



National Radio Astronomy Observatory

UVa – 2009 Sep 25



# Dark Energy and the Hubble Constant

Jim Condon

- 1) What is dark energy (DE)?
- 2) How does an accurate ( $\sigma < 3\%$ ) local measurement of the Hubble constant  $H_0$  plus CMB data constrain DE?
- 3) How can radio astrometry determine  $H_0$ ?
- 4) Bonus: accurate SMBH masses

## The Megamaser Cosmology Project

<http://wiki.gb.nrao.edu/bin/view/Main/MegamaserCosmologyProject>

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## $H_0$ and the “age problem” if $\Omega_m = 1$ (Carroll, Press, & Turner 1992, ARA&A, 30, 449)

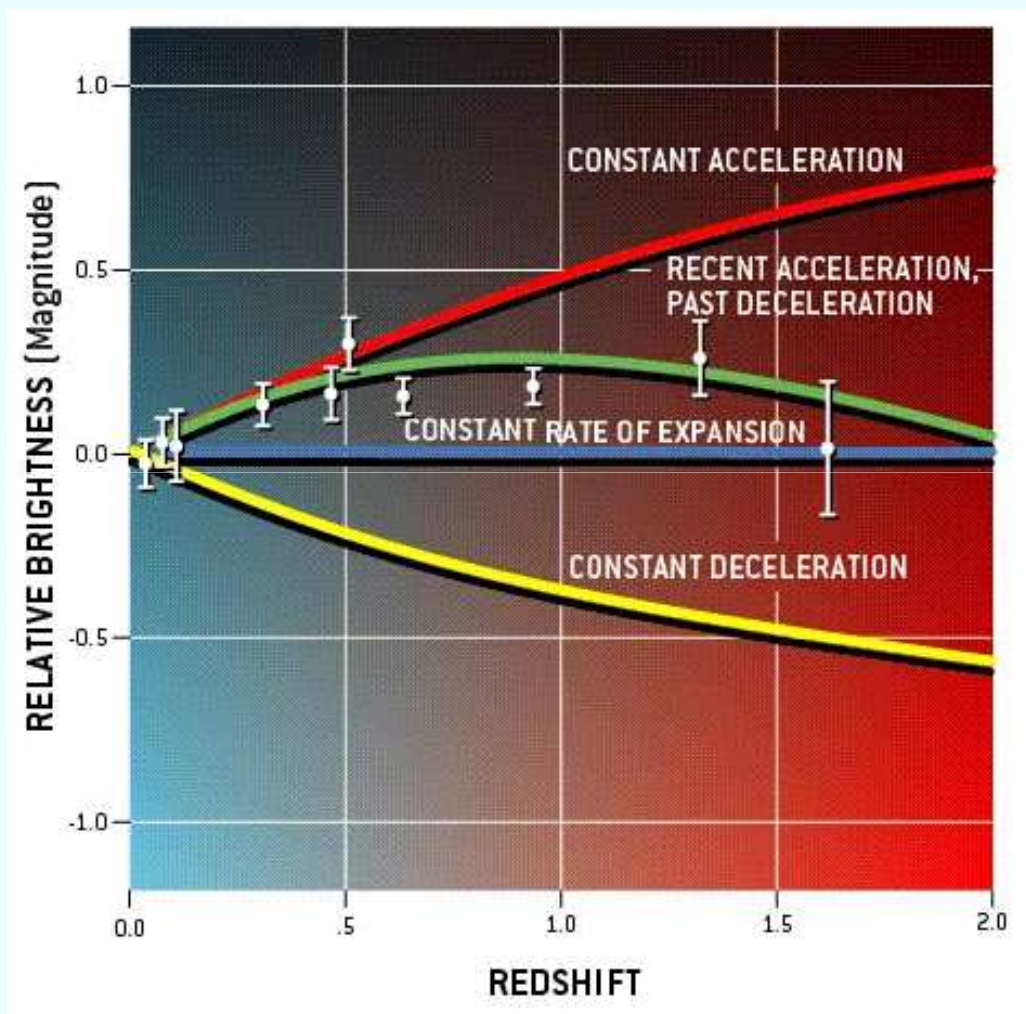
“Matter,” defined by  $p = 0$ , yields deceleration only, so the age of a matter-dominated universe is  $t_0 < 1 / H_0$ .

If  $\Omega_m = 1$  and  $H_0 = 72 \text{ km s}^{-1} \text{ Mpc}^{-1} = (13.6 \times 10^9 \text{ yr})^{-1}$ , then  $t_0 < \text{the age of the oldest stars}$ , so

Either  $H_0$  is too high or the expansion is not decelerating as fast as expected.

$$\frac{\ddot{a}}{a} = \frac{-\dot{a}^2}{2a^2}$$
$$a \propto t^{2/3} \quad \dot{a} \propto t^{-1/3}$$
$$\frac{\dot{a}}{a} = H = \frac{2}{3t}$$
$$t_0 = \frac{2}{3H_0} \approx 9 \text{ Gyr}$$

## Acceleration Observed



SNe type Ia used as relative standard candles indicate recent acceleration.



How can gravity make the universe accelerate?

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3c^2}(\rho + 3p).$$

Only energy density  $\rho$  and pressure  $p$  are relevant. For each constituent of the Universe, define  $w \equiv p / \rho$ . For nonrelativistic matter,  $w = 0$ ; for radiation,  $w = 1/3$ . Acceleration requires a sufficiently negative pressure  $w < -1/3$ ; e.g., the quantum vacuum has constant  $w = -1$  (but wildly wrong energy density). Is DE a variable “quintessence”? A better  $H_0$  constrains  $w$  via the expansion history of the universe.

## Conservation of stress-energy and the expansion of the universe

$$\dot{\rho} + 3\left(\frac{\dot{a}}{a}\right)(\rho + p) = 0$$

$$\frac{\dot{\rho}}{\rho} + \frac{3\dot{a}}{a}(1 + w) = 0$$

$$\text{matter } w = 0 \rightarrow \rho \propto a^{-3}$$

$$\text{radiation } w = 1/3 \rightarrow \rho \propto a^{-4}$$

$$\text{constant vacuum energy } \dot{\rho} = 0 \rightarrow w = -1$$

Radiation dominates at early times (small  $a$ ), then matter, and finally vacuum energy.

## How will it end?

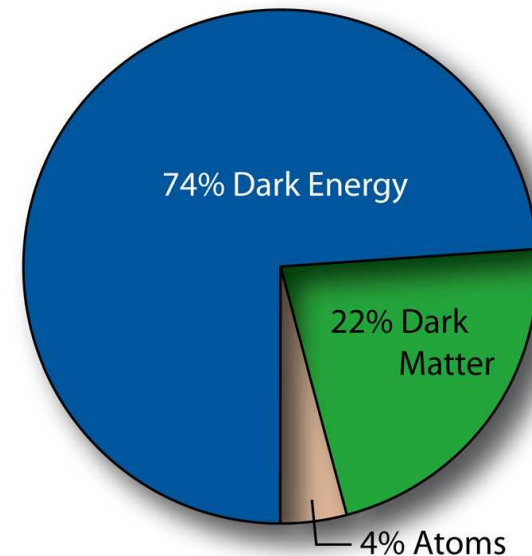
$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3c^2}\rho$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3c^2 a^3} \rightarrow a \propto t^{2/3} \quad (\text{matter})$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3c^2 a^4} \rightarrow a \propto t^{1/2} \quad (\text{radiation})$$

$$\left(\frac{\dot{a}}{a}\right)^2 = \text{constant} \rightarrow a \propto \exp(Ht) \quad (\text{vacuum})$$

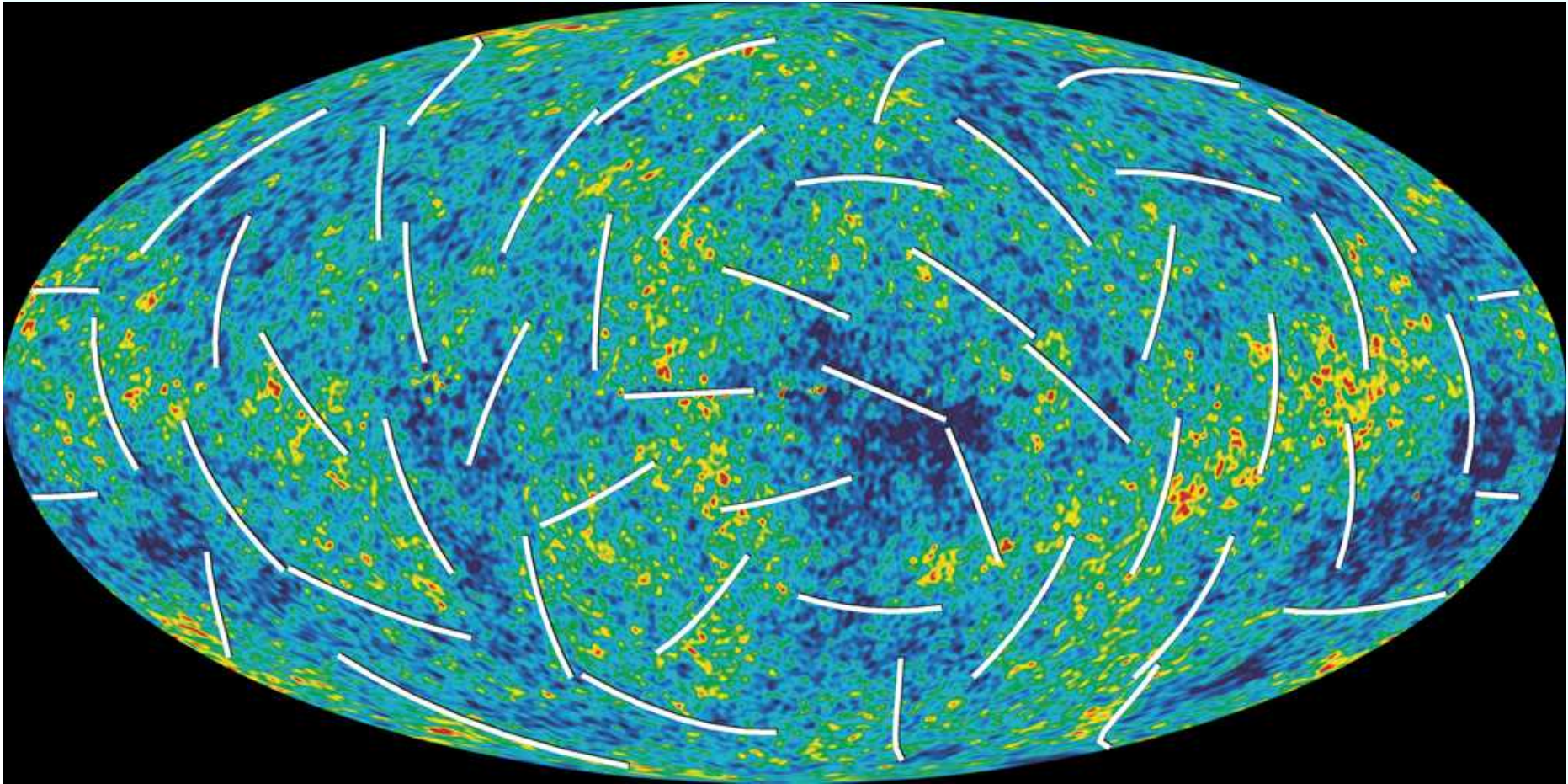
$$\rho_{\text{vac}} = \frac{3H^2 c^2}{8\pi G}, \quad H = H_0$$



DE dominates the future expansion of the universe, which will double in size every 14 Gyr and become very empty and dark.

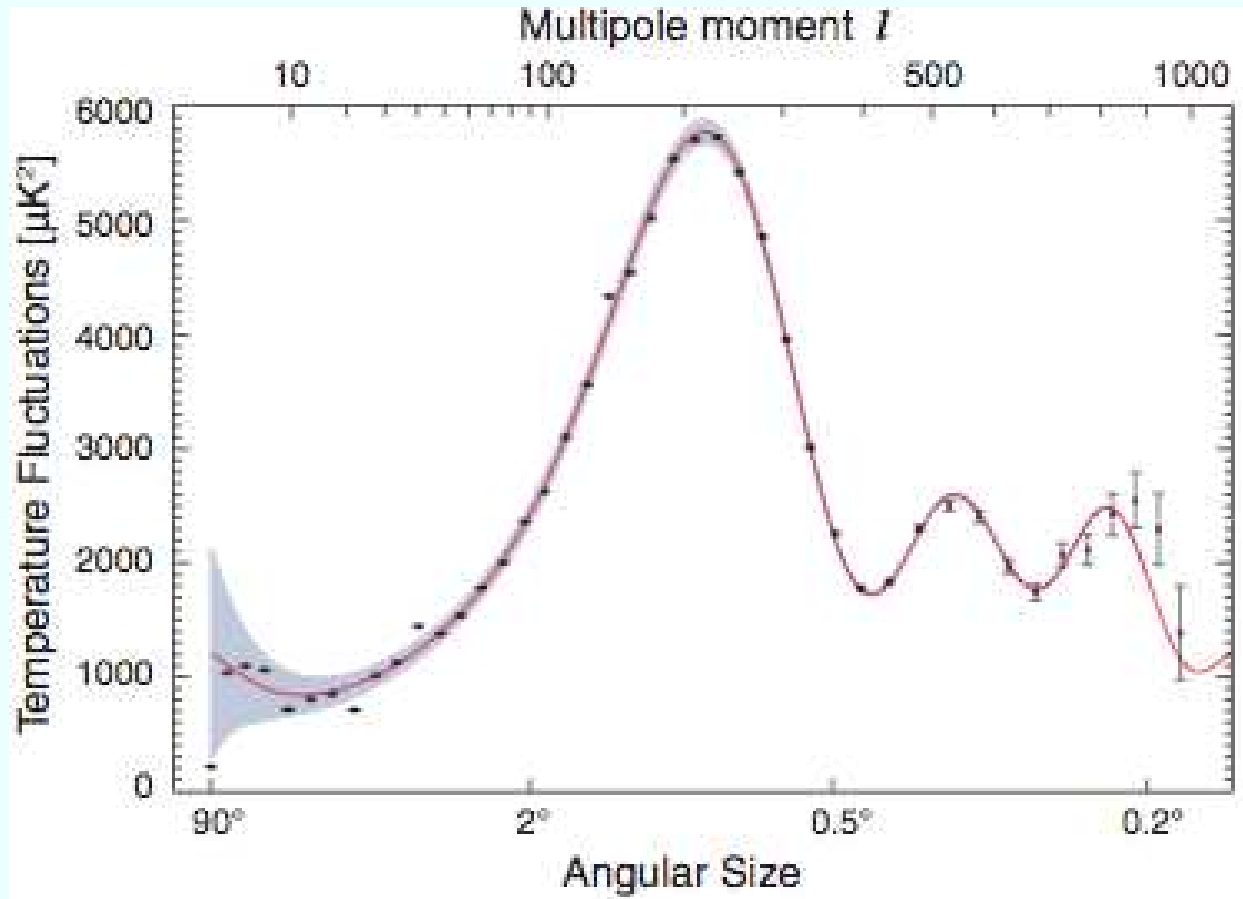


Absolute cosmic distances: constraining DE by measuring the expansion of the universe between  $z \sim 1089$  (CMB) and now ( $H_0$ )



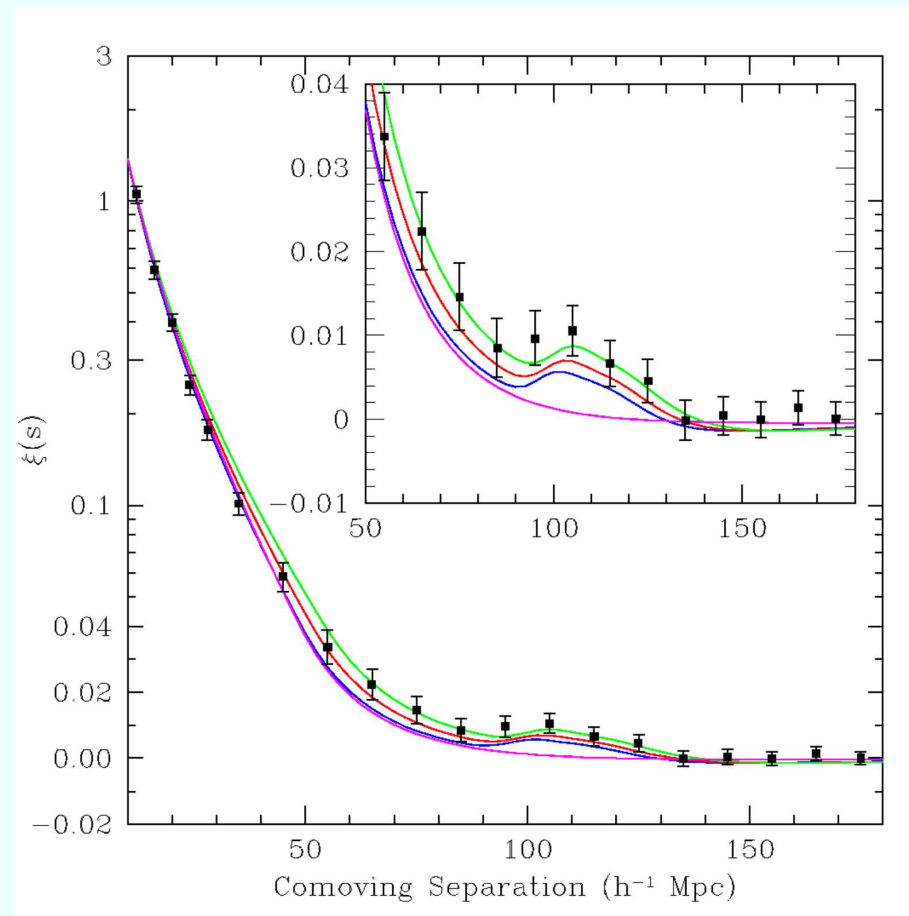


## WMAP 5-year TT power spectrum



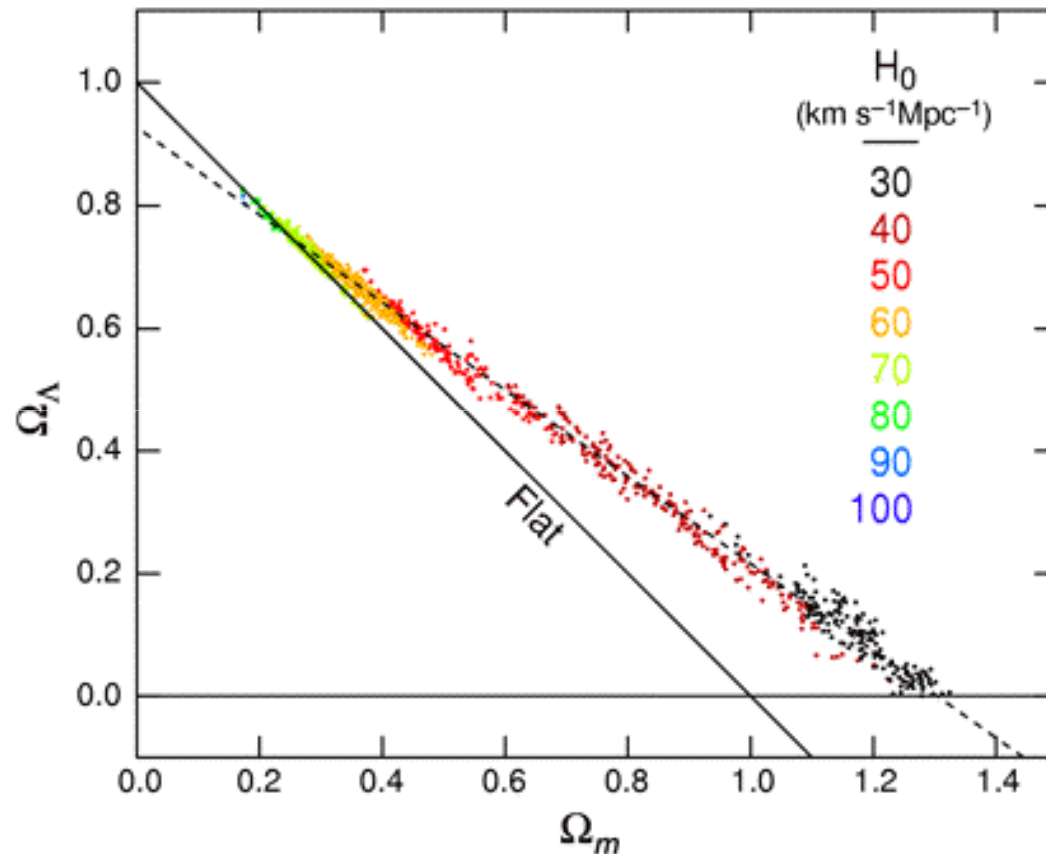
Absolute angular-size distance to  $z \sim 1089$   
= linear size (theory) / angular size (observed)

Baryonic acoustic oscillations of galaxies →  
statistical measurements of  $H$  at moderate  $z \sim 0.35$



Measures  $h = 105 \text{ Mpc} / 144 \text{ Mpc} = 0.73$  and the ratio  
of distances to  $z = 0.35$  and  $z = 1089$  to get  $\Omega_m = 0.27$ .  
(Eisenstein et al. 2005, ApJ, 633, 560)

## The CMB and $H_0$



Spergel et al., 2006

“While models with  $\Omega_{DE}=0$  are not disfavored by the WMAP data only, the combination of WMAP data plus measurements of the Hubble constant strongly constrain the geometry and composition of the universe”  
Spergel et al. 2006

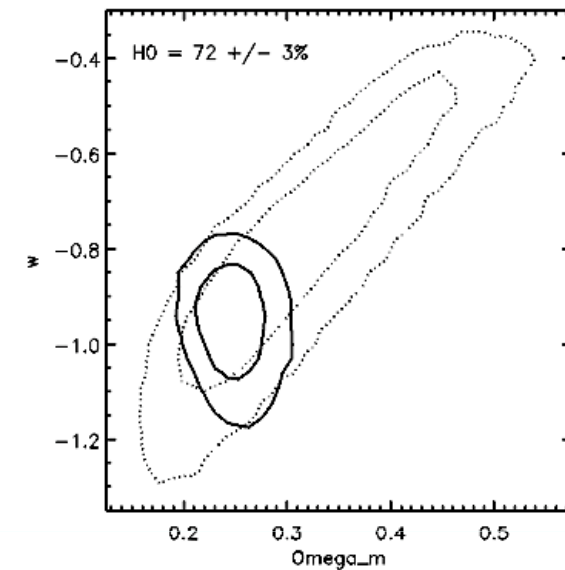
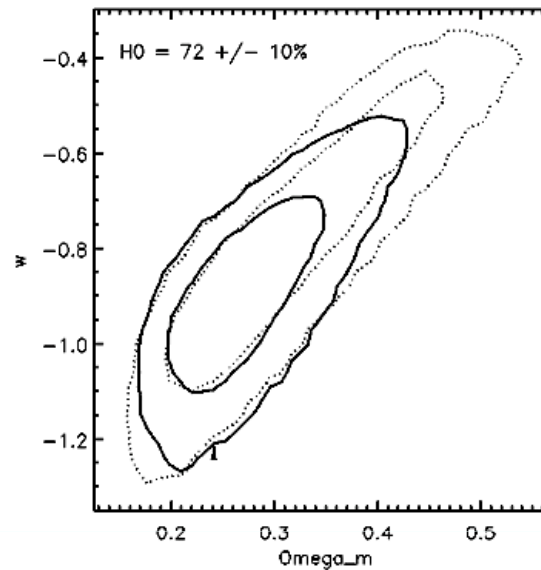
“The single most important complement to the CMB for measuring the DE equation of state at  $z \sim 0.5$  is a determination of the [local] Hubble constant to better than a few percent.”---Hu, W. 2005, “Dark Energy Probes in Light of the CMB,” ASPC 339, 215

# The Impact of an $H_0$ Prior

HST Key Project

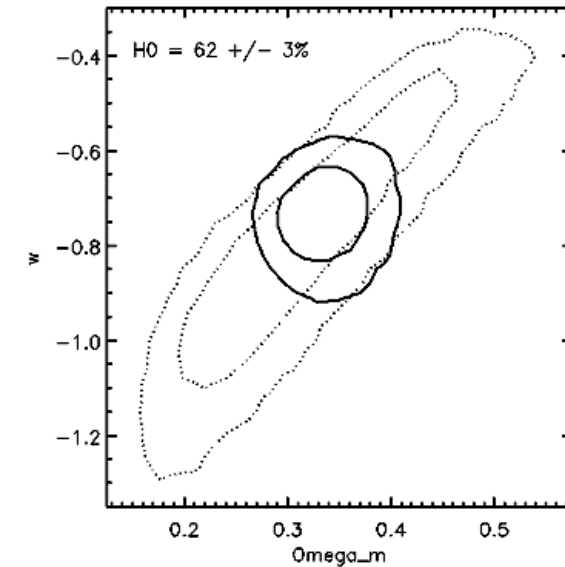
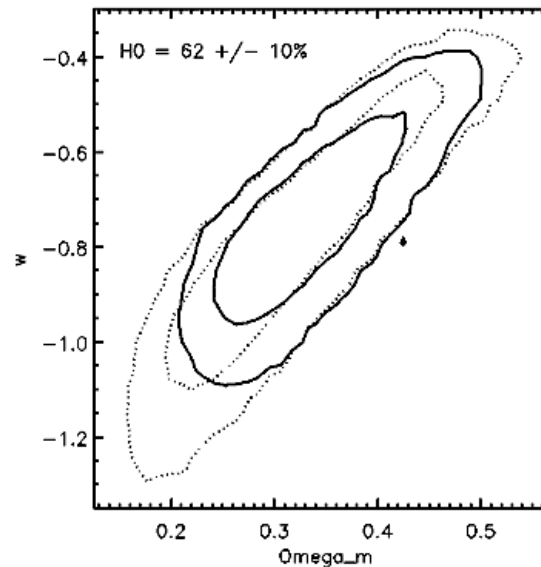
$$H_0 = 72$$

(Freedman et al. 2001)

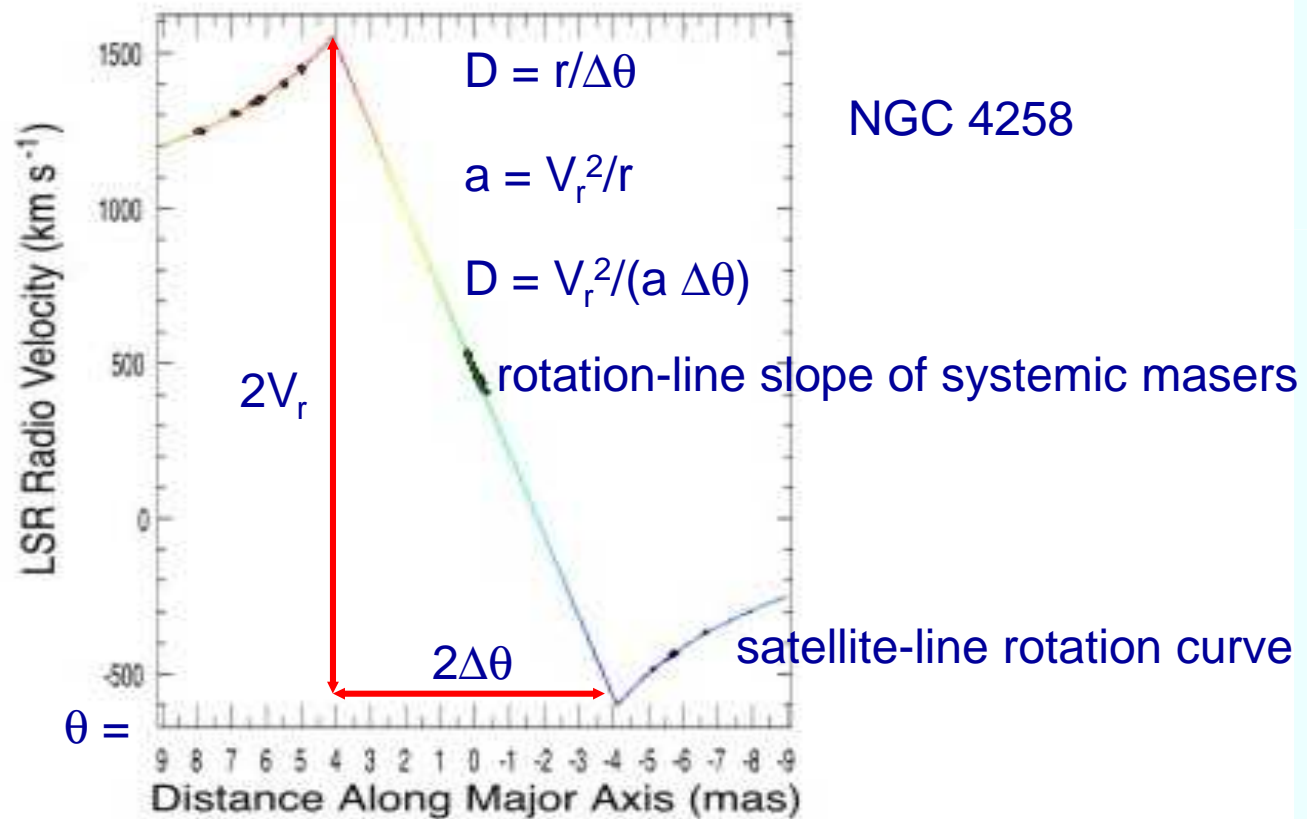
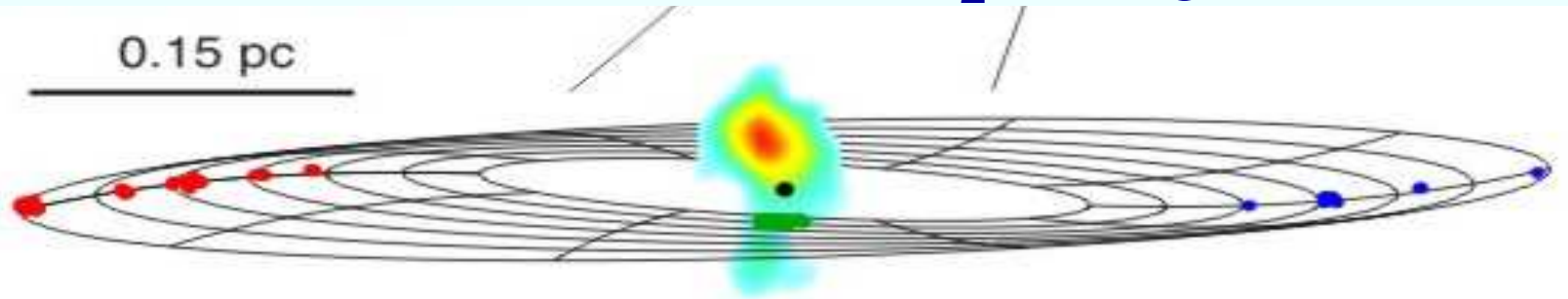


Sandage et al. (2006)

$$H_0 = 62$$



# Geometric Distances to H<sub>2</sub>O Megamasers





# Two methods to calculate the distance D

Rotation curve of satellite-line masers:

$$v_{\text{sat}}^2 \propto M/(D\theta_{\text{sat}}) \rightarrow M/D$$

Rotation-line slope of systemic masers:

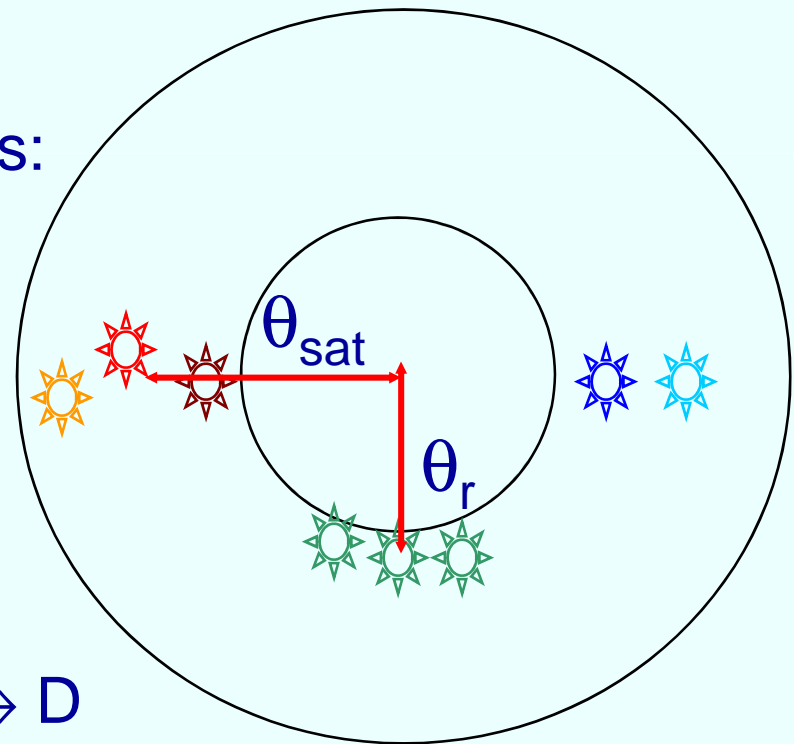
$$dv_{\text{sys}}/d\theta \propto [M/(D\theta_r^3)]^{1/2} \rightarrow \theta_r$$

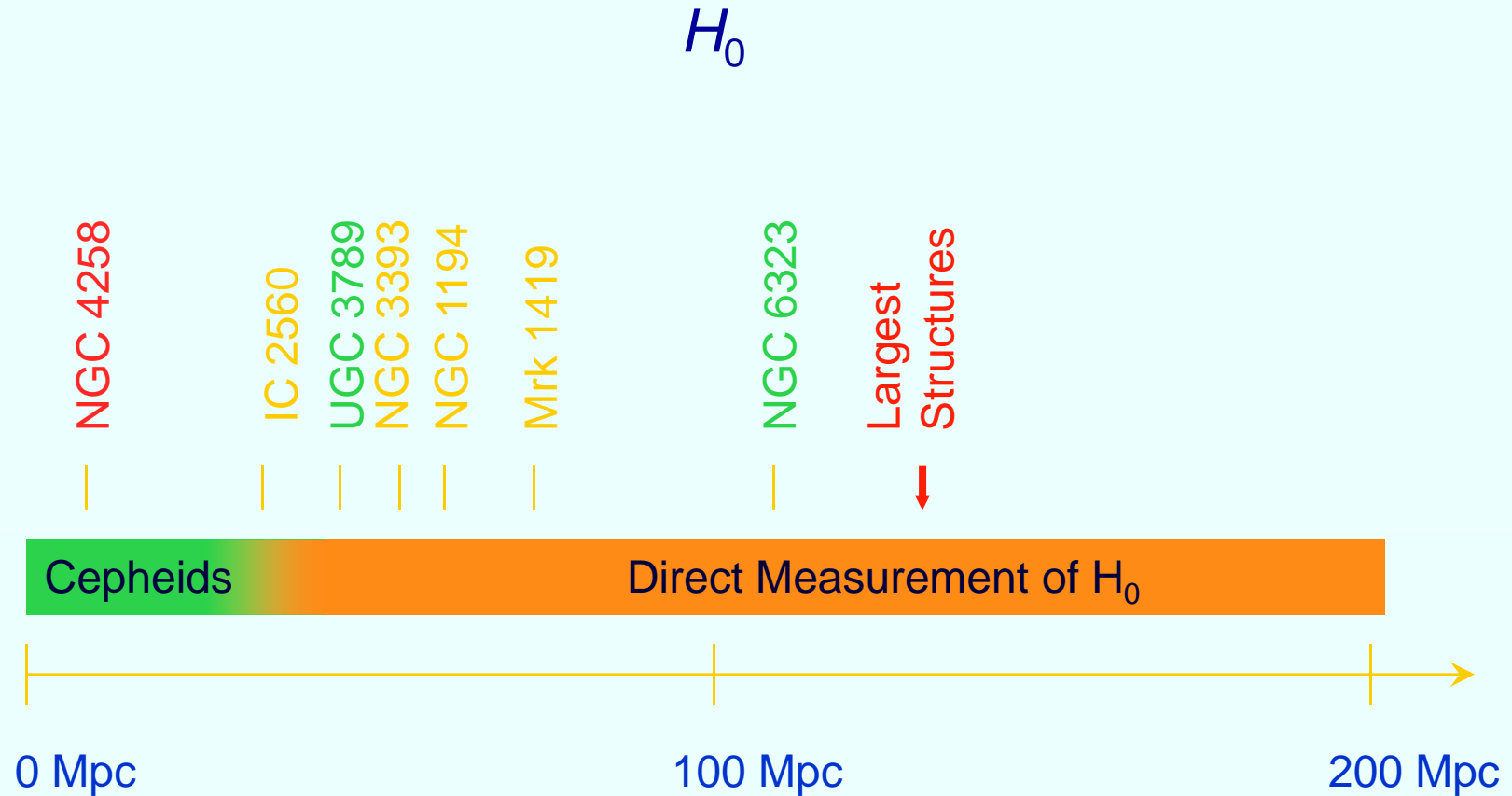
Acceleration of systemic masers:

$$(1) a_r \propto v_{\text{sys}}^2/(D\theta_r) \rightarrow D \rightarrow M$$

Proper motion of systemic masers:

$$(2) d\theta/dt = v_t/D \propto (M/D^3)^{1/2} \theta_r^{1/2} \rightarrow M \rightarrow D$$





- One method covers all scales out to the size of largest structures
- Maser distances can be used to calibrate other distance methods e.g. Cepheids, SN Ia, Tully-Fisher

## Megamaser Cosmology Project goals:

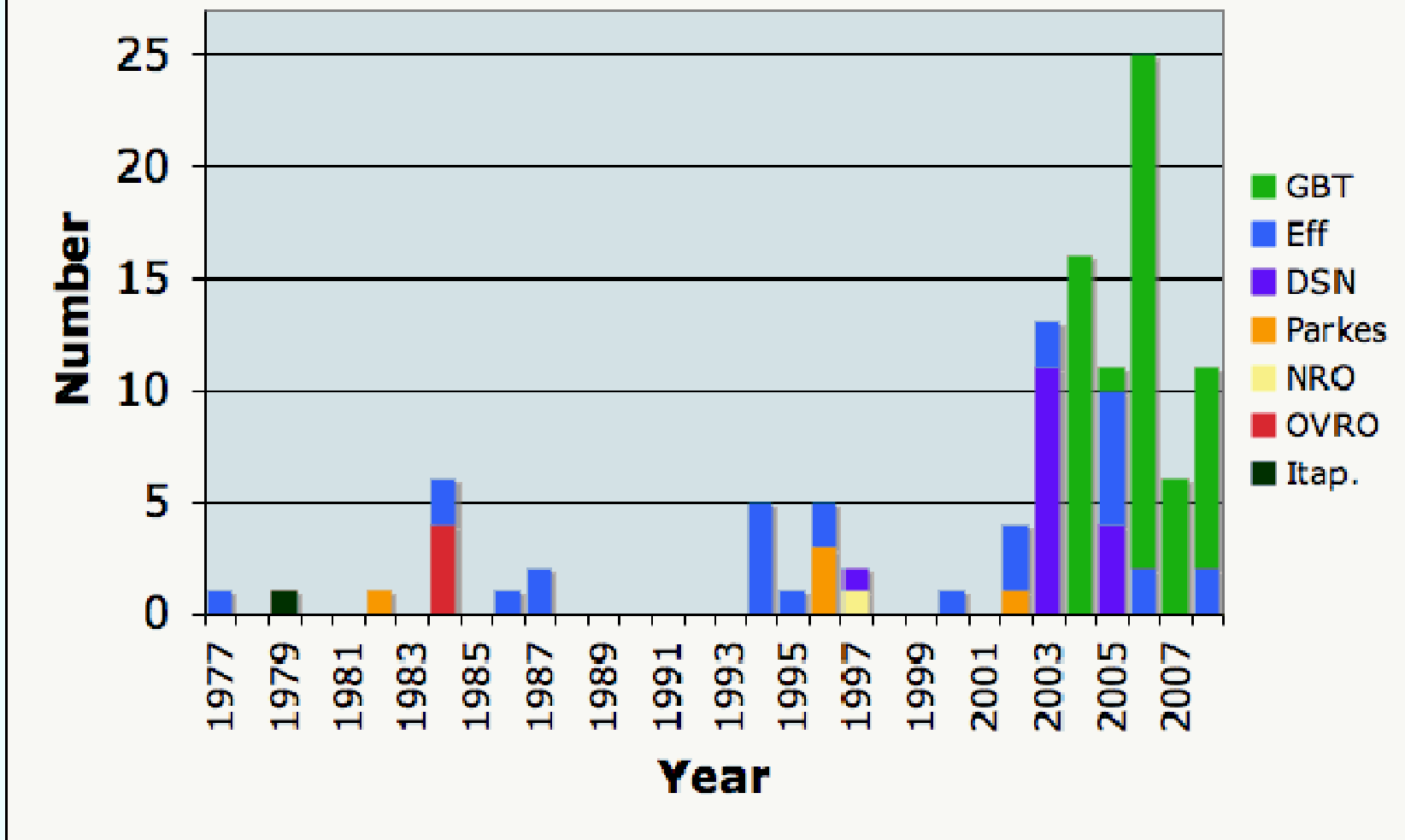
- Detect  $N > 10$  suitable  $\text{H}_2\text{O}$  megamasers (strong enough for VLBA+GBT, in edge-on disks) at distances  $D \sim 100$  Mpc (in Hubble flow) around the sky and measure their recession speeds
- Measure their geometric distances to  $\sim 10\%$  each via acceleration, mapping, and proper motion. Correct for known velocity fields to determine the average  $H_0$  within 3%, assuming random errors.

## Step 1: Detections and velocities



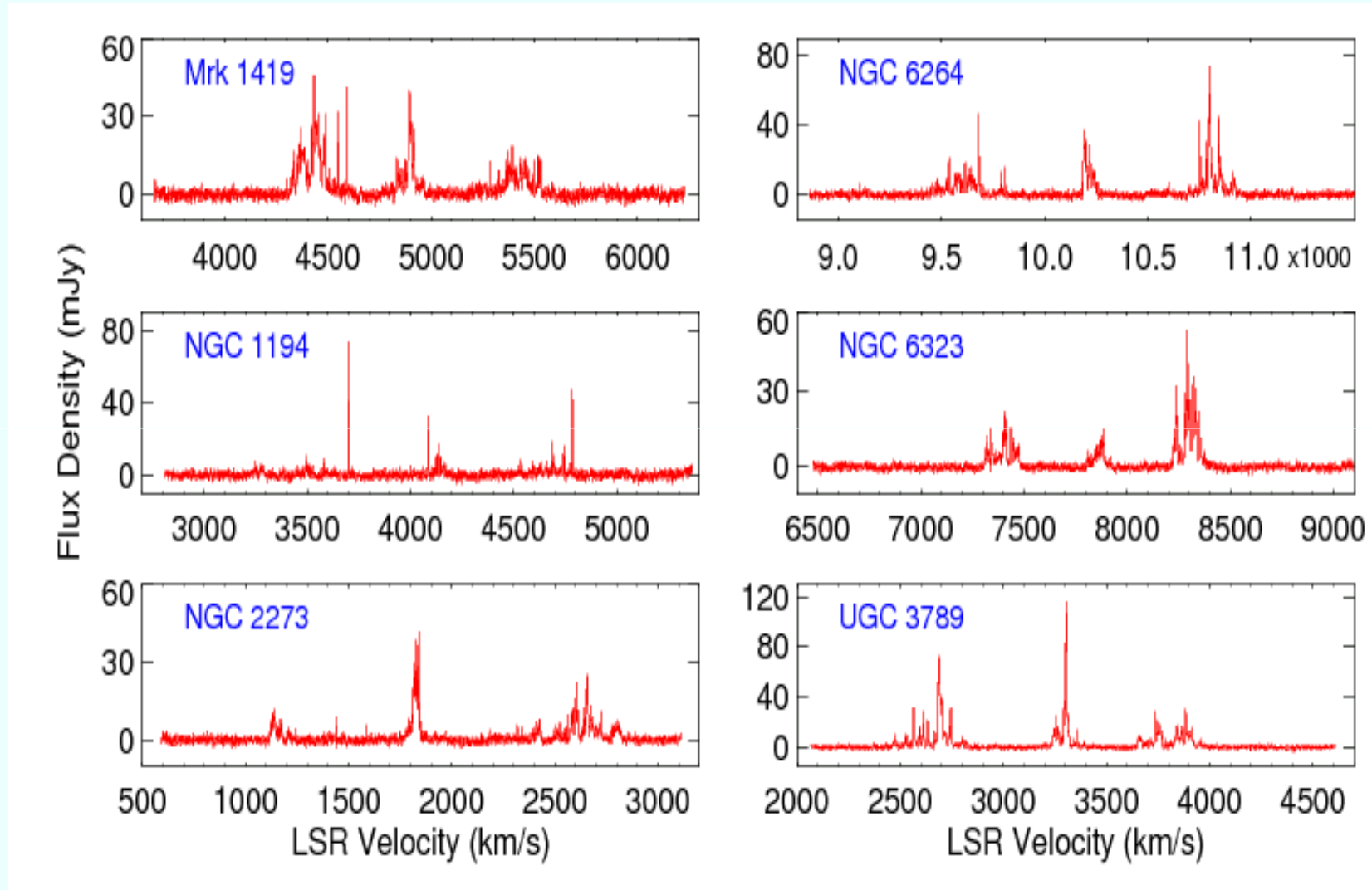
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## Extragalactic H<sub>2</sub>O Maser Discoveries by Year

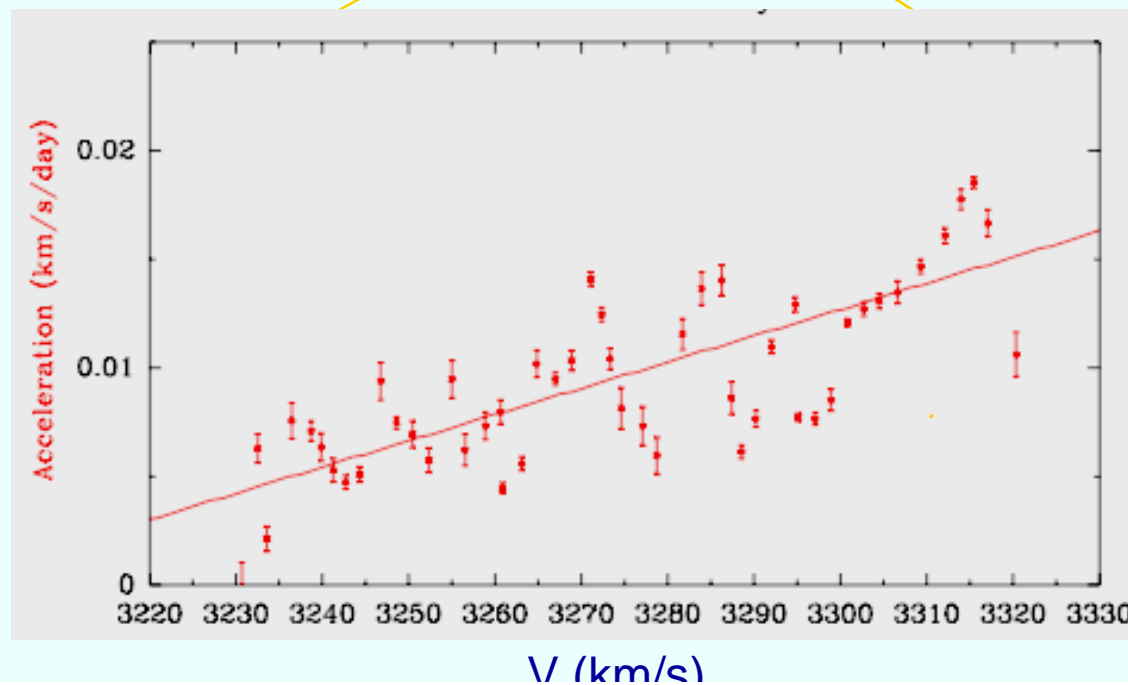
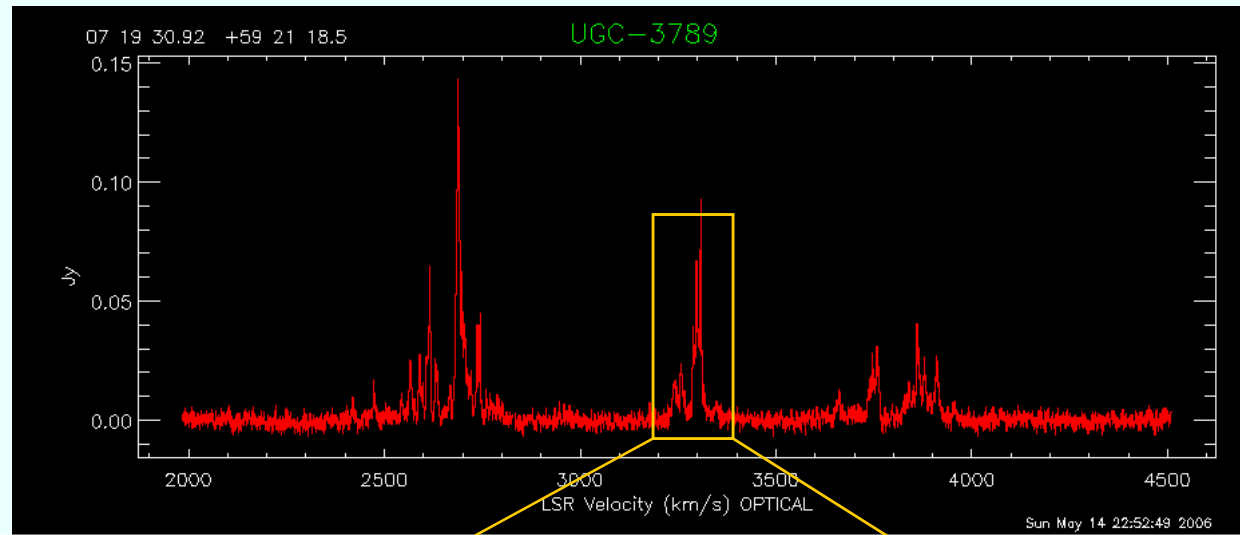




# GBT Spectra of Some Maser Disks

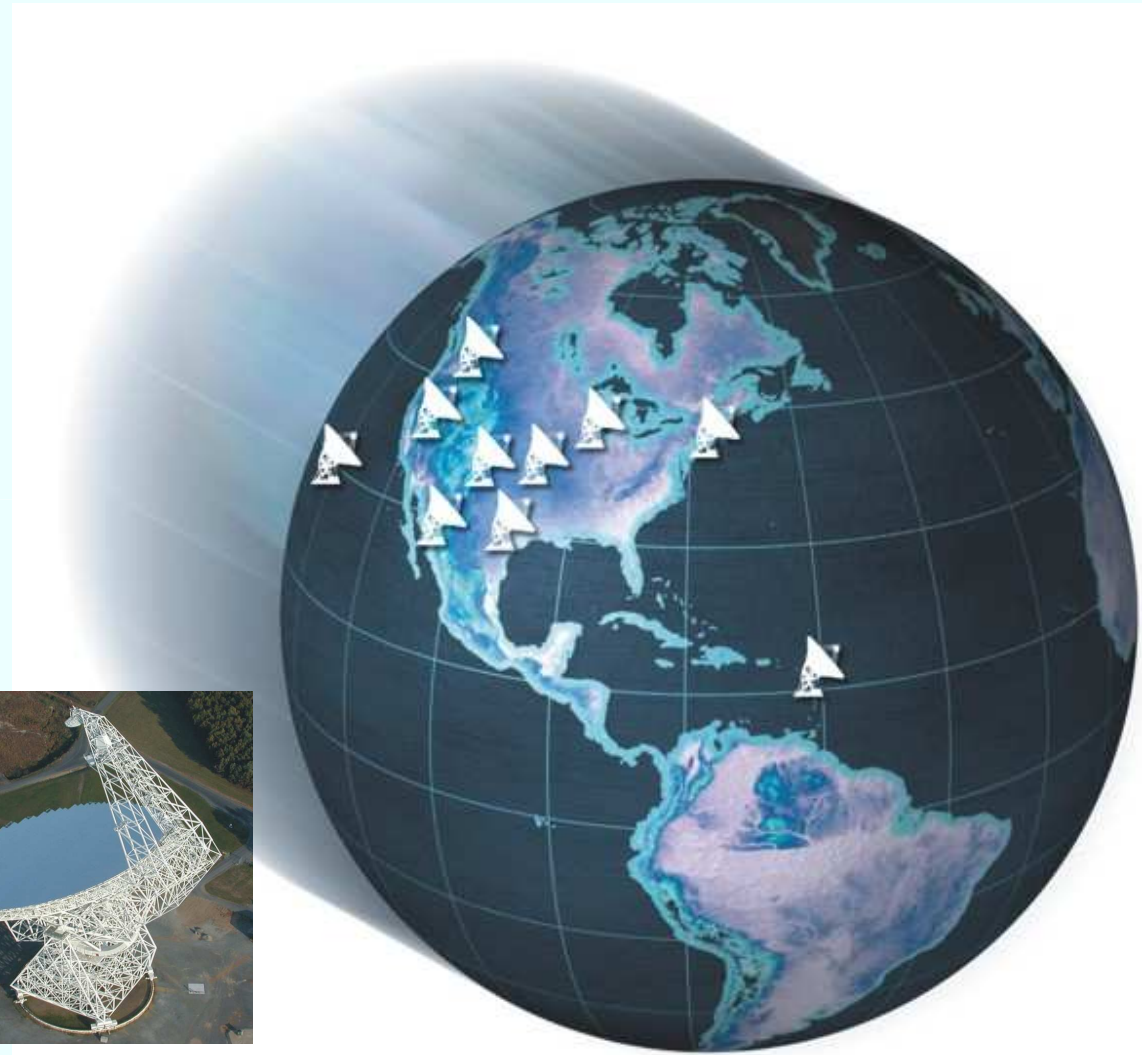


## Step 2: Measure Accelerations

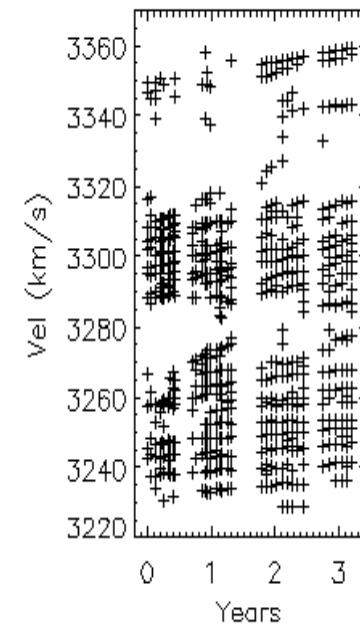
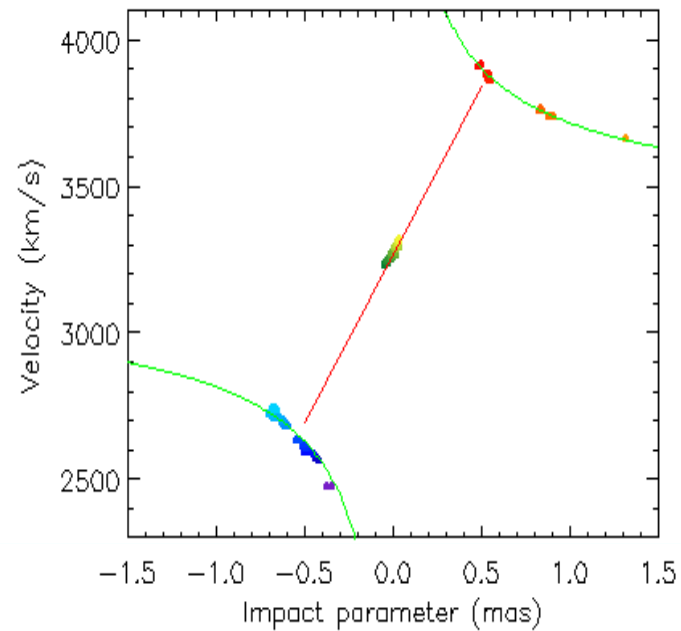
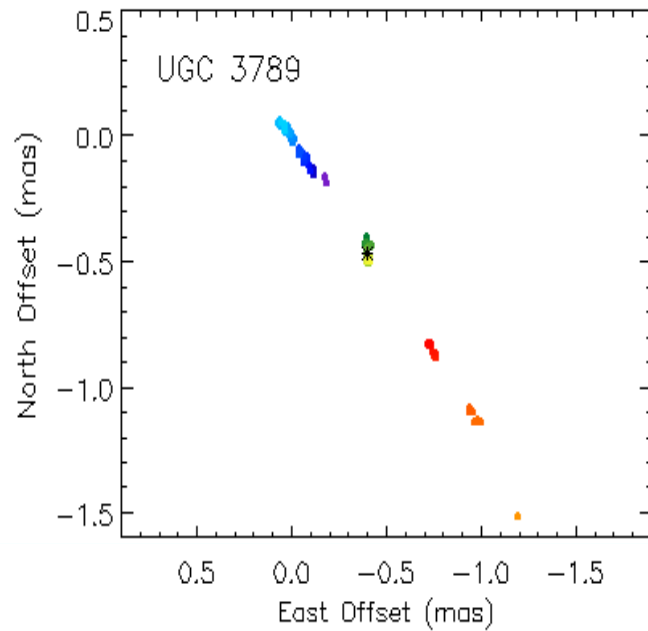


## Step 3: Imaging GBT + VLBA

The GBT lets us:  
Image fainter (more distant) H<sub>2</sub>O masers  
Use fainter (closer on the sky) continuum phase calibrators or even line self-calibration (NGC 1194 S > 500 mJy during flares)



# UGC 3789 Results



$R \sim 0.09 - 0.20 \text{ pc} \text{ (} 0.40 - 0.87 \text{ mas)}$

$V \sim 750 - 450 \text{ km/s}$

$M_{\text{bh}} \sim 1.2 \times 10^7 M_{\text{sun}}$

$a \sim 3.6 \text{ km s}^{-1} \text{ yr}^{-1} \text{ (mean value)}$

$D \sim 50 \text{ Mpc} \pm 13\%$

$H_0 \sim 71 \pm 10 \text{ km s}^{-1} \text{ Mpc}^{-1}$

# Supermassive black hole?

Or dense “star” cluster?

Plummer distribution:

$$\rho(r) = \rho_0 (1 + r^2/c^2)^{-5/2}$$

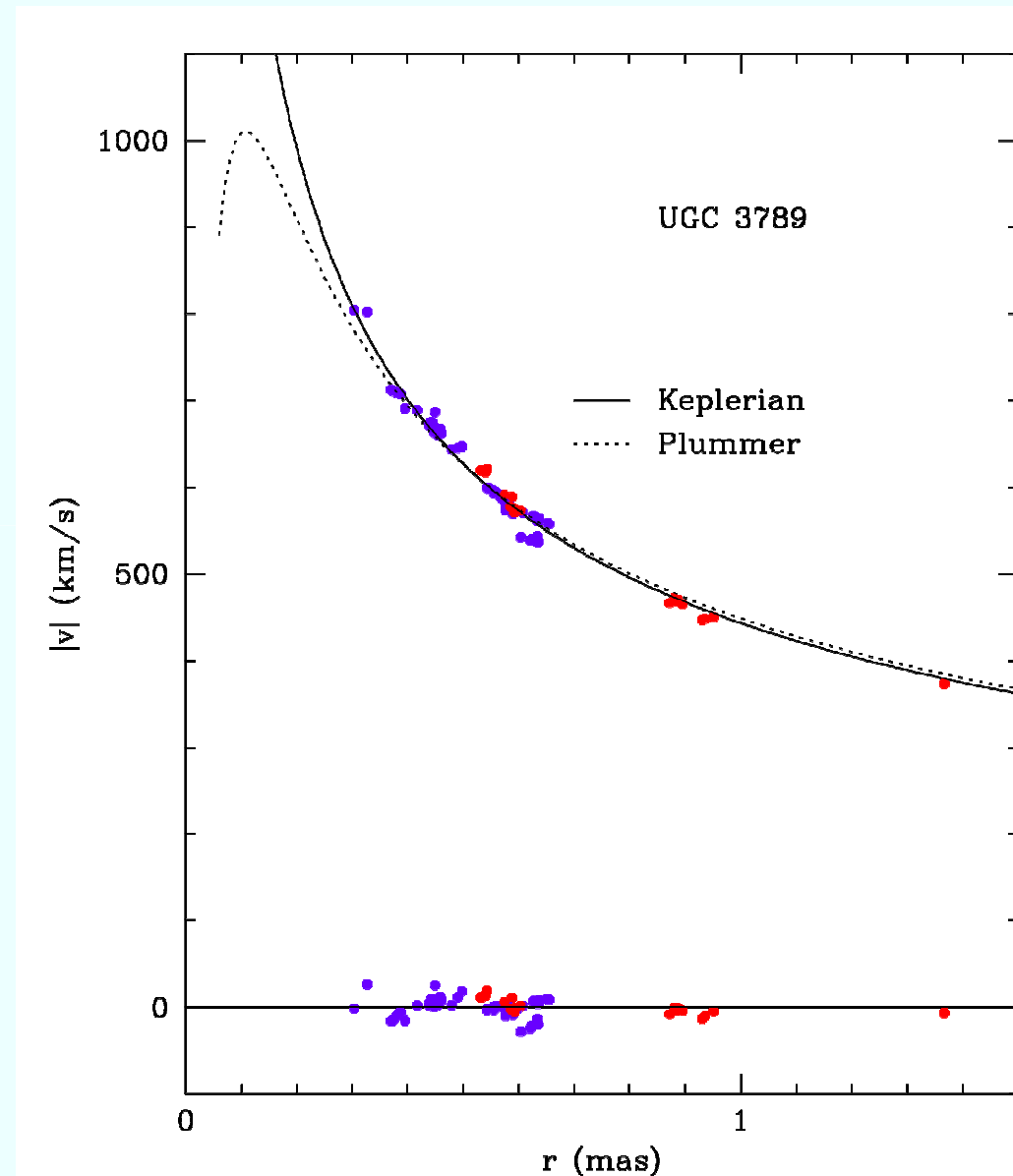
1. Evaporation if N small

2. Collisions if N large

$$\rho_0 > 4 \times 10^{11} M_{\text{sun}}/\text{pc}^3$$

$$m_* < 0.08 M_{\text{sun}} \quad N > 10^8$$

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# Direct measurements of SMBH masses

<b>Galaxy</b>	<b>Radius (pc)</b>	<b><math>M_{\text{bh}}</math> (<math>M_{\text{sun}}</math>)</b>
Mrk 1419	0.05 – 0.30	$7.5 \times 10^6$
NGC 1194	0.58 – 1.41	$6.6 \times 10^7$
NGC 2273	0.03 – 0.08	$7.6 \times 10^6$
NGC 6264	0.23 – 0.78	$2.5 \times 10^7$
NGC 6323	0.11 – 0.29	$1.0 \times 10^7$
UGC 3789	0.08 – 0.30	$1.1 \times 10^7$

## Summary

- An accurate ( $< 3\%$ ) measurement of  $H_0$  independent of the CMB and other techniques (e.g. distance ladder) is critical for characterizing dark energy, testing the flat  $\Lambda$ CDM model, and fixing fundamental cosmological parameters (e.g. deriving  $\Omega_m$  from the CMB observed  $\Omega_m h^2$ ).
- Recent observations of megamaser disks support the feasibility of using the GBT and VBLA to measure  $H_0$  directly.
- Accurate masses of SMBHs

## Summary

- An accurate ( $< 3\%$ ) measurement of  $H_0$  independent of the CMB and other techniques (e.g. distance ladder) is critical for characterizing dark energy, confirming the flat  $\Lambda$ CDM model, and fixing other cosmological parameters (e.g. deriving  $\Omega_m$  from the observed  $\Omega_m h^2$ ).
- Recent observations of megamaser disks support the feasibility of using the GBT and VBLA to measure  $H_0$  directly.