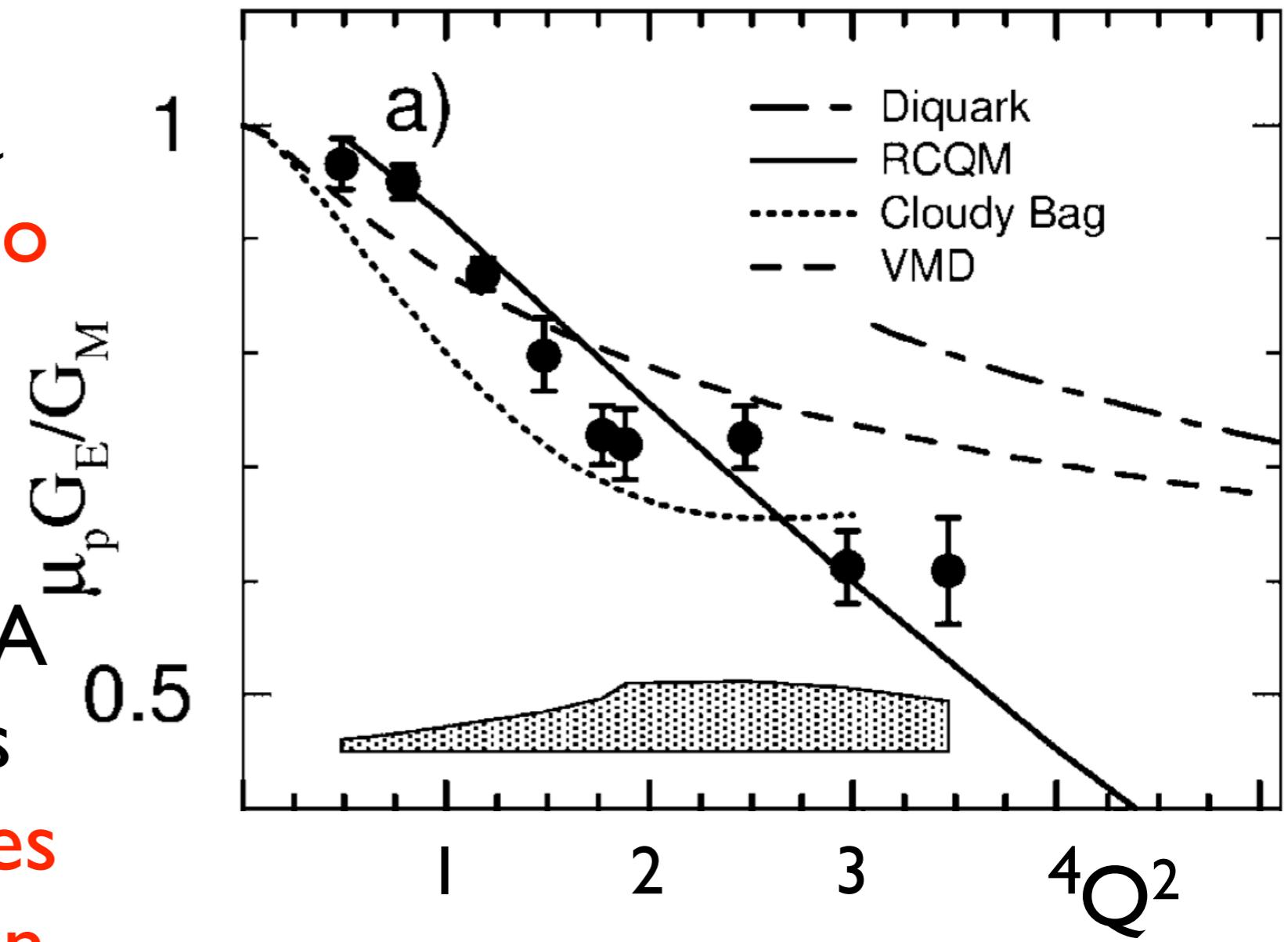
Gluon Orbital
Angular Momentum



The Motivation

Single-photon exchange predicts a constant GE/GM ratio

Indicators from Hall A in 2000 are that this doesn't hold - requires (at least!) two-photon exchange.



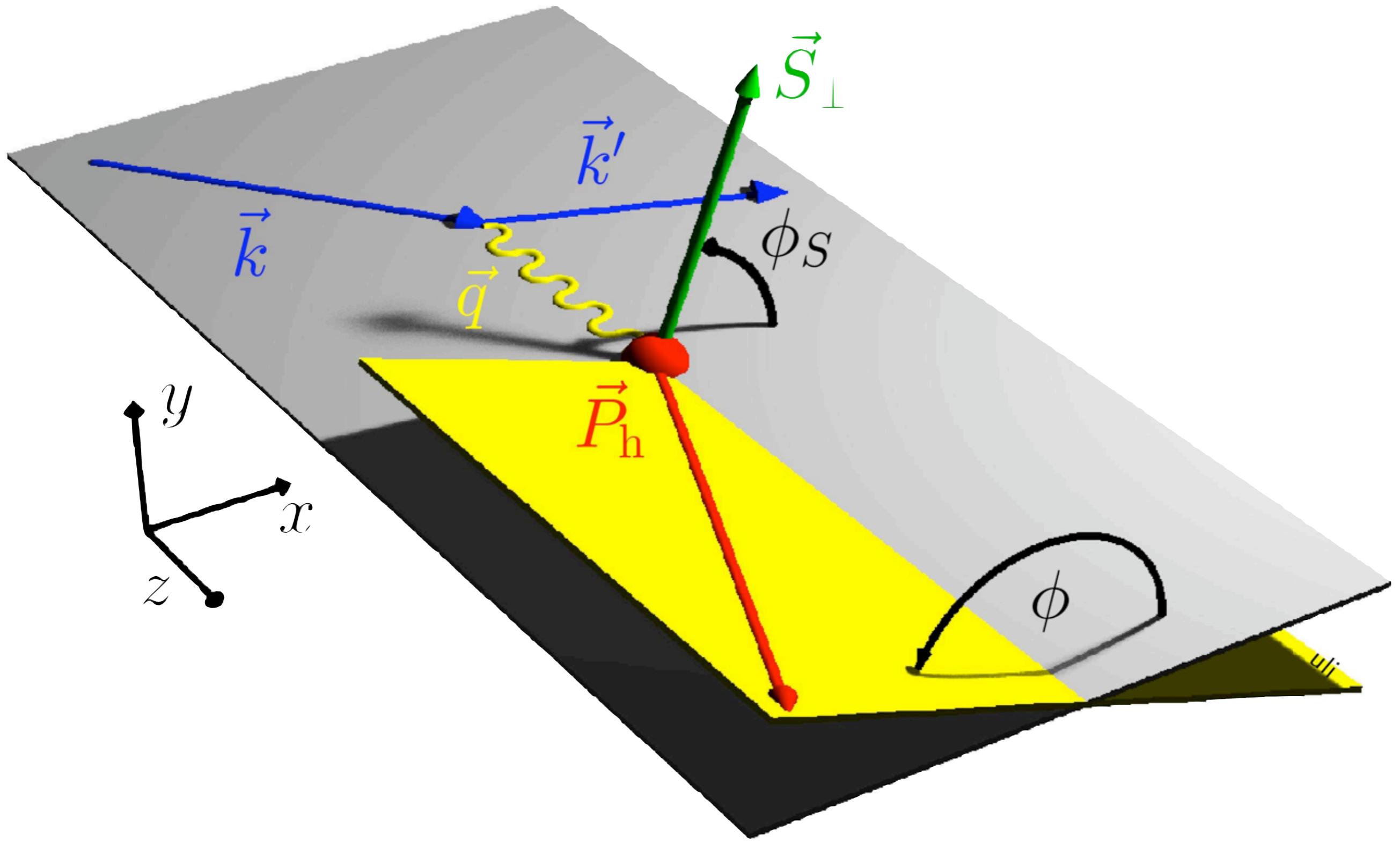
Consolidation



Structure Functions & TMDs Quark Polarization

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Nucleon Polarization

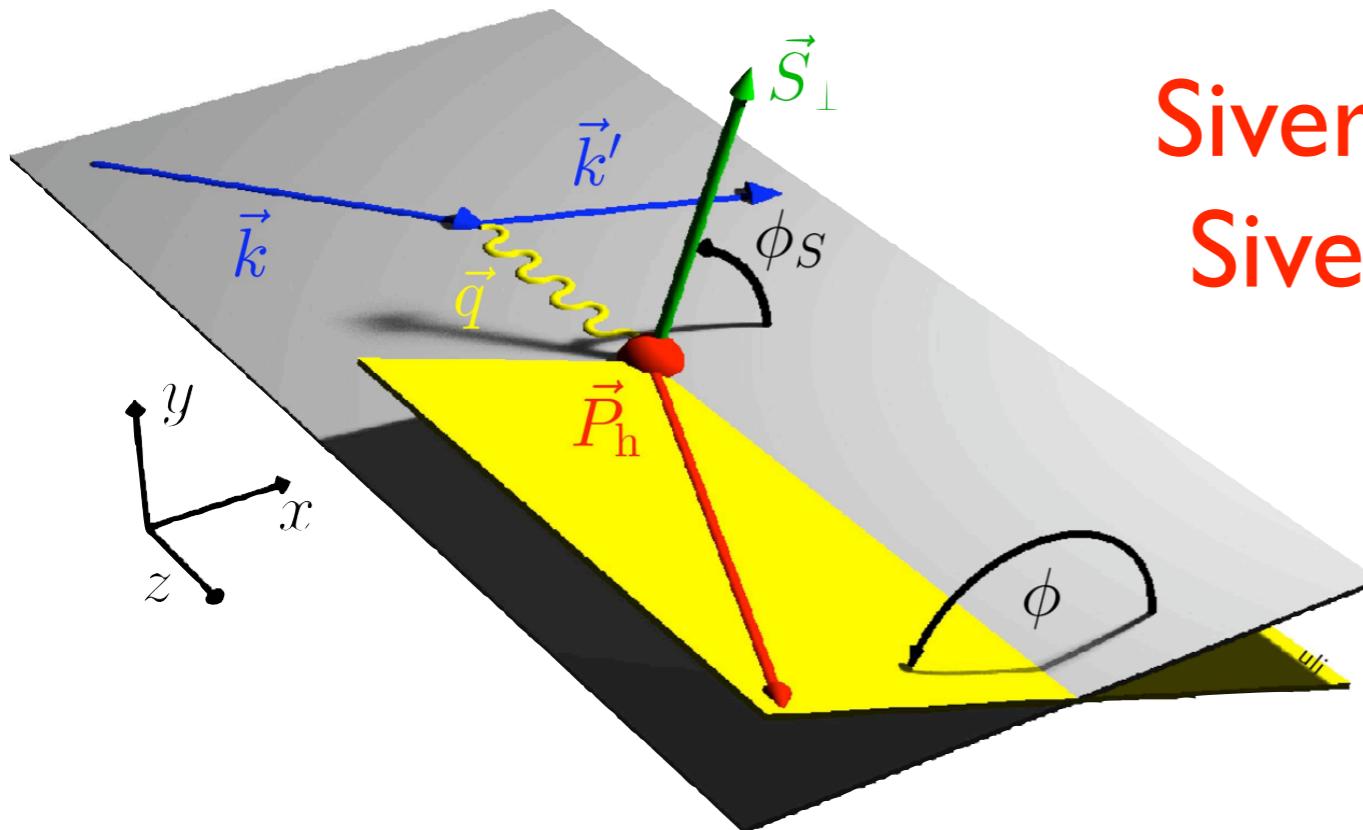


Semi-Inclusive DIS

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + d\sigma_{UU}^1 \cos(2\phi) + \frac{1}{Q} (d\sigma_{UU}^2 \cos \phi + \lambda_e d\sigma_{LU}^3 \sin \phi) \\
 & + S_L \left\{ d\sigma_{UL}^4 + \frac{1}{Q} (d\sigma_{UL}^5 \sin + \lambda_e [Q d\sigma_{LL}^6 + d\sigma_{UL}^7 \cos \phi]) \right\} \\
 & \text{Sivers Function} \qquad \qquad \qquad \text{Collins Effect} \\
 S_T \left\{ & d\sigma_{UT}^8 \sin(\phi - \phi_s) + d\sigma_{UT}^9 \sin(\phi + \phi_s) + d\sigma_{UT}^{10} \sin(3\phi - \phi_s) \right. \\
 & \left. + \frac{1}{Q} [d\sigma_{UT}^{11} \sin(2\phi - \phi_s) + d\sigma_{UT}^{12} \sin \phi_s] \right. \\
 & \left. + \lambda_e [d\sigma_{LT}^{13} \cos(\phi - \phi_s) + \frac{1}{Q} d\sigma_{LT}^{14} \cos \phi_s + \frac{1}{Q} d\sigma_{LT}^{15} \cos(2\phi - \phi_s)] \right\}
 \end{aligned}$$

cos-phi moments

Semi-Inclusive DIS



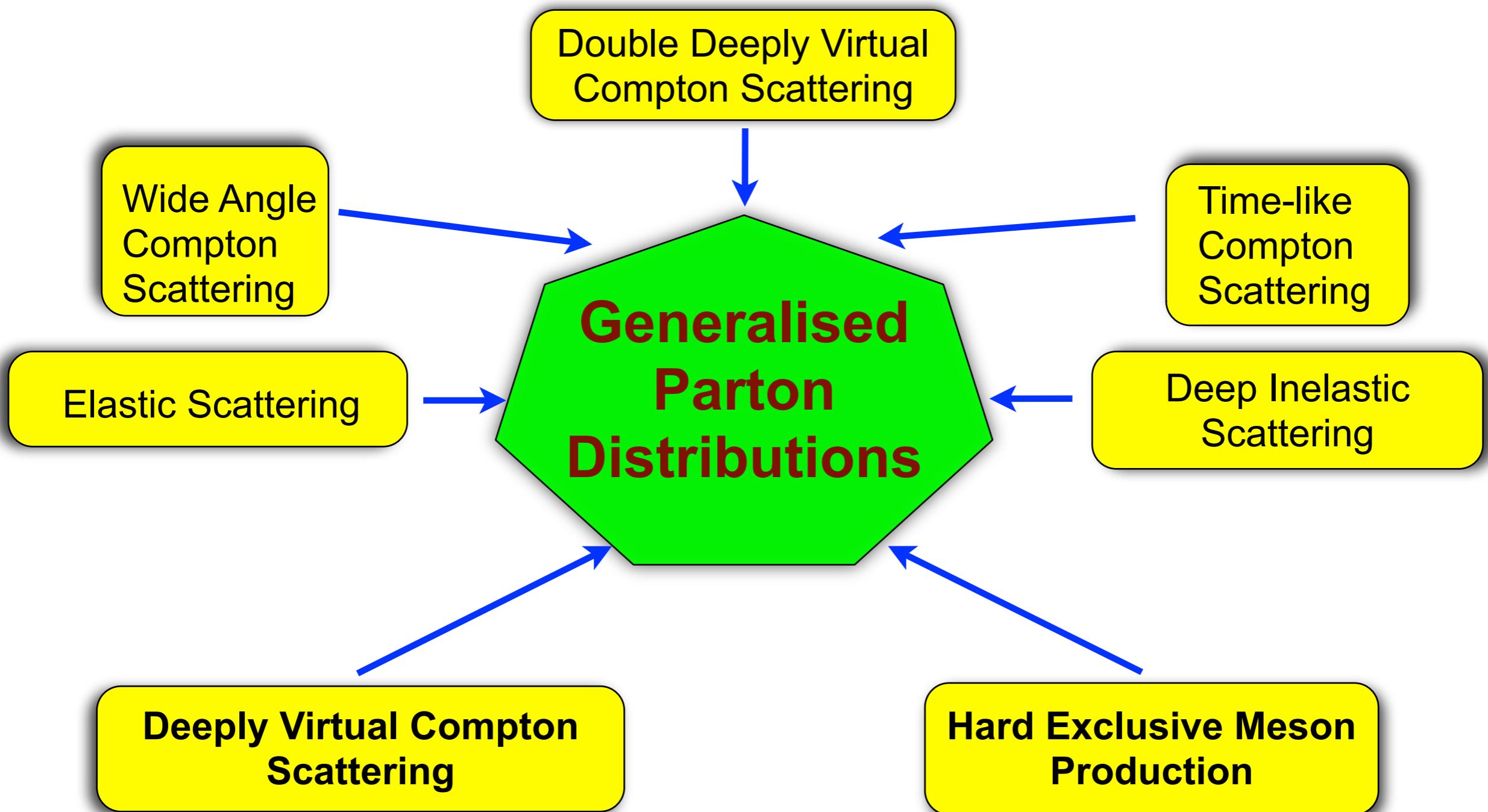
Sivers moment allows access to
Sivers function \Rightarrow quark OAM

Collins moment allows
extraction of **transversity**

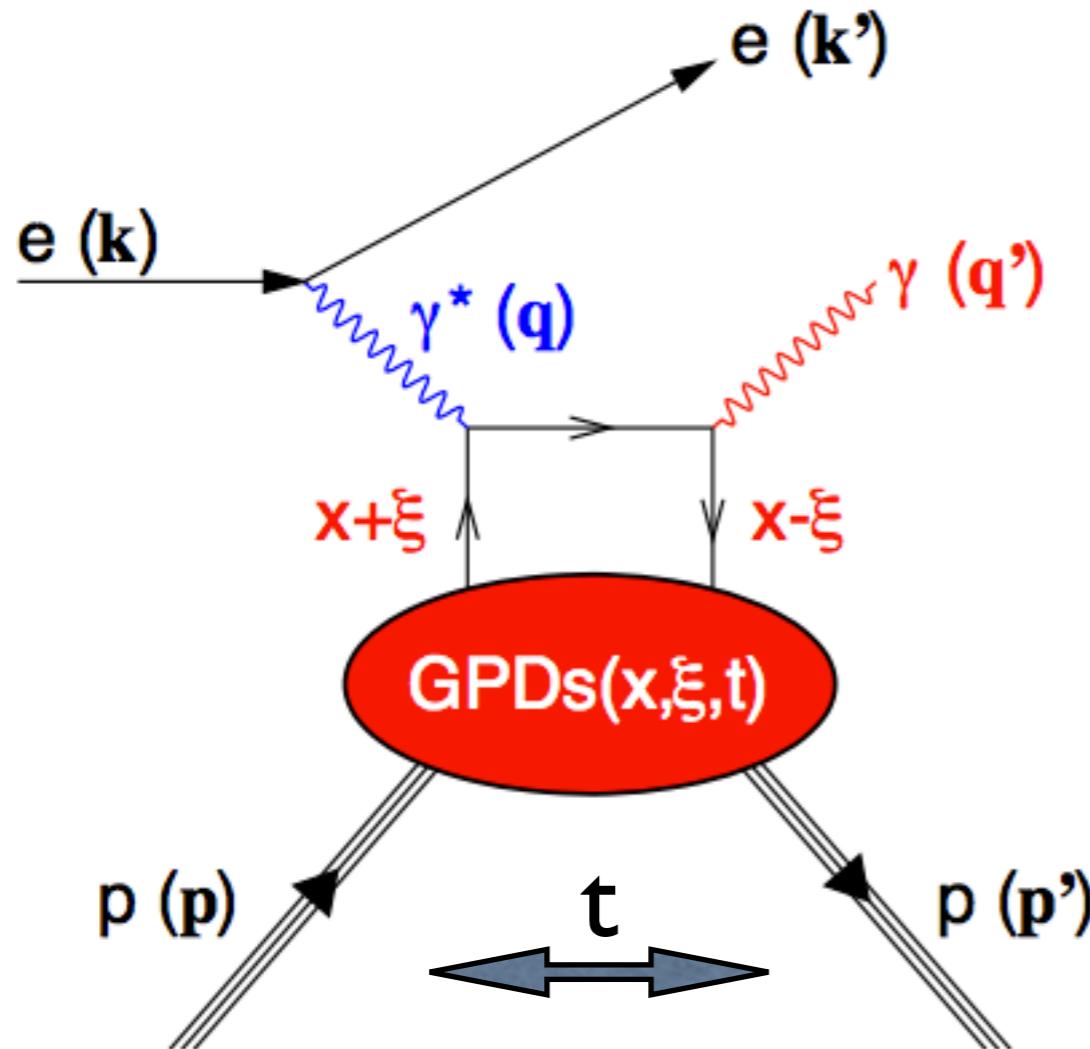
$$d\sigma_{UT}^8 \propto |S_T| \left[\frac{\vec{P}_T \cdot \hat{P}_{h,\perp}}{M_h} f_{1T}^{\perp q}(x, p_T^2) * D_1^q(z, k_T^2) \right]$$

$$d\sigma_{UT}^9 \propto |S_T| \left[\frac{\vec{k}_T \cdot \hat{P}_{h,\perp}}{M_h} h_1(x, p_T^2) * H_1^{\perp q}(z, k_T^2) \right]$$

Generalised Parton Distributions



GPDs



t - Mandelstam variable
(squared momentum transfer to nucleon)

x - Fraction of nucleon's longitudinal momentum carried by active quark

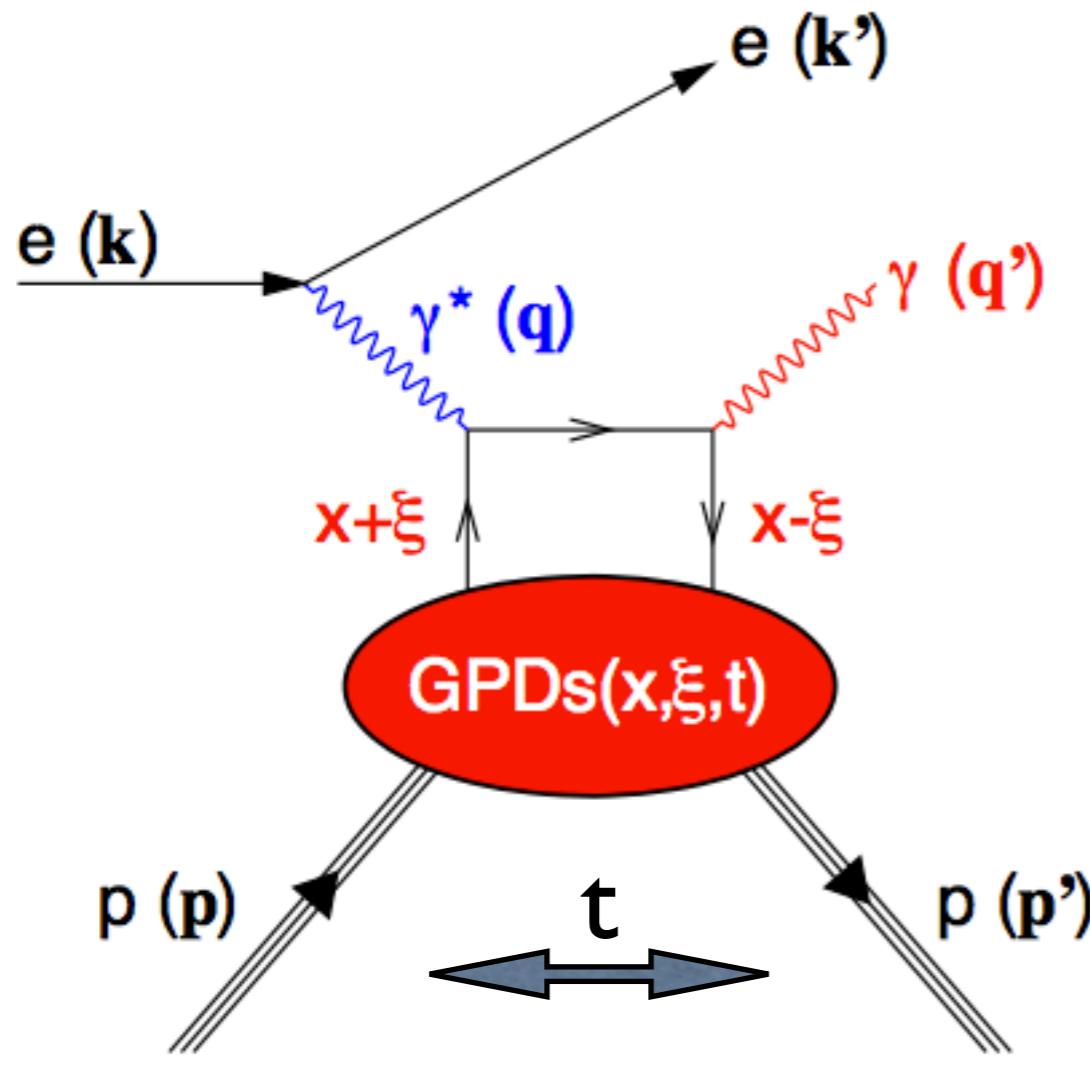
ξ - half the change in the longitudinal momentum of the active quark.

$$\Delta\Sigma + L_Q = J_Q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 [H(x, \xi, t) + E(x, \xi, t)] x dx$$

“Ji’s Relation”

Phys. Rev. Lett. 78:610, 1997

GPDs



Four GPDs: $H, \tilde{H}, E, \tilde{E}$

Constrained by PDFs and
Form Factors

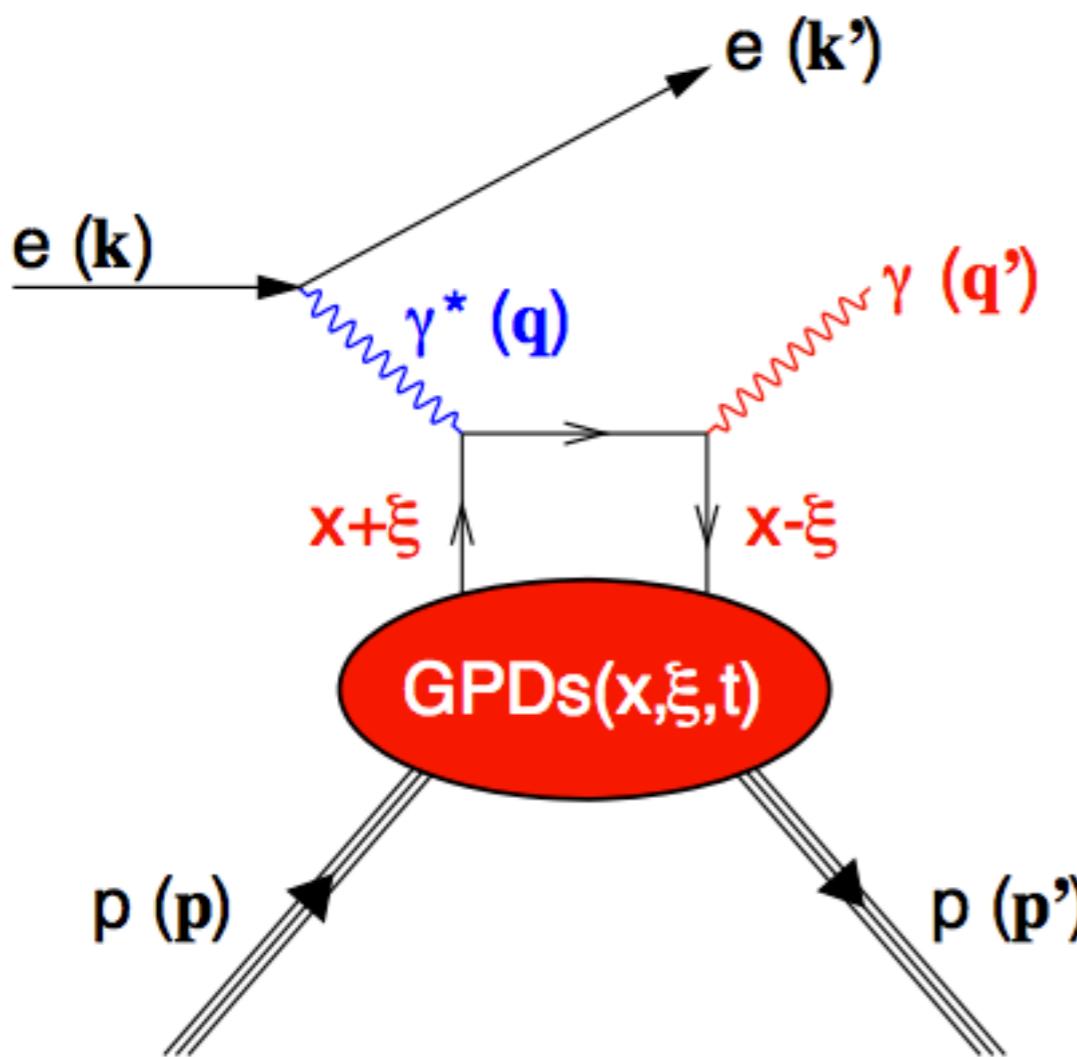
Offer a possible solution to
the spin crisis!

$$\Delta\Sigma + L_Q = J_Q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 [H(x, \xi, t) + E(x, \xi, t)] x dx$$

“Ji’s Relation”

Phys. Rev. Lett. 78:610, 1997

Exclusive Physics



$$\frac{d\sigma}{dx_B dQ^2 d|t| d\phi} = \frac{x_B e^6 |\tau|^2}{32(2\pi)^4 Q^4 \sqrt{1 + \epsilon^2}}$$

$$|\tau|^2 = |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + \underbrace{\tau_{\text{BH}} \tau_{\text{DVCS}}^* + \tau_{\text{BH}}^* \tau_{\text{DVCS}}}_{\mathcal{I}}$$

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+(\phi) - d\sigma^-(\phi)}{d\sigma^+(\phi) + d\sigma^-(\phi)}$$

$$\mathcal{A}_{\text{LU}}(\phi) \equiv \frac{[\sigma^{\rightarrow\leftarrow}(\phi) + \sigma^{\rightarrow\Rightarrow}(\phi)] - [\sigma^{\leftarrow\leftarrow}(\phi) + \sigma^{\leftarrow\Rightarrow}(\phi)]}{[\sigma^{\rightarrow\leftarrow}(\phi) + \sigma^{\rightarrow\Rightarrow}(\phi)] + [\sigma^{\leftarrow\leftarrow}(\phi) + \sigma^{\leftarrow\Rightarrow}(\phi)]}$$

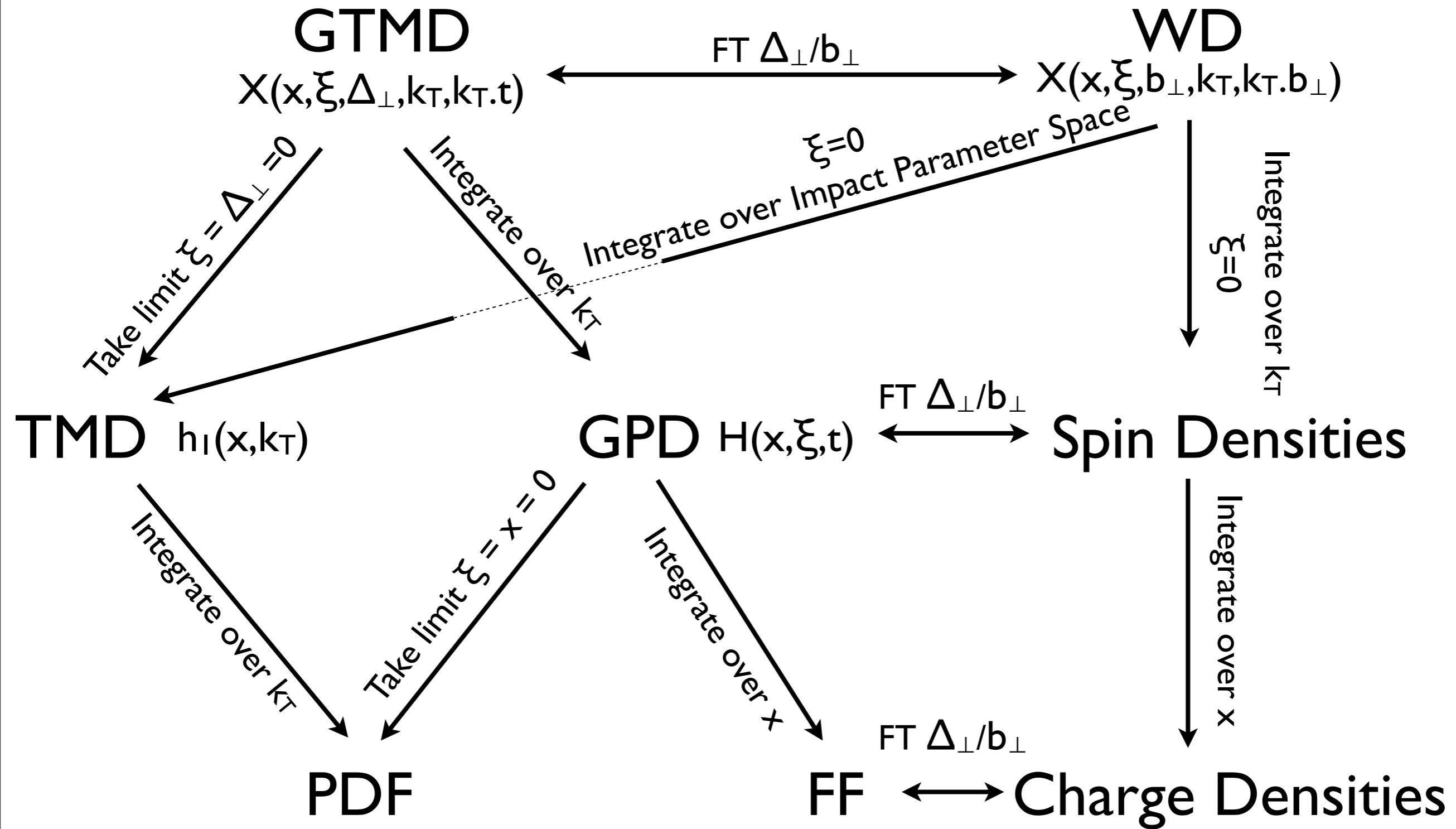
$$\mathcal{A}_{\text{UL}}(\phi) \equiv \frac{[\sigma^{\leftarrow\Rightarrow}(\phi) + \sigma^{\rightarrow\Rightarrow}(\phi)] - [\sigma^{\leftarrow\leftarrow}(\phi) + \sigma^{\rightarrow\leftarrow}(\phi)]}{[\sigma^{\leftarrow\Rightarrow}(\phi) + \sigma^{\rightarrow\Rightarrow}(\phi)] + [\sigma^{\leftarrow\leftarrow}(\phi) + \sigma^{\rightarrow\leftarrow}(\phi)]}$$

$$\mathcal{A}_{\text{LL}}(\phi) \equiv \frac{[\sigma^{\rightarrow\Rightarrow}(\phi) + \sigma^{\leftarrow\leftarrow}(\phi)] - [\sigma^{\leftarrow\Rightarrow}(\phi) + \sigma^{\rightarrow\leftarrow}(\phi)]}{[\sigma^{\rightarrow\Rightarrow}(\phi) + \sigma^{\leftarrow\leftarrow}(\phi)] + [\sigma^{\leftarrow\Rightarrow}(\phi) + \sigma^{\rightarrow\leftarrow}(\phi)]}$$

Wigner Distributions & GTMDs

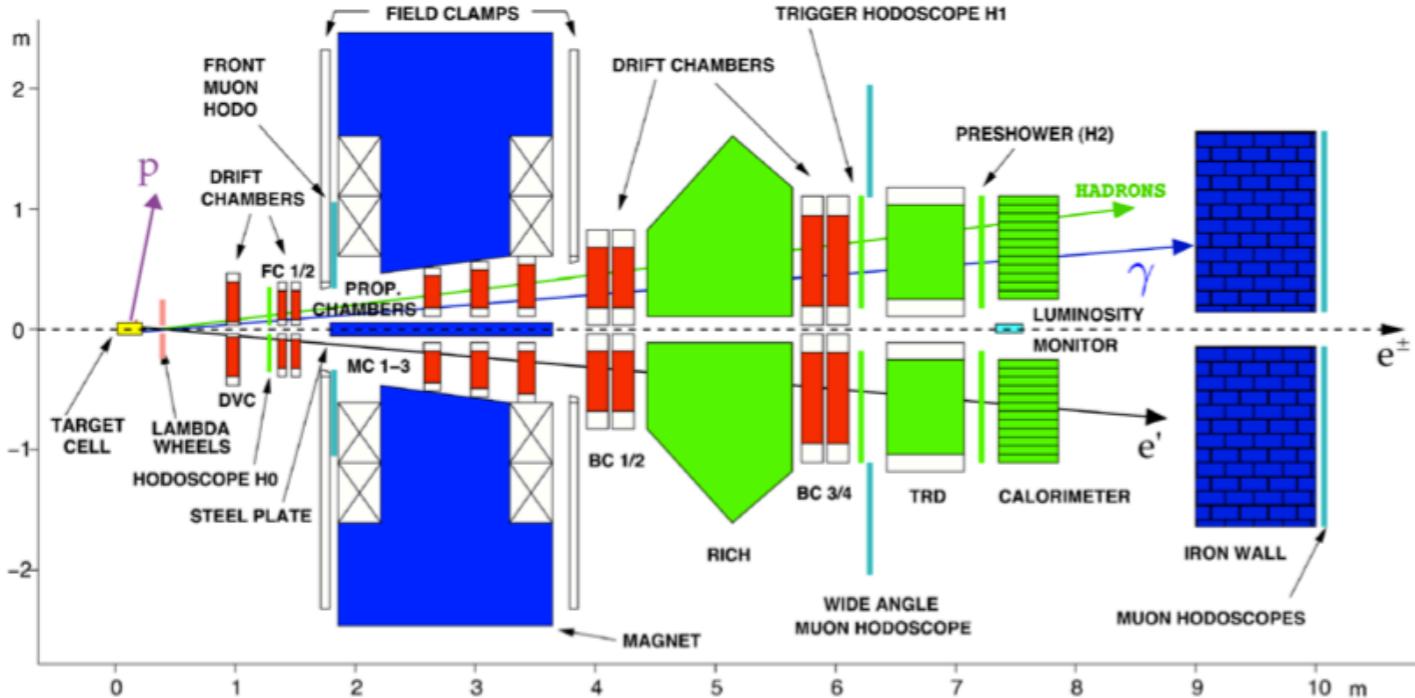
- Holy grail is WDs and GTMDs; not currently accessible through experiment
- Can access TMDs and GPDs experimentally
- WDs and GTMDs reduce to ‘ordinary distributions’ as limits and moments

Distribution Graph

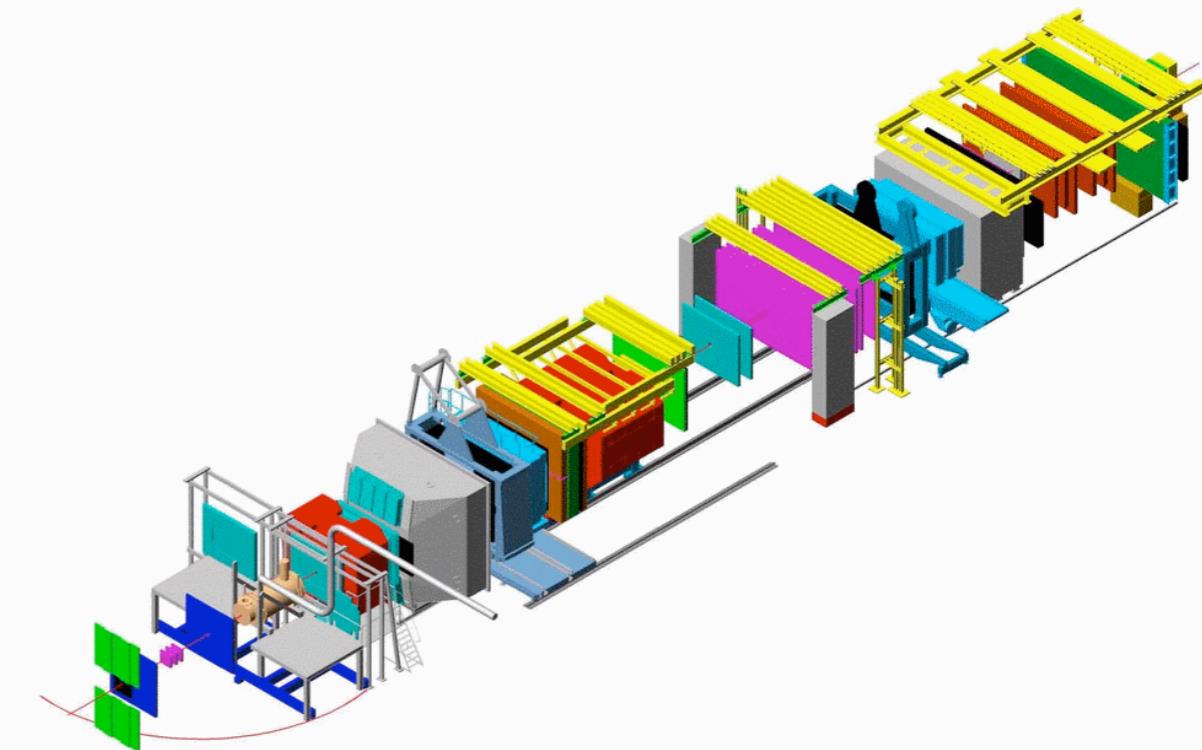
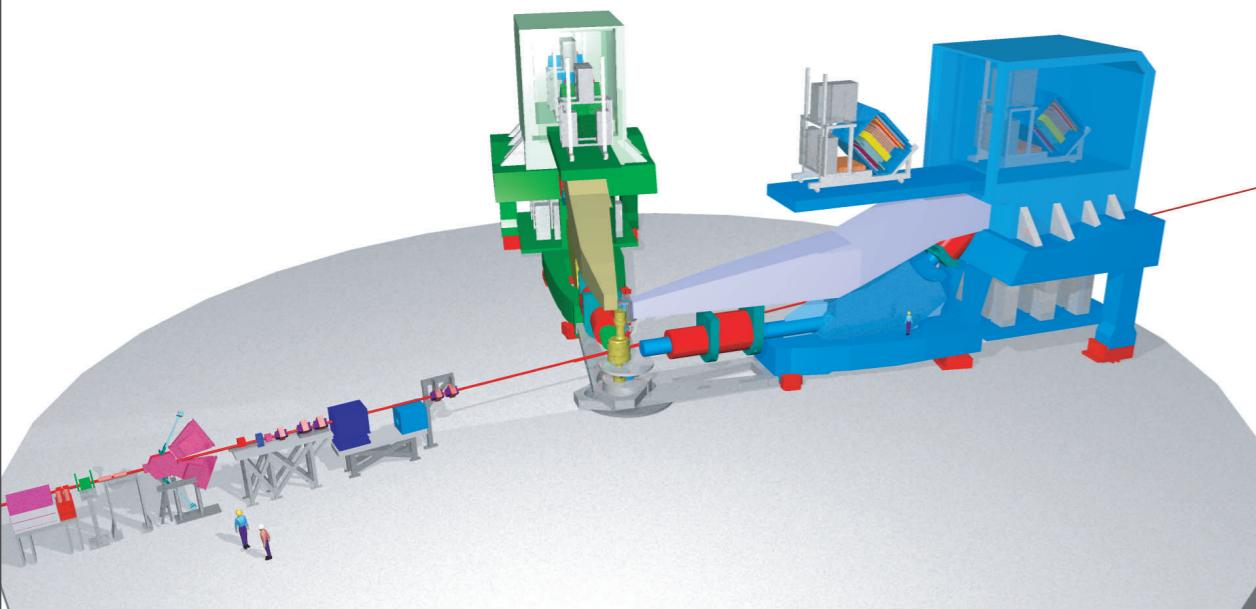
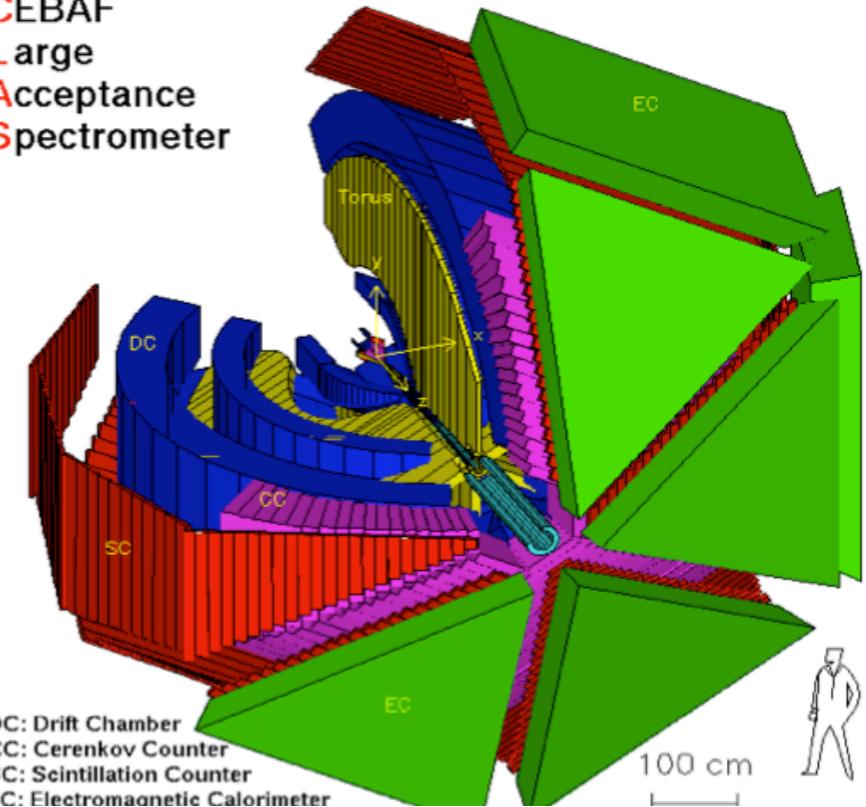


Experimental Access

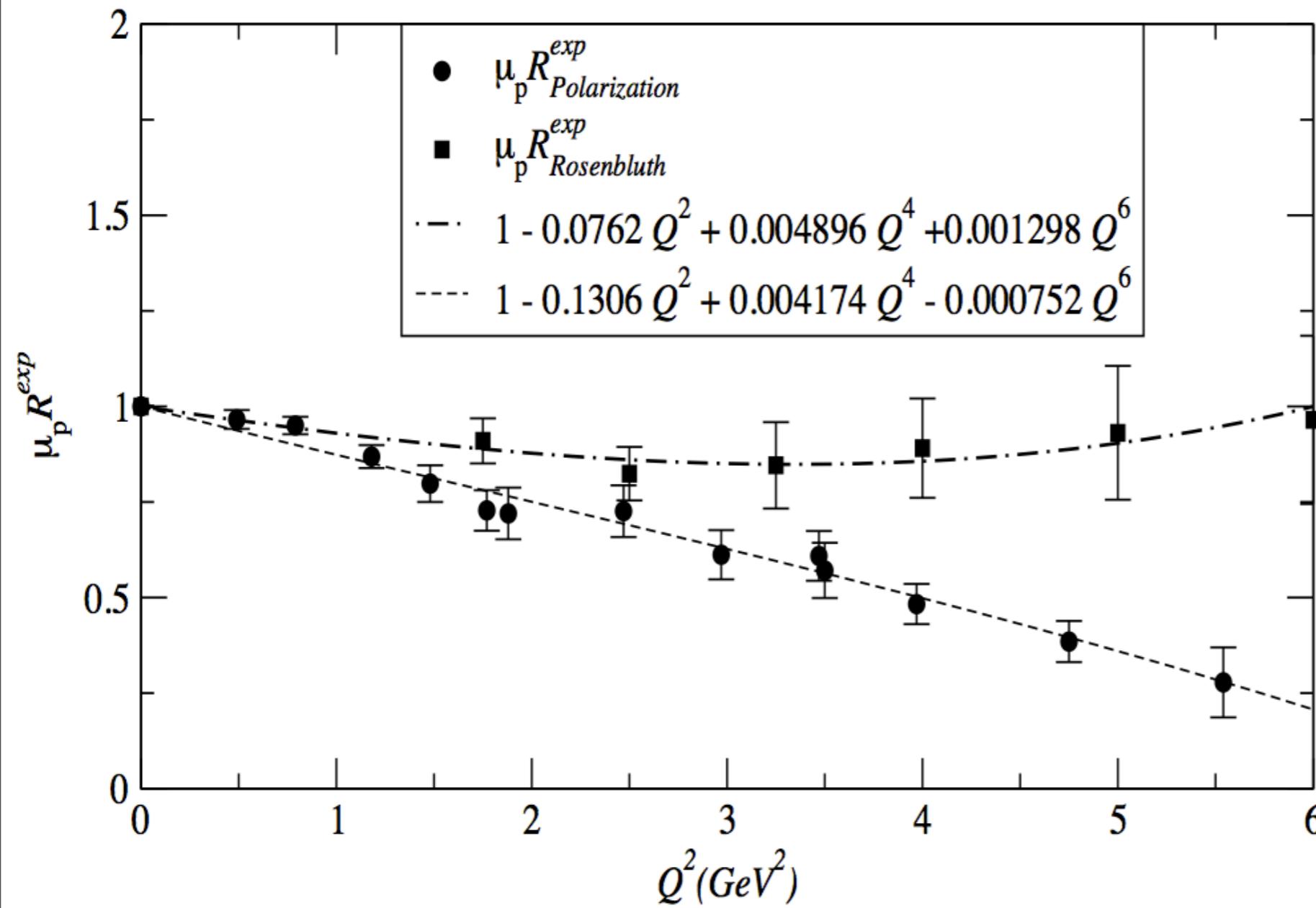
“Current” Experiments



CEBAF
Large
Acceptance
Spectrometer



Form Factors



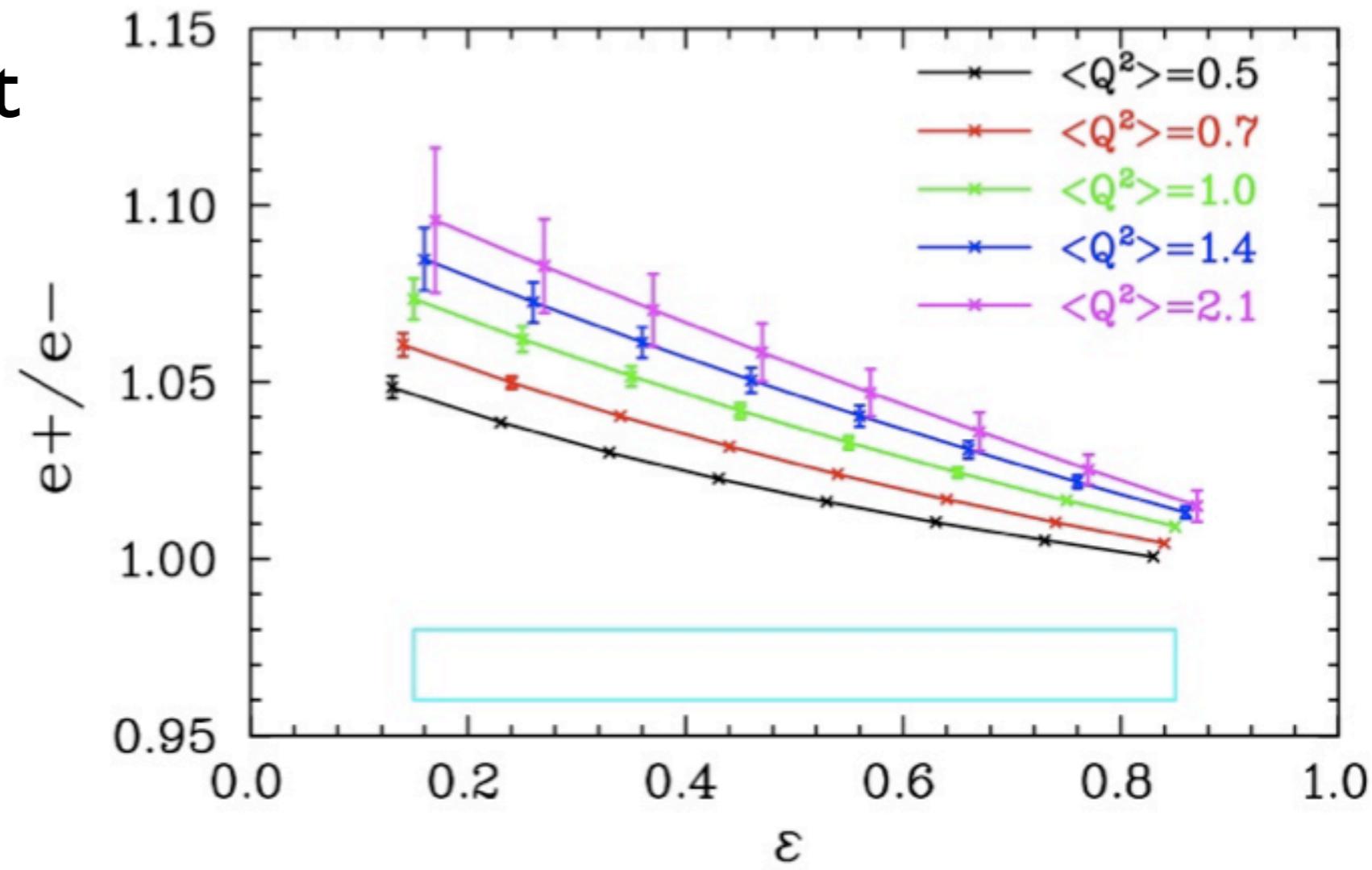
Race to check the calculations with data!

Can a 2γ -exchange correction explain the difference between Rosenbluth and Polarization transfer methods?

Form Factors

“Dirty” e^+/e^- beam at CLAS has high statistical precision across many bins

Novel beam technique presents challenges to the calculation of systematic errors

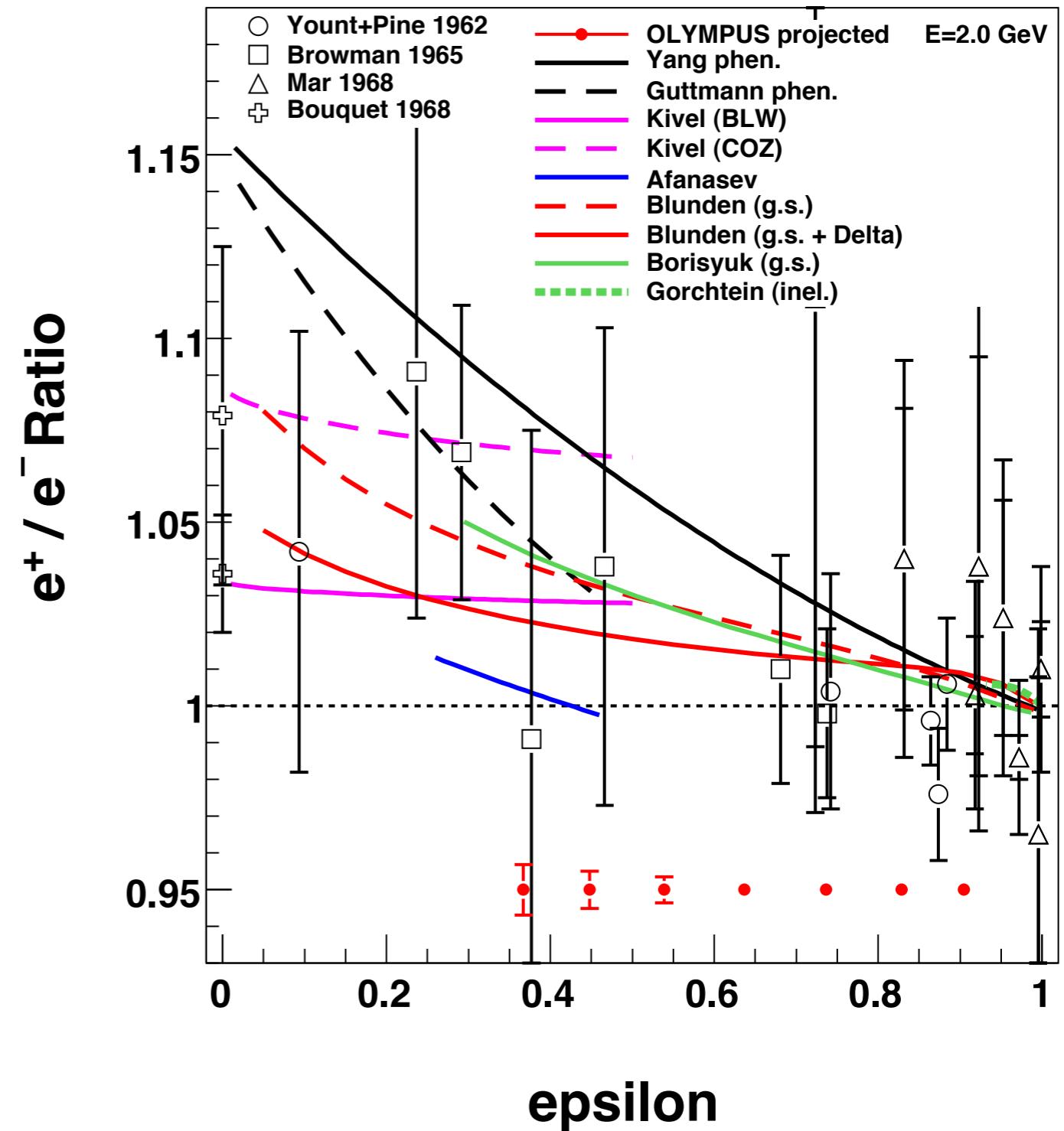


Data taken and currently undergoing analysis!

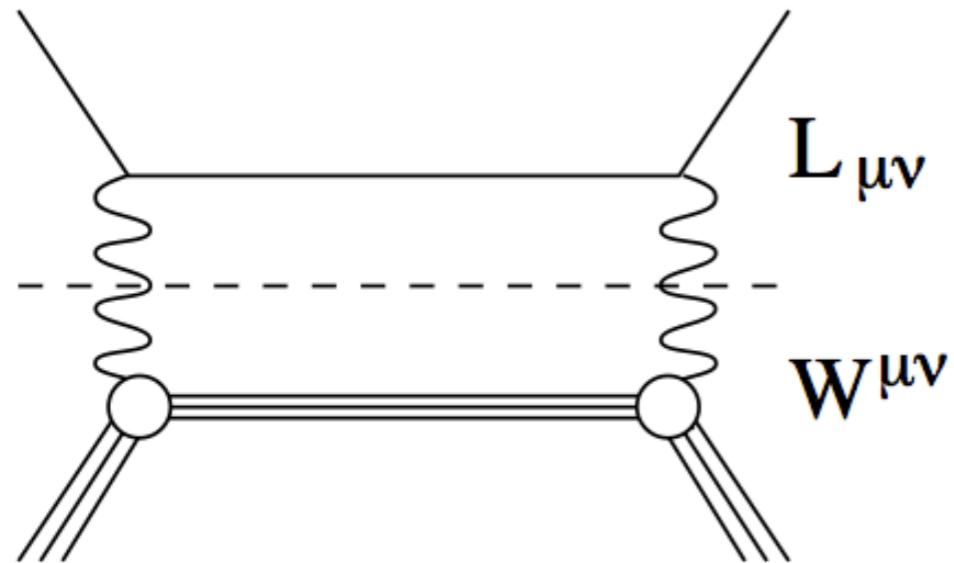
Form Factors

OLYMPUS transported
BLAST to
DORIS@DESY and plan
to take data next year

Reuse of understood
equipment \Rightarrow quick
analysis and simple
uncertainty calculations



Structure Functions



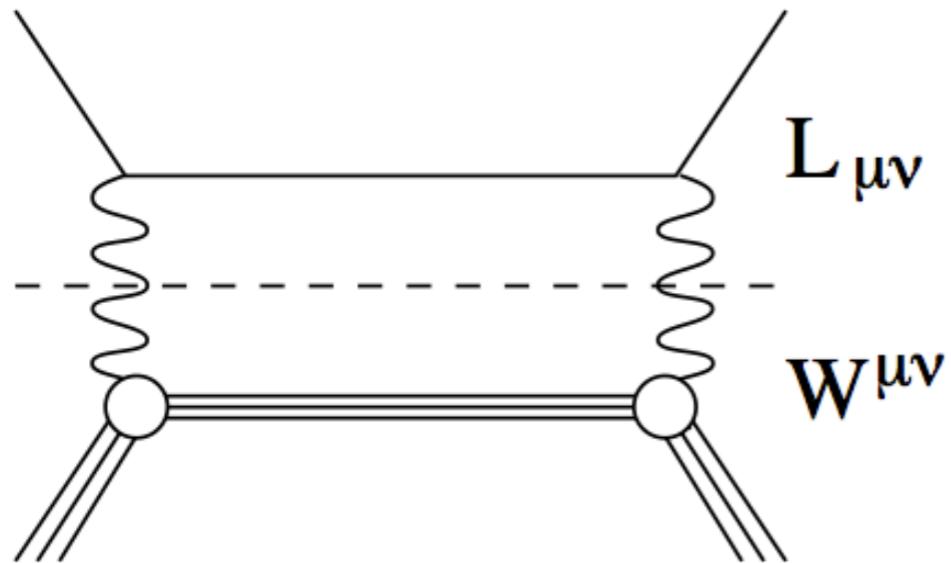
Deep Inelastic Scattering (DIS)

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha^2}{2MQ^4} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$$

$$L_{\mu\nu} = 2[k_\mu k'_\nu + k'_\mu k_\nu - g_{\mu\nu}(k \cdot k' - m^2) - i\epsilon_{\mu\nu\alpha\beta} s_l^\alpha q^\beta]$$

$$\begin{aligned} W_{\mu\nu} &= F_1(-g_{\mu\nu} + \frac{q_\mu q_\nu}{p \cdot q}) + \frac{F_2}{p \cdot q} (p_\mu - \frac{p \cdot q q_\mu}{q^2})(p_\nu - \frac{p \cdot q q_\nu}{q^2}) \\ &+ \frac{i g_1}{p \cdot q} \epsilon_{\mu\nu\lambda\sigma} q^\lambda s_h^\sigma + \frac{i g_2}{(f \cdot q)^2} \epsilon_{\mu\nu\lambda\sigma} q^\lambda (p \cdot q s_h^\sigma - s_h \cdot q p^\sigma) \end{aligned}$$

Structure Functions



Deep Inelastic Scattering (DIS)

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha^2}{2MQ^4} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$$

$$L_{\mu\nu} = 2[k_\mu k'_\nu + k'_\mu k_\nu - g_{\mu\nu}(k \cdot k' - m^2) - i\epsilon_{\mu\nu\alpha\beta} s_l^\alpha q^\beta]$$

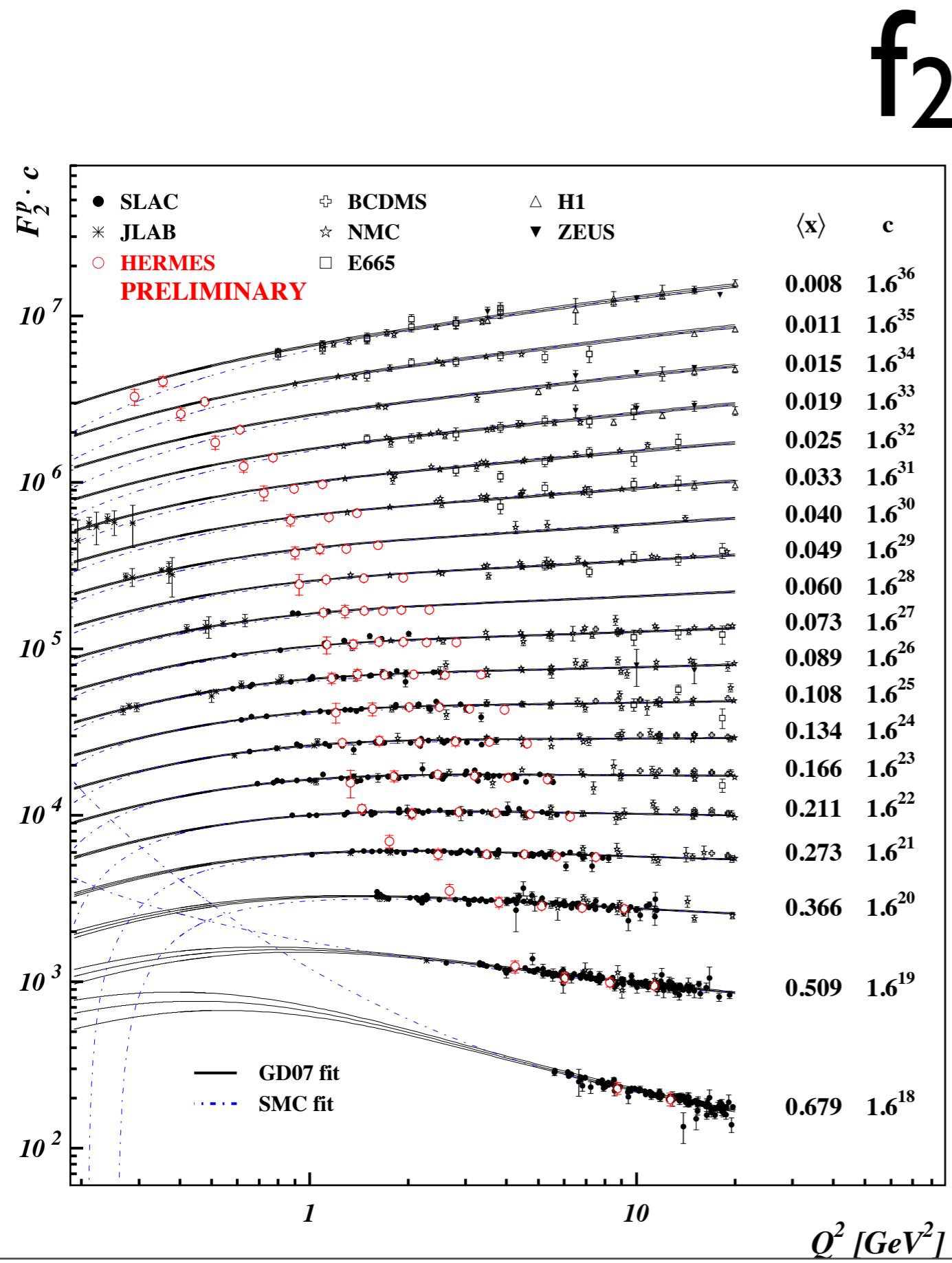
$$\begin{aligned} W_{\mu\nu} &= F_1 \left(-g_{\mu\nu} + \frac{q_\mu q_\nu}{p \cdot q} \right) + \frac{F_2}{p \cdot q} \left(p_\mu - \frac{p \cdot q q_\mu}{q^2} \right) \left(p_\nu - \frac{p \cdot q q_\nu}{q^2} \right) \\ &+ \frac{i g_1}{p \cdot q} \epsilon_{\mu\nu\lambda\sigma} q^\lambda s_h^\sigma + \frac{i g_2}{(f \cdot q)^2} \epsilon_{\mu\nu\lambda\sigma} q^\lambda (p \cdot q s_h^\sigma - s_h \cdot q p^\sigma) \end{aligned}$$

Structure Functions

Quark Polarization

		U	L	T
U		f_1		h_1^\perp
L			g_{1L}	h_{1L}^\perp
T		f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

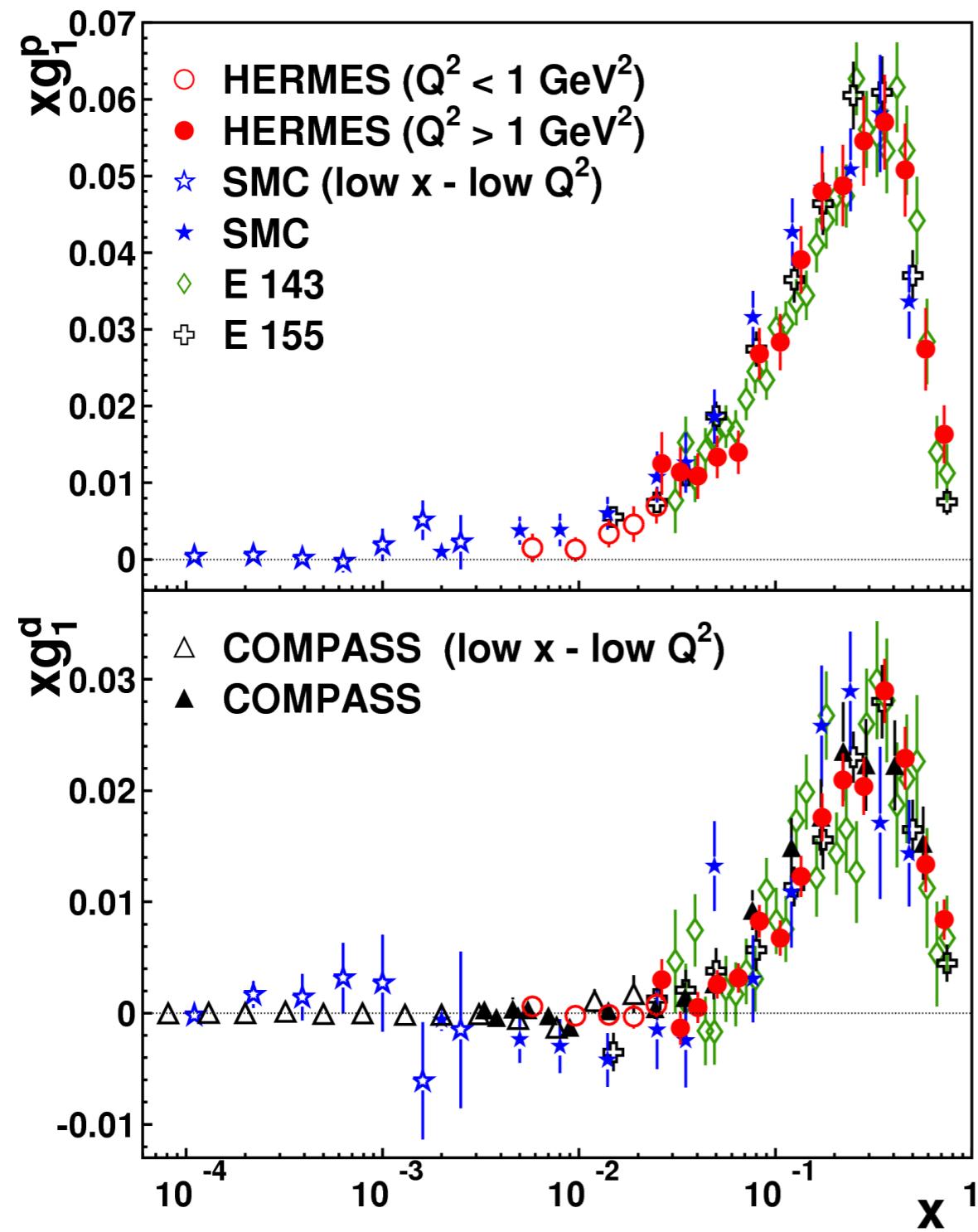
Y-axis label: Nucleon Polarization



f_2 is well mapped-out at a large x-range by fixed-target and collider experiments

f_2 is easily the
best
understood
structure
function!

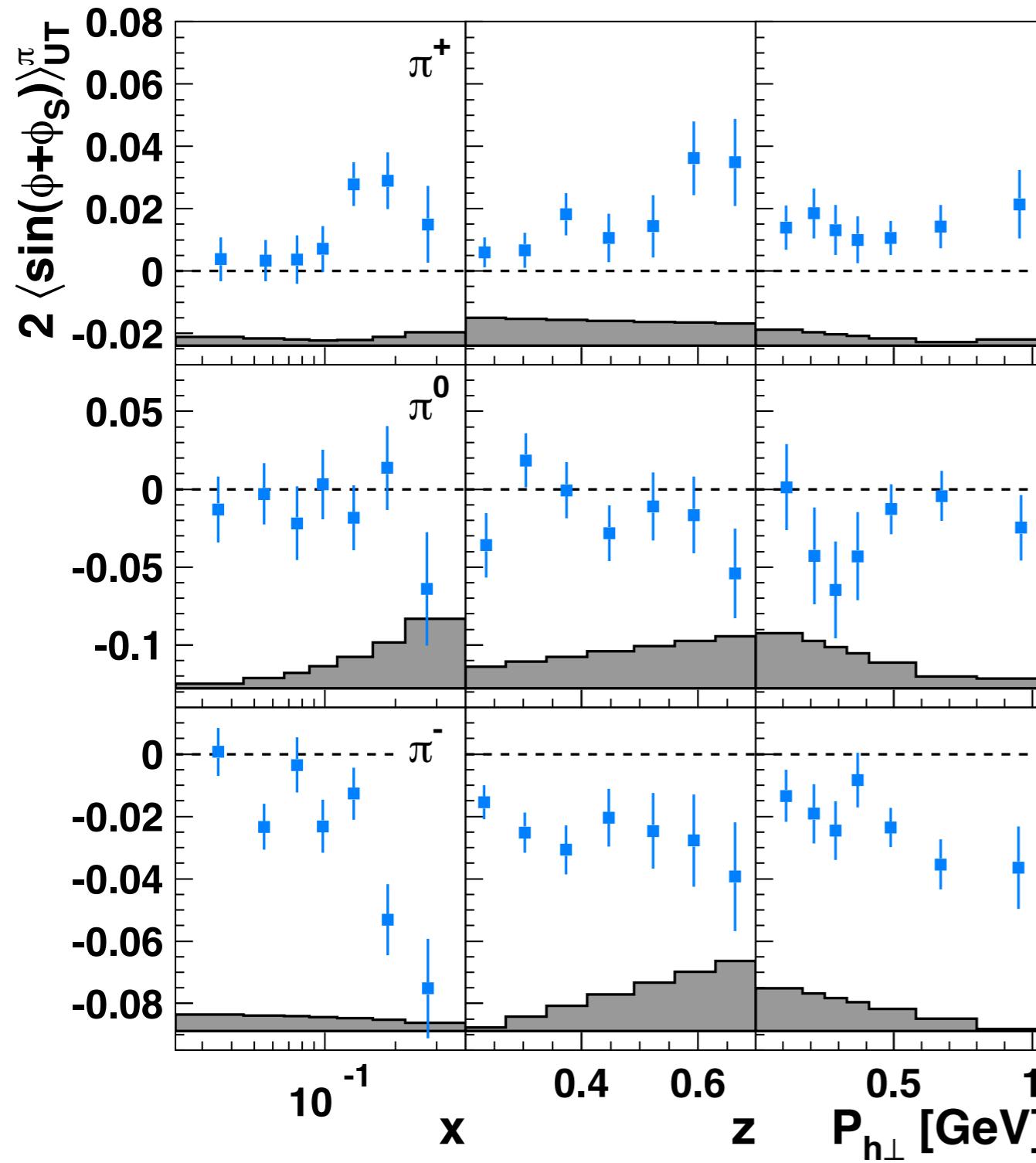
g_I



$g_I(x)$ measured in the
valence region and
into the sea

Measurements imply
an unpolarized sea

Results from HERMES

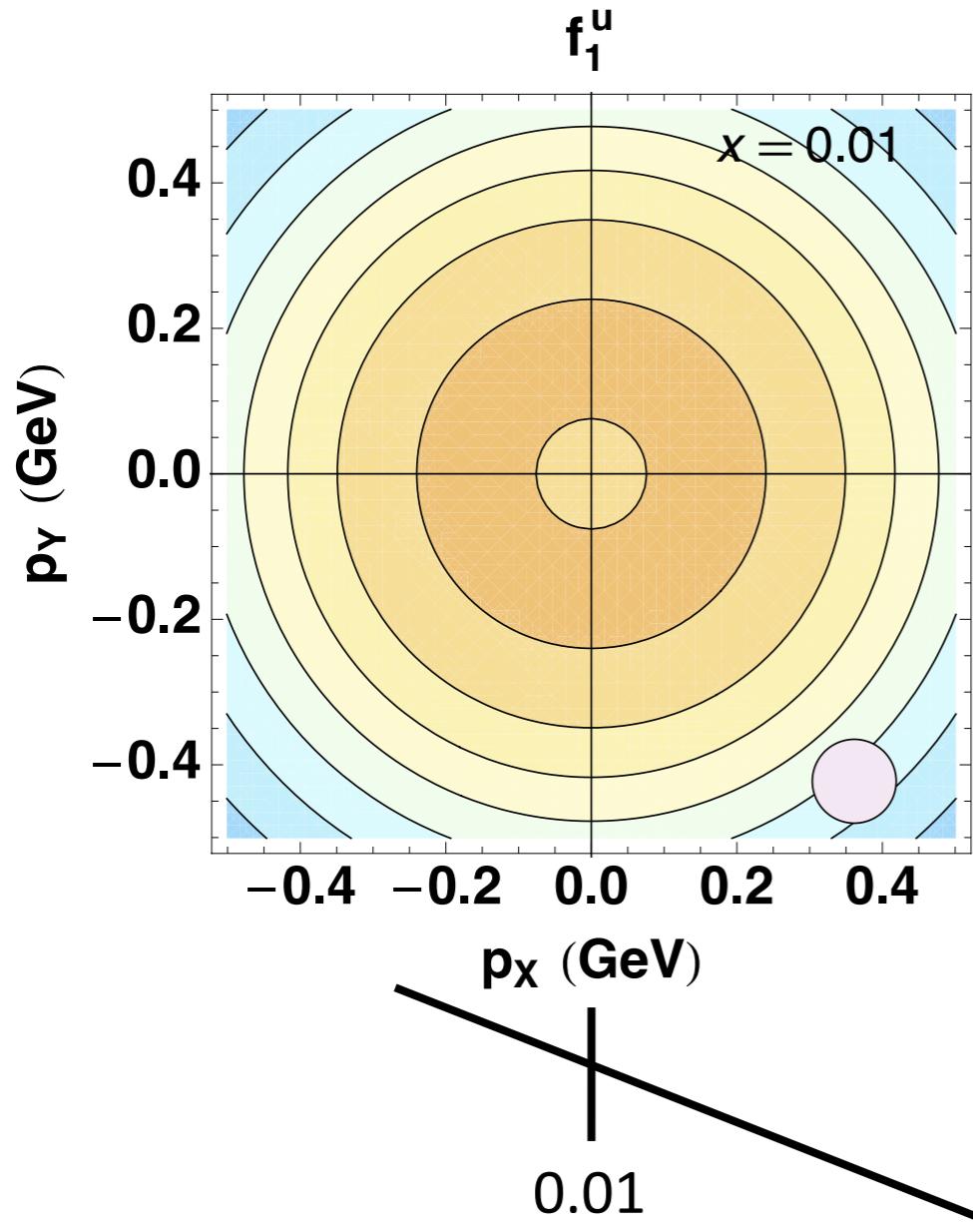


Collins moments for
pions **allows access** to h_1

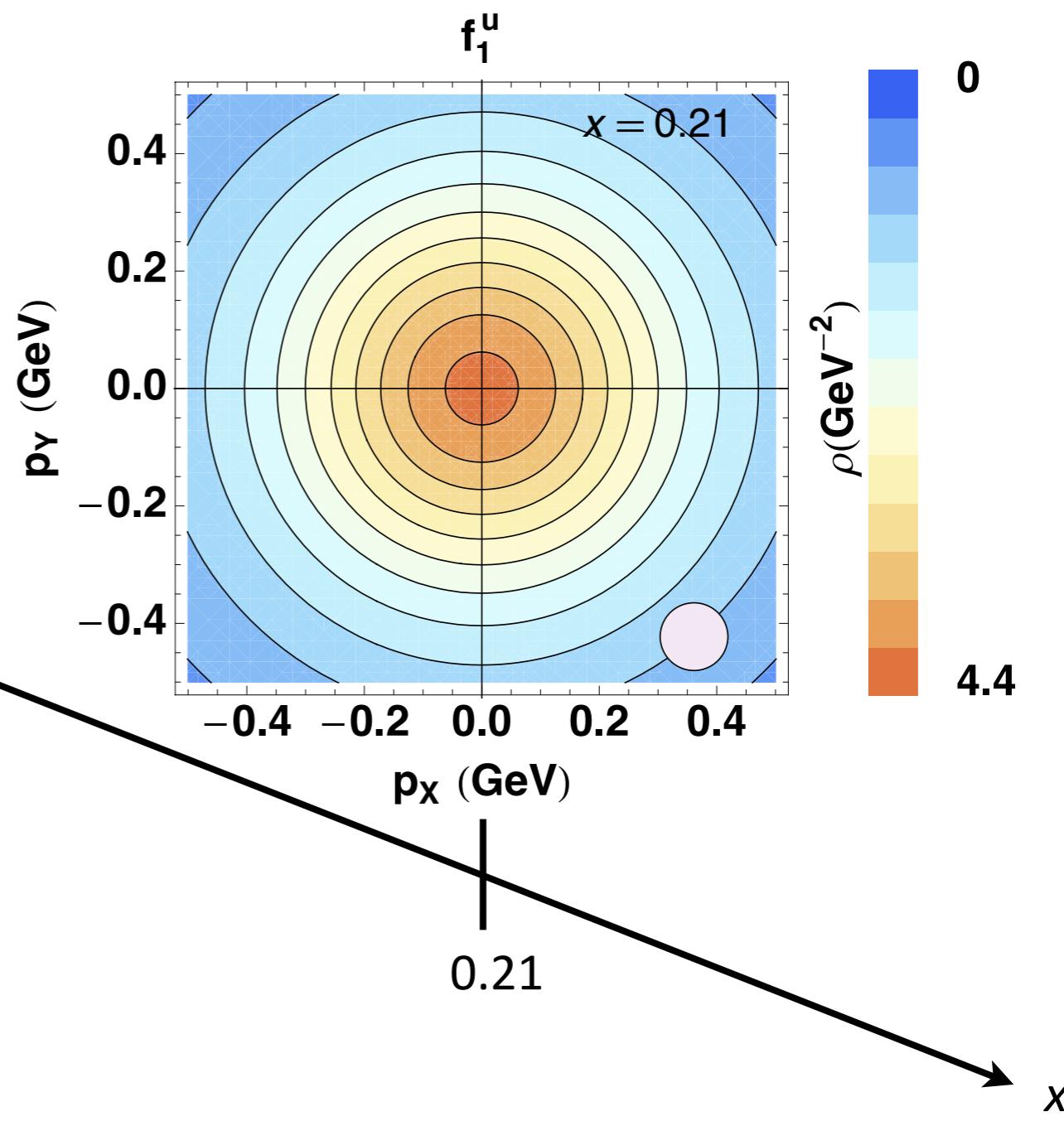
**Use meson charges as
quark flavor filters!**

Significant differences
between quark flavors
shows that $h_{1(u)} \neq h_{1(d)}$

TMDs: tomography in momentum space



Based on model calculation
A.B., Conti, Guagnelli, Radici, arXiv:1003.1328



TMDs

Quark Polarization

		U	L	T
Nucleon Polarization	U	f_1		h_1^\perp
	L		g_{1L}	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

TMDs

Quark Polarization

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Nucleon Polarization

Unpolarized, helicity, transversity and Sivers
distributions are familiar to most!

TMDs

Quark Polarization

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Nucleon Polarization

Indications of Boer-Mulders from unpolarized lepton-nucleon scattering

TMDs

Quark Polarization

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Nucleon Polarization

The x -dependence may be known, but the k_T -dependence almost never is!

Results from HERMES

Semi-Inclusive Deep Inelastic Scattering

- Sivers moment \Rightarrow quark OAM
- Different meson-types provide a flavor-filter

Results from HERMES

Positive!

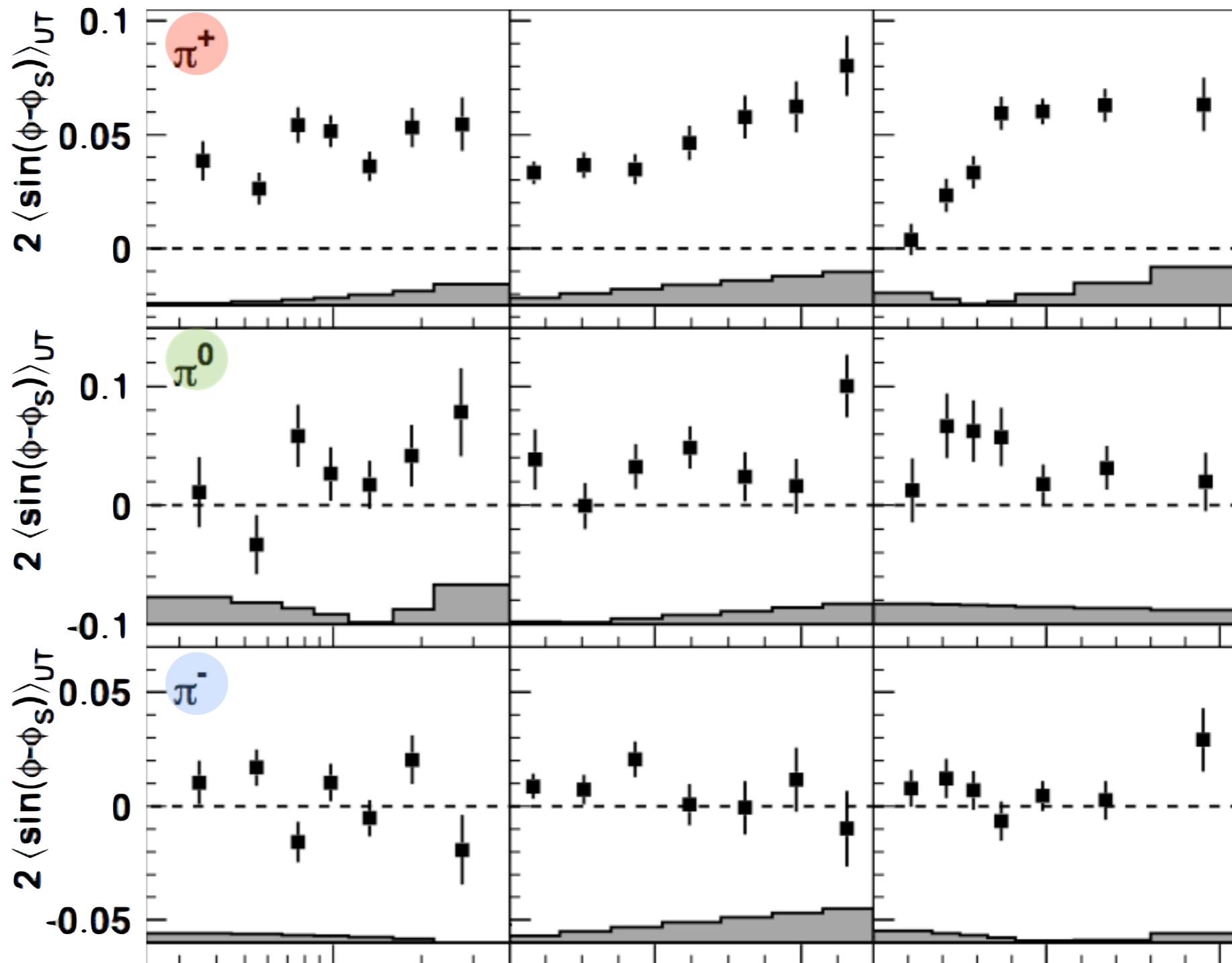
$u\bar{d}$

Positive?

uu or dd

Zero!

$d\bar{u}$



Results from HERMES

Sivers Moments

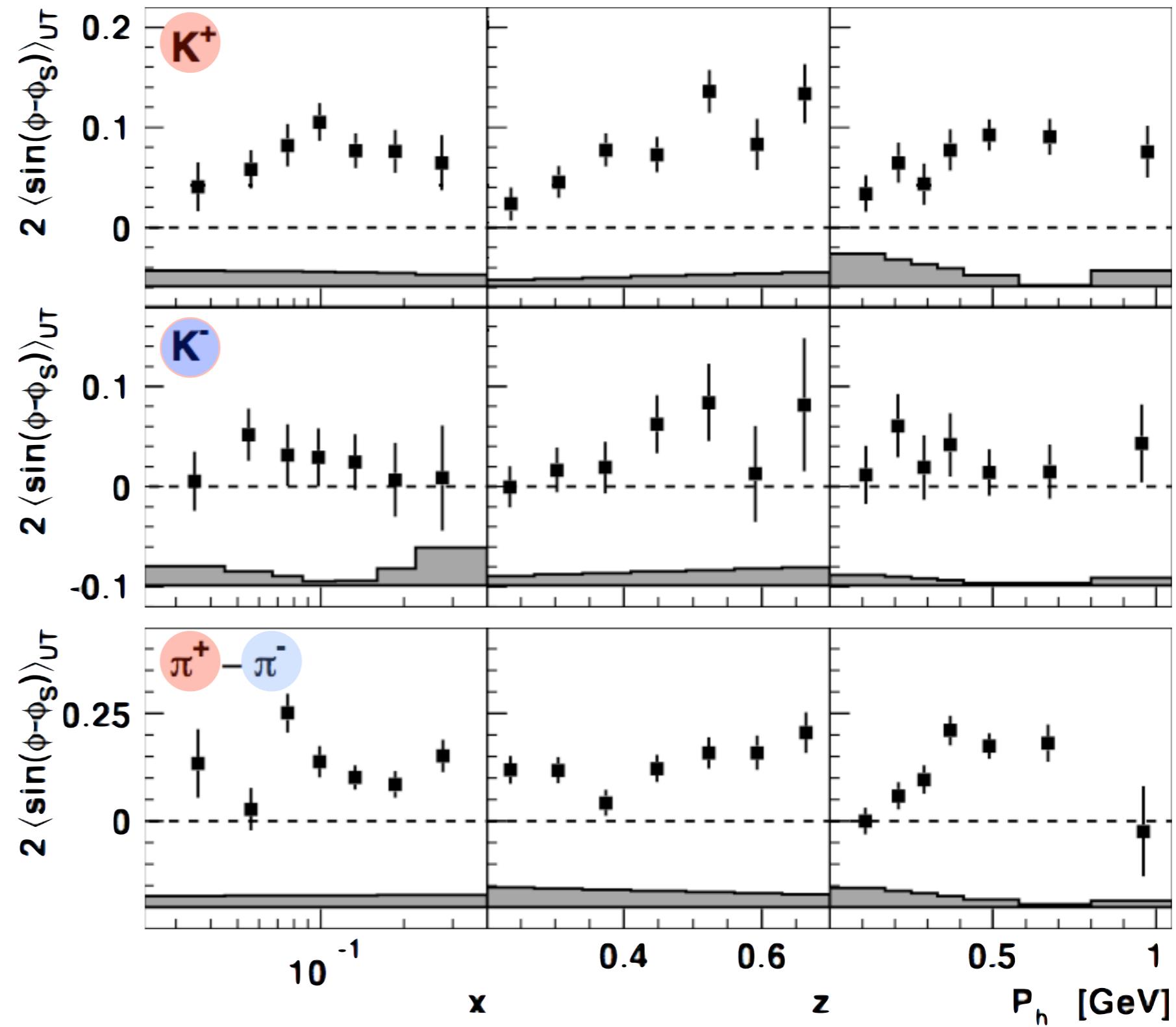
Positive!

$u\bar{s}$

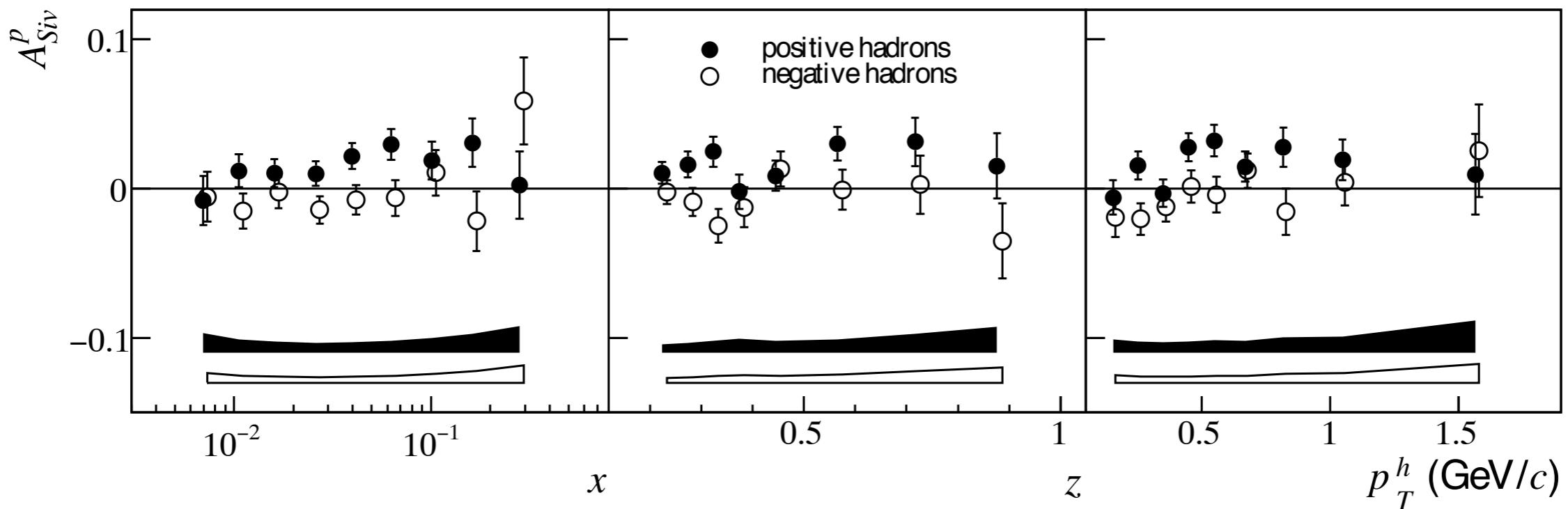
Positive?

$s\bar{u}$

Valence



Results from COMPASS

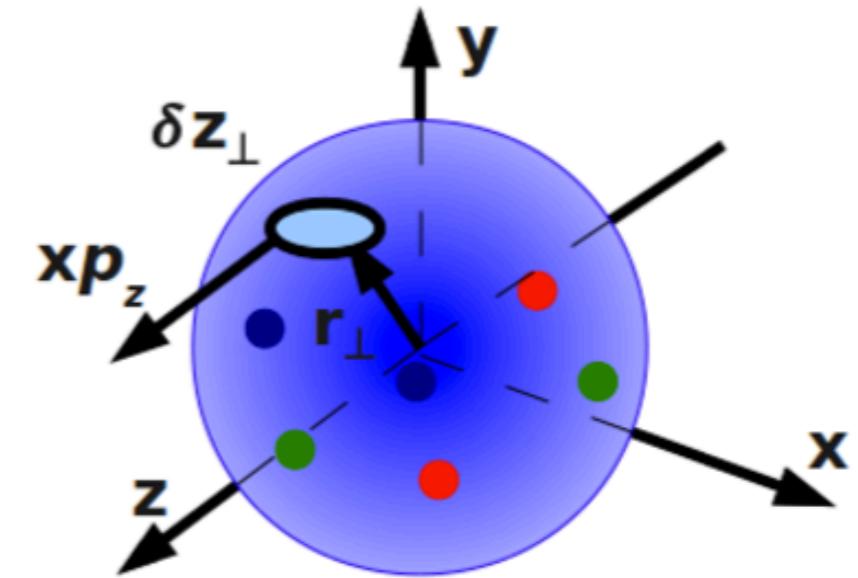
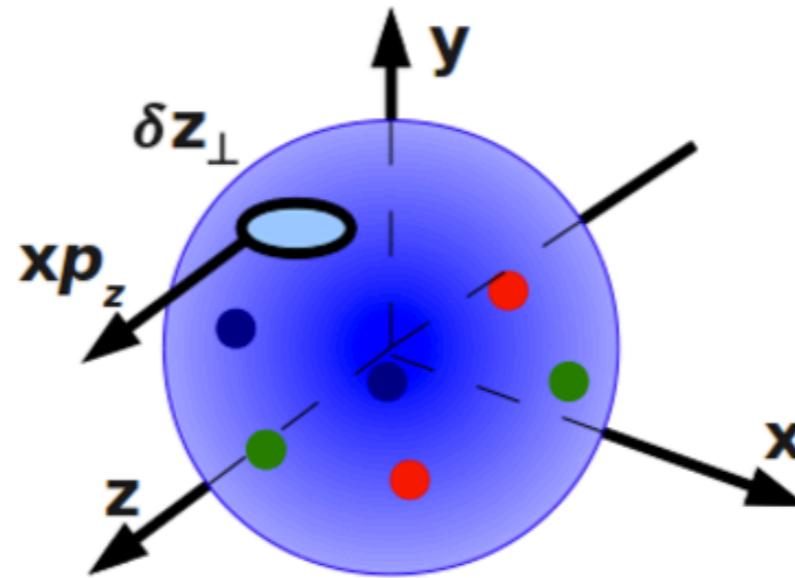
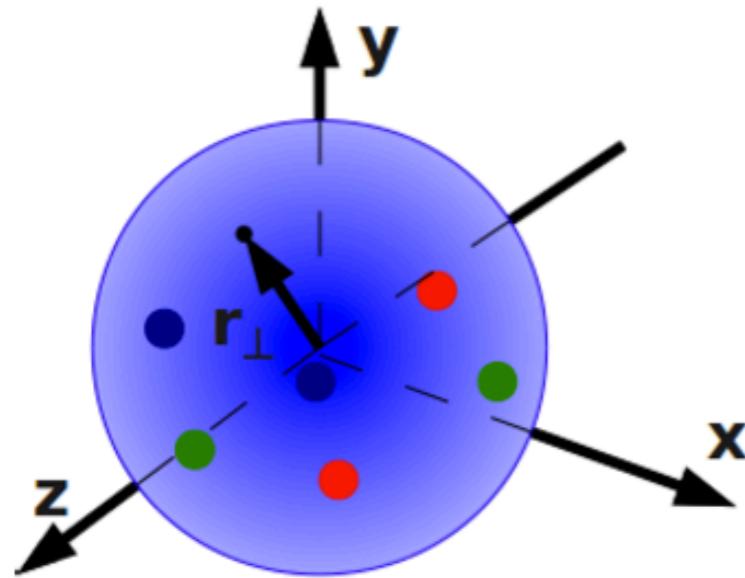


Results from COMPASS confirm HERMES observations

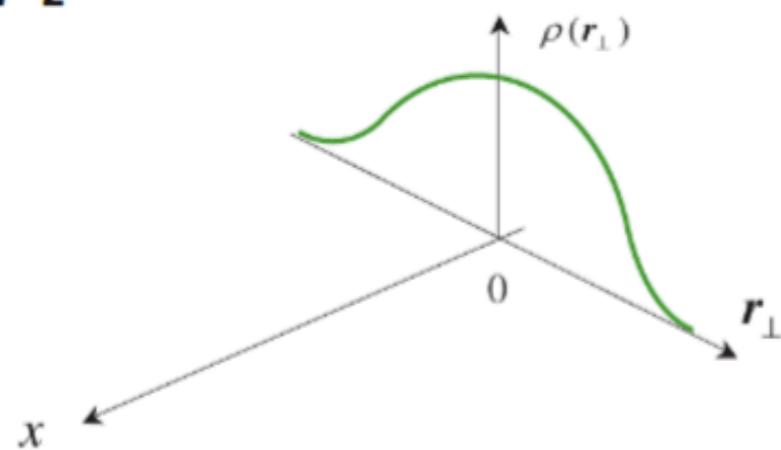
SIDIS

- Results indicate that $h_{1u}(x) \neq h_{1d}(x)$ and $f_{1\perp}(x, k_T) \neq 0$ for up-quarks or sea quarks
- Gives rise to a picture of the nucleon as having up quarks with transverse momentum but “stationary” down quarks
- Results are not thorough: cannot extract a picture of nucleon structure (valence, sea and glue) from these alone!

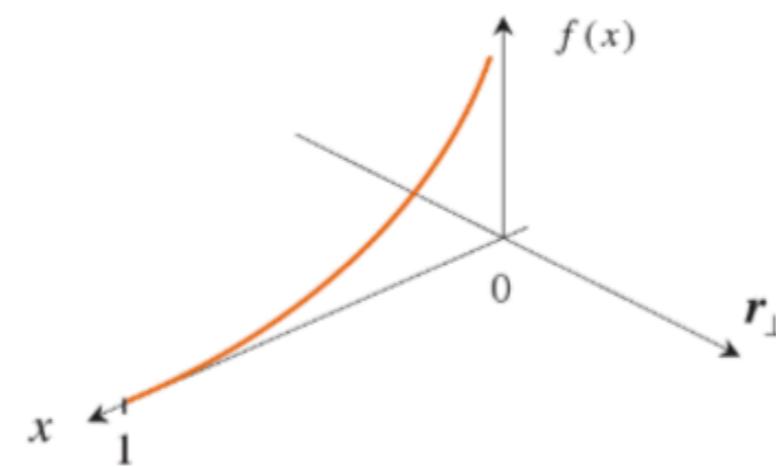
GPDs



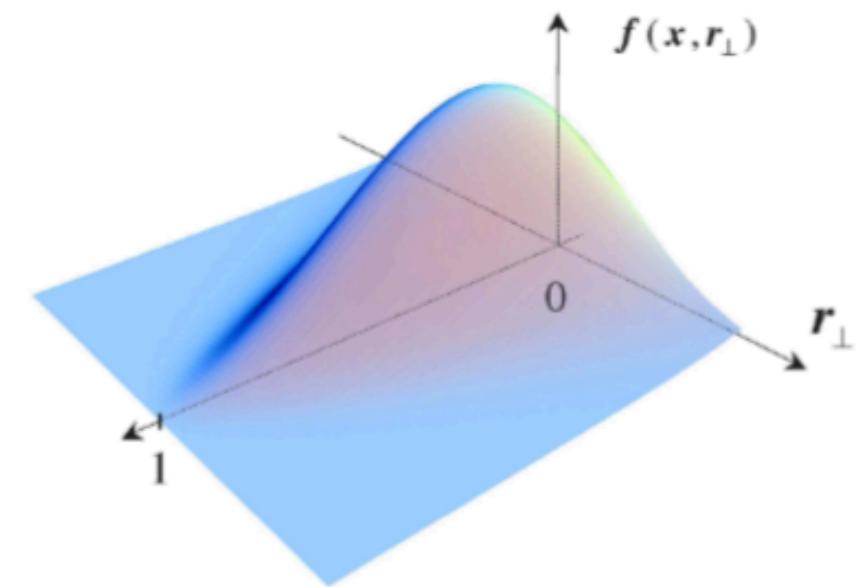
$p_z \rightarrow \infty$



Form Factors (FFs)

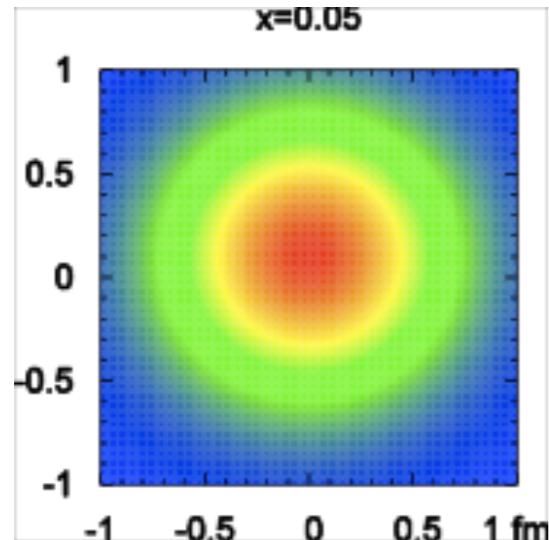


Parton Distribution Functions (PDFs)

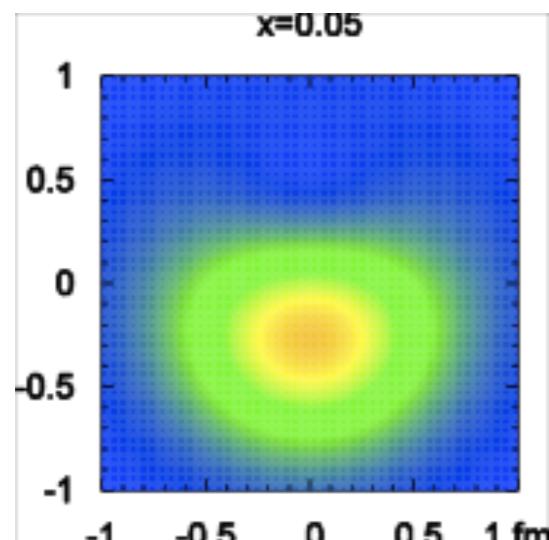


Generalised Parton Distributions (GPDs)

GPDs



Up Quarks



Down Quarks

“Hadron Tomography” is the phrase du jour

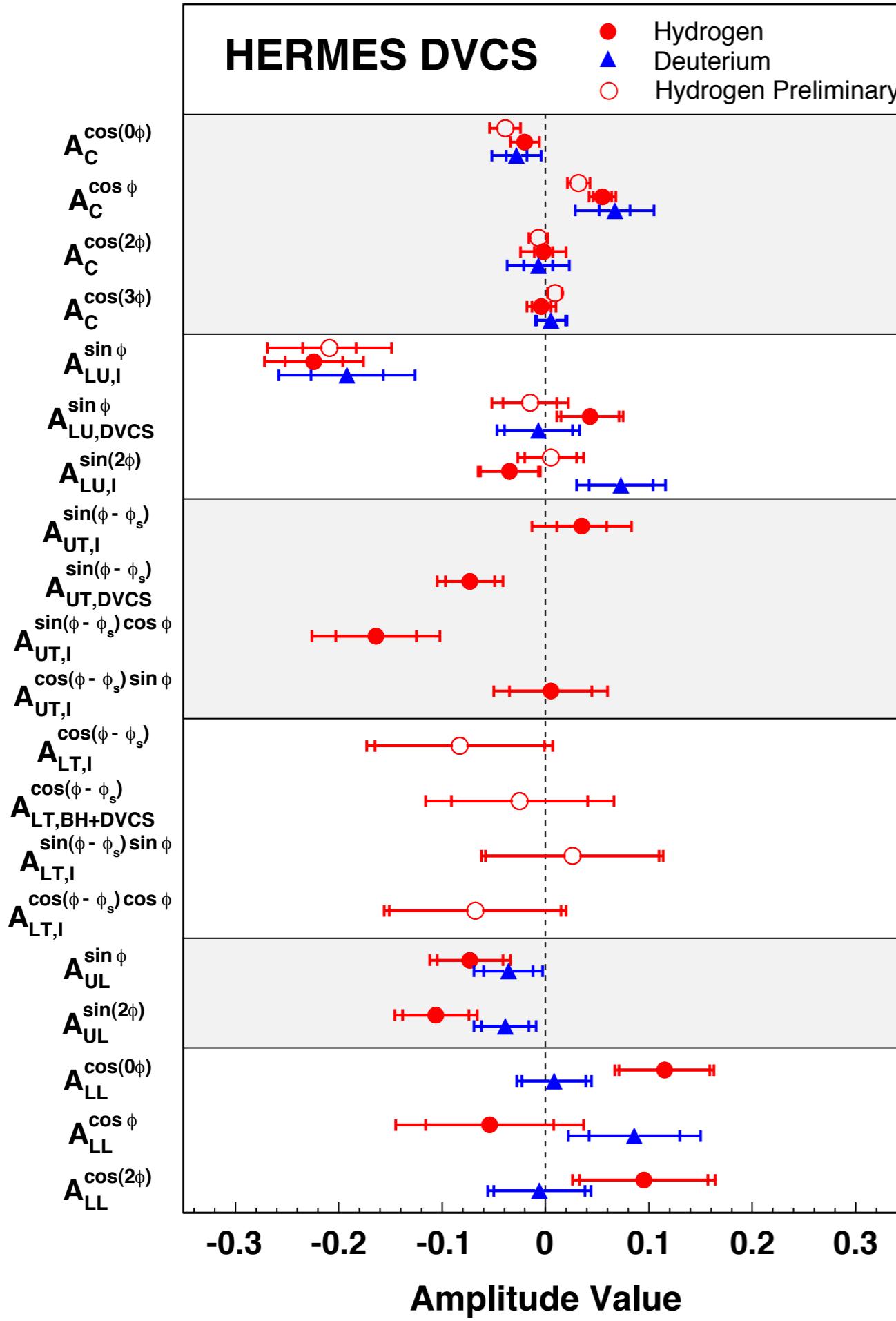
Simple models trained with meson data already illustrate the intuitive picture offered by GPDs

Not simple to get to GPD information: go through CFFs first!

Results from HERMES

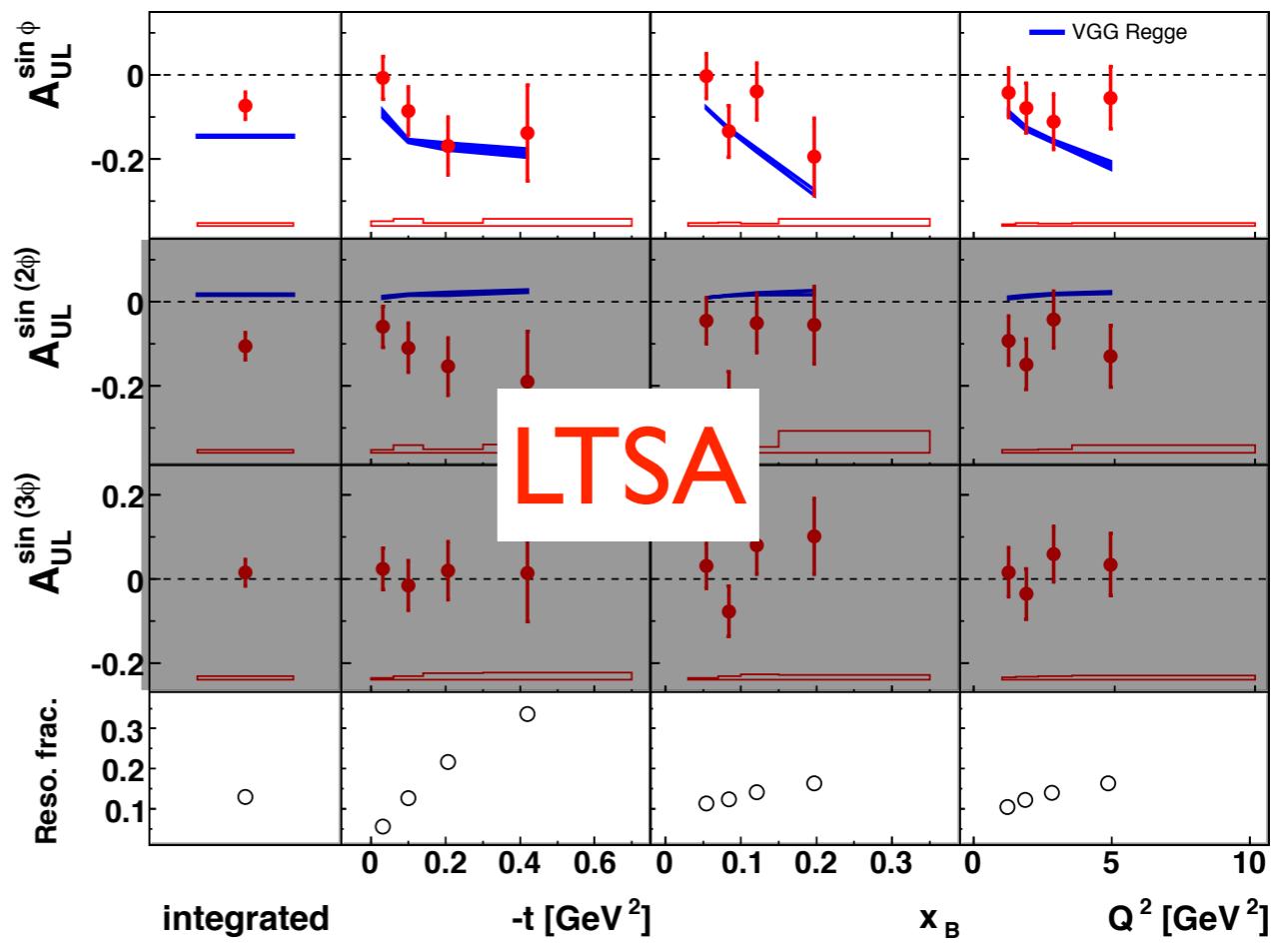
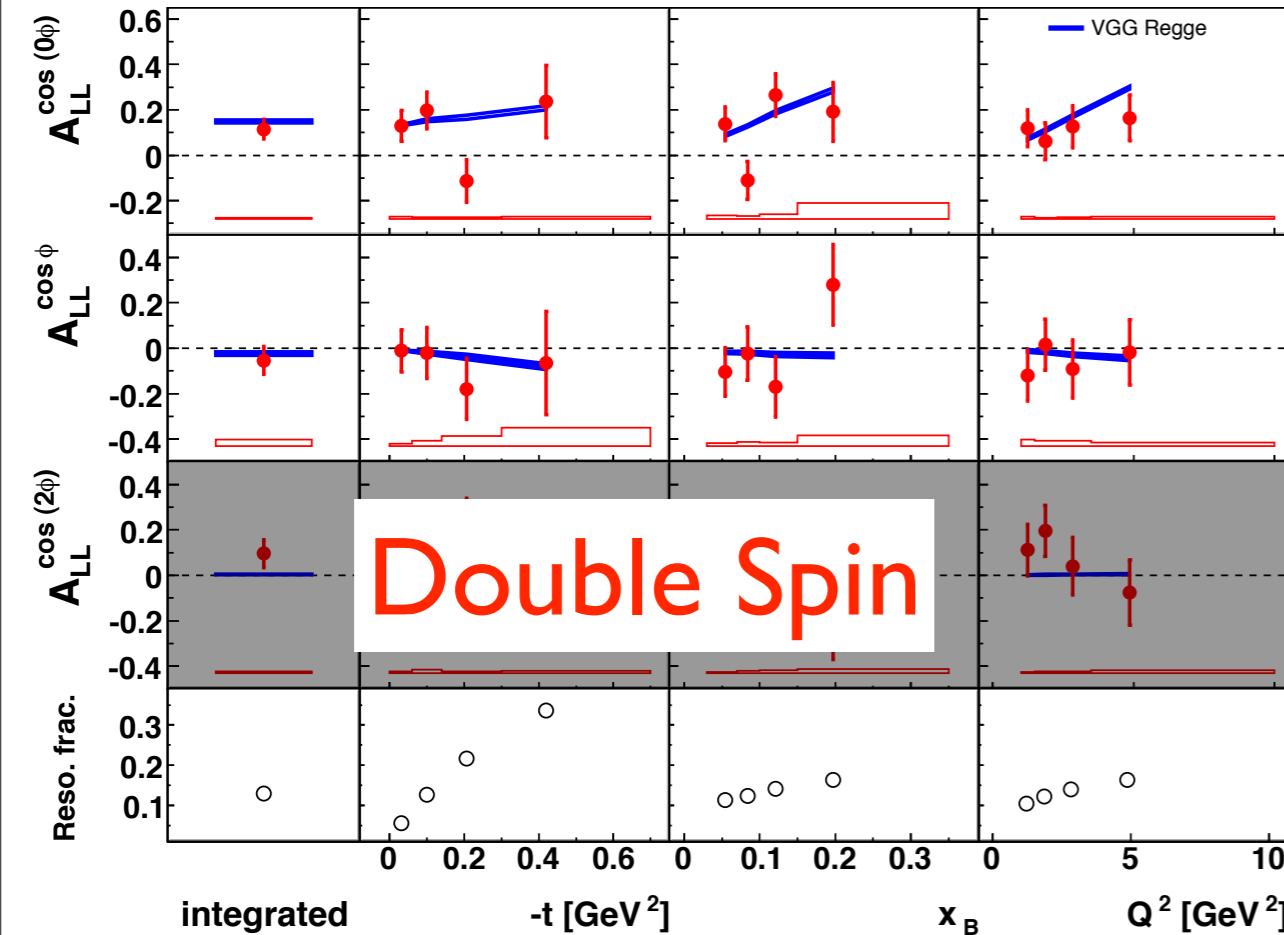
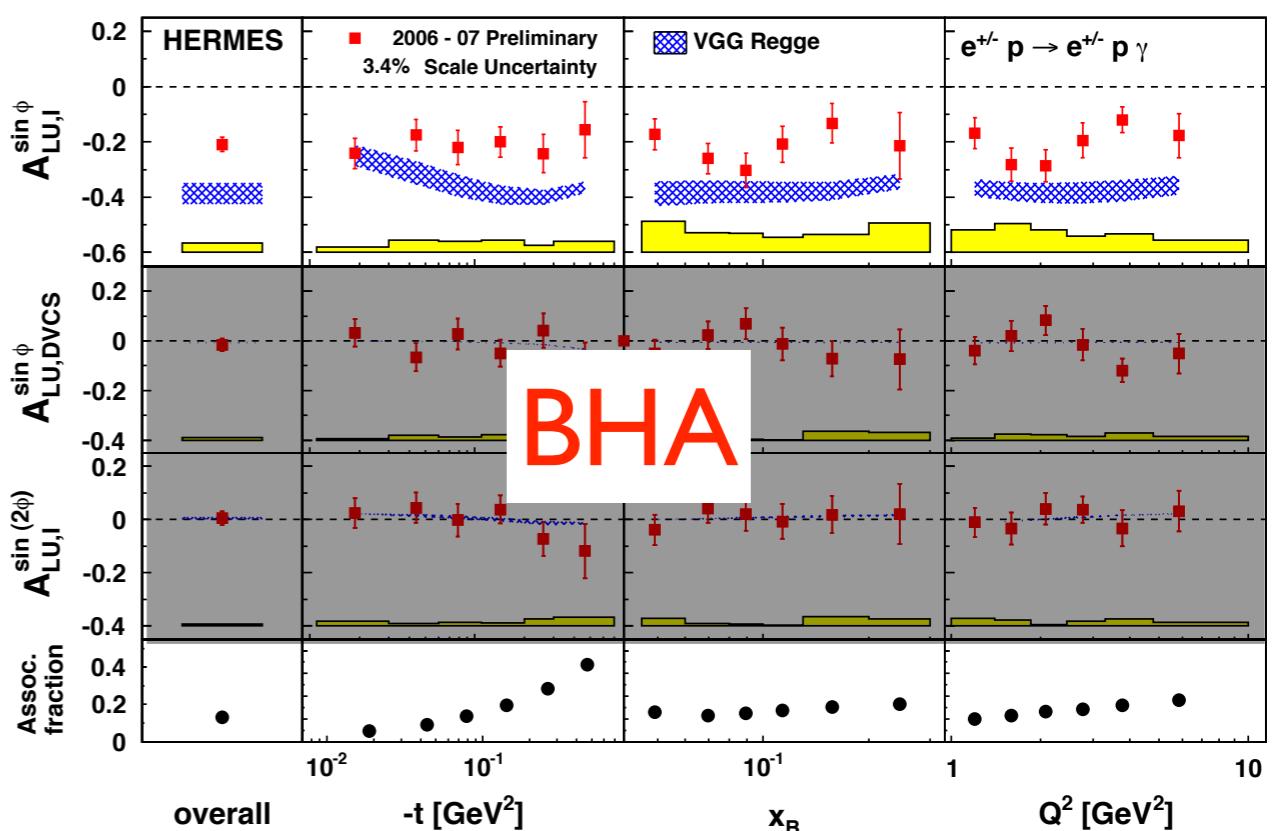
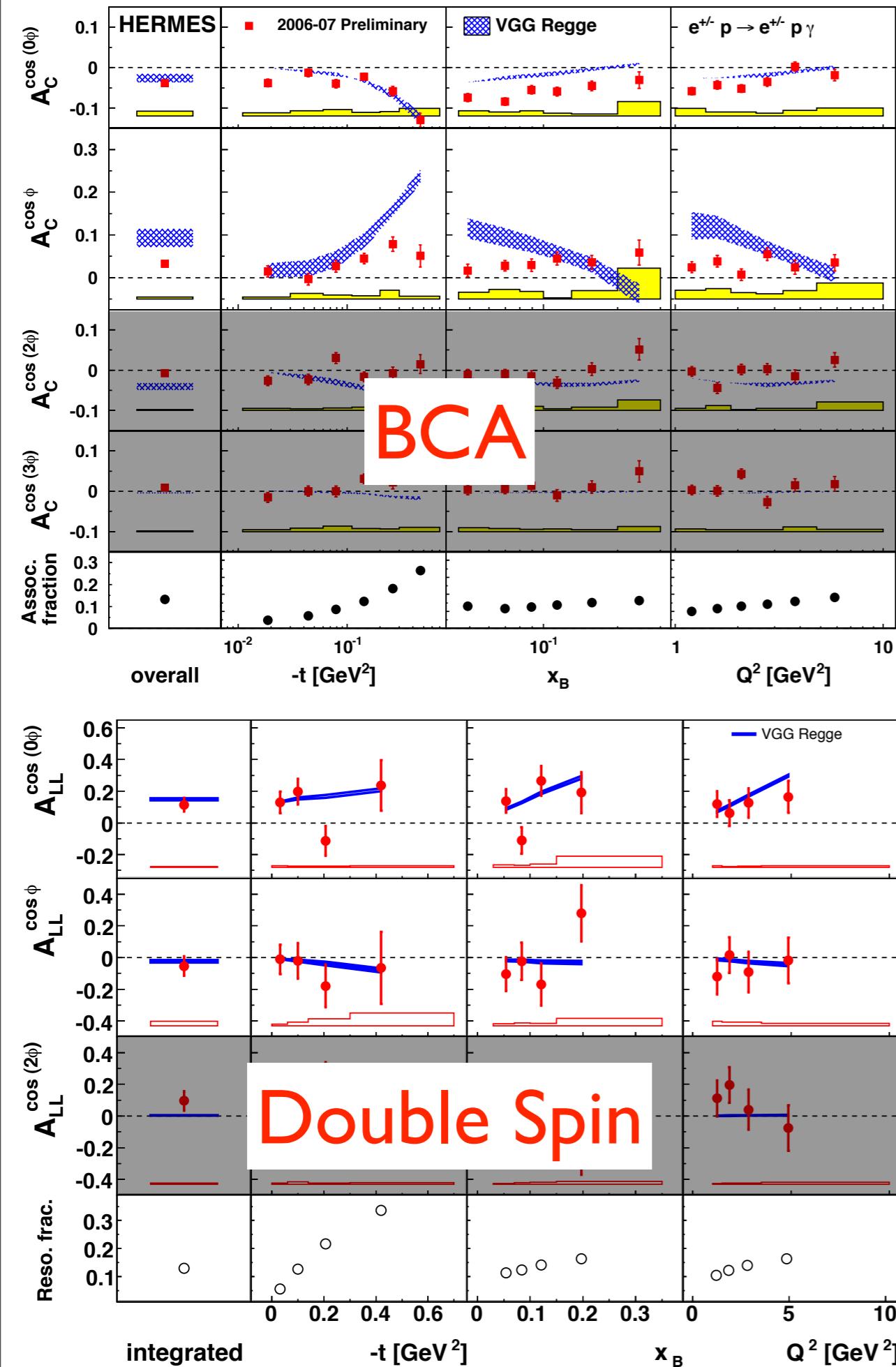
Exclusive Physics Results

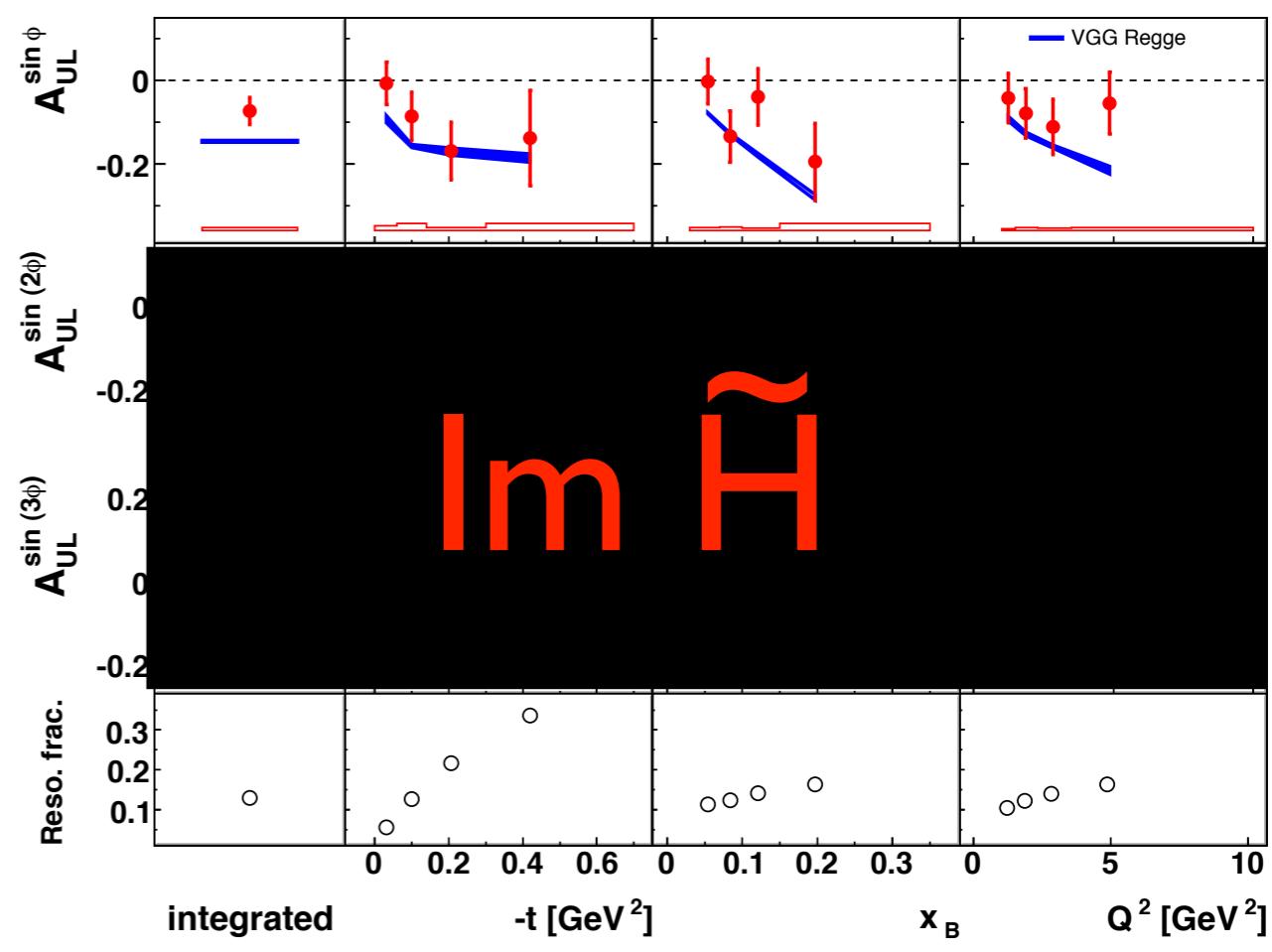
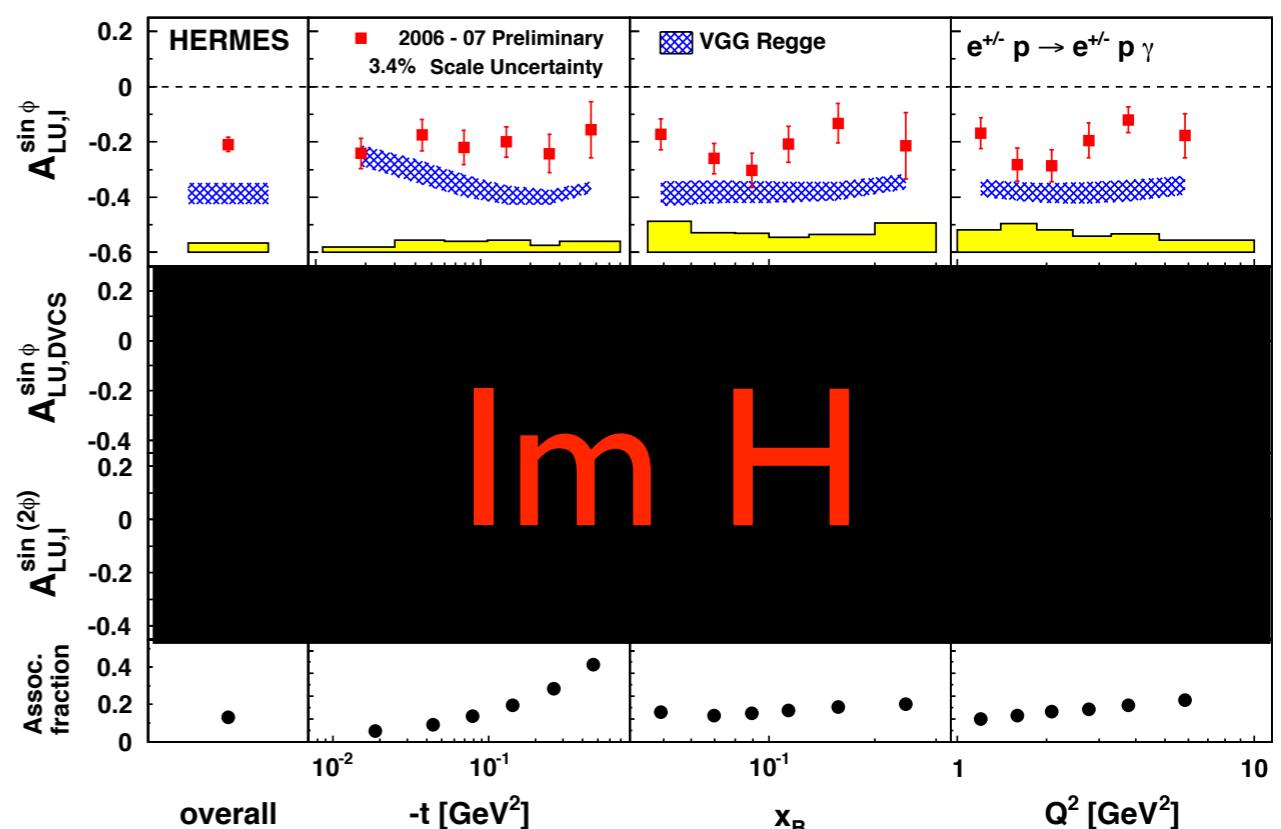
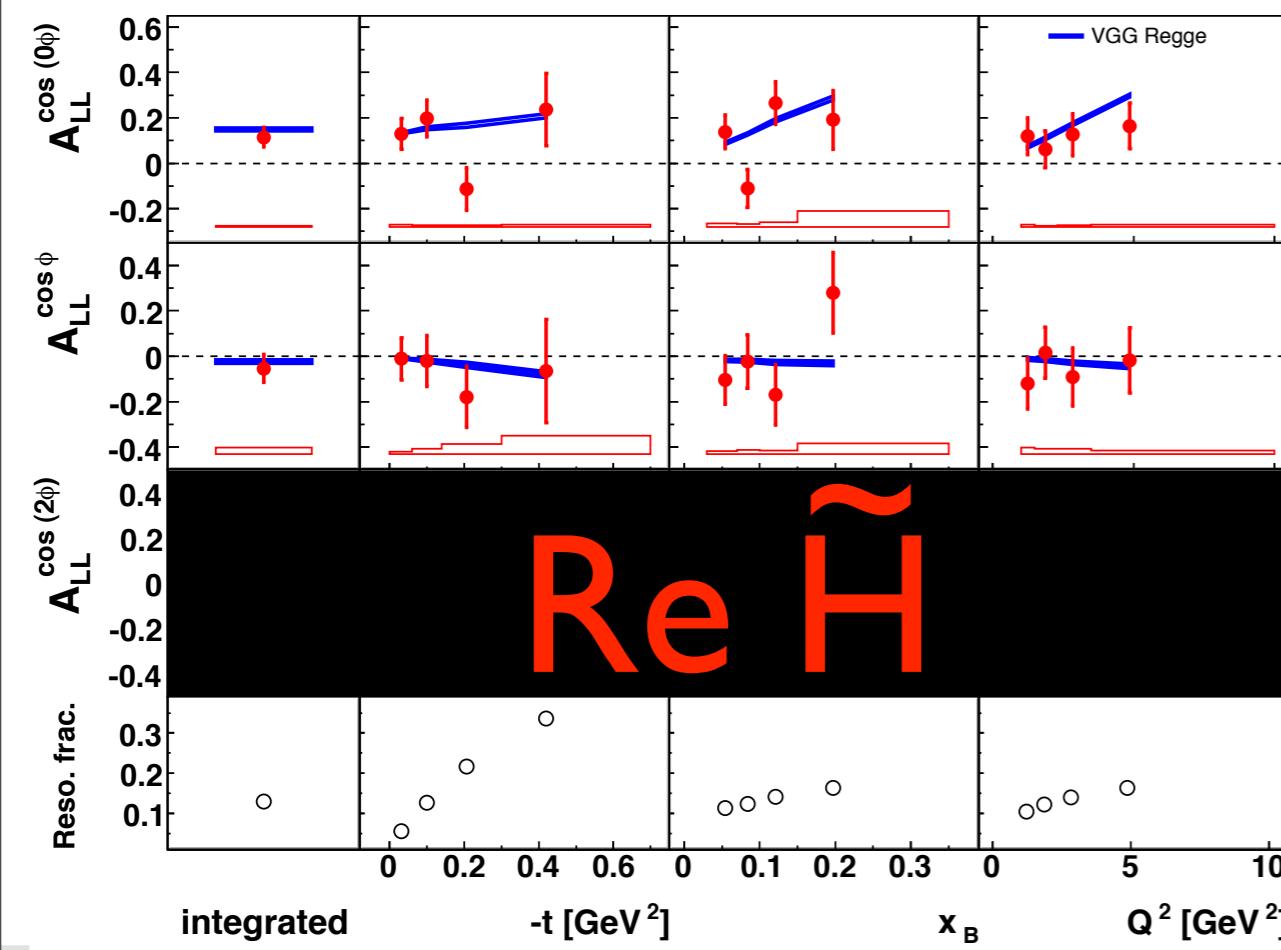
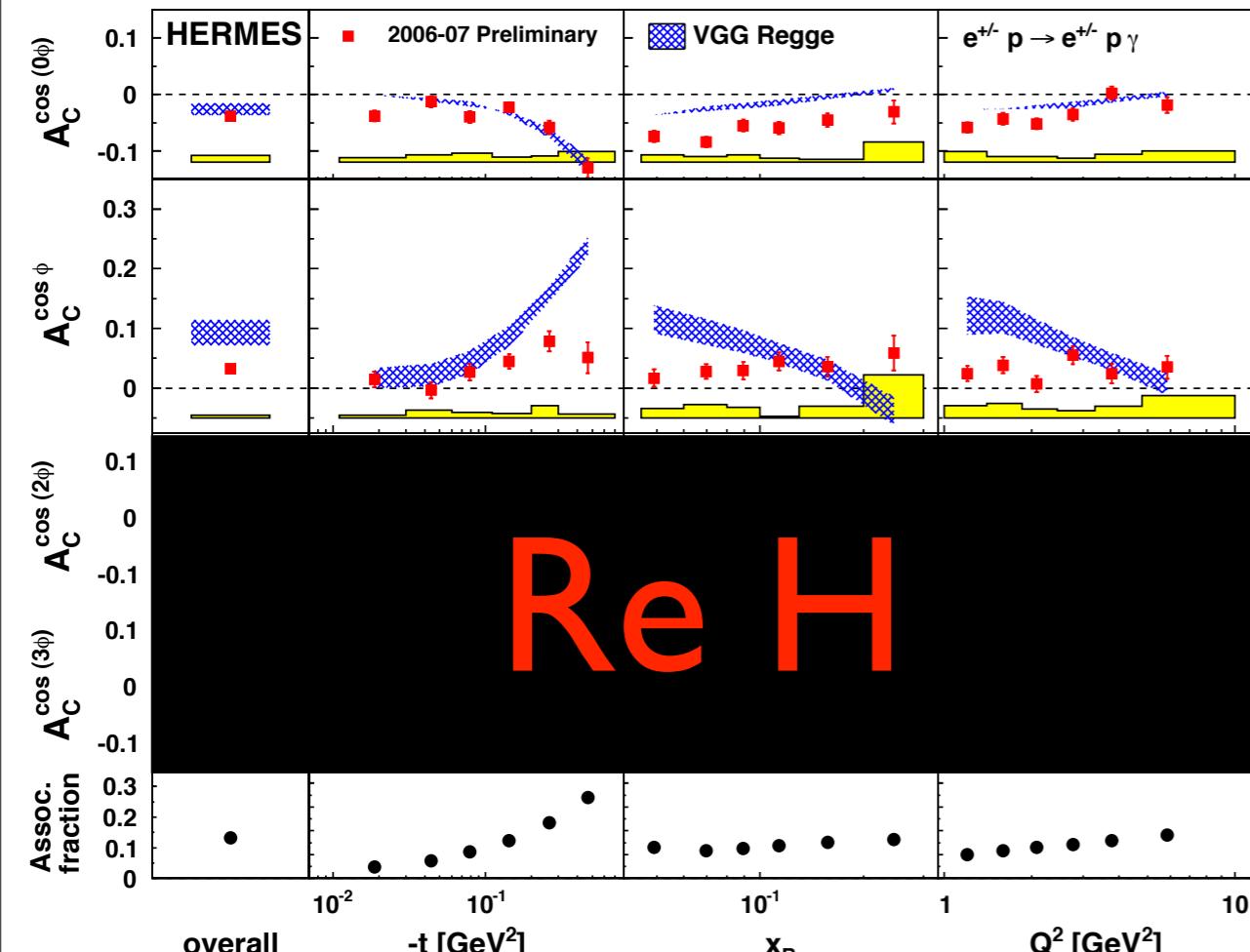
- DVCS allows the cleanest access to GPDs
- Mesons allow access to GPDs that would otherwise be difficult to access through DVCS
- HERMES has the most diverse set of DVCS measurements in the world



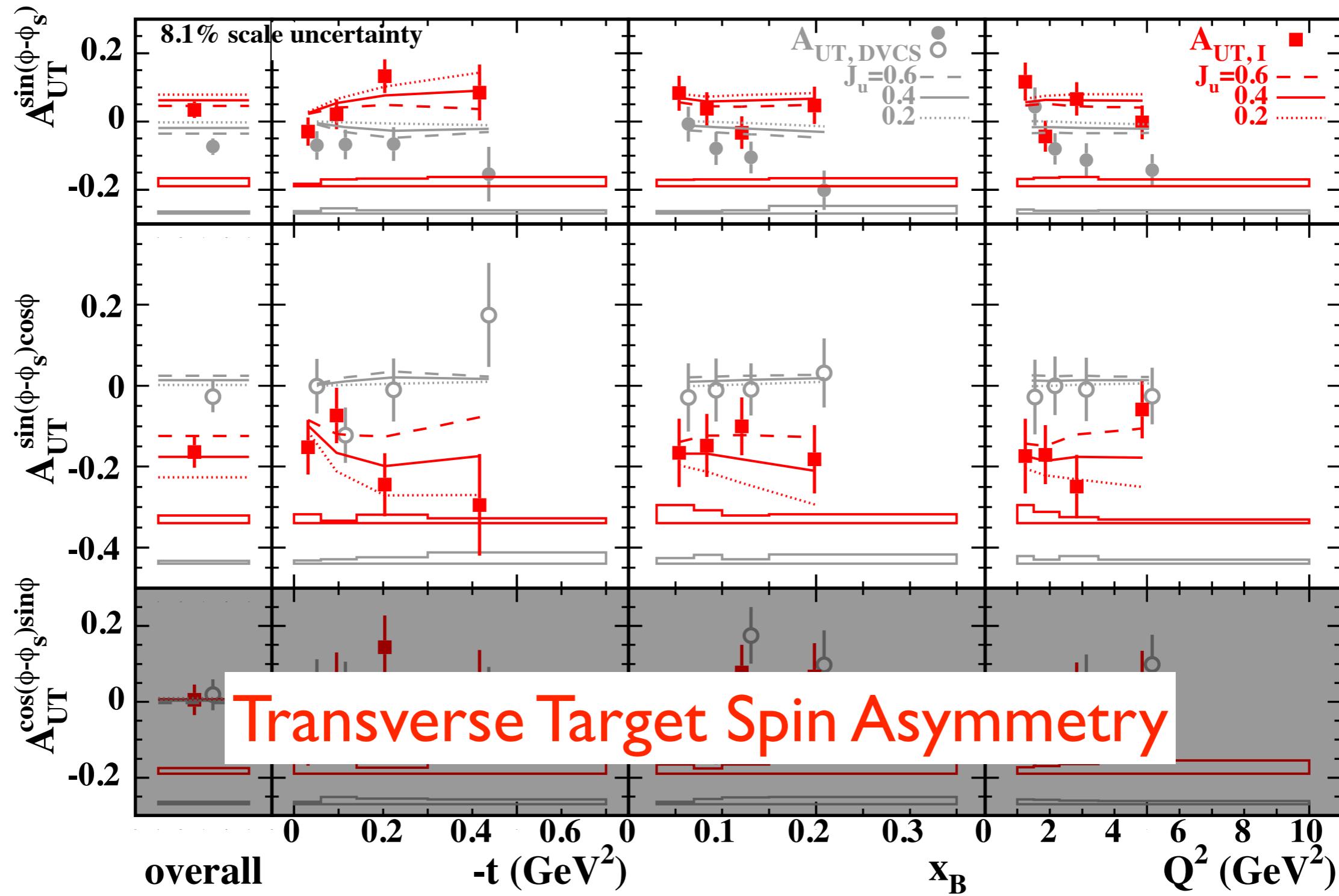
Both beam charges allows access to both the interference and DVCS terms of the amplitudes

Polarized targets are very important: allow access to both real and imaginary parts of 3 out of 4 CFFs

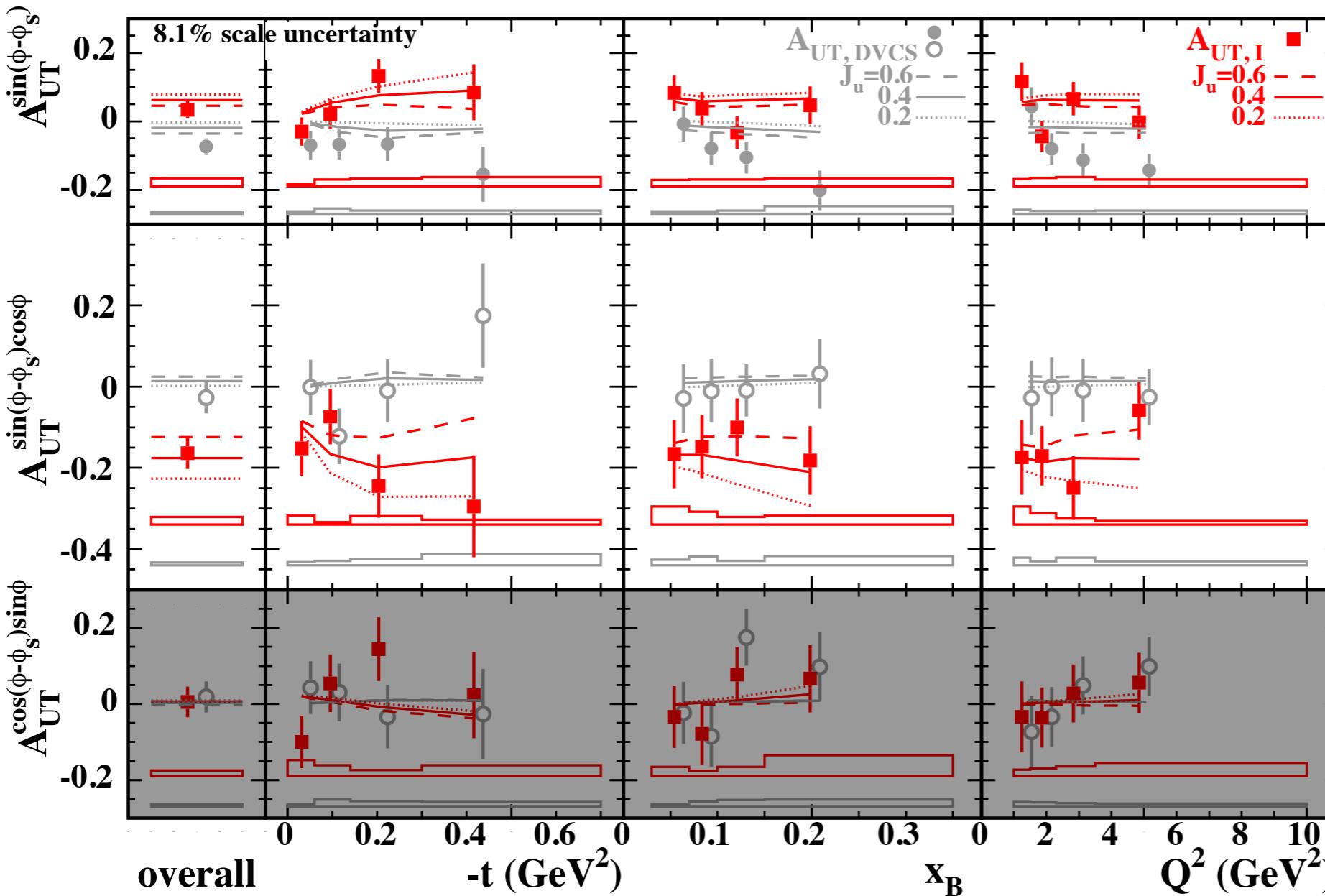




Results from HERMES



Results from HERMES



Data lacks the precision to
differentiate between model flavours

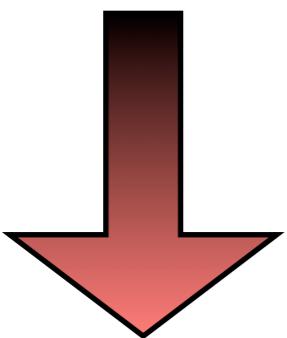
Sensitivity to
 $\text{Im}(E)$

Sensitivity to
 $\text{Re}(E)$

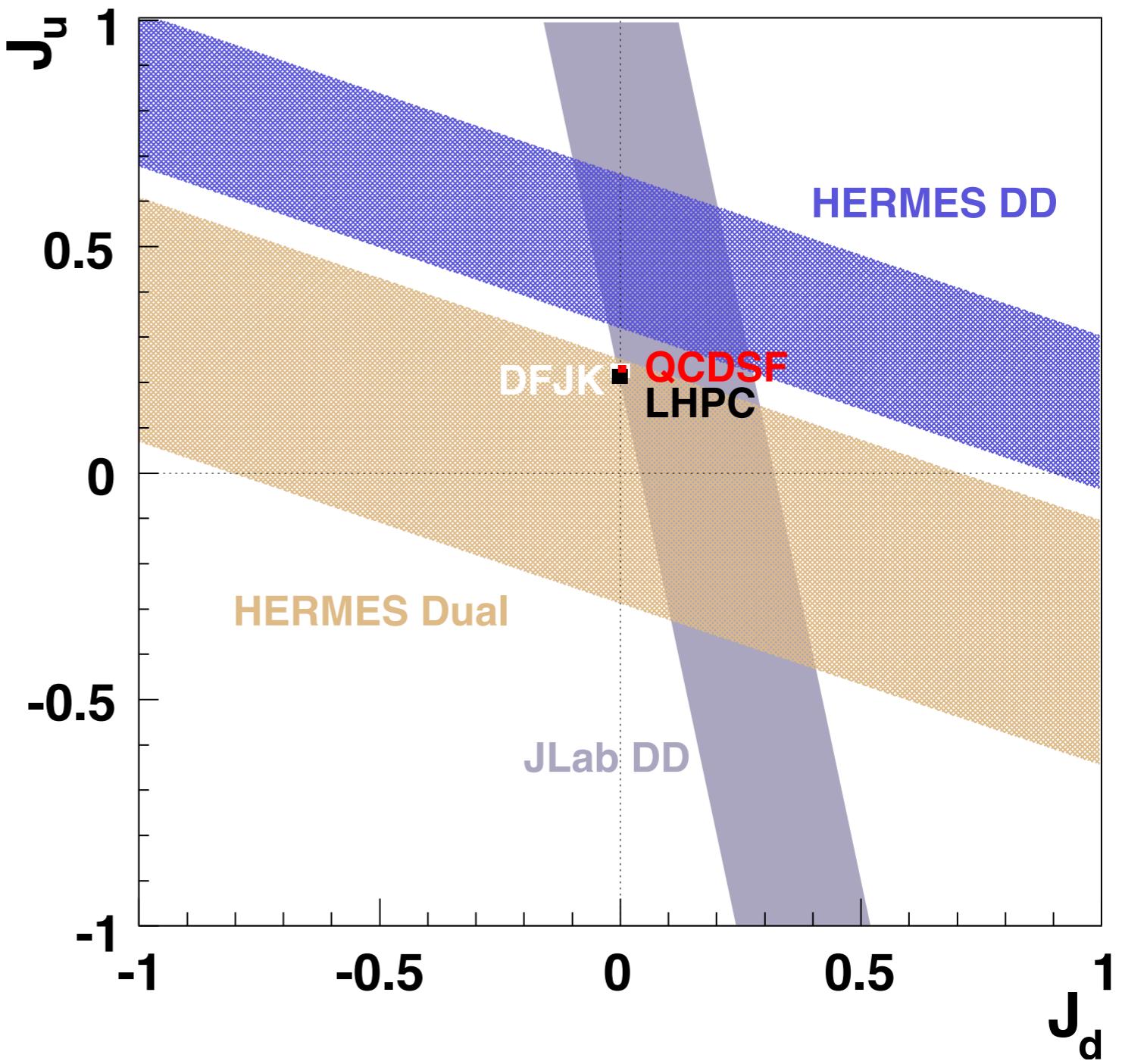
Where is the
next
measurement
coming from?

Results from HERMES

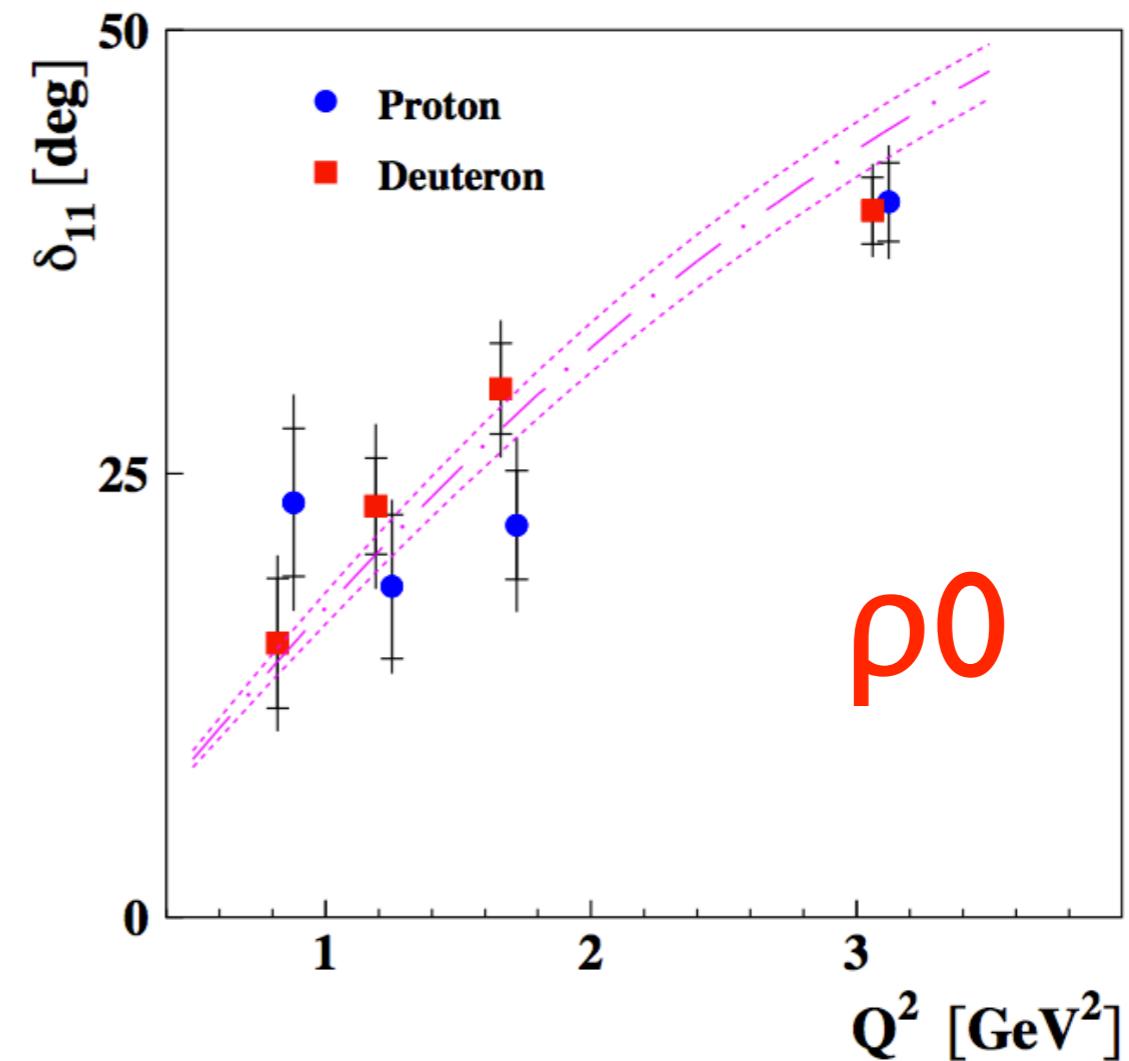
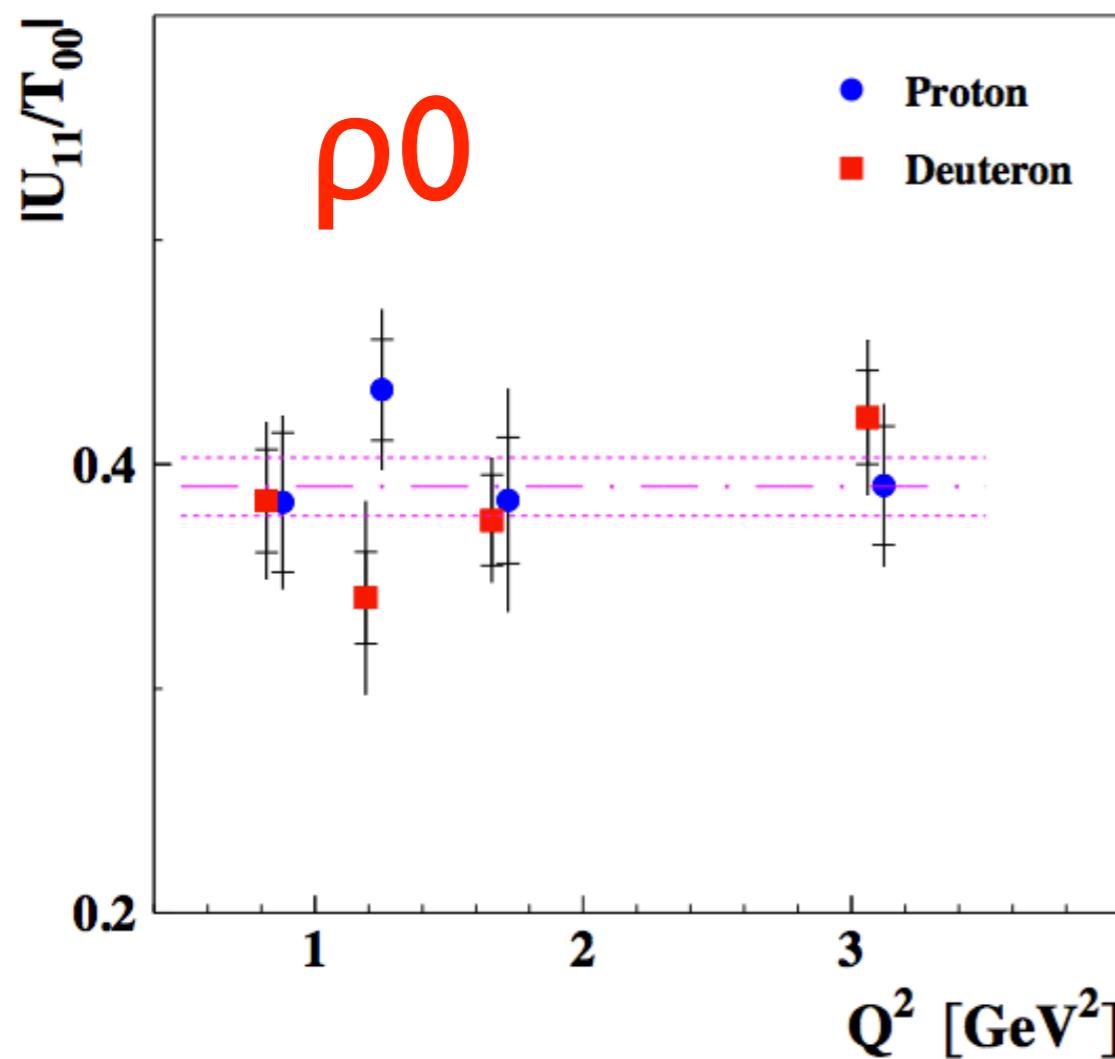
Access to E gives
access to J_d for **CQSM**
parameterisation



**Opens the door to
model-dependent
constraints!**



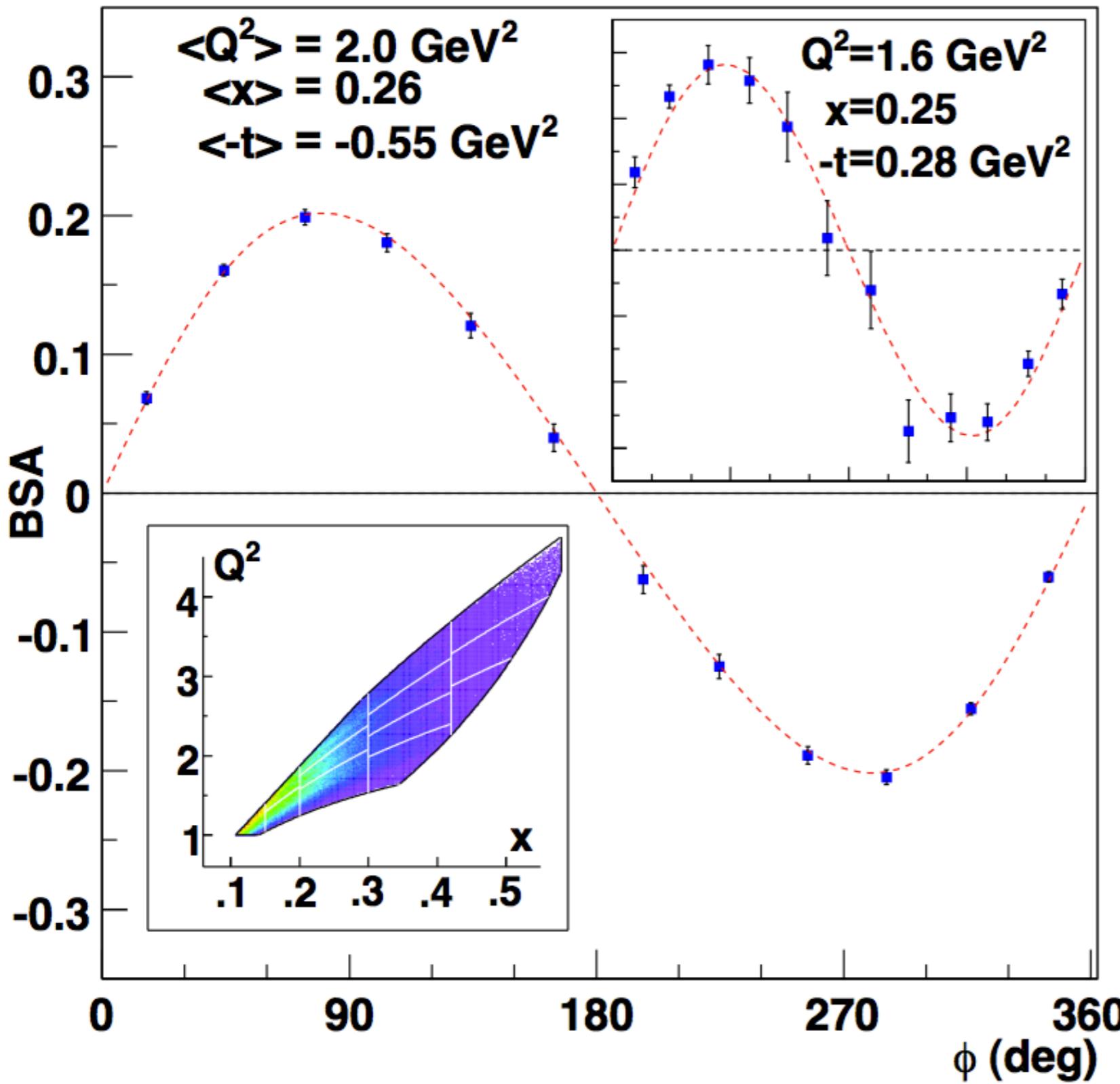
Results from HERMES



Evidence of **UPE** for ρ^0
mesons @ HERMES

Contradiction to GPD-based models!

Results from CLAS

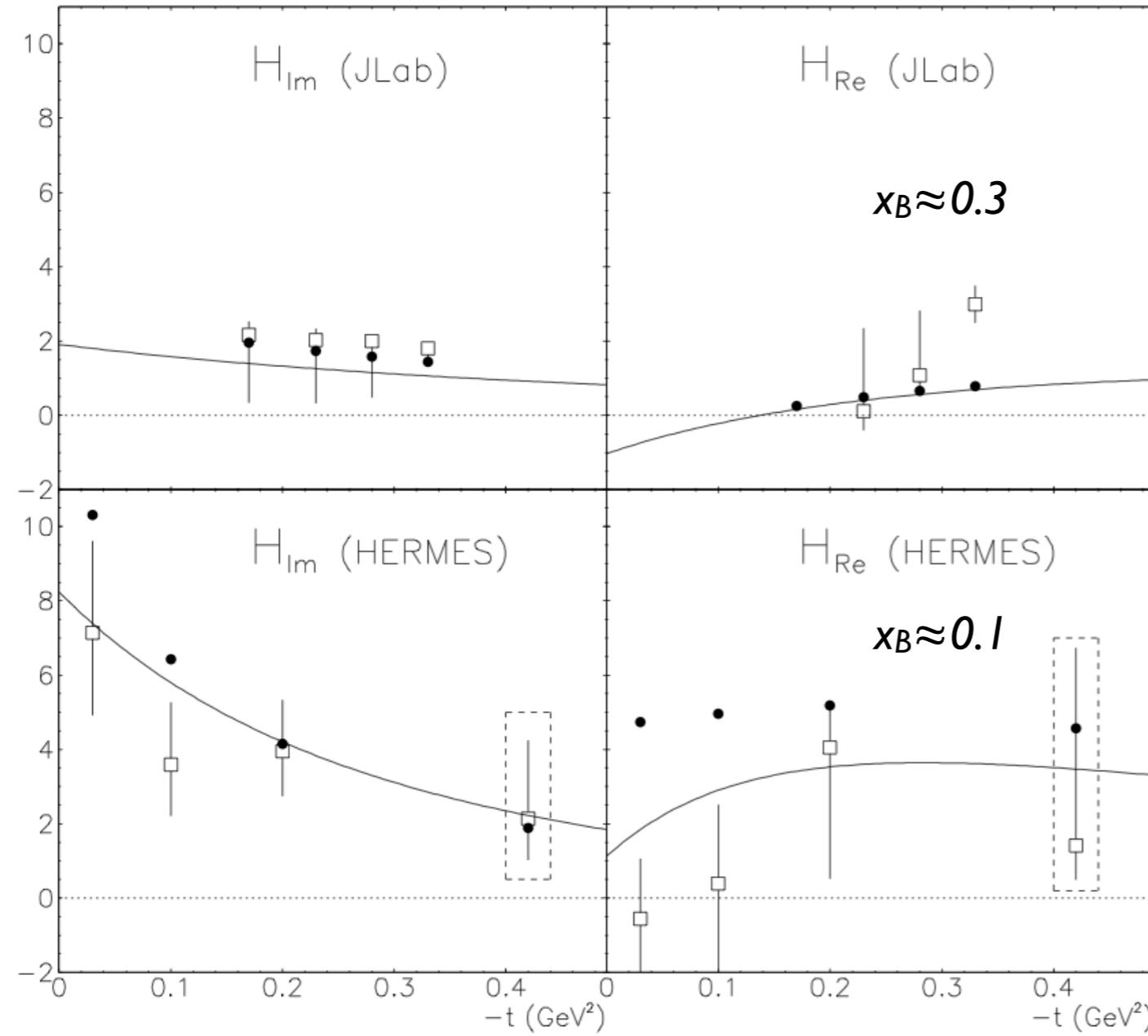


DVCS A_{LU}
asymmetries
measured in bins of
 x_B & Q^2

Very precise
measurements over a
wide range in x_B

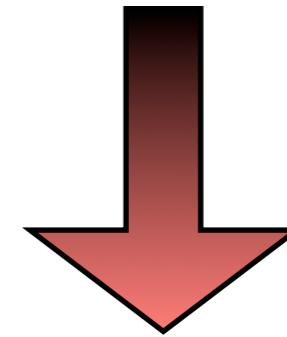
GPDs

M. Guidal



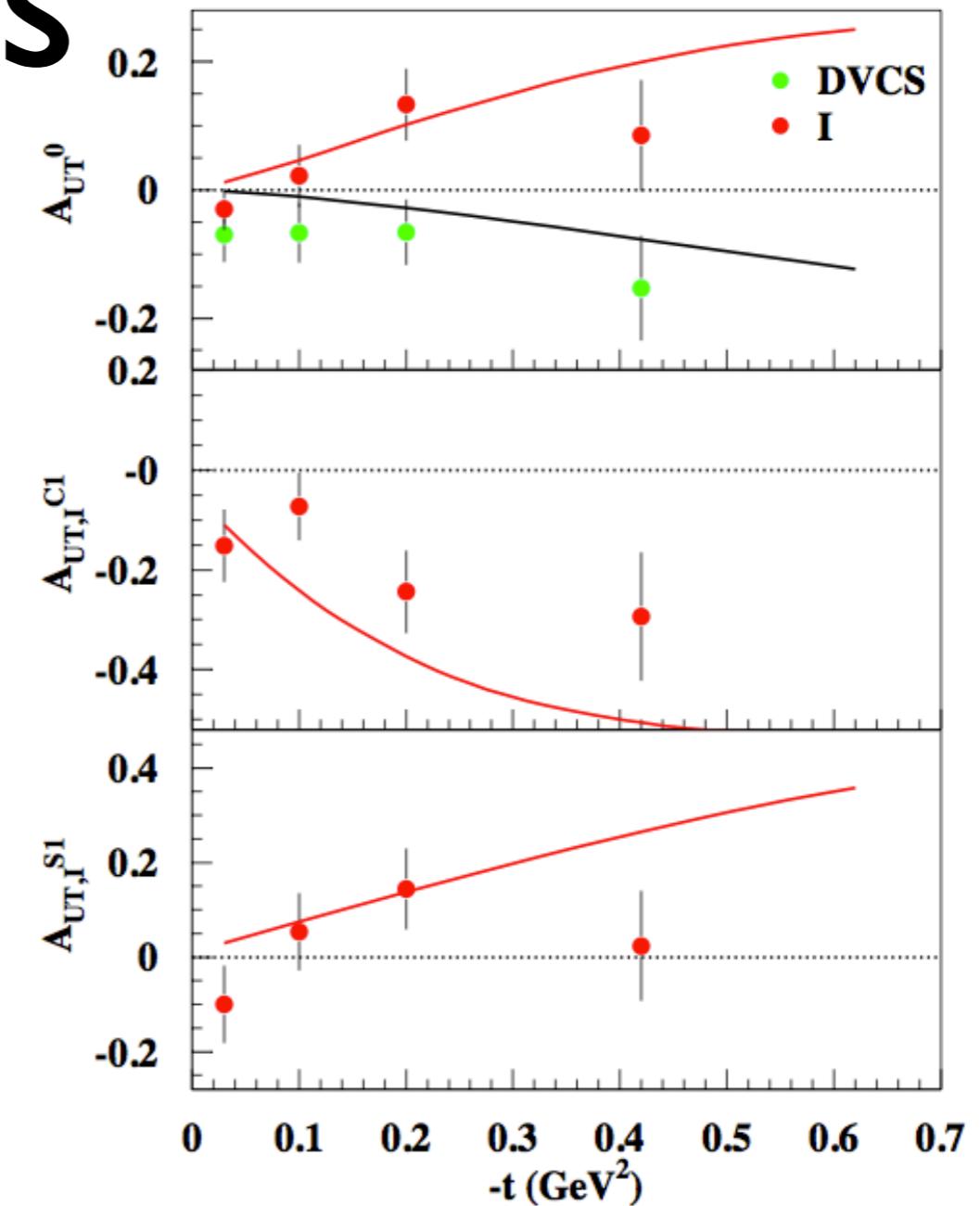
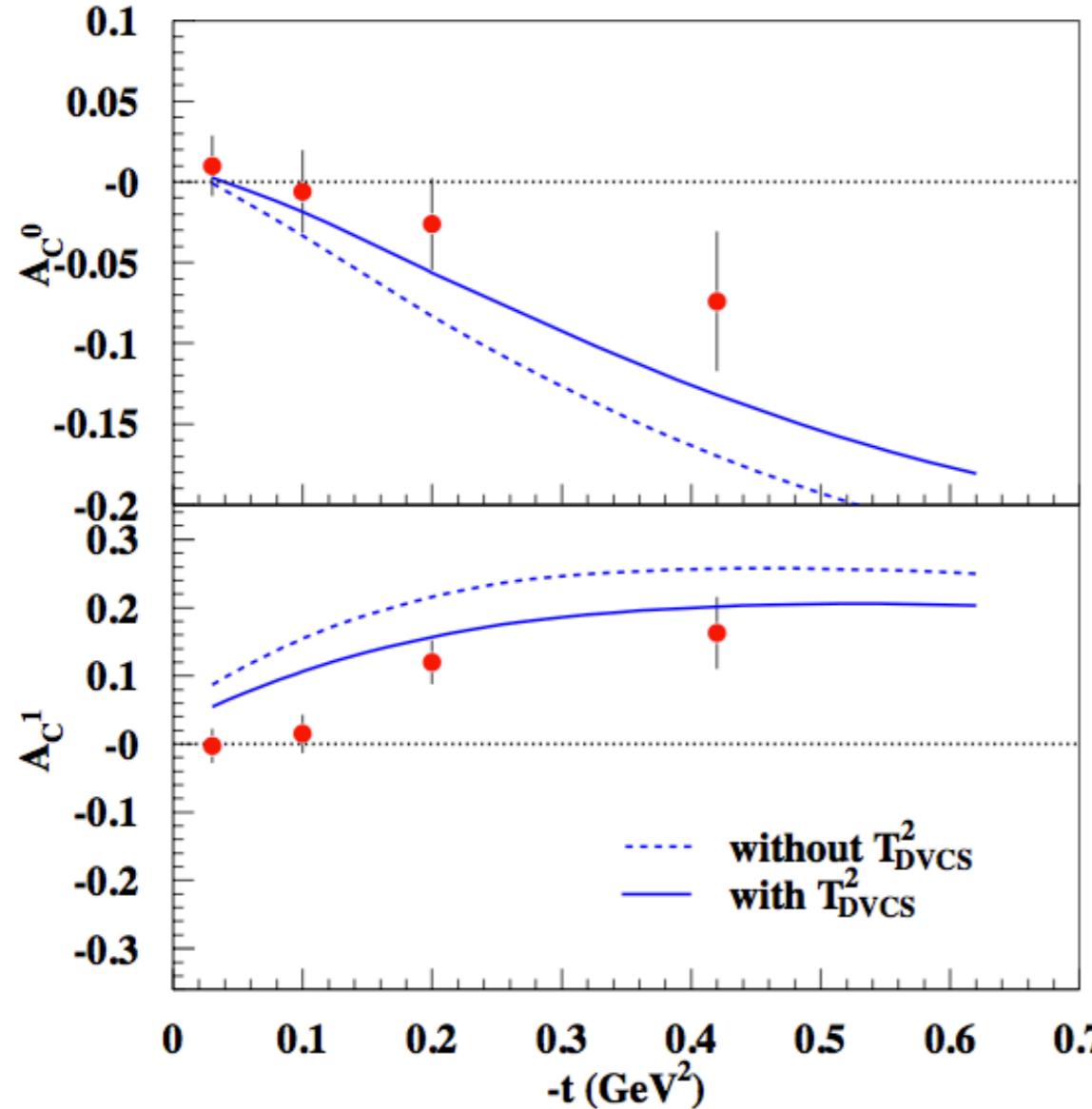
- Previous input to models

Extracted from fits to fixed-target data



Already we see that the previous input to models was good, but not right!

GPDs



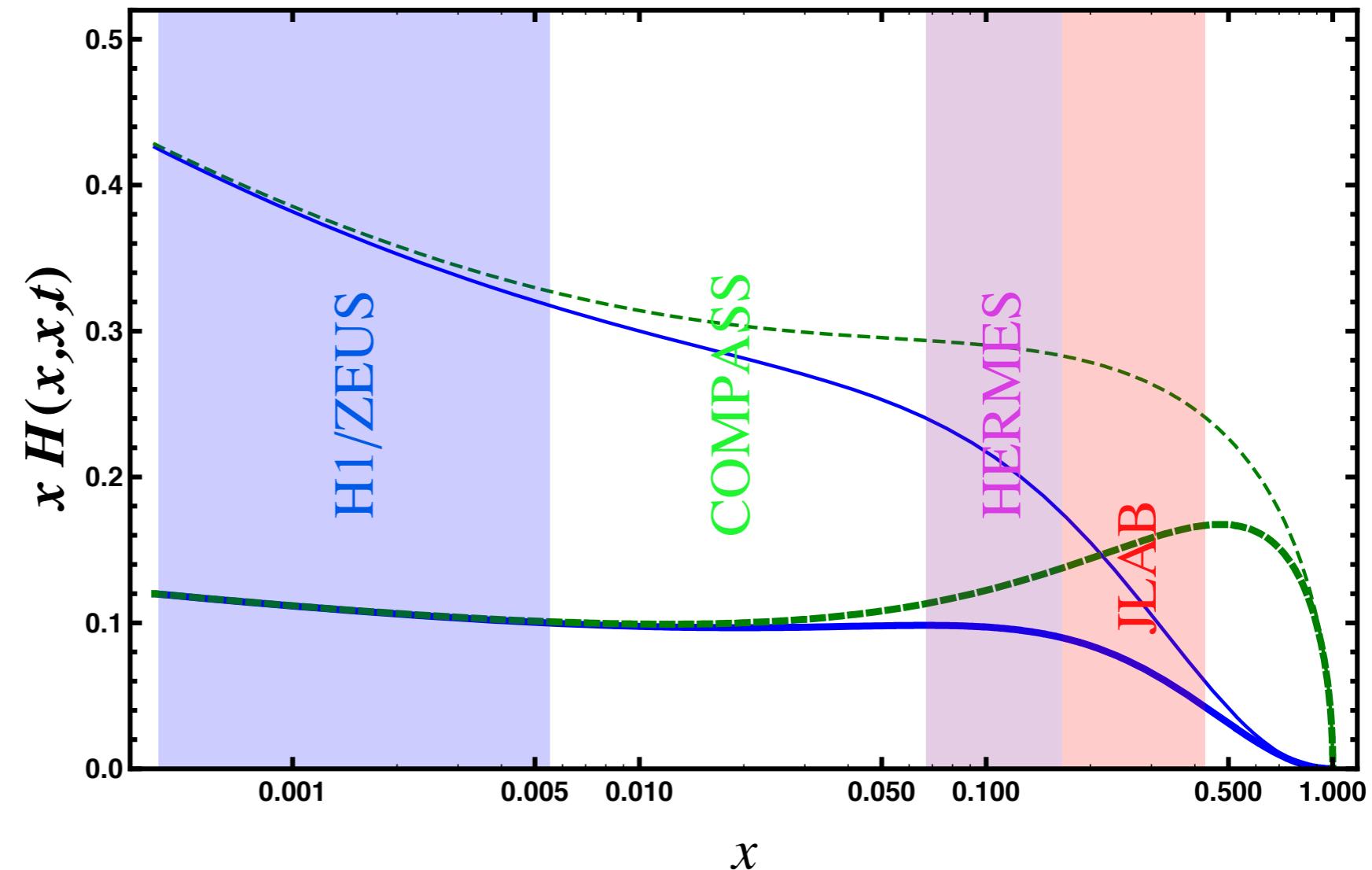
Models trained on JLab data (Liuti, Goldstein & Hernandez) have predictive power for HERMES asymmetry amplitudes!

GPDs

Müller &
Kumerički
attempt to
extract GPDs
from LCWF
models

Factorized t -
dependence

Regge t -
dependence

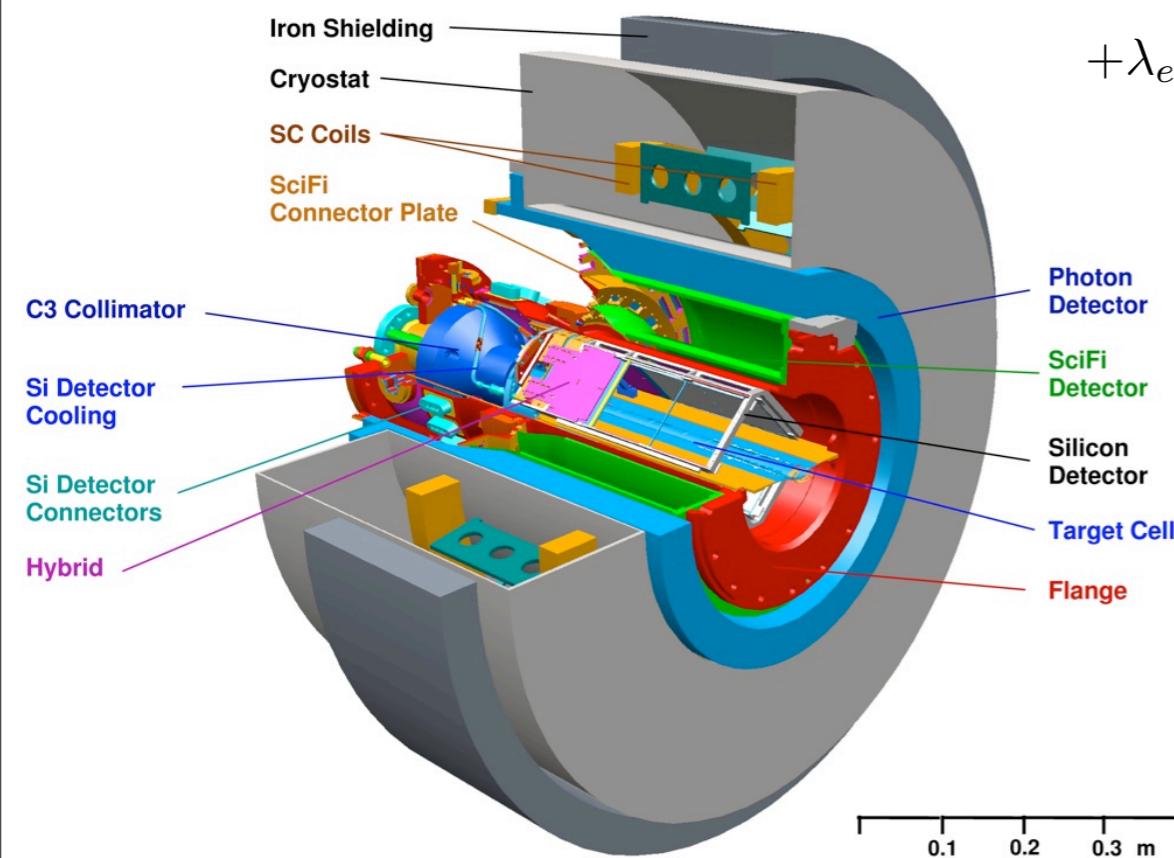


Hall A cross-sections make a
large difference!

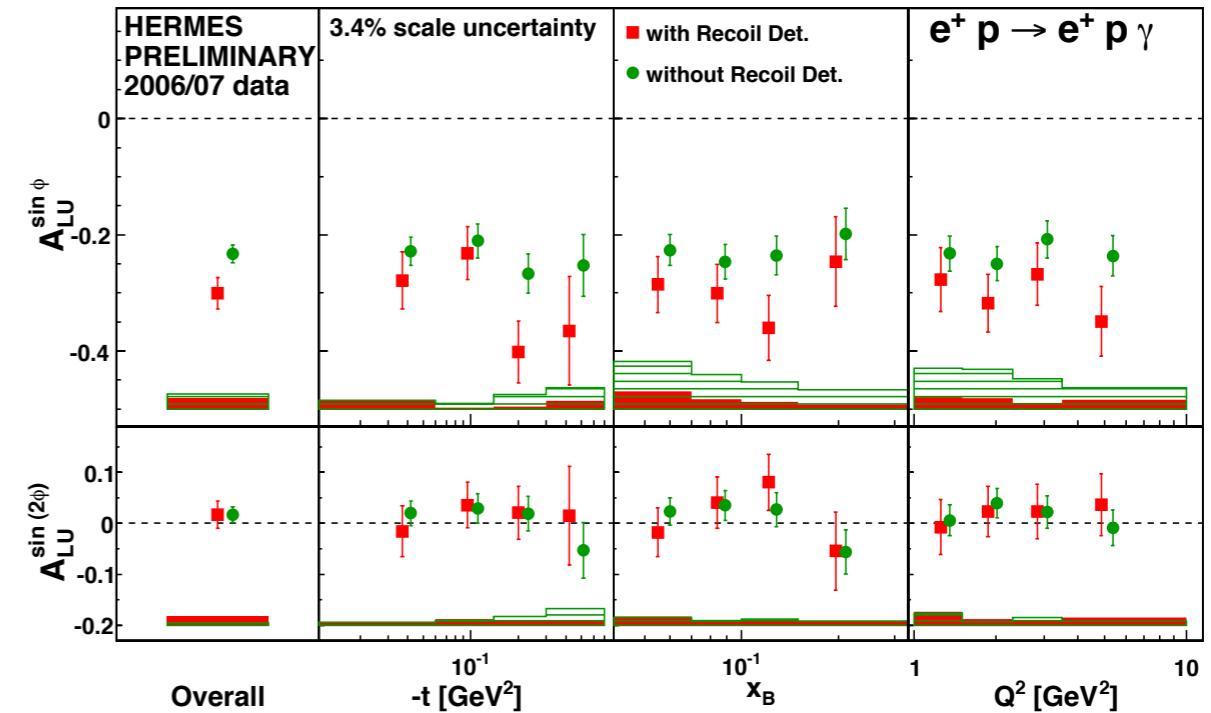
Future @ HERMES

Still 9 papers in
draft status

Almost 20 analyses
ongoing!



$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + d\sigma_{UU}^1 \cos(2\phi) + \frac{1}{Q} (d\sigma_{UU}^2 \cos \phi + \lambda_e d\sigma_{LU}^3 \sin \phi) \\
 & + S_L \left\{ d\sigma_{UL}^4 + \frac{1}{Q} (d\sigma_{UL}^5 \sin + \lambda_e [Q d\sigma_{LL}^6 + d\sigma_{UL}^7 \cos \phi]) \right\} \\
 & \quad \text{cos-phi moments} \\
 & \quad \text{Sivers Function} \quad \text{Collins Effect} \\
 S_T \left\{ & d\sigma_{UT}^8 \sin(\phi - \phi_s) + d\sigma_{UT}^9 \sin(\phi + \phi_s) + d\sigma_{UT}^{10} \sin(3\phi - \phi_s) \right. \\
 & \left. + \frac{1}{Q} [d\sigma_{UT}^{11} \sin(2\phi - \phi_s) + d\sigma_{UT}^{12} \sin \phi_s] \right\} \\
 & + \lambda_e [d\sigma_{LT}^{13} \cos(\phi - \phi_s) + \frac{1}{Q} d\sigma_{LT}^{14} \cos \phi_s + \frac{1}{Q} d\sigma_{LT}^{15} \cos(2\phi - \phi_s)] \}
 \end{aligned}$$



F

u

t

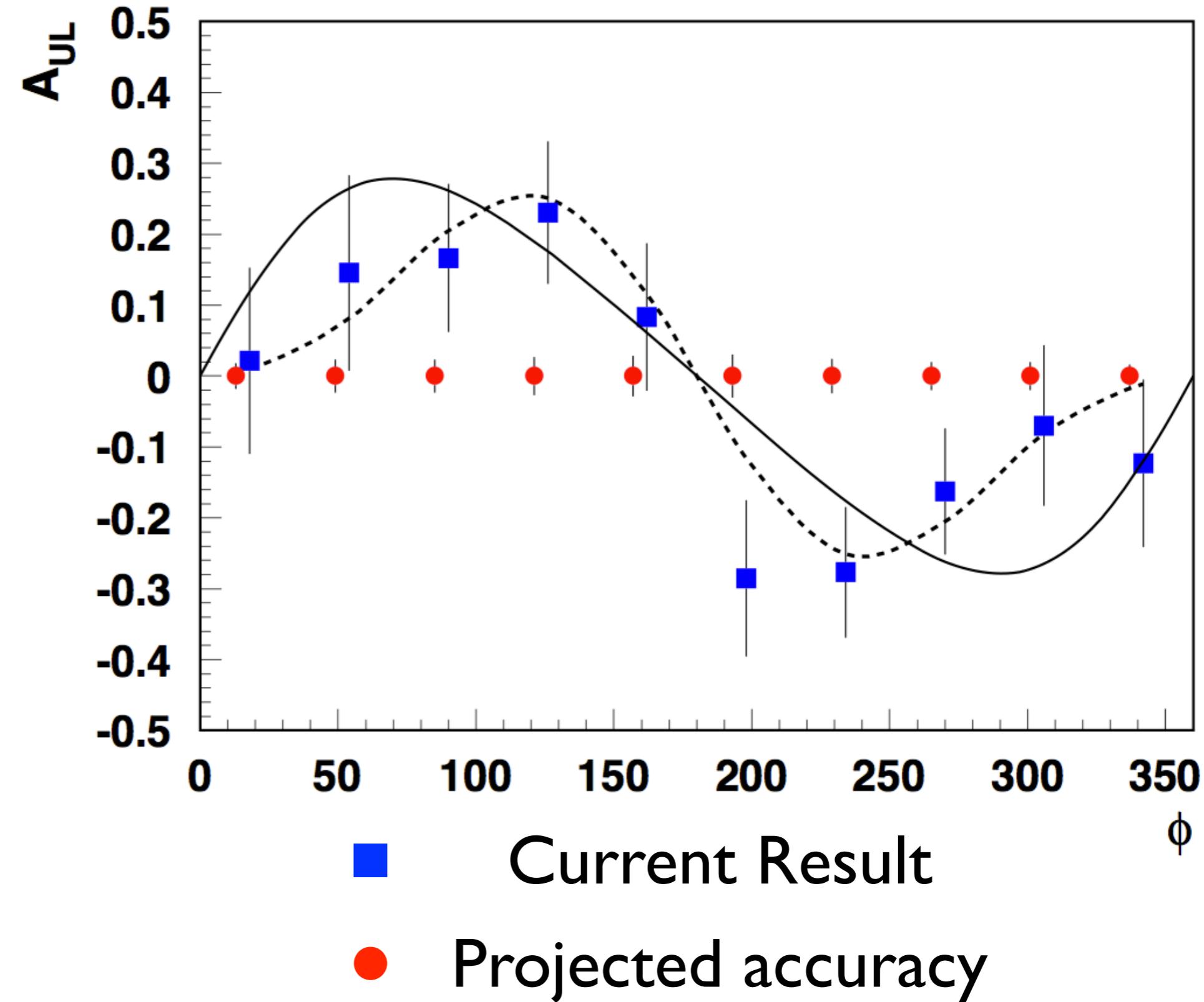
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r

e

@

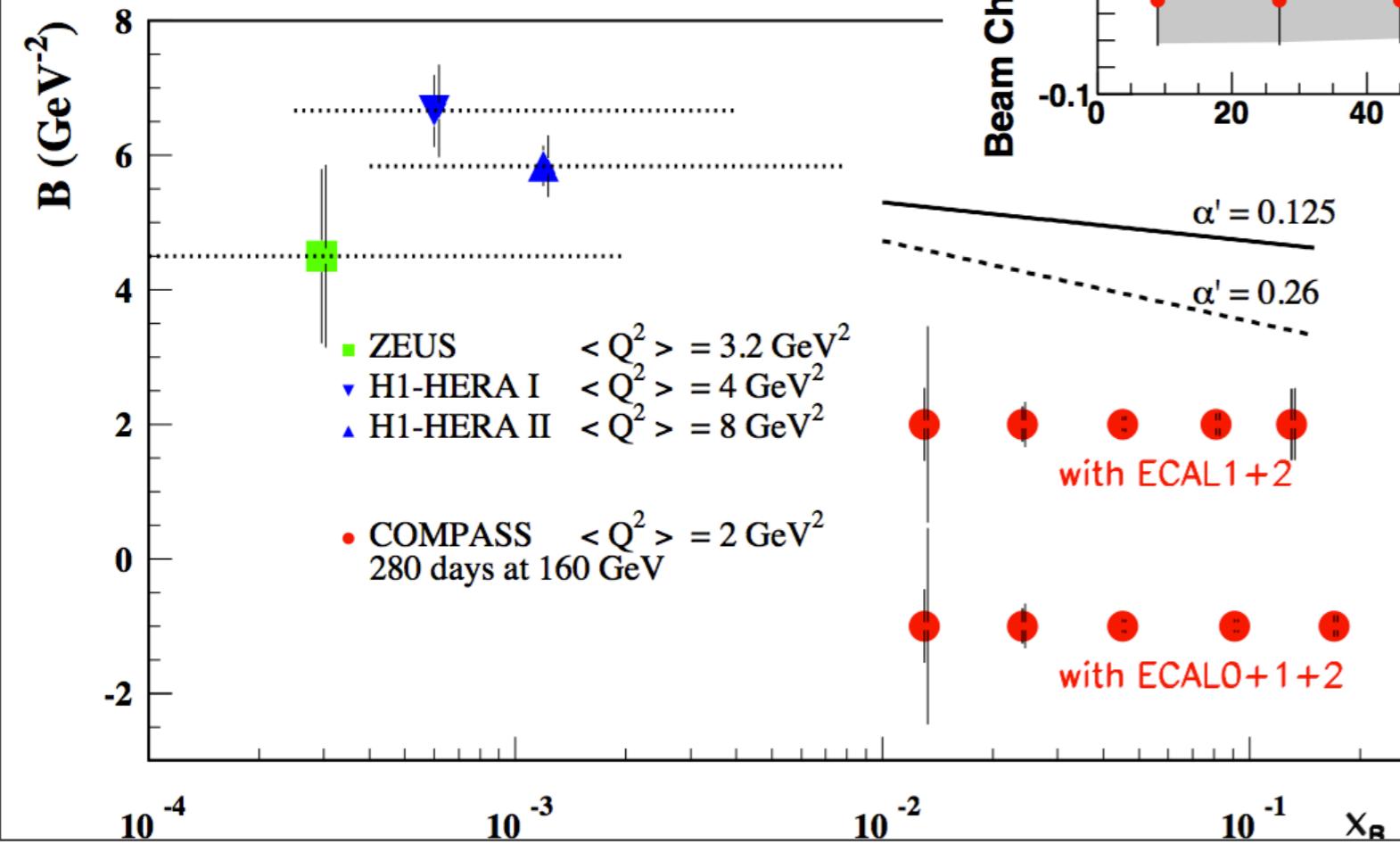
J
L
a
b



Experiment currently under analysis
should allow access to A_{LU} , A_{UL} and A_{LL}

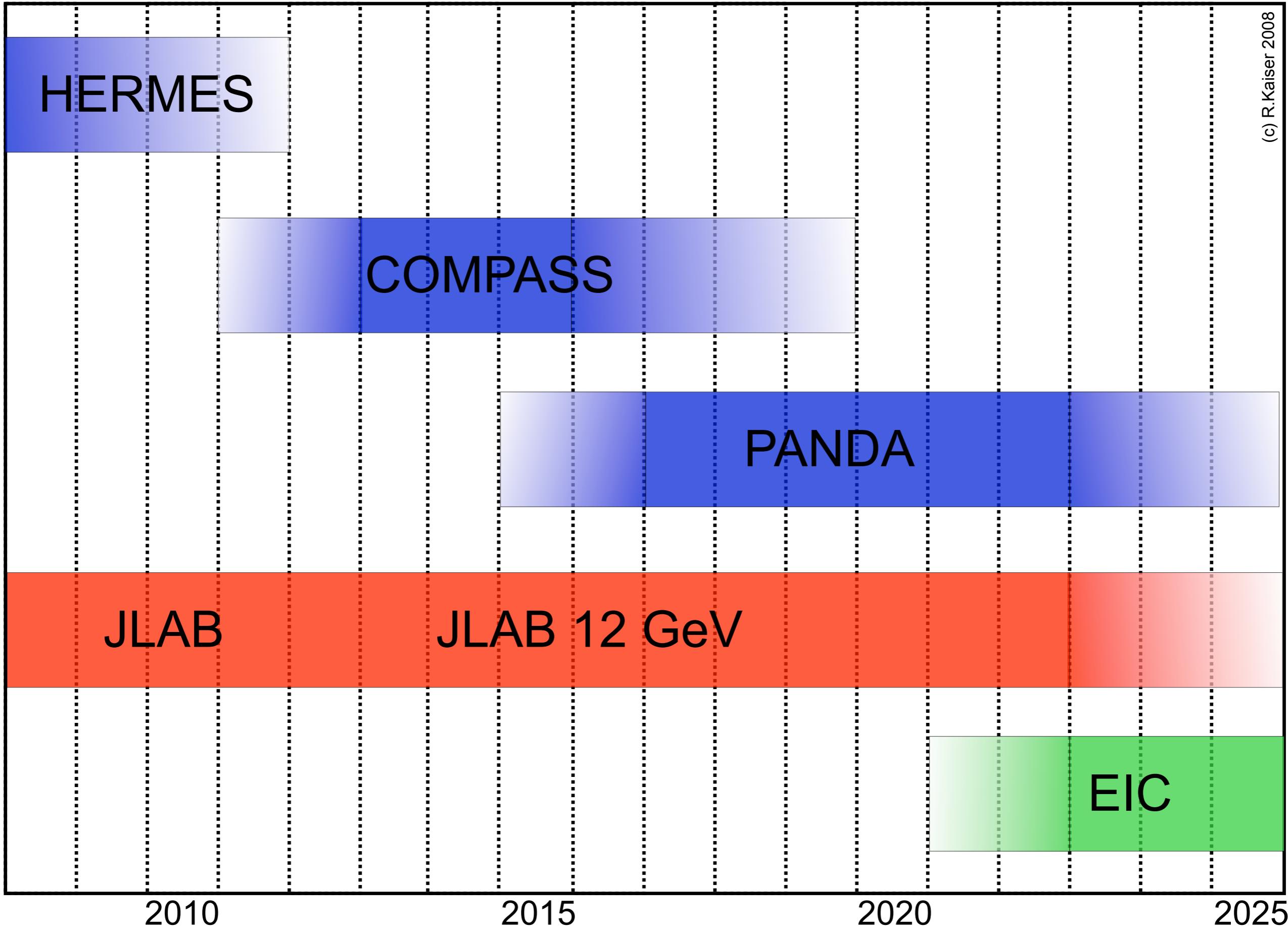
Future @ COMPASS

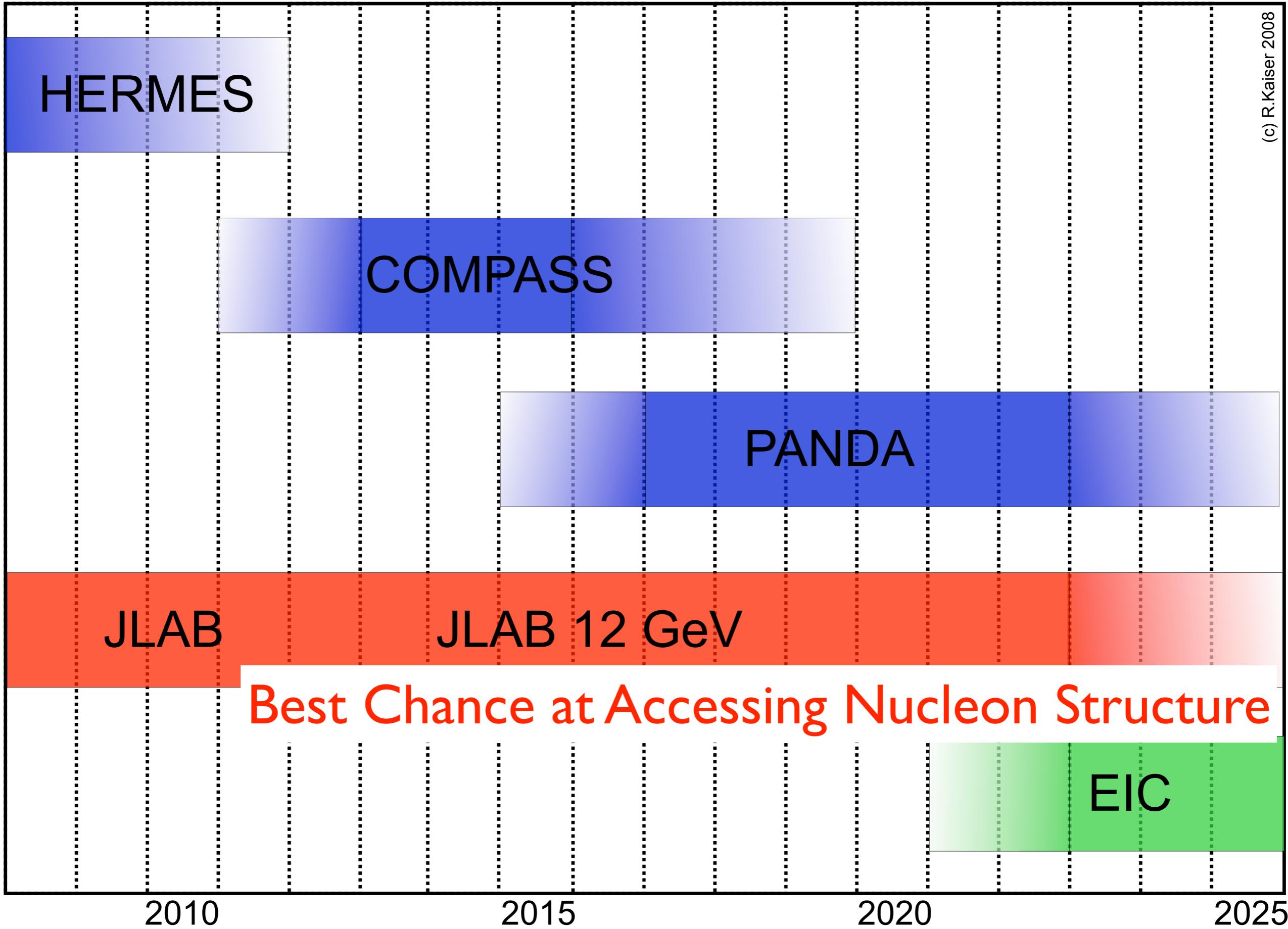
COMPASS GPD
Program aims to
access $\text{Im}(H)$ and
 $\text{Re}(H)$



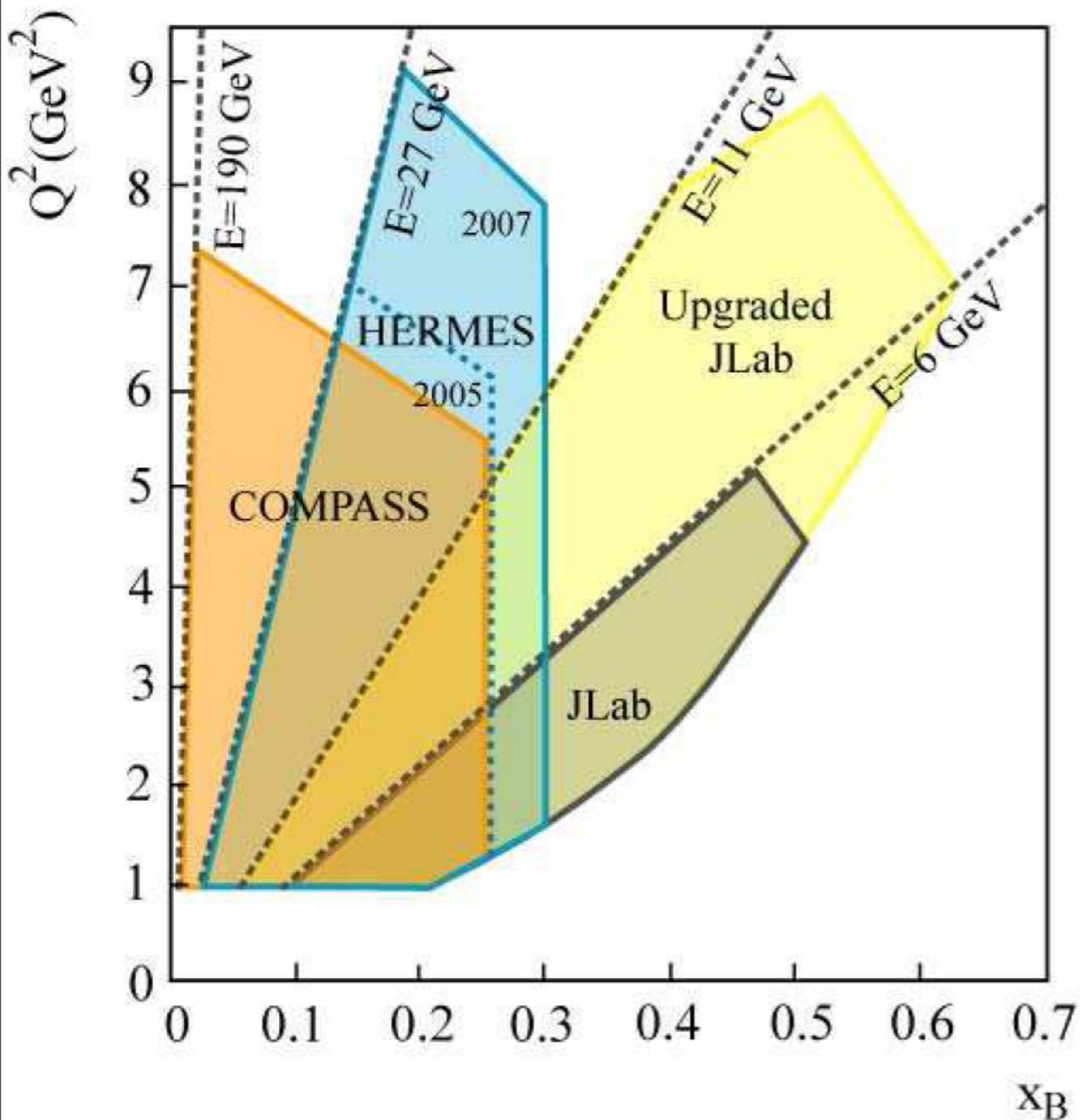
Upcoming COMPASS
data will determine
the GPD t-
dependence: **Regge?**
Factorized? **Something
else?**







JLab @ 12 GeV

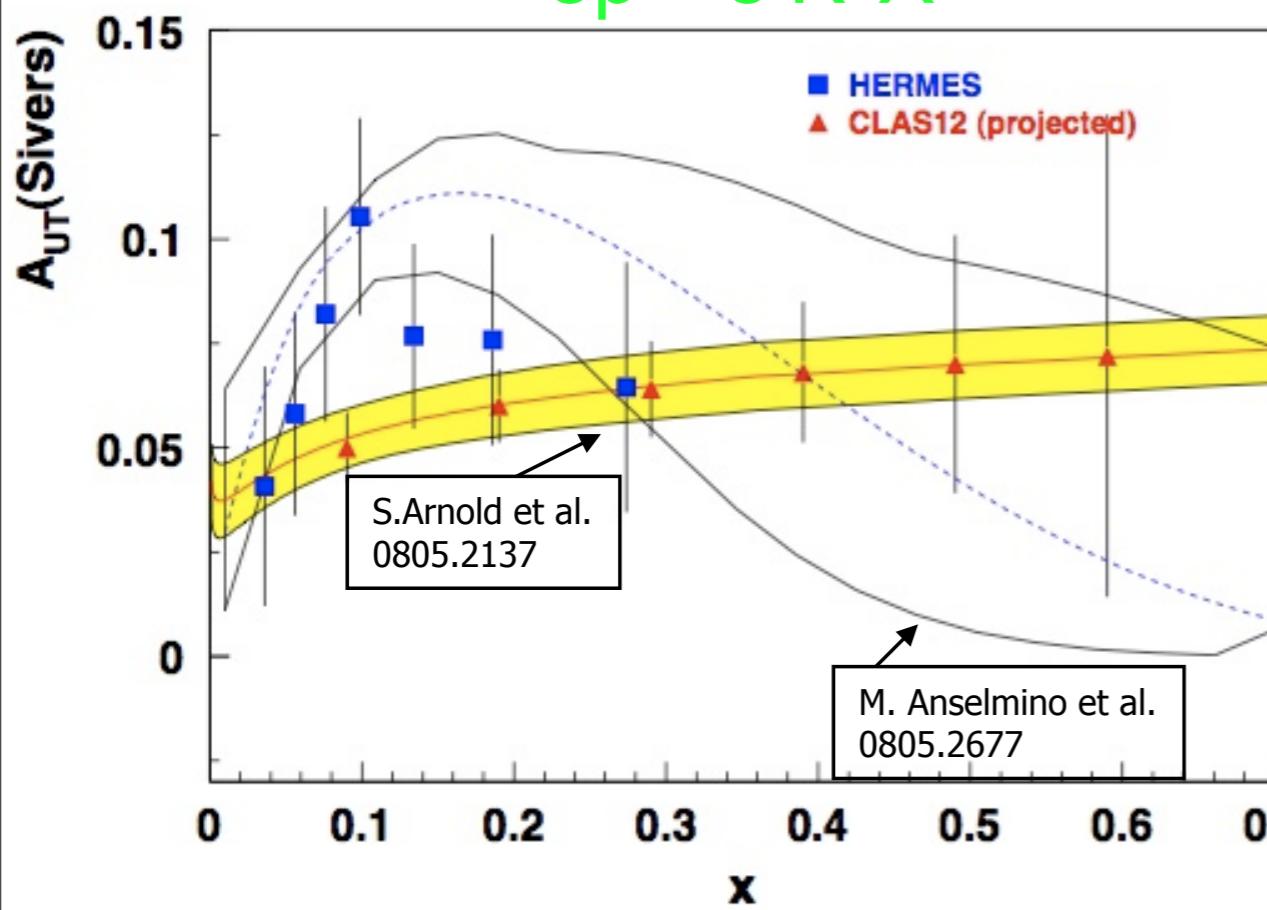


Expanded kinematic coverage allows expanded physics program

Ambitious plans to do DVCS on neutron at Halls A and B; help map out Sivers moments with precision enough to distinguish models

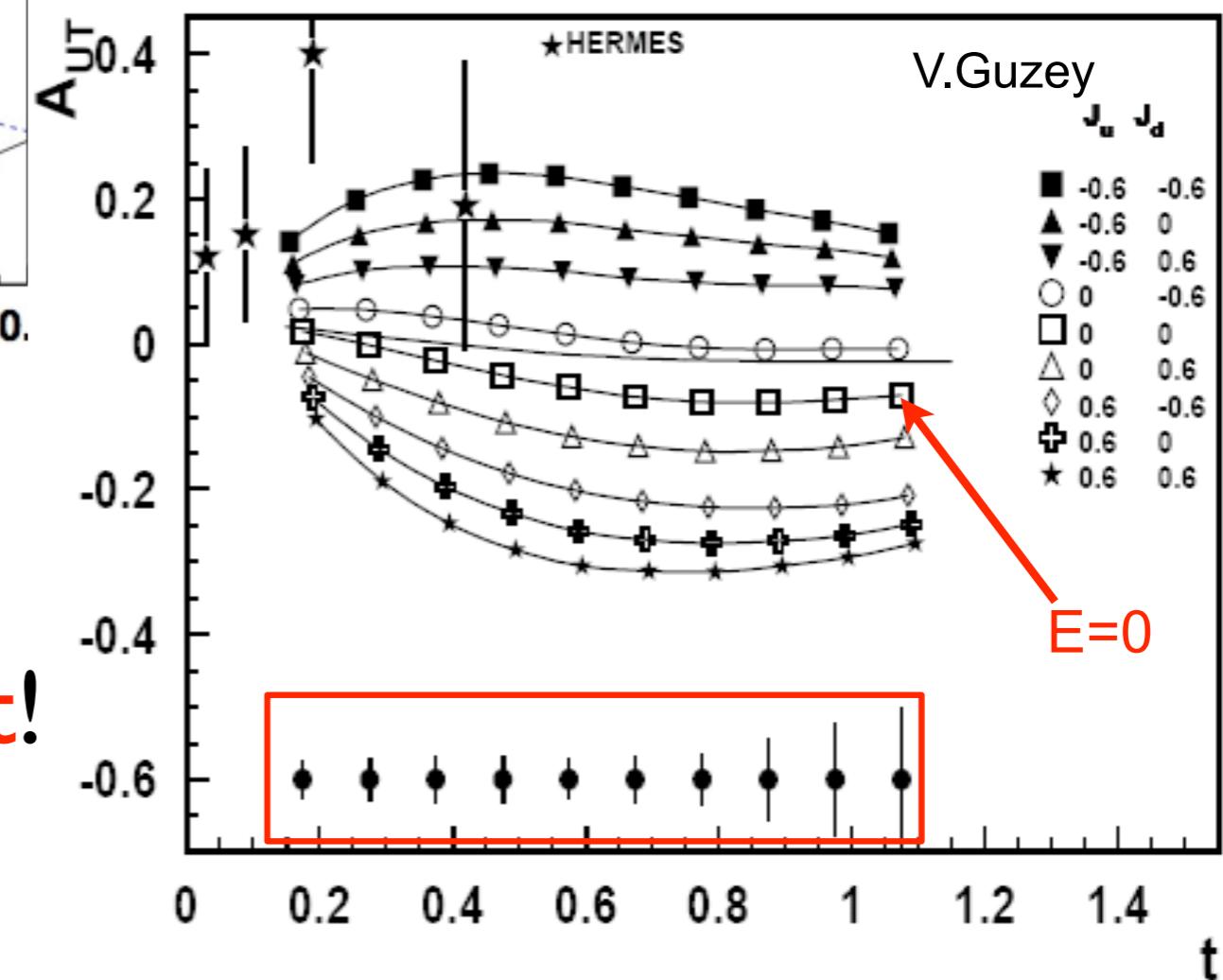
CLAS 12

$ep \rightarrow e' K^+ X$



Sivers moment will help confirm Quark OAM

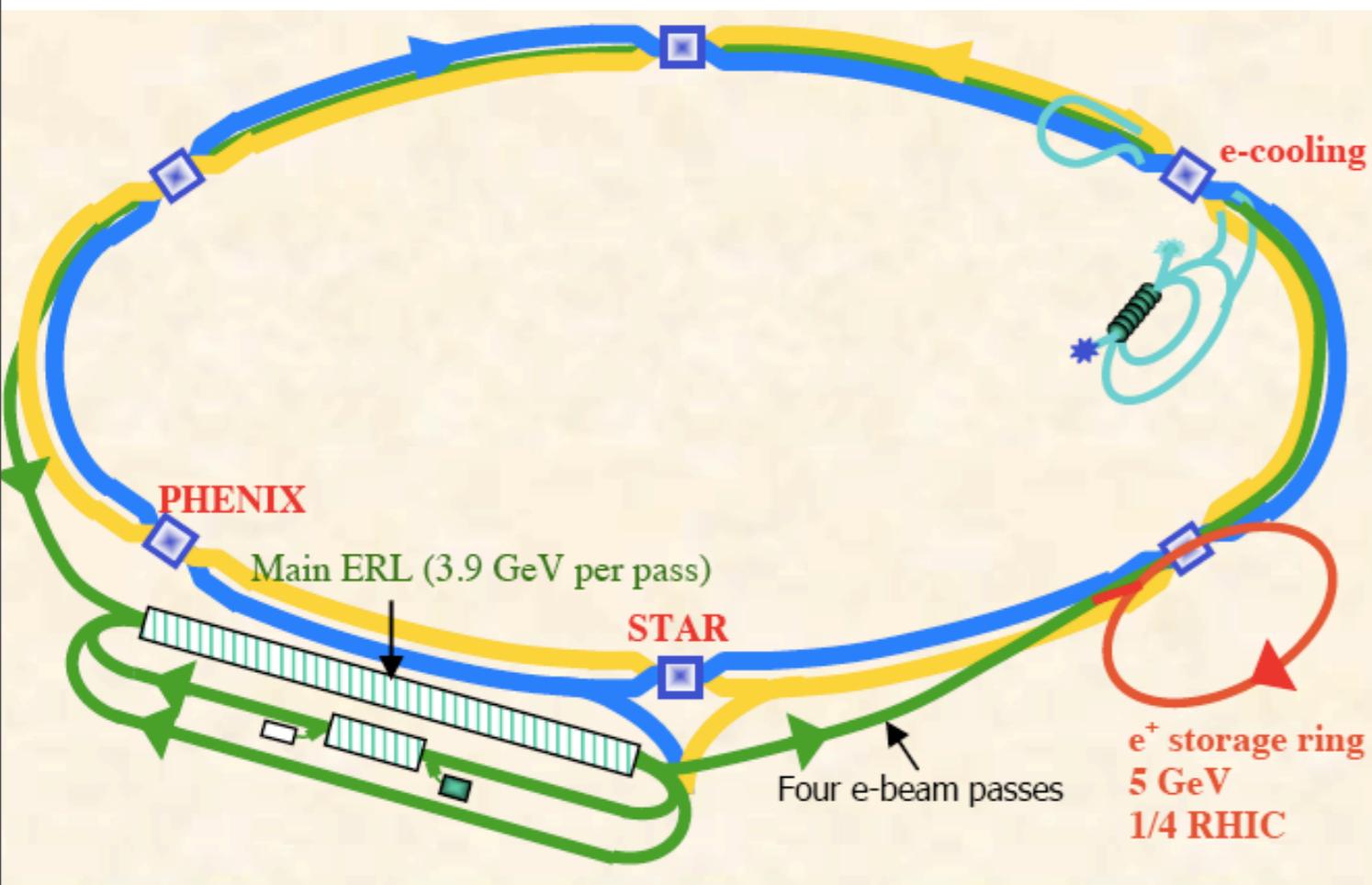
proton $x=0.25, Q^2=2.0$



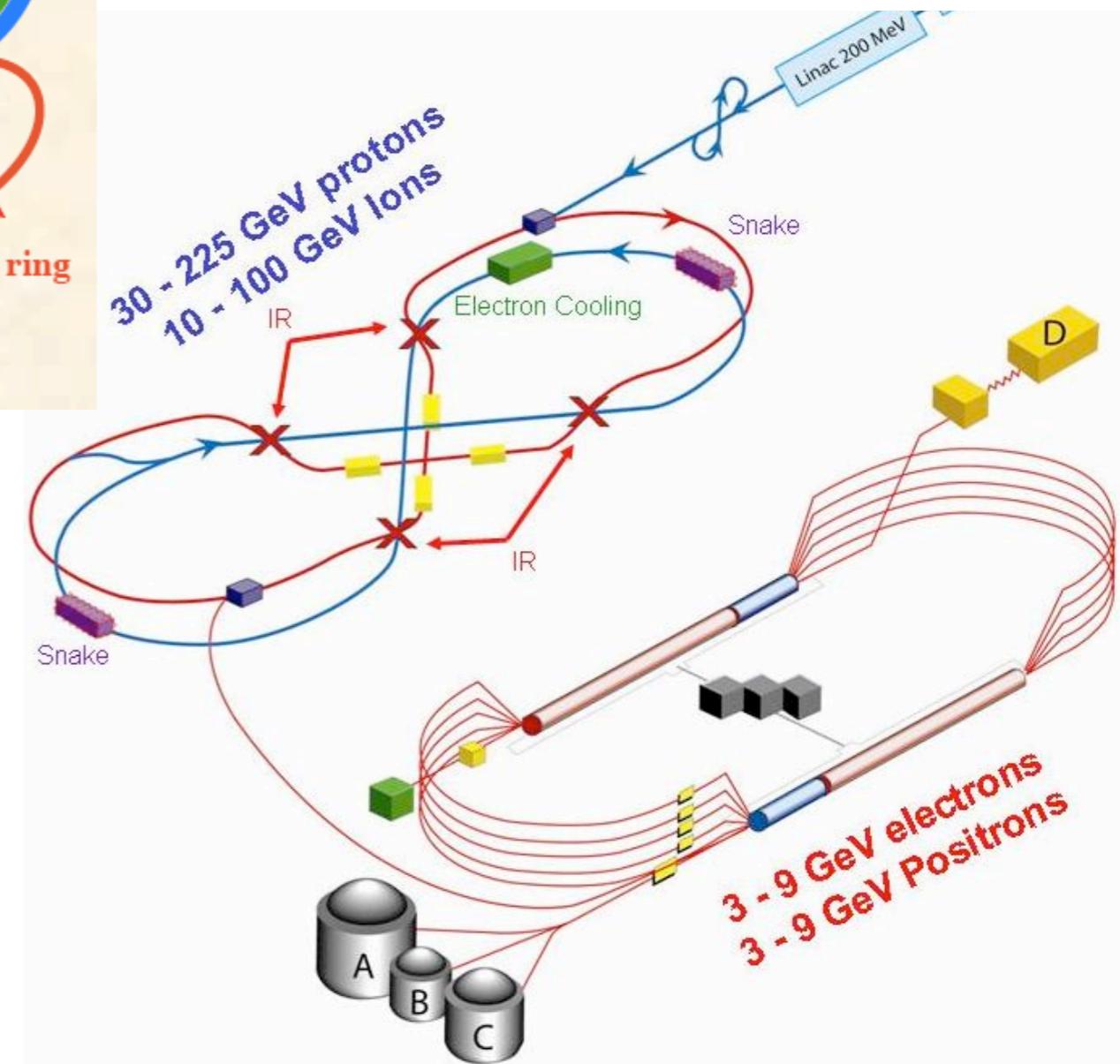
Measurement of TTSA in DVCS may help quantify it!

EIC

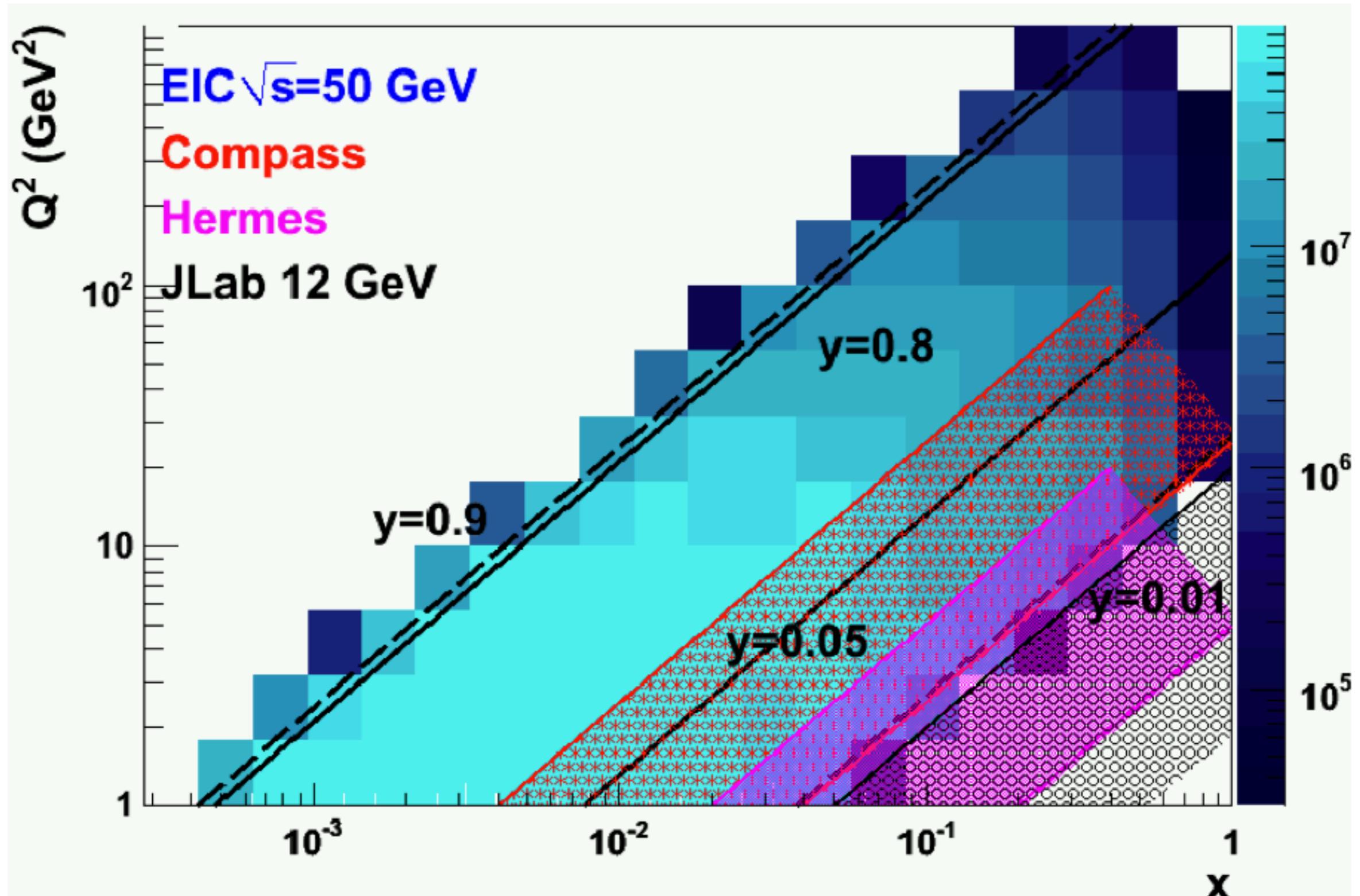
Two competing designs:
the resultant choice will
decide the precise
physics coverage



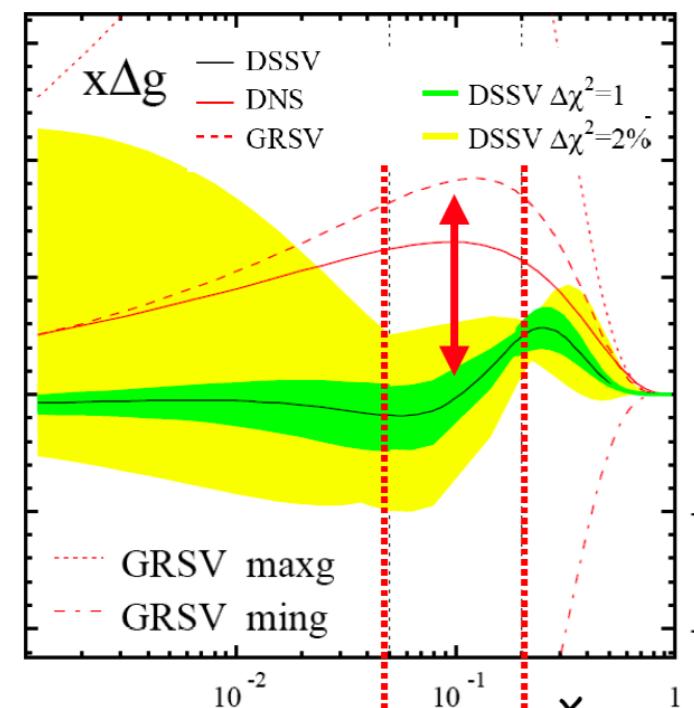
Will be built as a
machine to access sea
quarks and gluons: map
out distributions in
heretofore unexplored
areas!



EIC



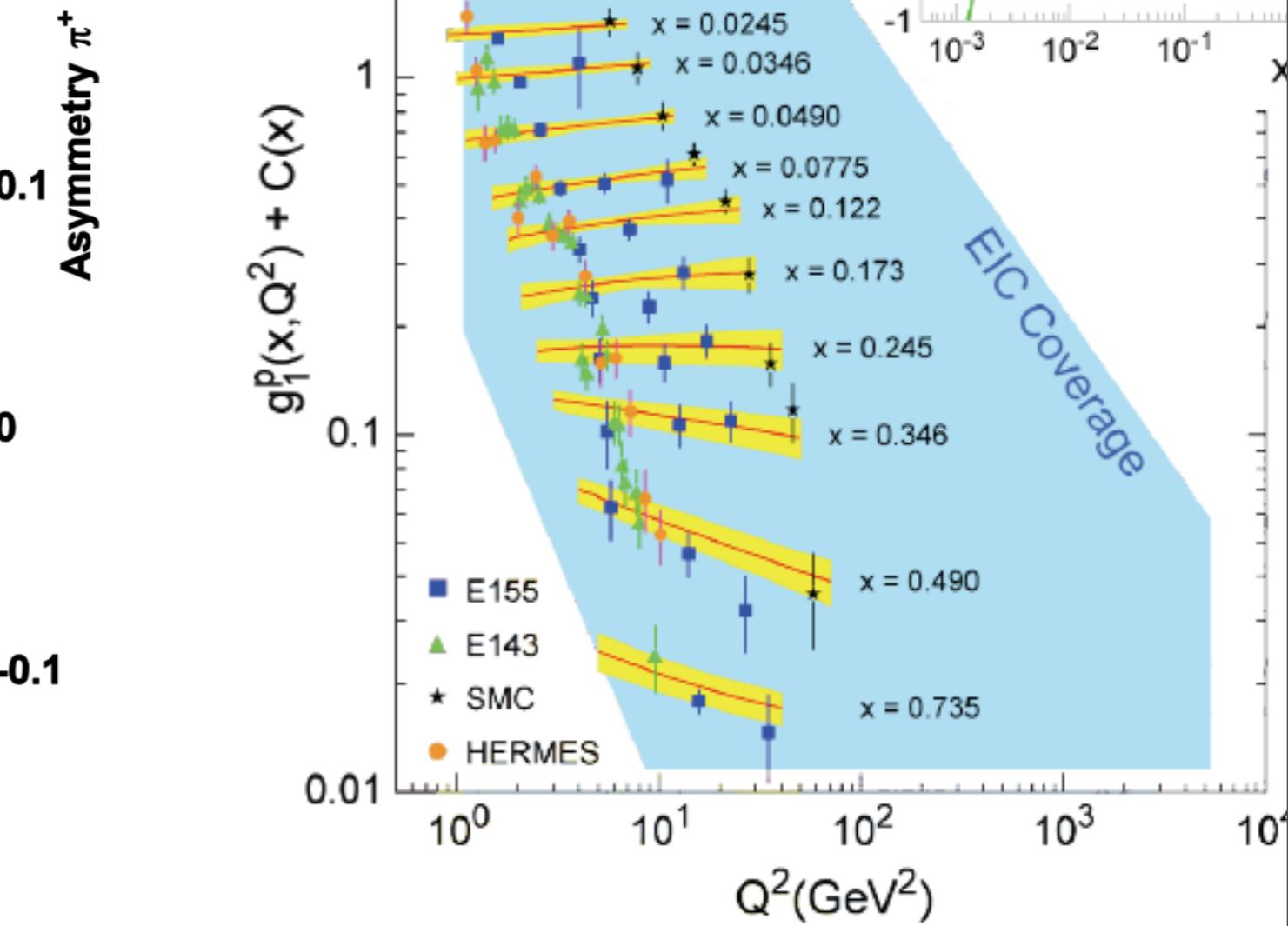
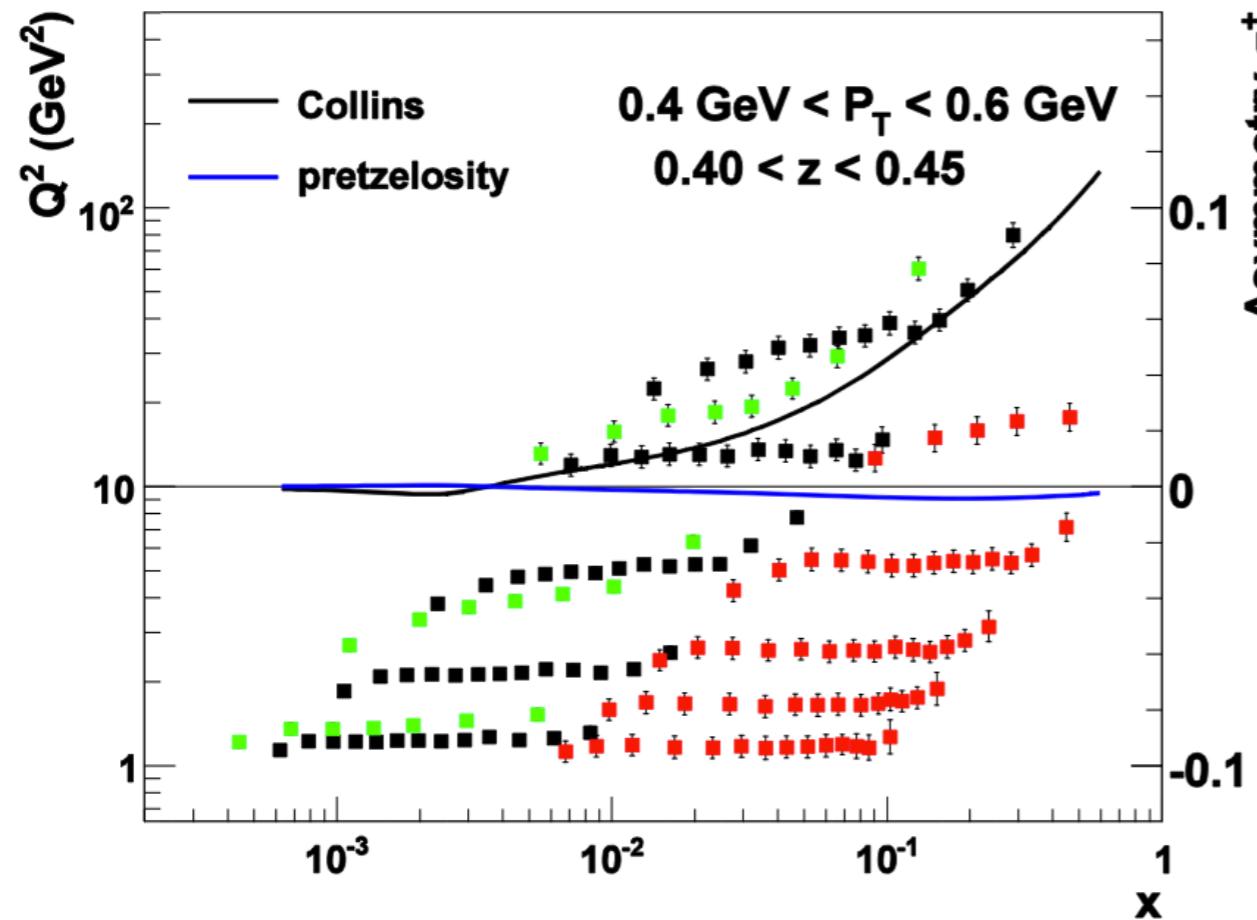
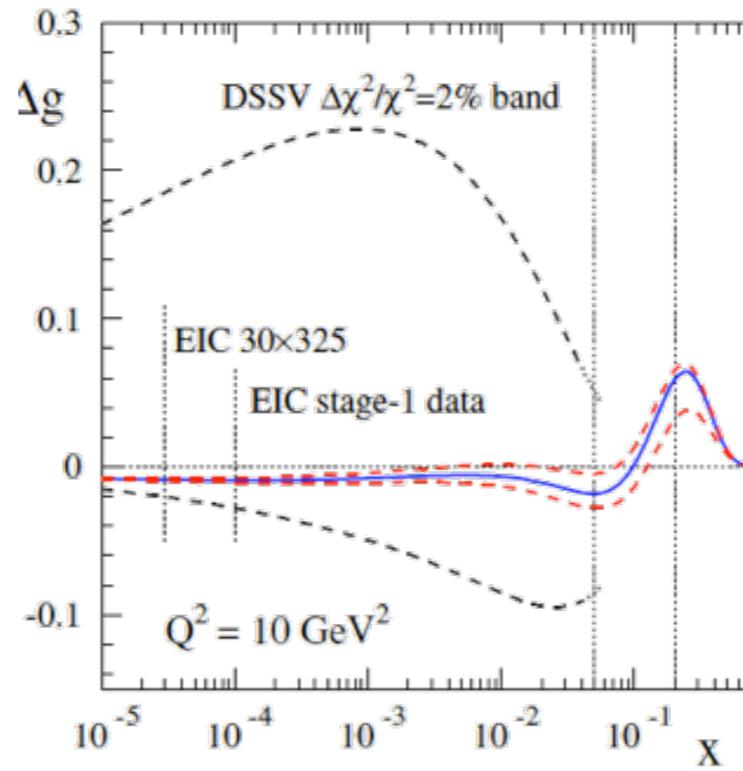
EIC



small- x
 $0.001 \leq x \leq 0.05$

RHIC range
 $0.05 \leq x \leq 0.2$

large- x
 $x \geq 0.2$



Summary

- One message of nucleon structure physics is that the **first thought is invariably incorrect**
- Theoretical calculations from 15 years ago are **still beyond the grasp of current experiments** - but getting closer all the time!
- Two-way street: a lot of **experimental data is not yet used** by theorists either!

Summary

- TMDs and GPDs currently offer the best route to understanding nucleon structure
- We can access those through SIDIS and DVCS and DVMP
- Look to JLab@12GeV and EIC for precise measurements