

The Quantum Mechanics of Global Warming

Brad Marston

Brown University

University of Virginia

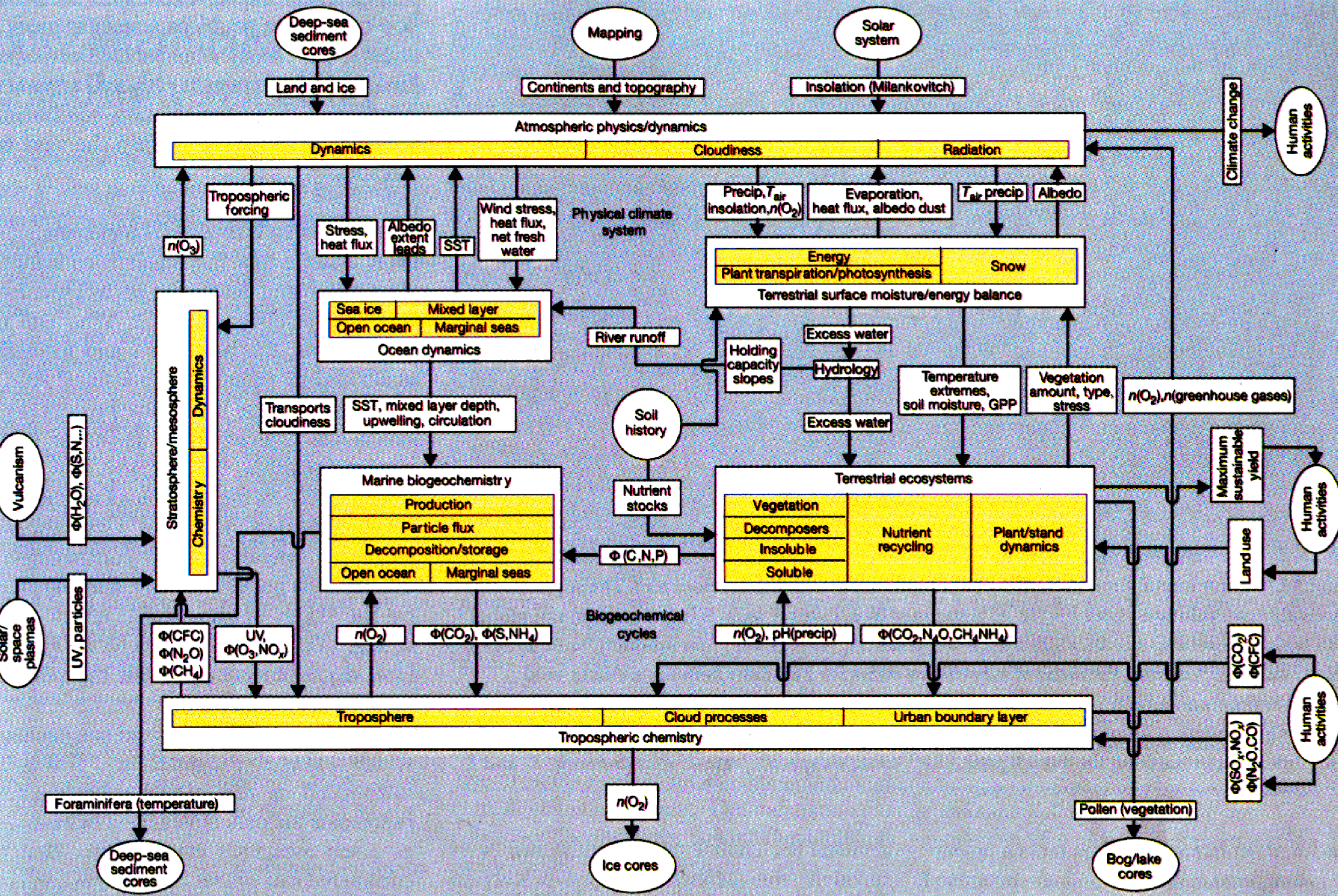
April 17, 2009

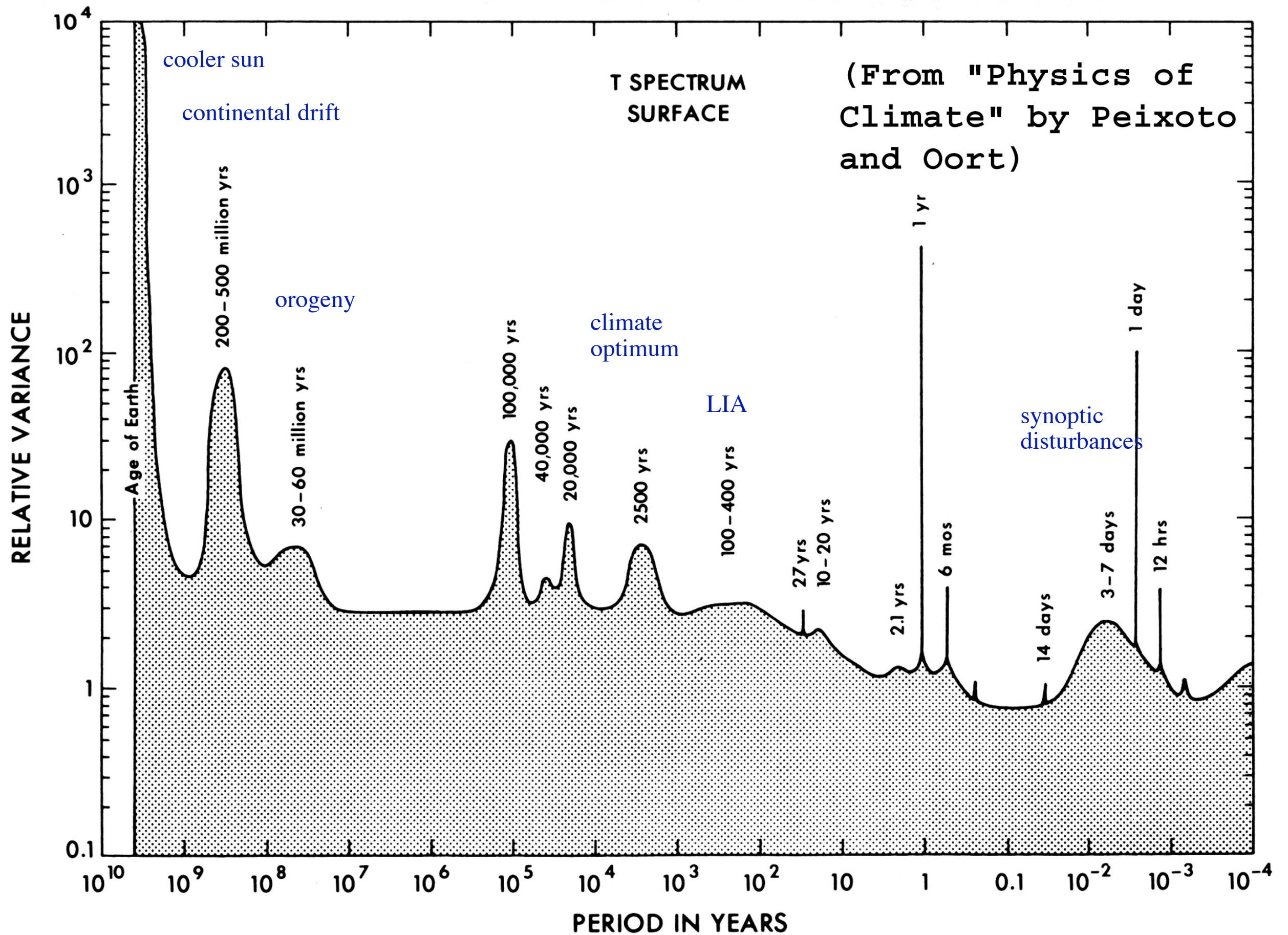


Richardson's Human Weather Computer (1917 --1922)



“Lewis Fry Richardson’s imaginary ‘forecast factor’ would have employed some 64,000 human computers to keep up with the pace of the weather, The workers sit in tiers inside a great spherical theater; the director, atop a pedestal in the middle, shines a beam of light on those places where the calculation is getting ahead or falling behind.” [Brian Hayes, *American Scientist* **80**, 10 -- 14 (2001).]





Outline

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- Quantum Mechanics #1: blackbody radiation

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- Ecosystems and feedbacks

Crisis in 19th Century Classical Physics

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$$Intensity = function(Temperature, frequency)$$

Crisis in 19th Century Classical Physics

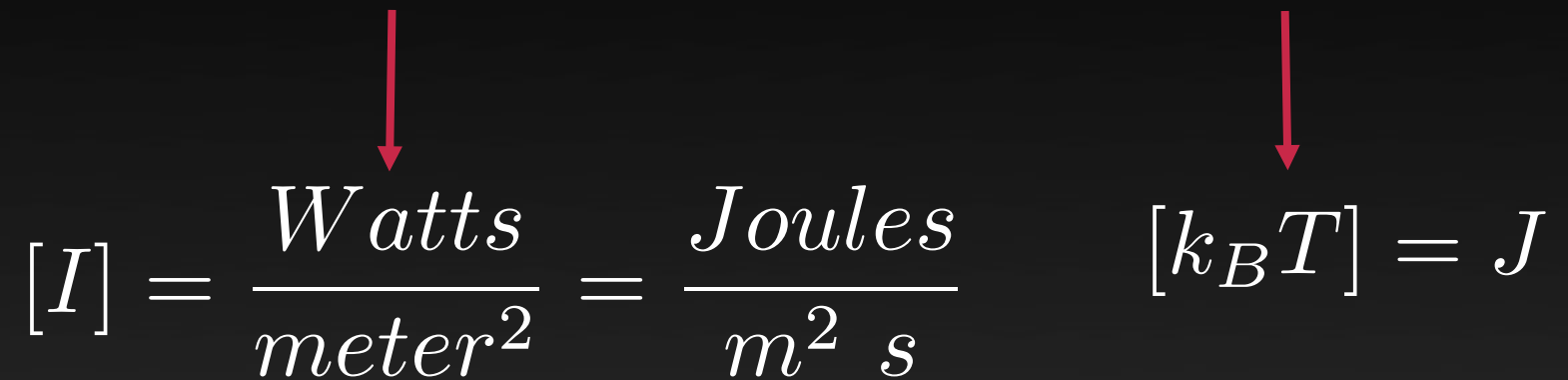
Intensity = function(Temperature, frequency)



$$[I] = \frac{Watts}{meter^2} = \frac{Joules}{m^2 s}$$

Crisis in 19th Century Classical Physics

Intensity = function(Temperature, frequency)




The diagram illustrates the relationship between the functional form of the Rayleigh-Jeans law and the units of its variables. At the top, the equation $Intensity = function(Temperature, frequency)$ is shown in italics. Two red arrows point downwards from the words "Intensity" and "Temperature" to their respective unit expressions below. The unit for Intensity is given as $[I] = \frac{Watts}{meter^2} = \frac{Joules}{m^2 s}$. The unit for Temperature is given as $[k_B T] = J$.

$$[I] = \frac{Watts}{meter^2} = \frac{Joules}{m^2 s} \quad [k_B T] = J$$


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$$c = 3 \times 10^8 \text{ m/s} \quad \text{speed of light}$$

$$k_B = 1.38 \times 10^{-23} \text{ J/K} \quad \text{Boltzmann's constant}$$

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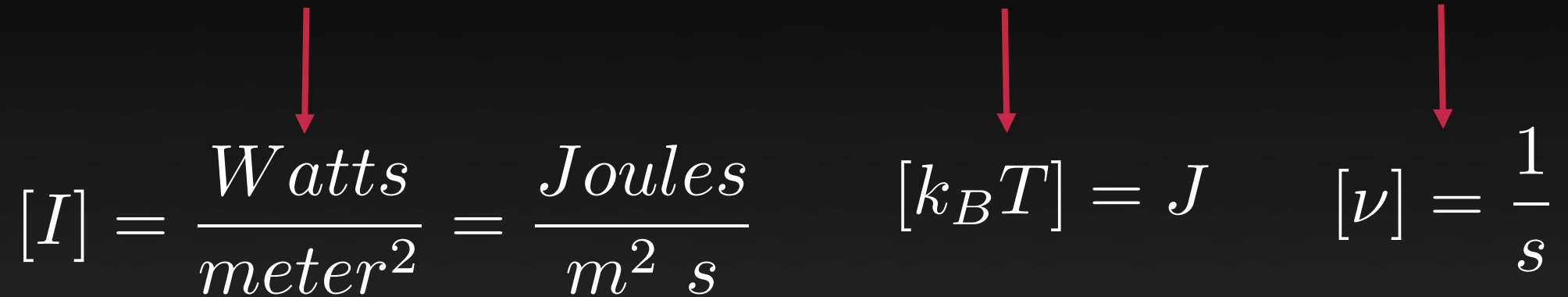


Diagram showing the units derived from the function statement above:

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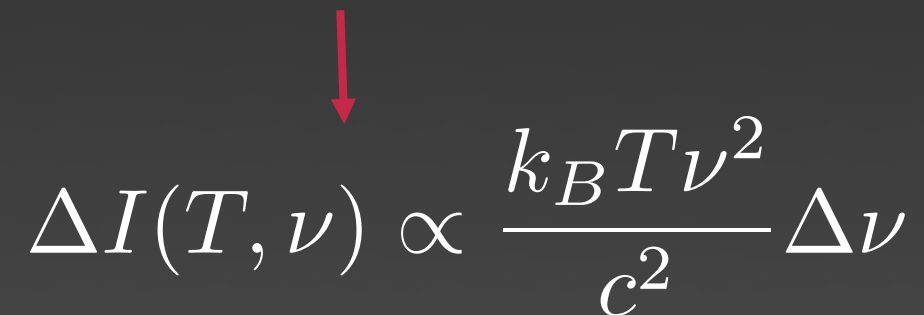


Diagram showing the units derived from the constants above:

$$\Delta I(T, \nu) \propto \frac{k_B T \nu^2}{c^2} \Delta \nu$$

Crisis in 19th Century Classical Physics

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UV Catastrophe!

The Solution: Quanta

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New constant of nature makes it possible to write the correct intensity.

$$\begin{aligned}\Delta I(T, \nu) &= \frac{2\pi h\nu^3}{c^2} \frac{1}{e^{h\nu/k_B T} - 1} \Delta\nu \\ &\rightarrow \frac{2\pi k_B T \nu^2}{c^2} \Delta\nu \text{ for } k_B T \gg h\nu \\ &\rightarrow 0 \text{ for } \nu \rightarrow \infty\end{aligned}$$

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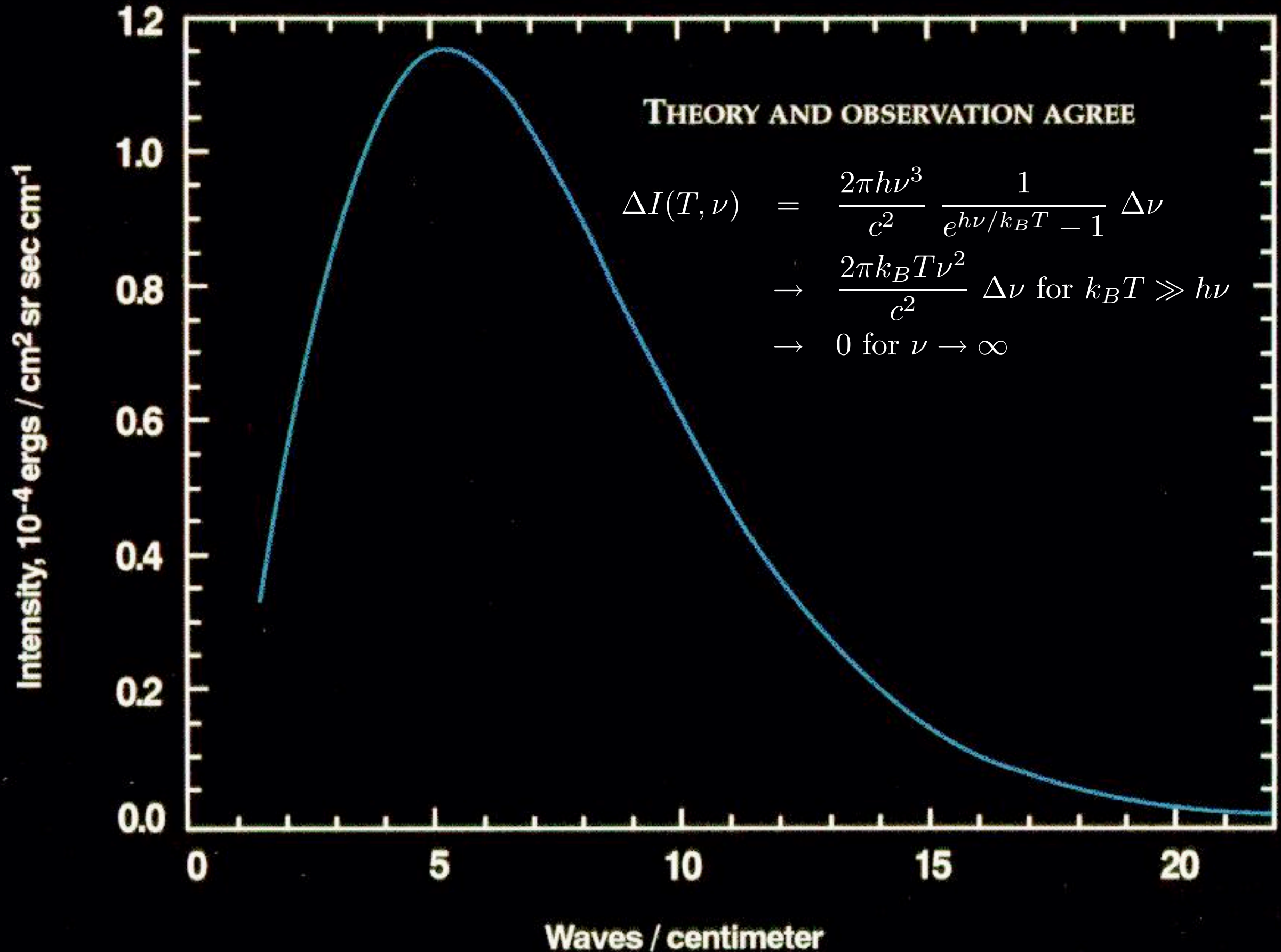
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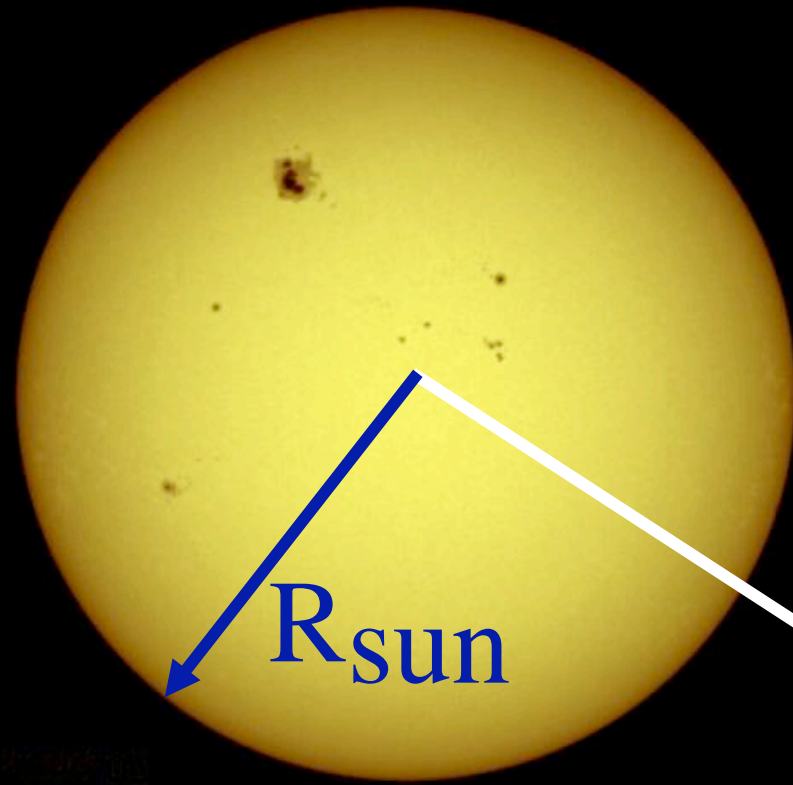
Now we can do that sum over frequency!

$$\begin{aligned}I &= \sigma T^4 \\ \sigma &\equiv \frac{2\pi^5 k_B^4}{15h^3 c^2} = 5.67 \times 10^{-8} \frac{W}{m^2 K^4}\end{aligned}$$

COSMIC MICROWAVE BACKGROUND SPECTRUM FROM COBE

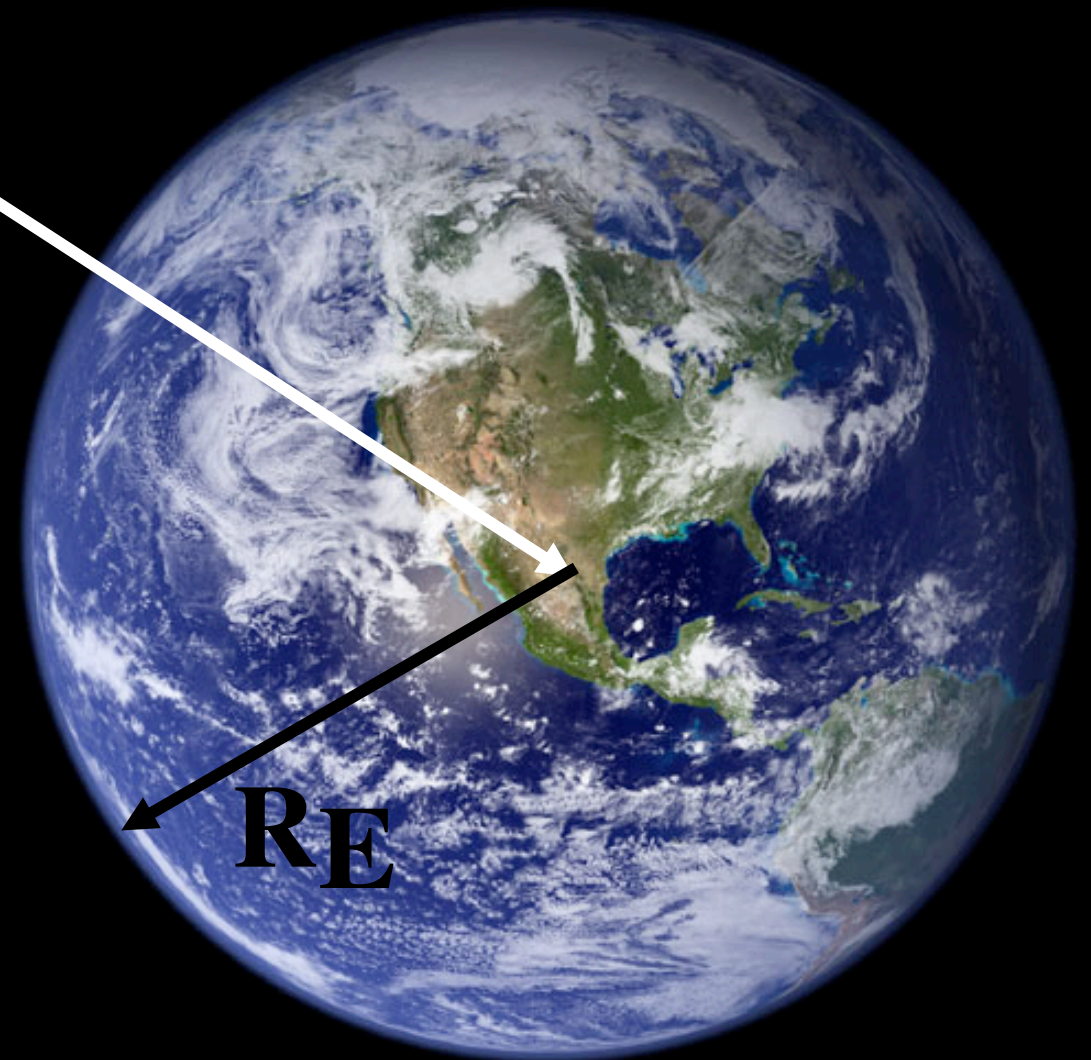


Temperature of the Earth

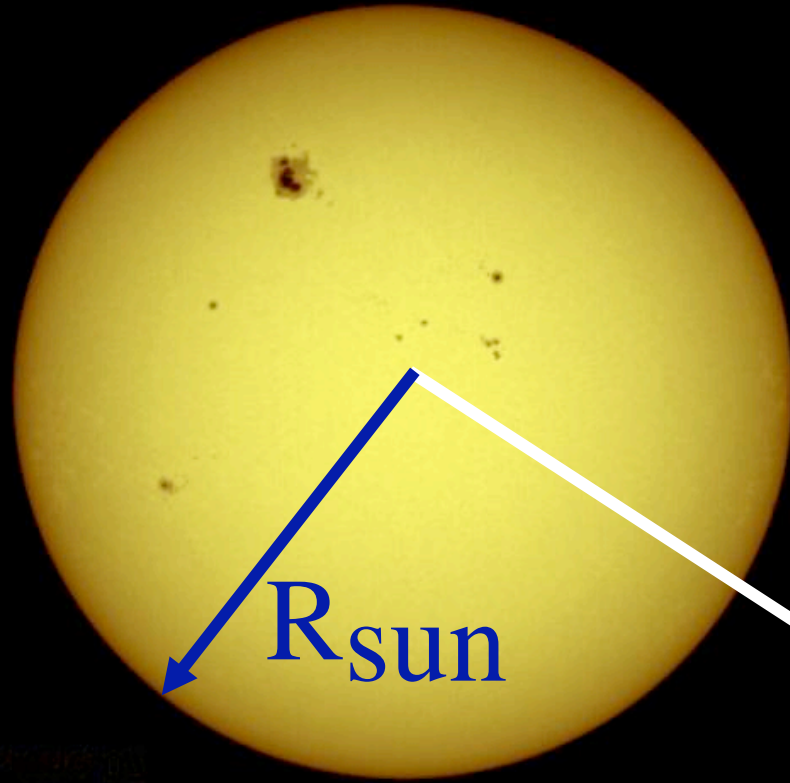


The earth is (almost) in a thermal steady state: it emits as much radiation as it receives from the sun.

r_E



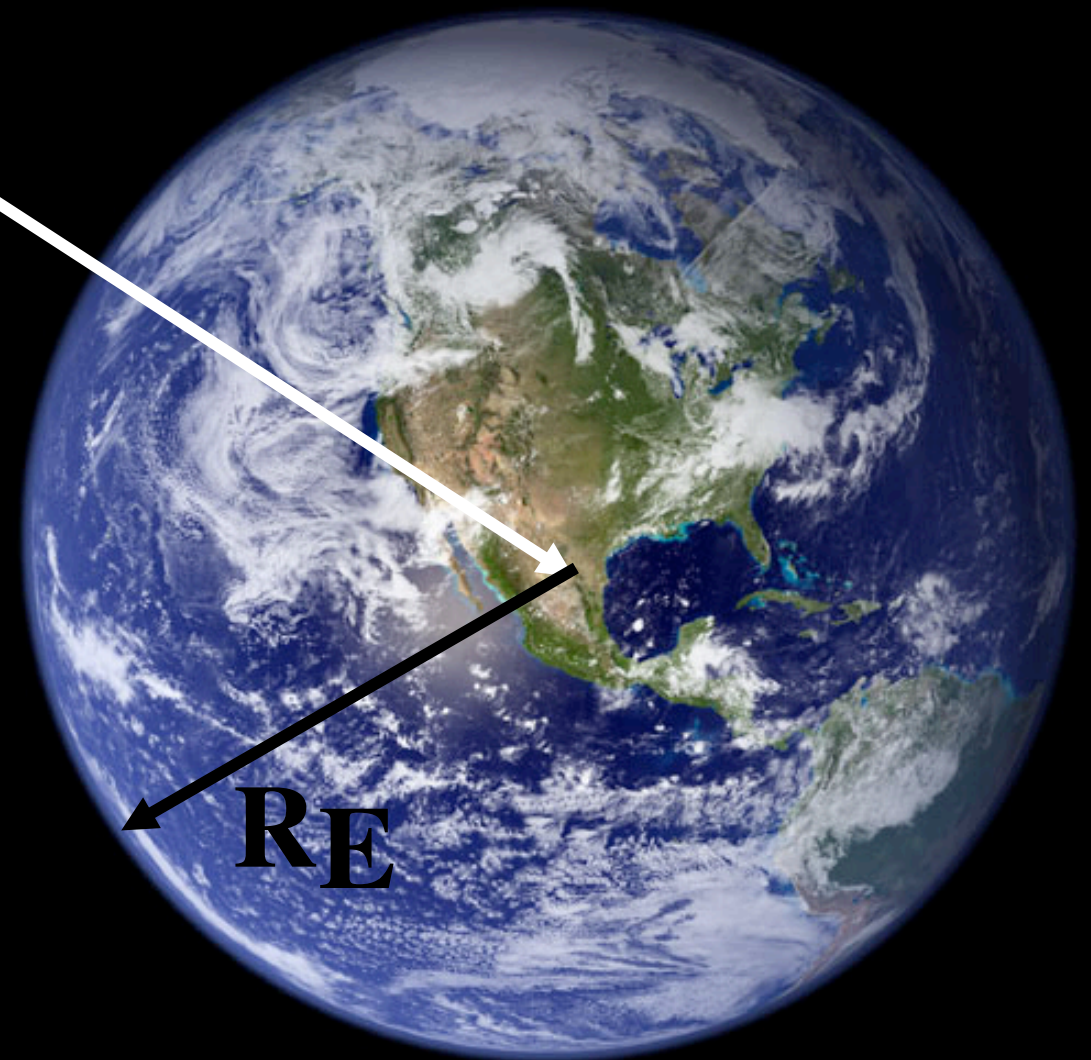
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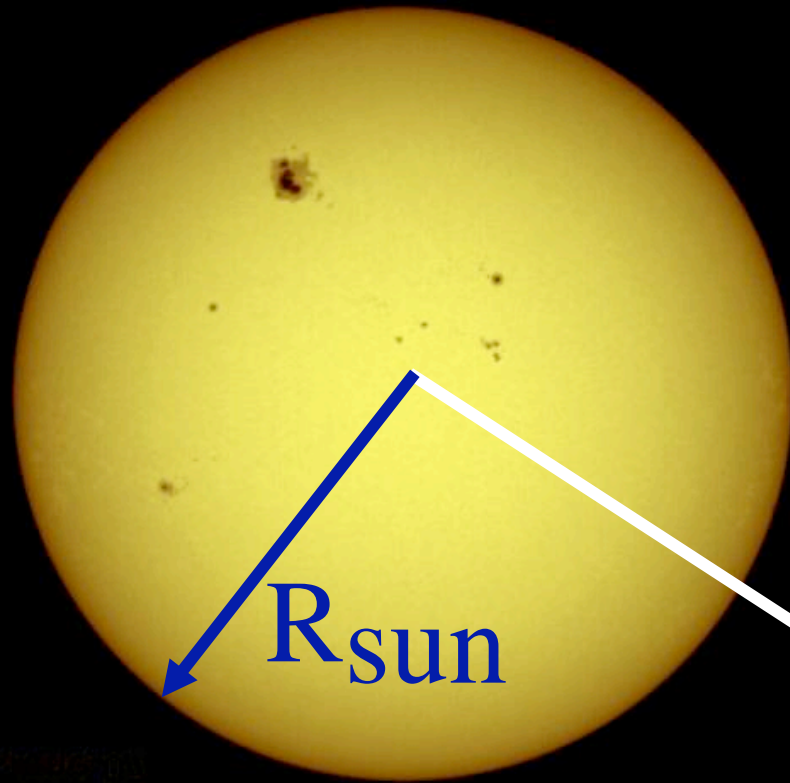
The earth is (almost) in a thermal steady state: it emits as much radiation as it receives from the sun.

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Albedo = $a = 30\%$ visible light reflected directly back to space (“earthshine” on the new moon).



Temperature of the Earth

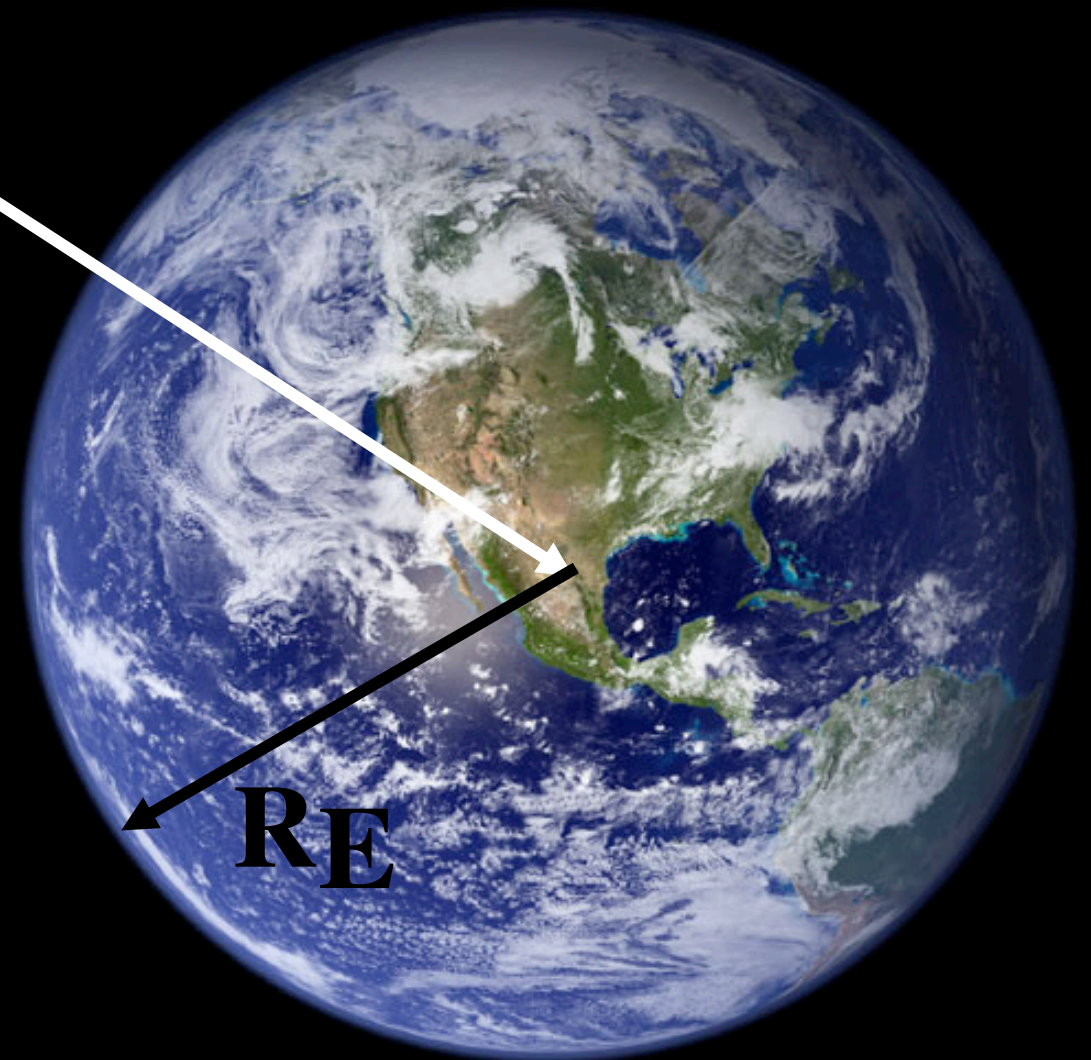


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$$fraction = \frac{\pi R_E^2}{4\pi r_E^2} \times (1 - a)$$



Energy Balance

$$\begin{aligned} \textit{Luminosity} &= \textit{Area} \times \textit{Intensity} \\ &= 4\pi R_{sun}^2 \times \sigma T_{sun}^4 \end{aligned}$$

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$$\frac{\pi R_E^2}{4\pi r_E^2} (1 - a) 4\pi R_{sun}^2 \sigma T_{sun}^4 = 4\pi R_E^2 \sigma T_E^4$$

Energy Balance

$$Luminosity = Area \times Intensity$$

$$= 4\pi R_{sun}^2 \times \sigma T_{sun}^4 \quad \text{Space}$$

incoming
energy flux



outgoing
energy flux (IR)



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Space

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energy flux



outgoing
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$$\frac{\cancel{\pi} \cancel{R_E^2}}{\cancel{4\pi} \cancel{r_E^2}} (1 - a) \cancel{4\pi} \cancel{R_{sun}^2} \cancel{\sigma} T_{sun}^4 = \cancel{4\pi} \cancel{R_E^2} \cancel{\sigma} T_E^4$$

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$$r_E = 150 \times 10^9 m$$

$$R_{sun} = 6.96 \times 10^8 m$$

$$T_{sun} = 5,800 K$$

Energy Balance

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T_E

$=$

$$(1 - a)^{1/4} \sqrt{\frac{R_{sun}}{2r_E}} T_{sun}$$

\approx

$$251 K = -22 C$$

Energy Balance

$$Luminosity = Area \times Intensity$$

$$= 4\pi R_{sun}^2 \times \sigma T_{sun}^4 \quad \text{Space}$$

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T_E

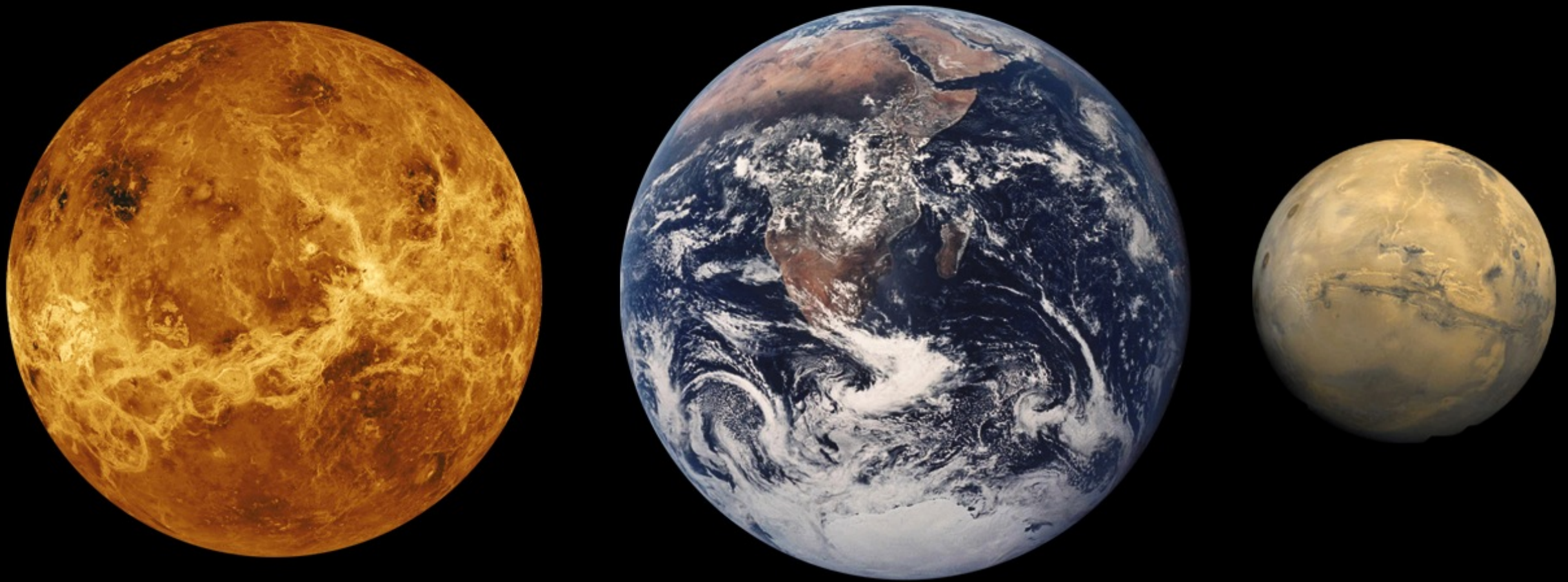


$$T_E = (1 - a)^{1/4} \sqrt{\frac{R_{sun}}{2r_E}} T_{sun}$$

$$\approx 251 K = -22 C$$

FREEZING

Terrestrial Planets



Planet	Earth
calculated temperature	-18 °C
actual temperature	15 °C
greenhouse warming	33 °C

Planet	Earth	Mars
calculated temperature	-18 °C	-56 °C
actual temperature	15 °C	-53 °C
greenhouse warming	33 °C	3 °C

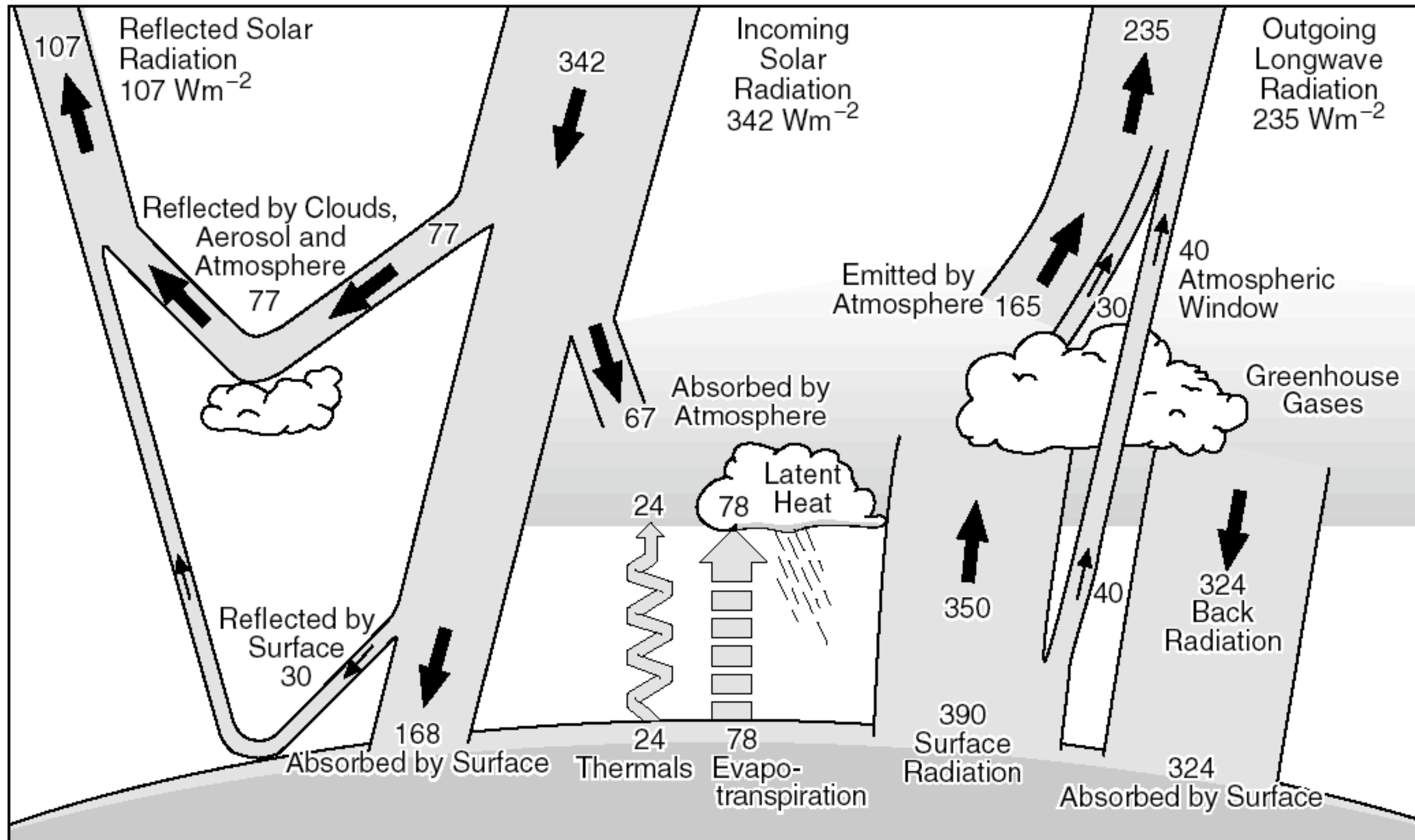
Planet	Earth	Mars	Venus
calculated temperature	-18 °C	-56 °C	-39 °C
actual temperature	15 °C	-53 °C	427 °C
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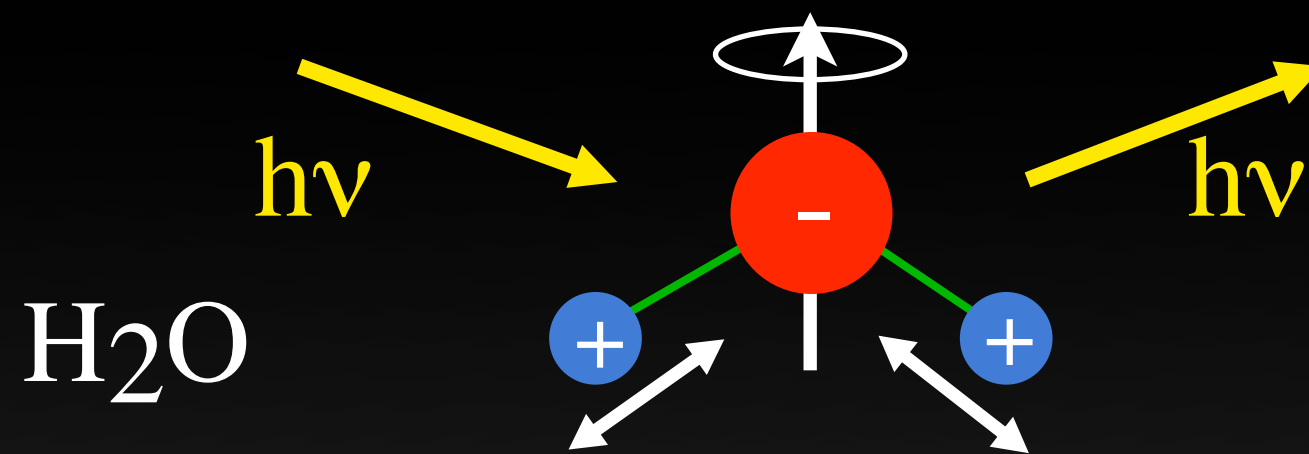
Water Vapour: 65% Carbon Dioxide: 21%



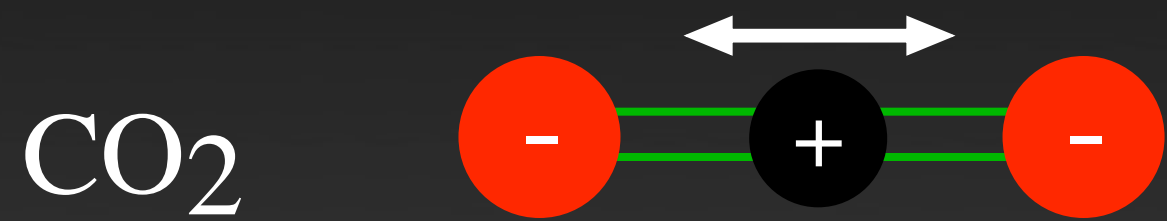
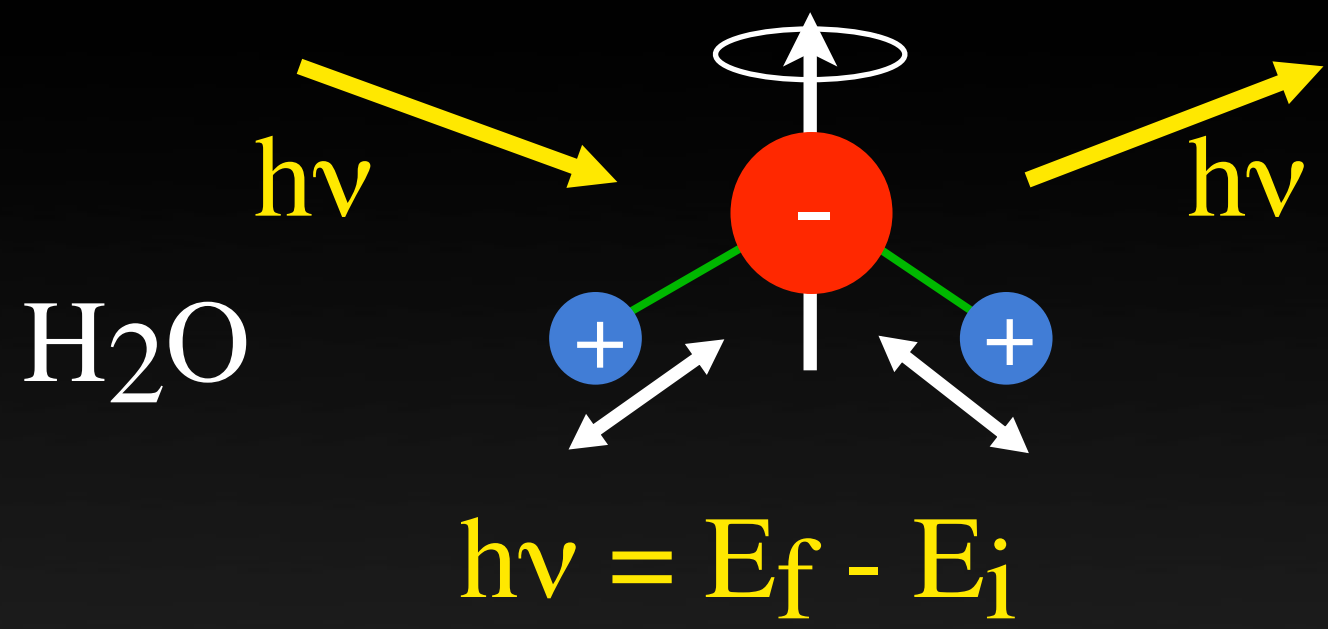
Why We Aren't Freezing

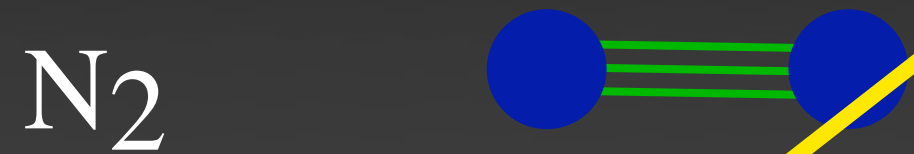
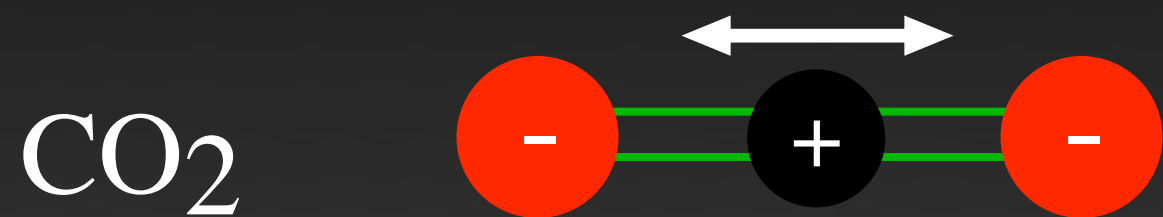
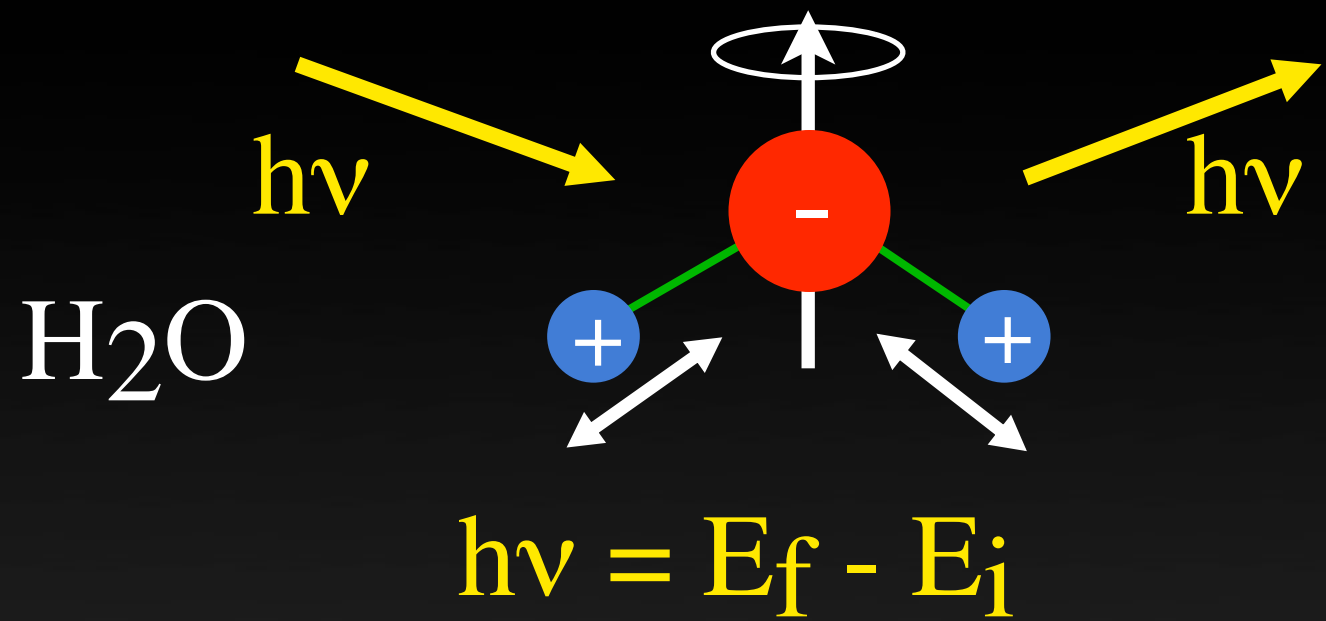


from *Climate Change 1995: The Science of Climate Change*



$$h\nu = E_f - E_i$$

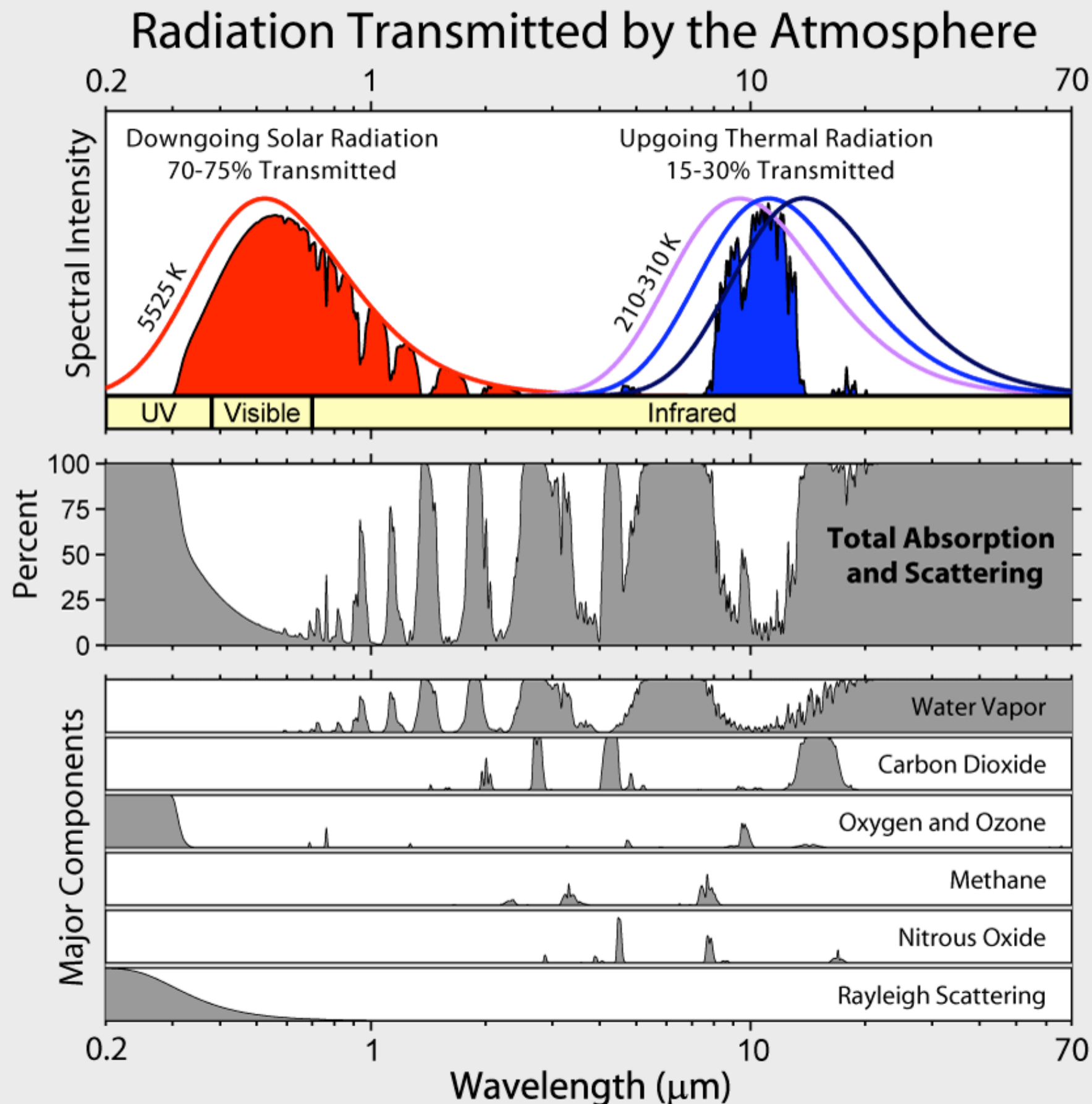




Transparent

Principal greenhouse
gas: water vapor

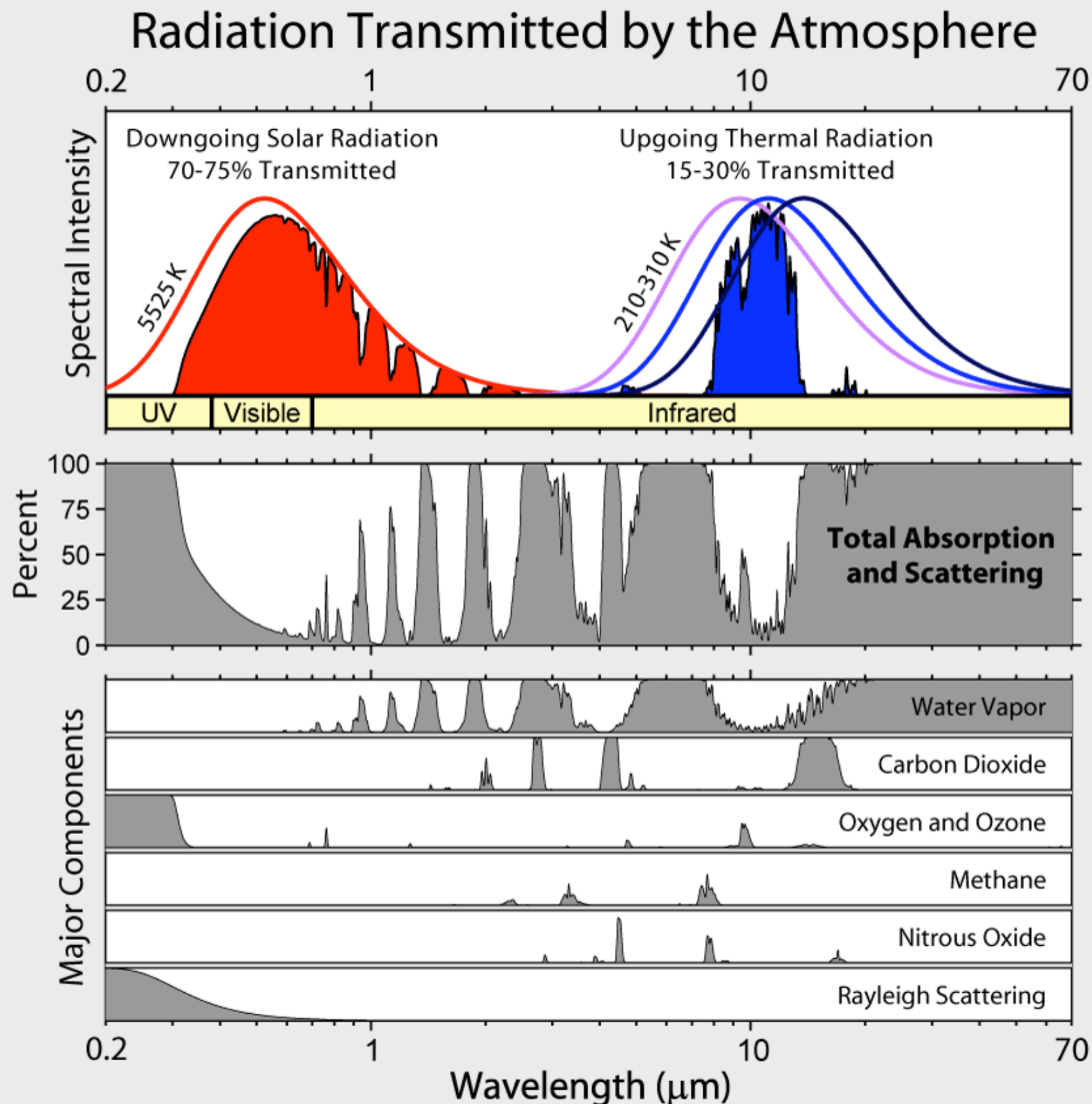
Secondary: carbon
dioxide, methane,
CFC's, ...



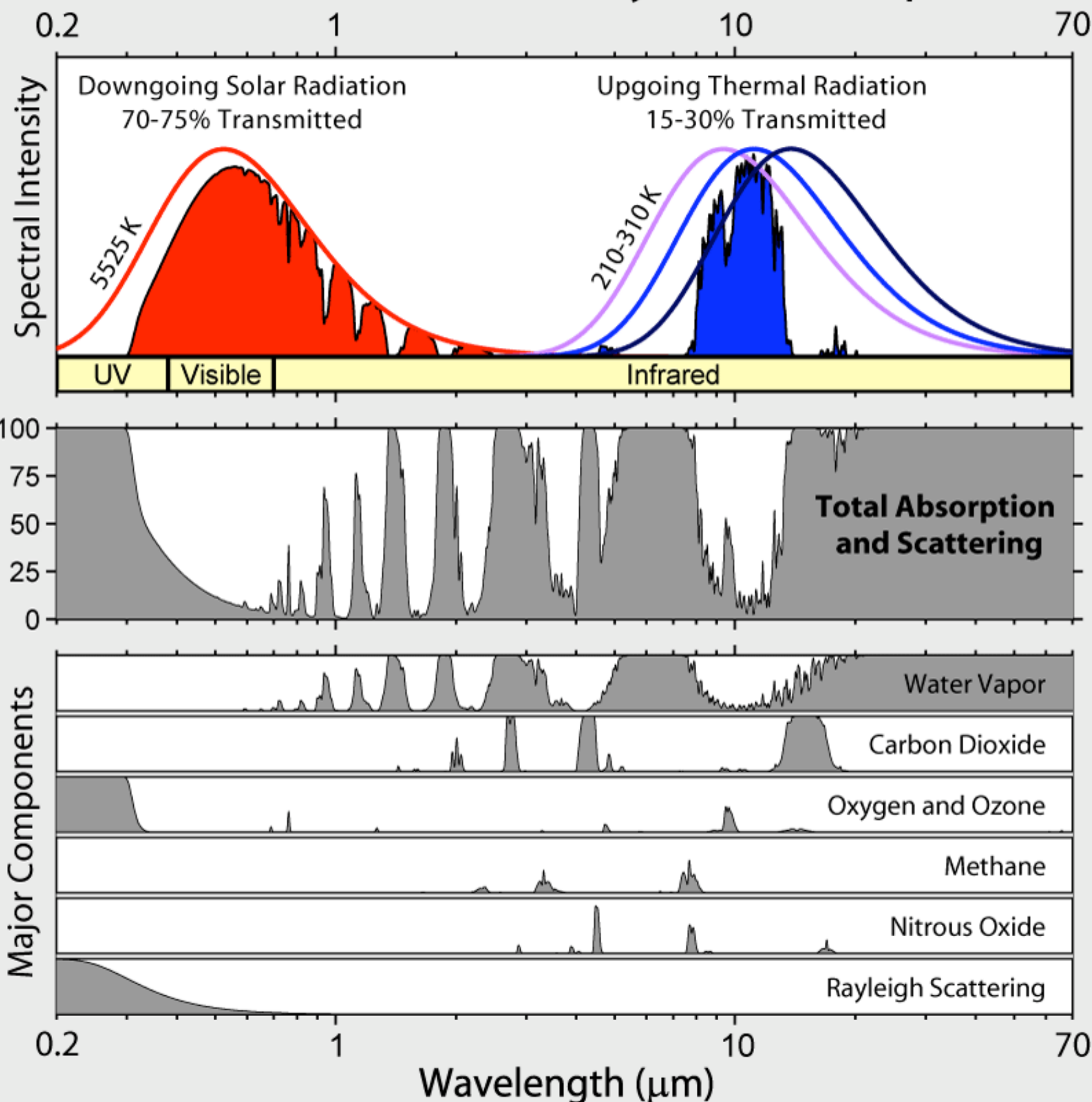
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Absorption lines are
pressure-broadened



Radiation Transmitted by the Atmosphere



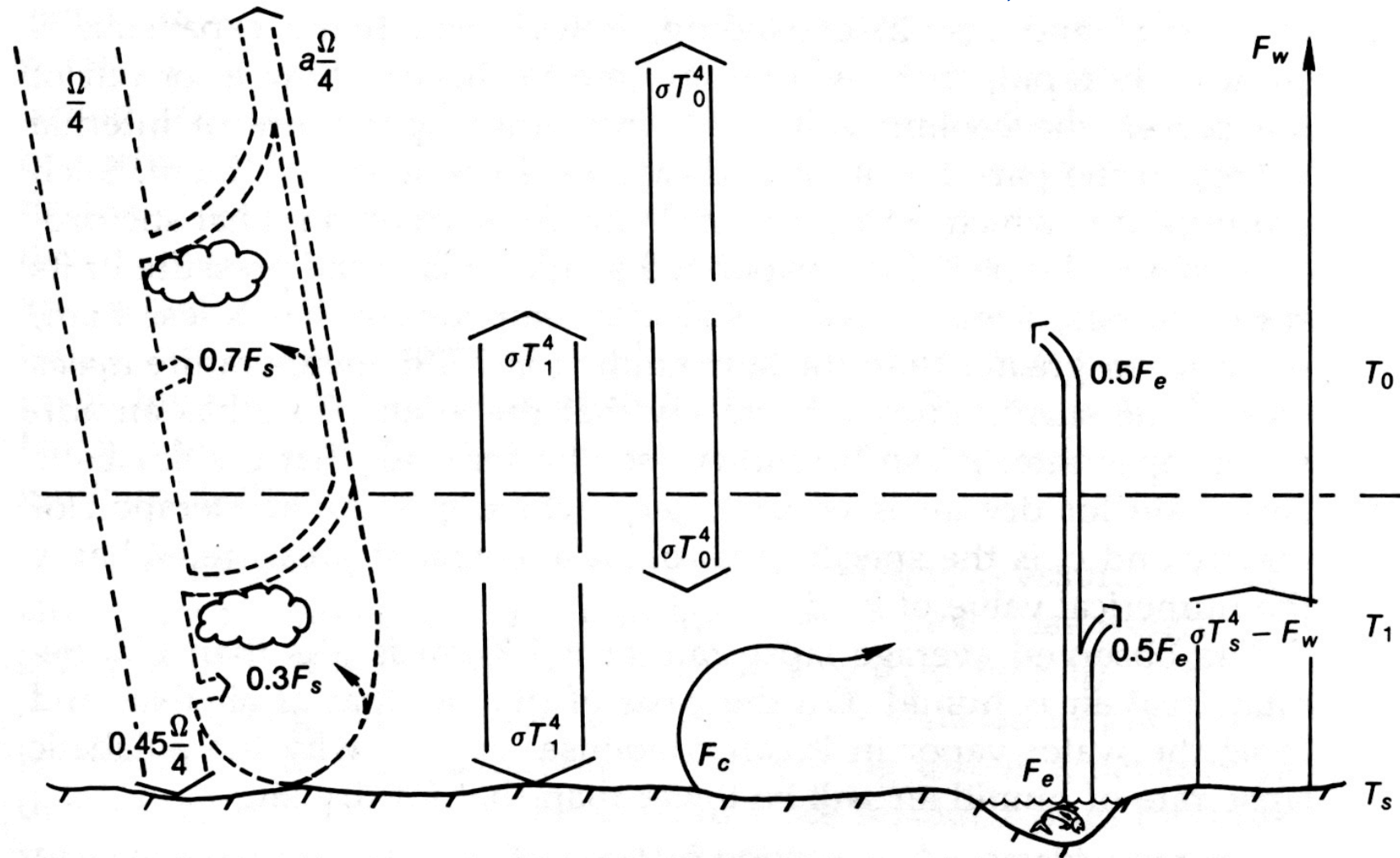
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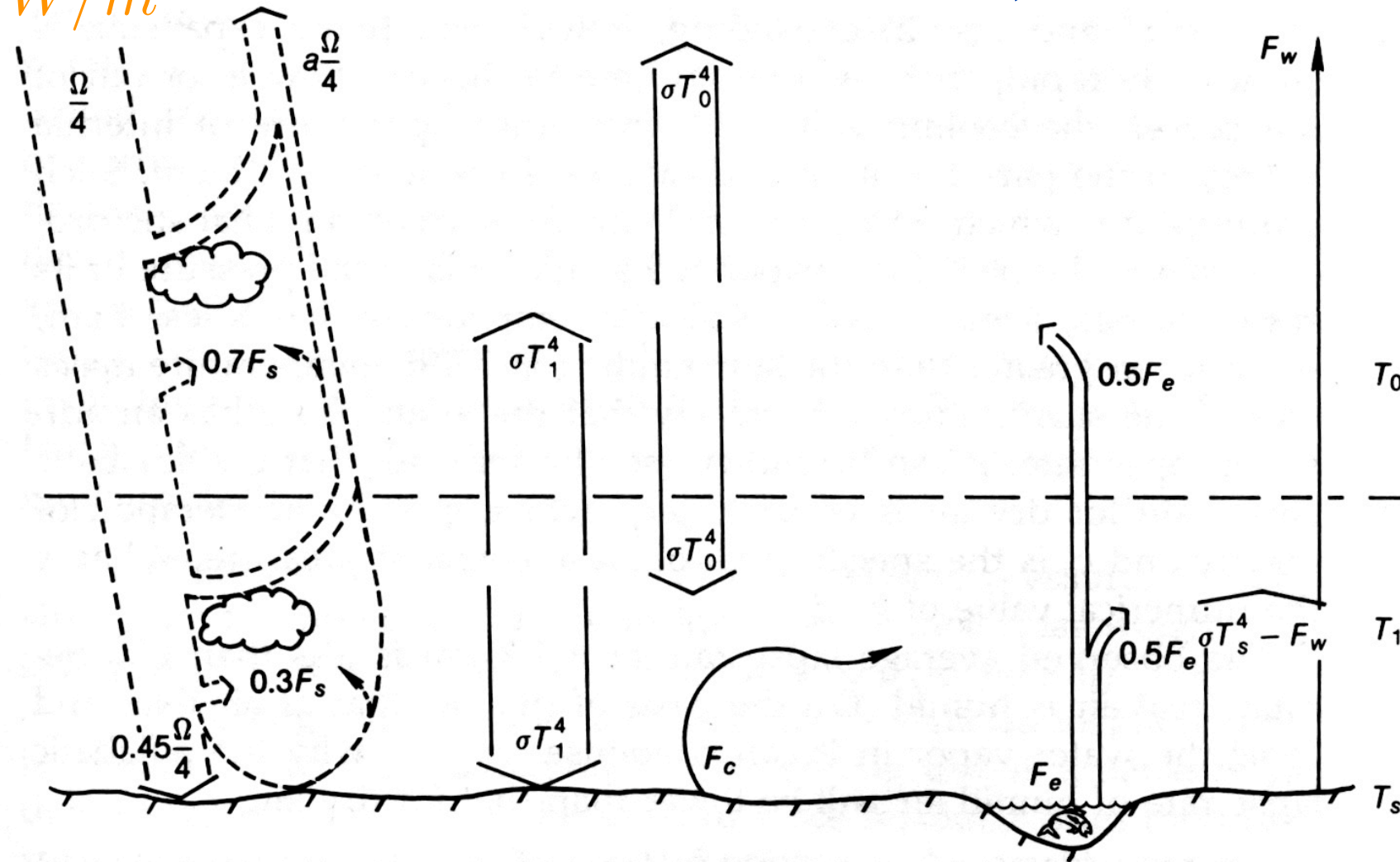
IR photons are on average absorbed and emitted about 2x on way out to space

John Harte, *Consider a Spherical Cow*



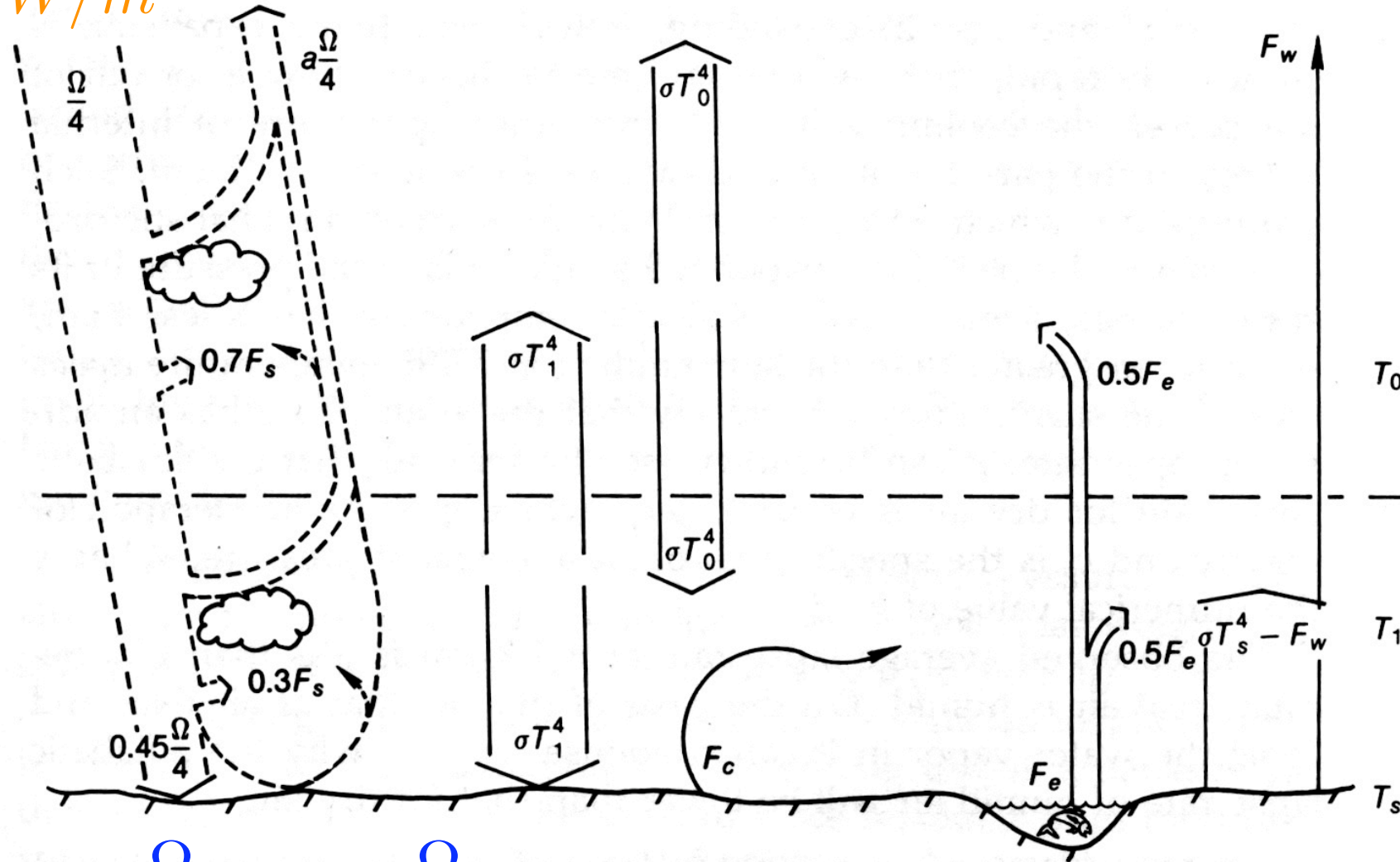
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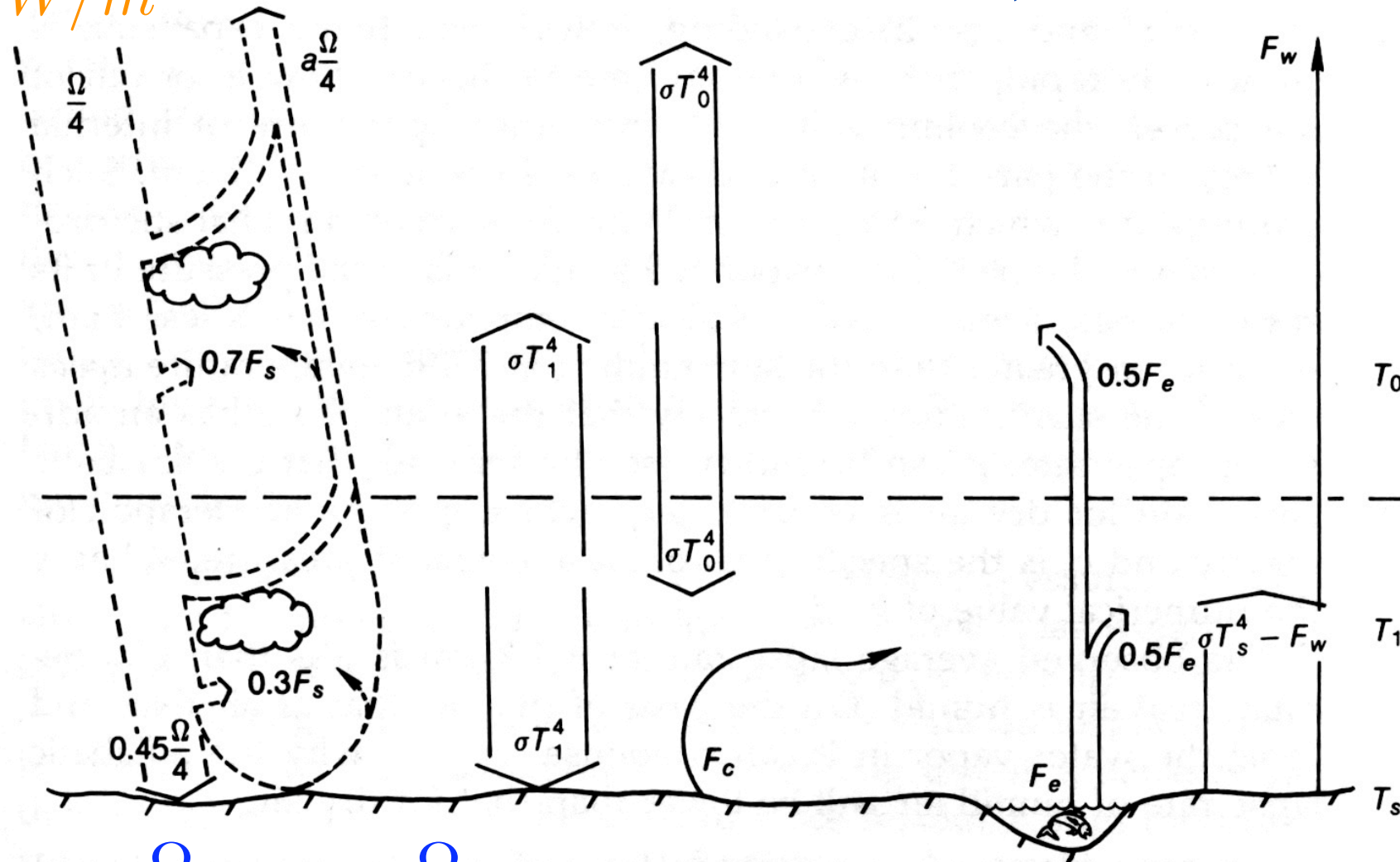
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$$\begin{aligned}\frac{\Omega}{4} &= a\frac{\Omega}{4} + \sigma T_0^4 + F_w \\ 2\sigma T_0^4 &= \sigma T_1^4 + 0.5F_e + 0.7F_s \\ 2\sigma T_1^4 &= \sigma T_0^4 + \sigma T_s^4 - F_w + F_c + 0.5F_e + 0.3F_s\end{aligned}$$

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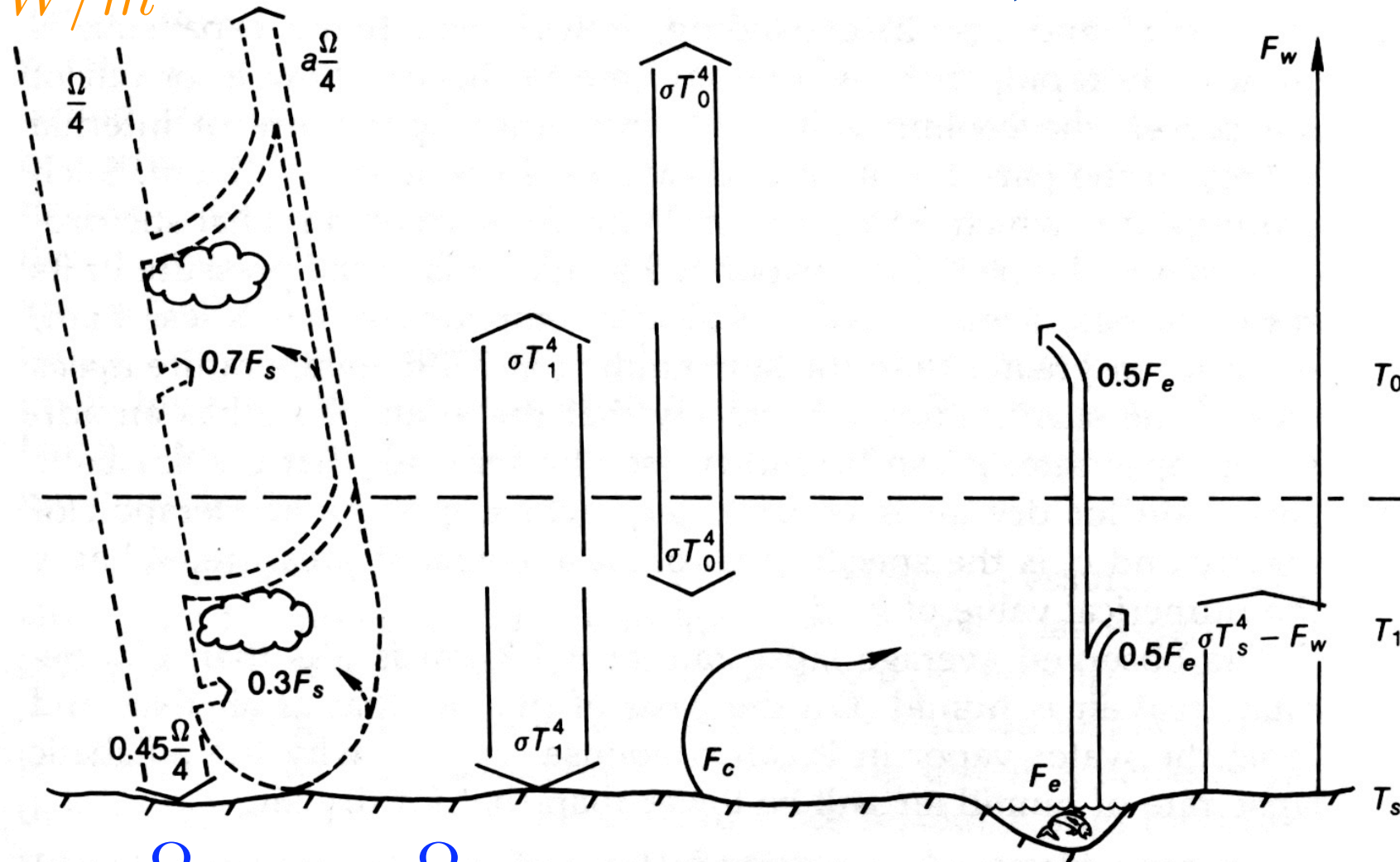
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- $F_s \approx 86 \text{ W/m}^2$ Solar flux absorbed by atmosphere
- $F_e \approx 80 \text{ W/m}^2$ Latent heat from evaporating water
- $F_w \approx 20 \text{ W/m}^2$ IR flux directly to space
- $F_c \approx 17 \text{ W/m}^2$ Convective heat transfer

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$$T_0 = 250K$$

$$T_1 = 278K$$

$$T_s = 289K = 16C$$

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Excellent agreement
for such a simple model

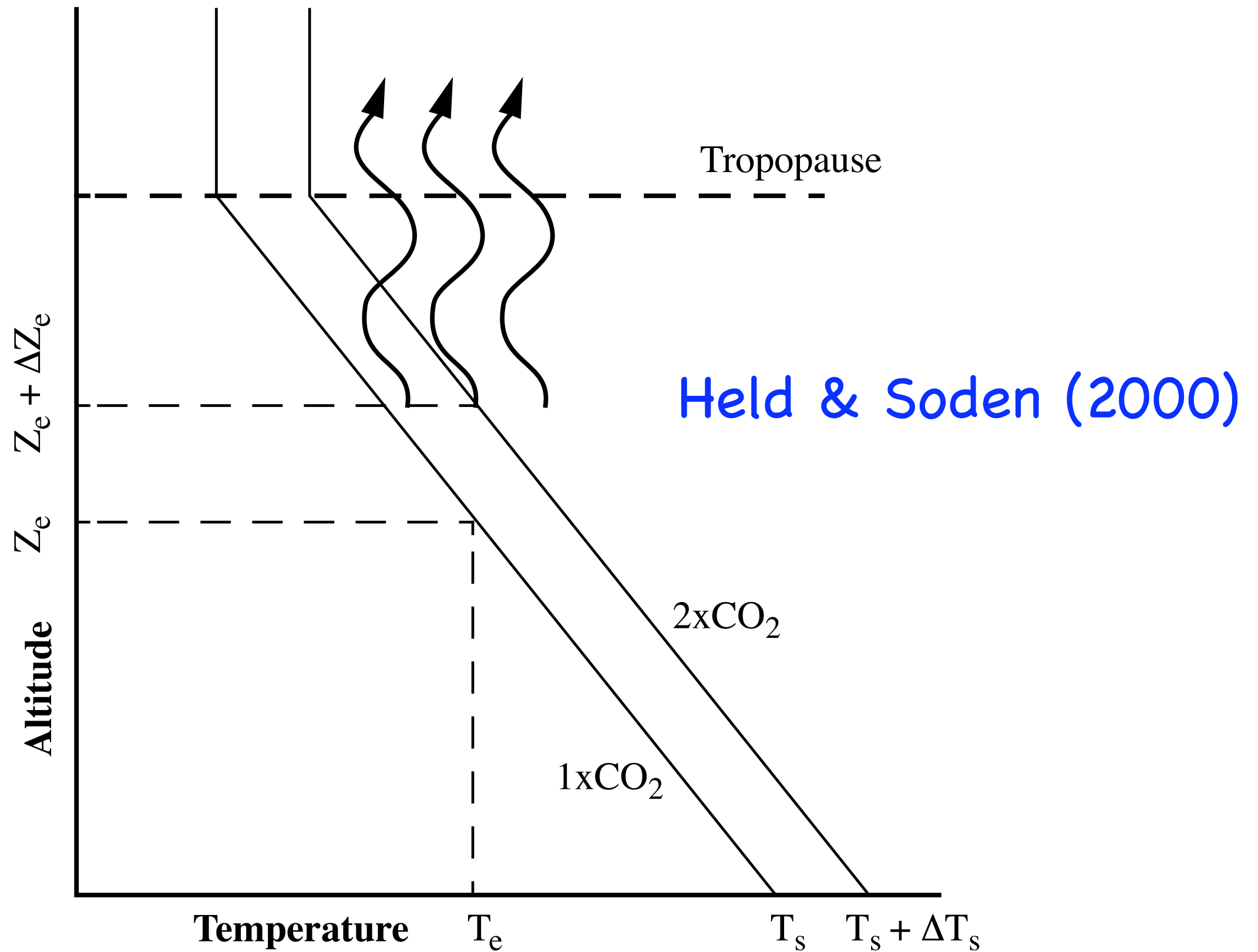
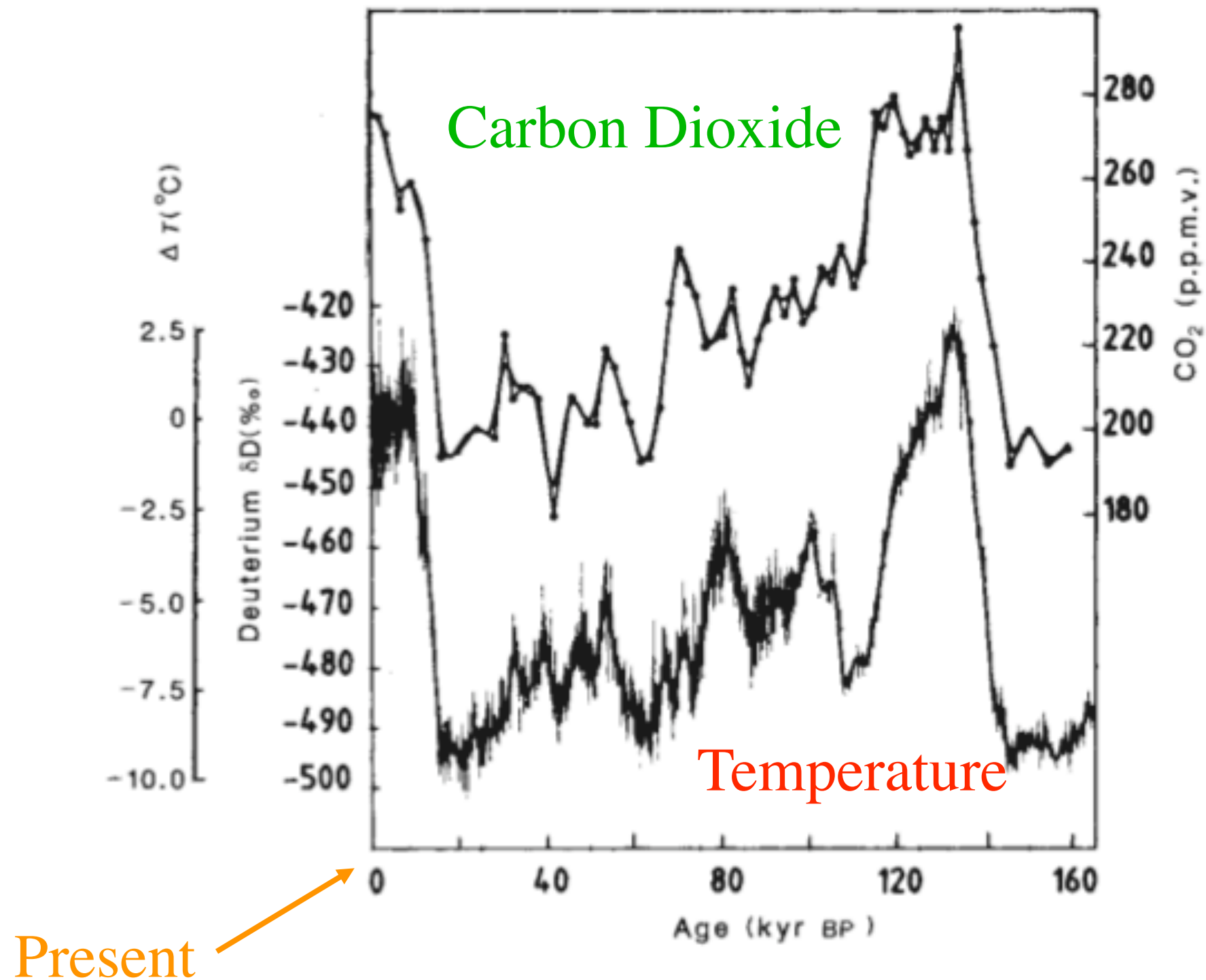


Figure 1 Schematic illustration of the change in emission level (Z_e) associated with an increase in surface temperature (T_s) due to a doubling of CO₂ assuming a fixed atmospheric lapse rate. Note that the effective emission temperature (T_e) remains unchanged.

The Past 160,000 Years

J. M. Barnola *et al.*, Nature **329**, 408 (1987)



Quantum Zero-Point Motion

(Harold Urey, “The thermodynamic properties of isotopic substances,” 1946)

Quantum Zero-Point Motion

Classically: All motion ceases at absolute zero temperature.
Everything freezes into a solid.

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Quantum physics: There is still some motion even at $T = 0$.
This is why liquid helium never freezes!

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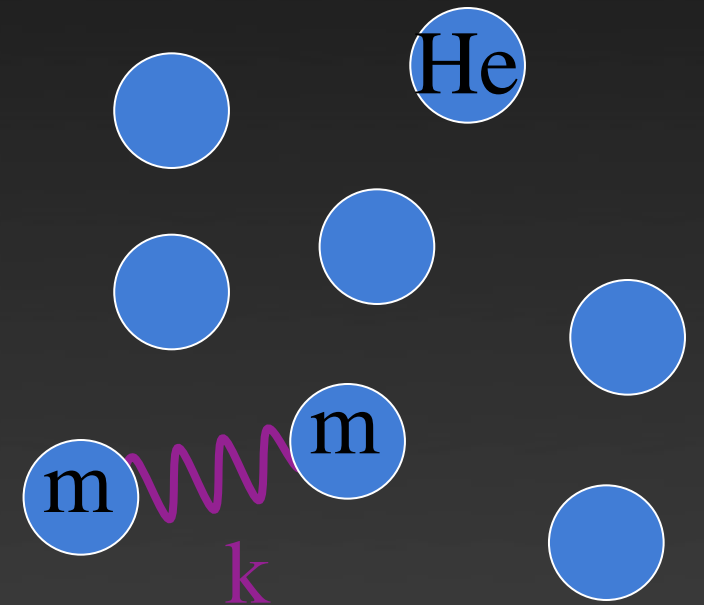
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Small mass --> large
quantum zero-point
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$$E_0 = \frac{1}{2} h\nu$$



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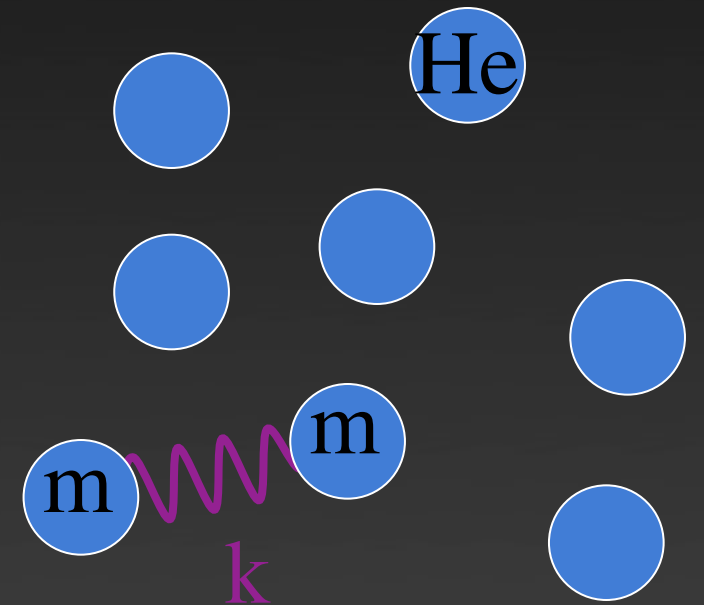
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^{18}O versus ^{16}O in H_2O : Classically both molecules have same energy.

Quantum zero-point energy means that ^{18}O water is slightly less likely to evaporate during cold spells.

(Harold Urey, "The thermodynamic properties of isotopic substances," 1946)

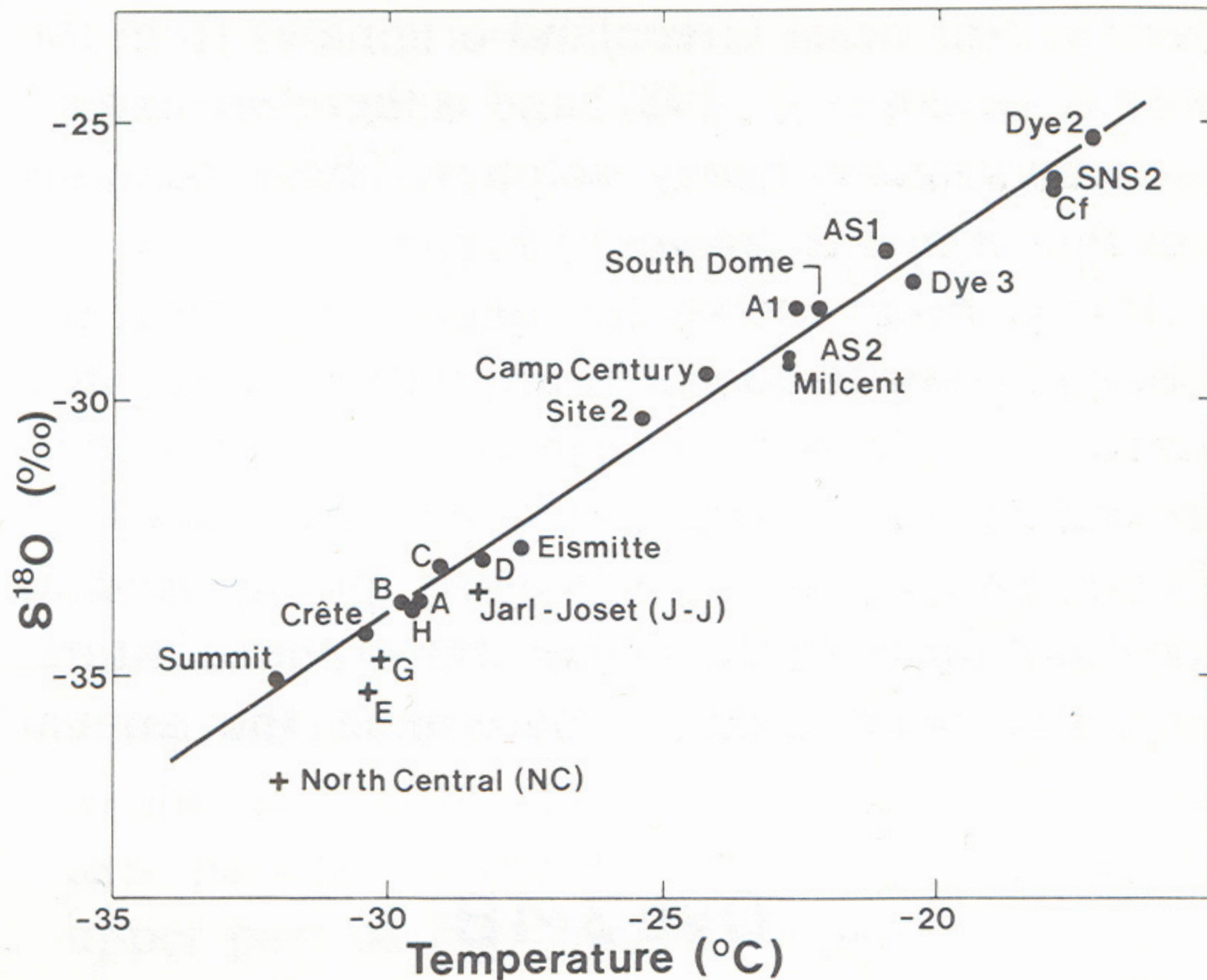
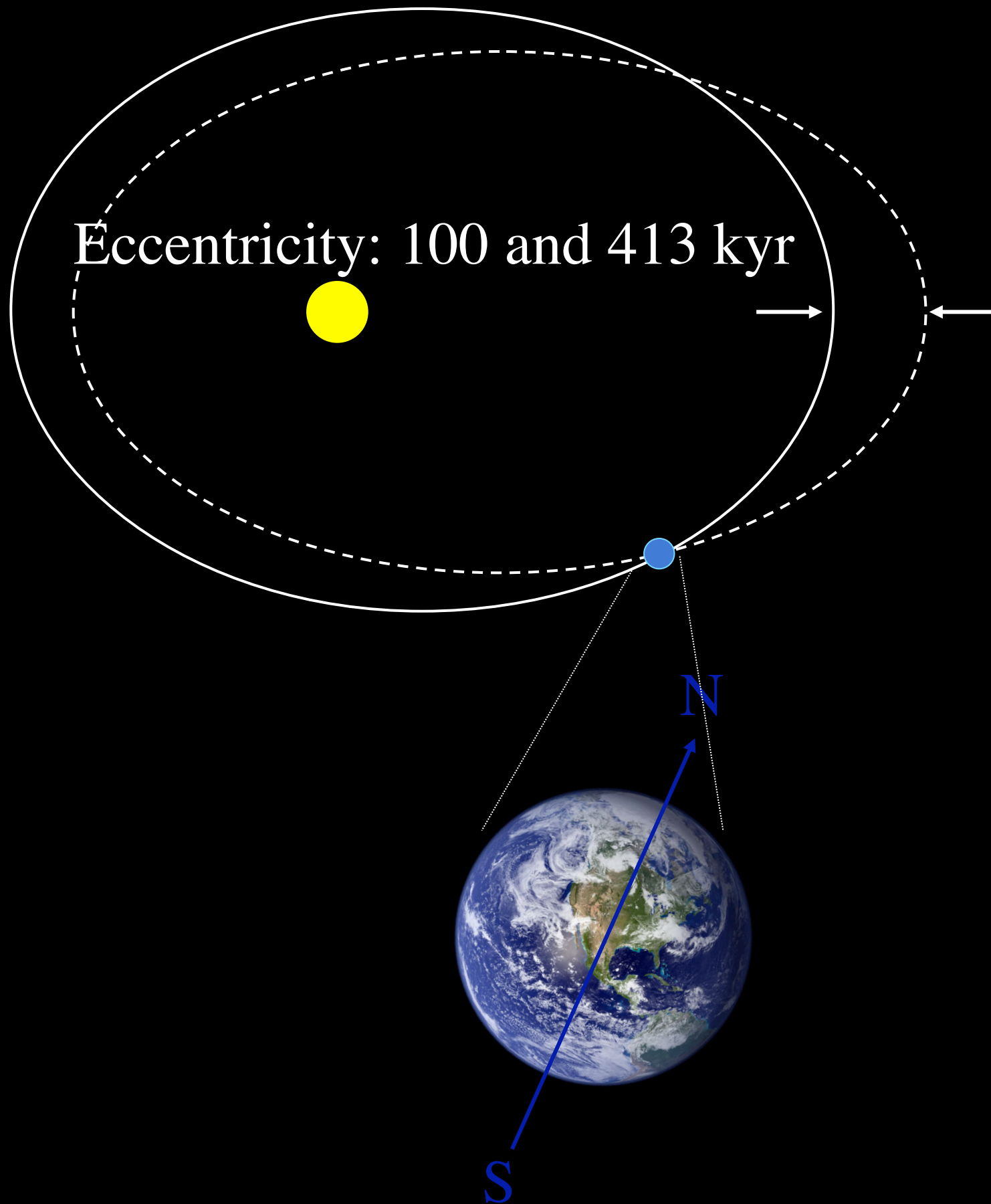


Fig. 3. Mean $\delta^{18}O$ of snow deposited on the Greenland ice sheet plotted against the annual mean surface temperature as represented by the temperature at 10 or 20 m depths.

S. J. Johnsen *et al.* Tellus **41B**, 452 (1989)



α Draconis
(2000 BC)



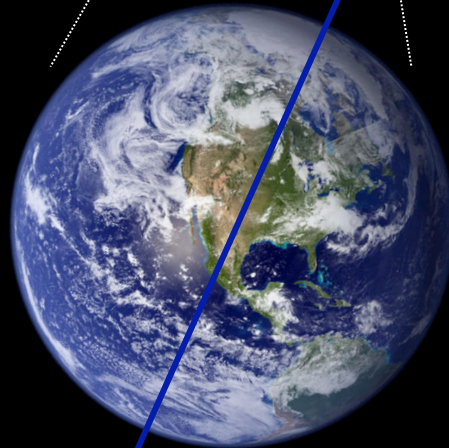
Polaris
(now)

Precession: 19 to 23 kyr

Eccentricity: 100 and 413 kyr



N



S



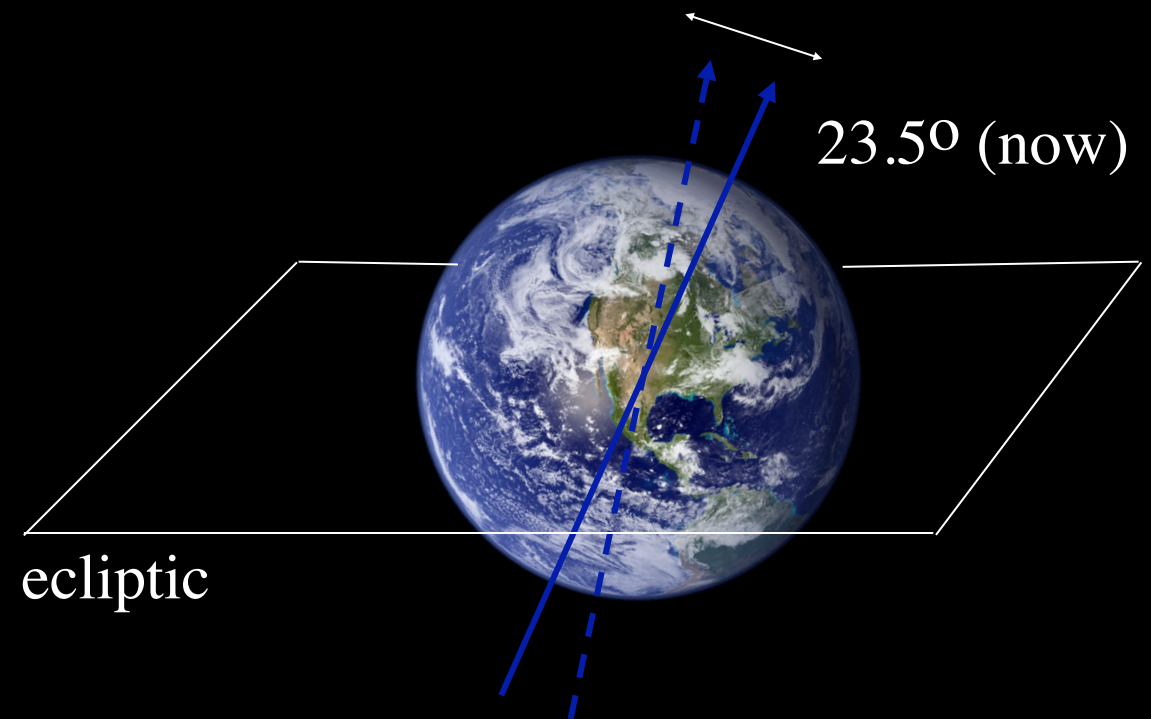
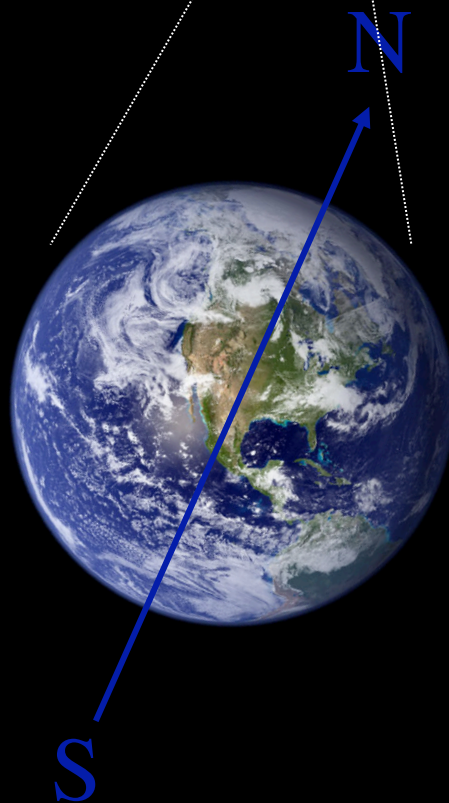
α Draconis
(2000 BC)



Polaris
(now)

Precession: 19 to 23 kyr

Eccentricity: 100 and 413 kyr



Change in tilt of axis
“obliquity”: 41 kyr

Spectral Analysis of Isotope Records

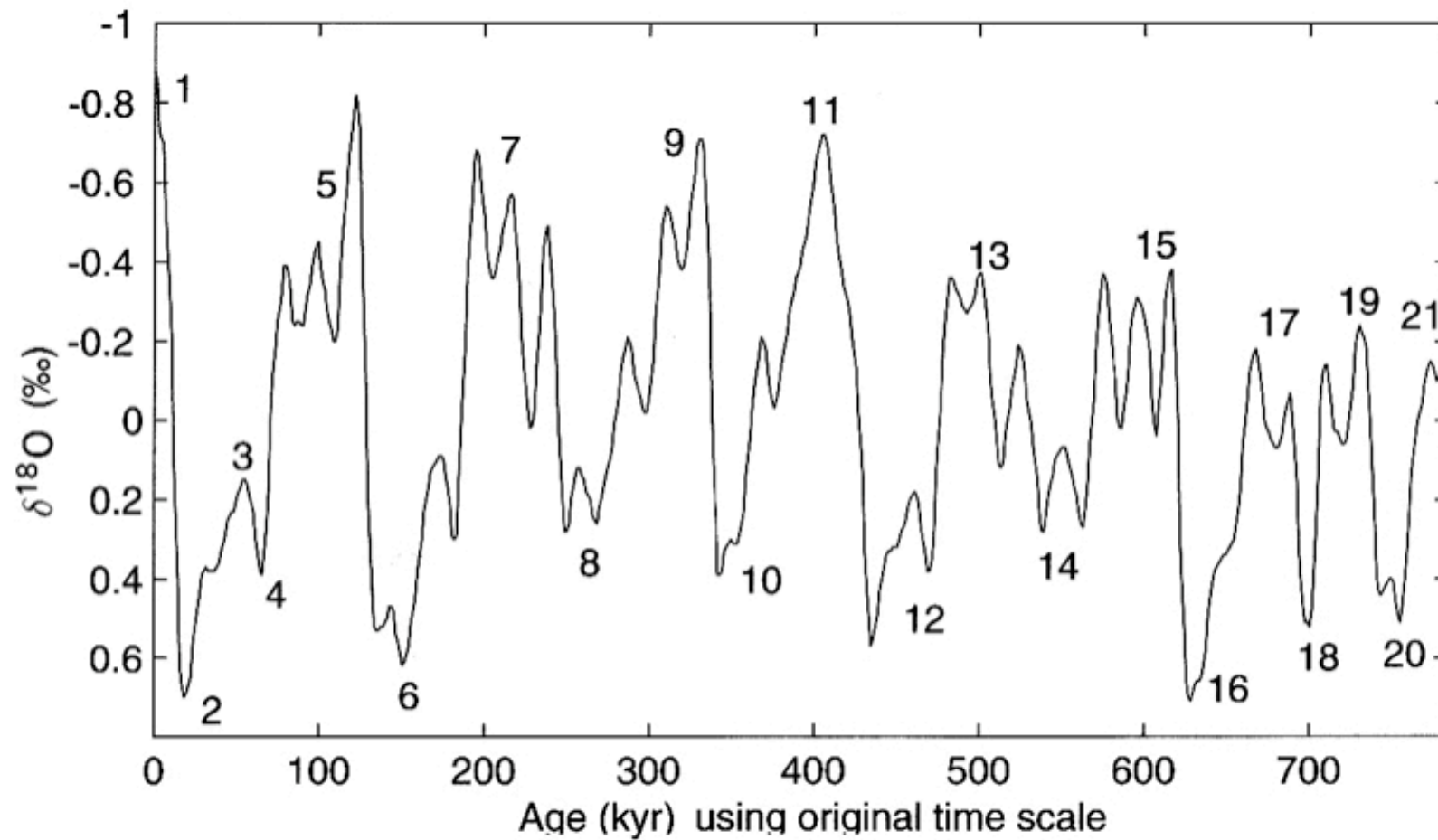


Fig. 4.4. SPECMAP $\delta^{18}\text{O}$ stack with marine isotope stage numbers.

Figures from *Ice Ages and Astronomical Causes: Data, Spectral Analysis, and Mechanisms* by R. Muller and G. MacDonald

Spectral Analysis of Isotope Records

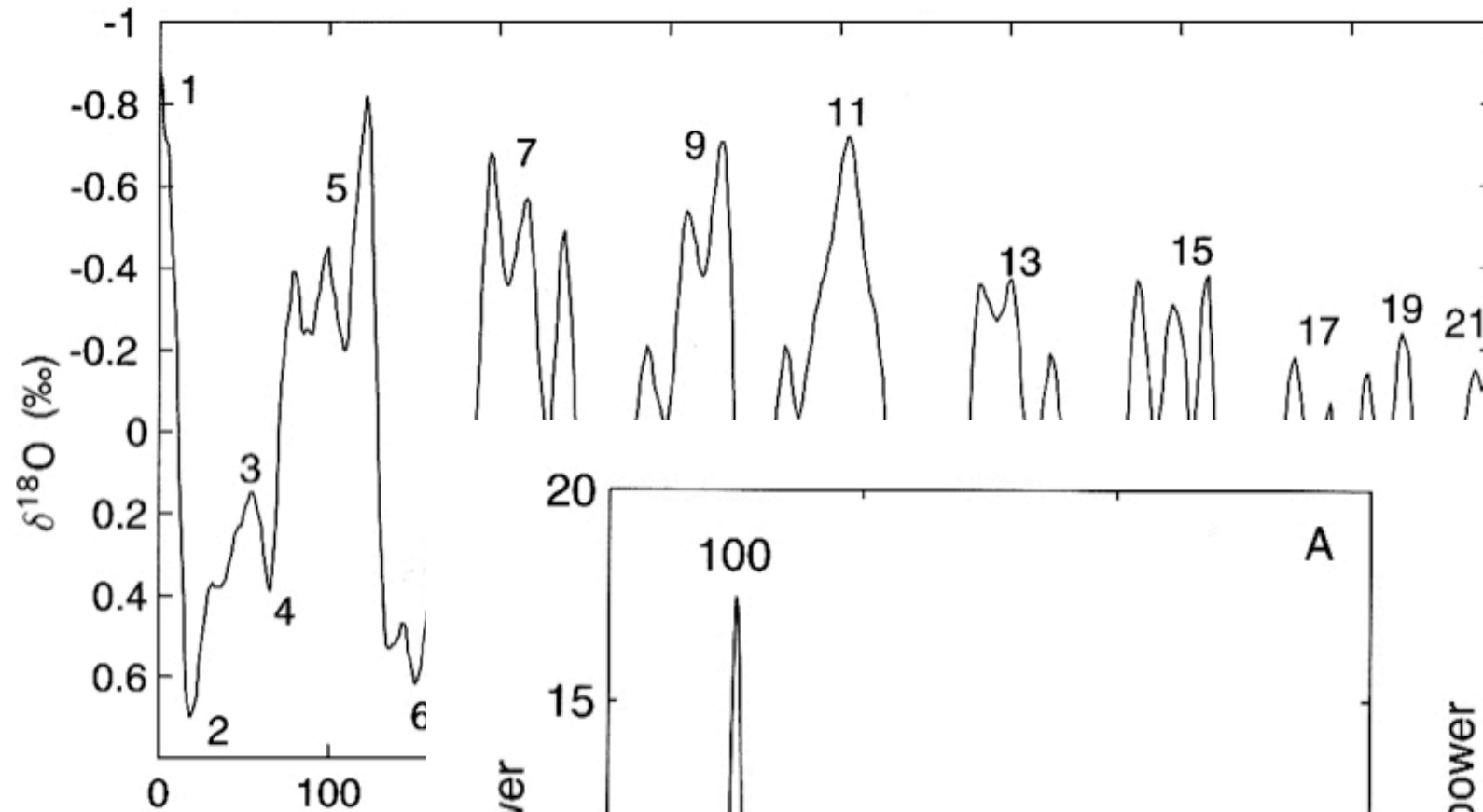


Fig. 4.4. SPECM

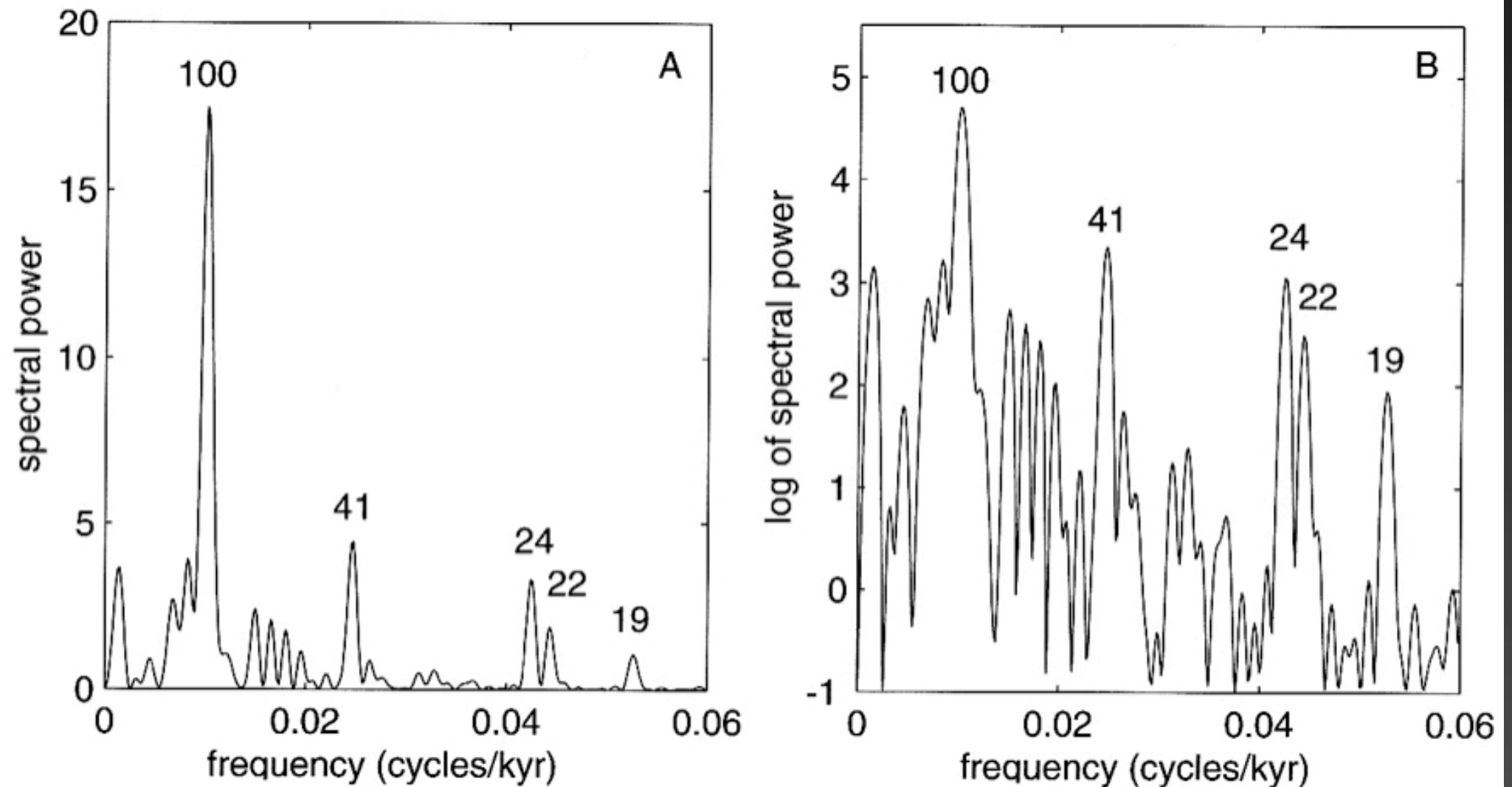


Fig. 4.5. Spectrum of original SPECMAP stack.

Figures from *Ice Ages and Astronomical Causes: Data, Spectral Analysis, and Mechanisms* by R. Muller and G. MacDonald

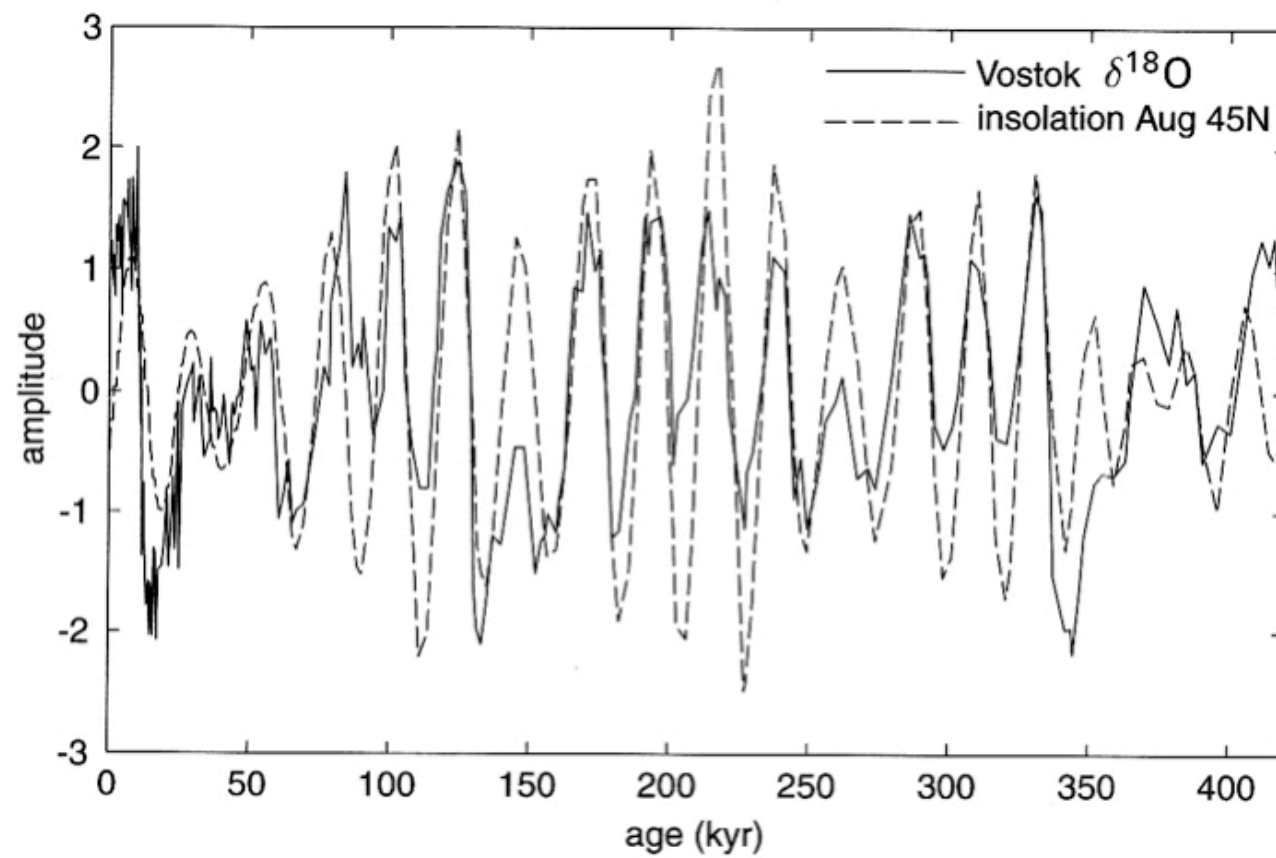


Fig. 4.40. Vostok oxygen and August 45N insolation. No phase lag used.

What amplifies orbital forcing to produce ice ages?

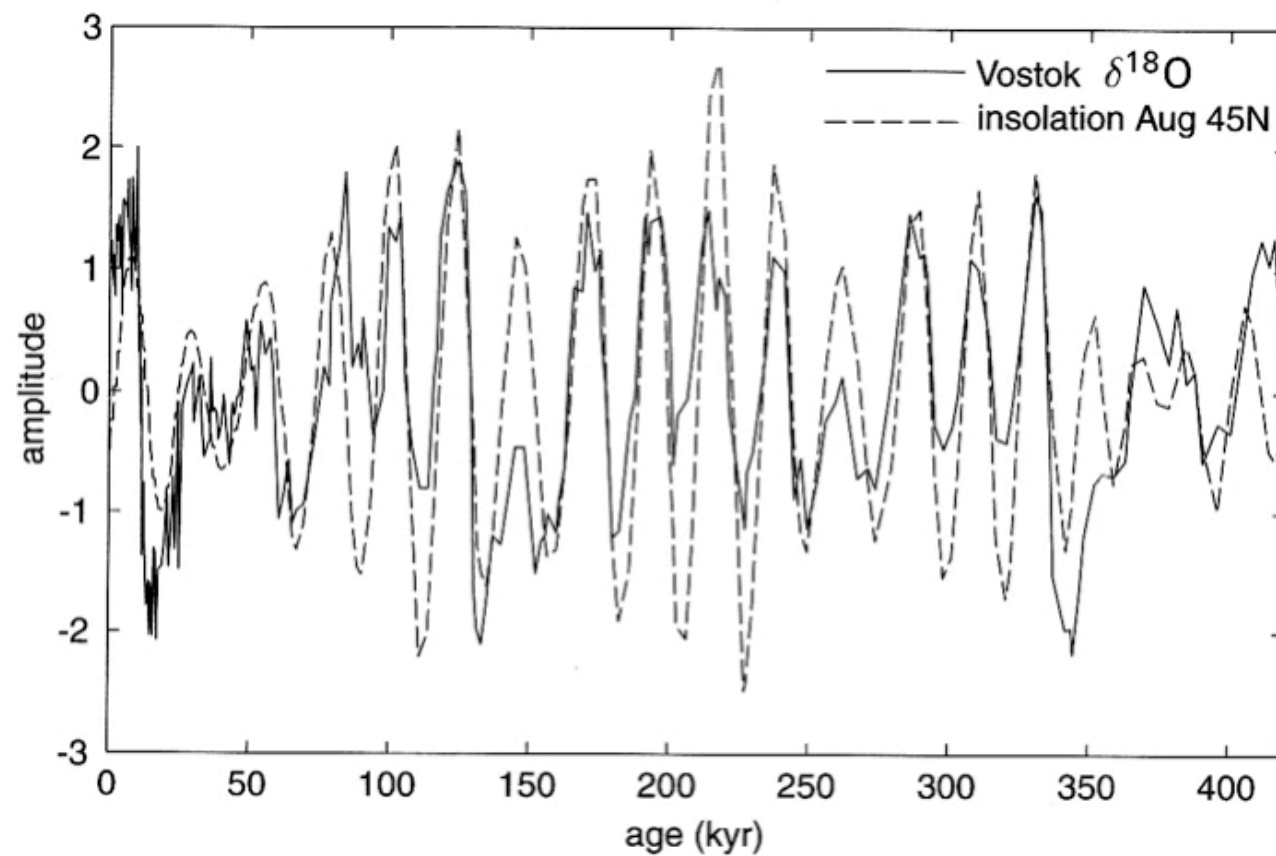


Fig. 4.40. Vostok oxygen and August 45N insolation. No phase lag used.

What amplifies orbital forcing to produce ice ages?

Why does 100 kyr eccentricity period dominate climate signal?

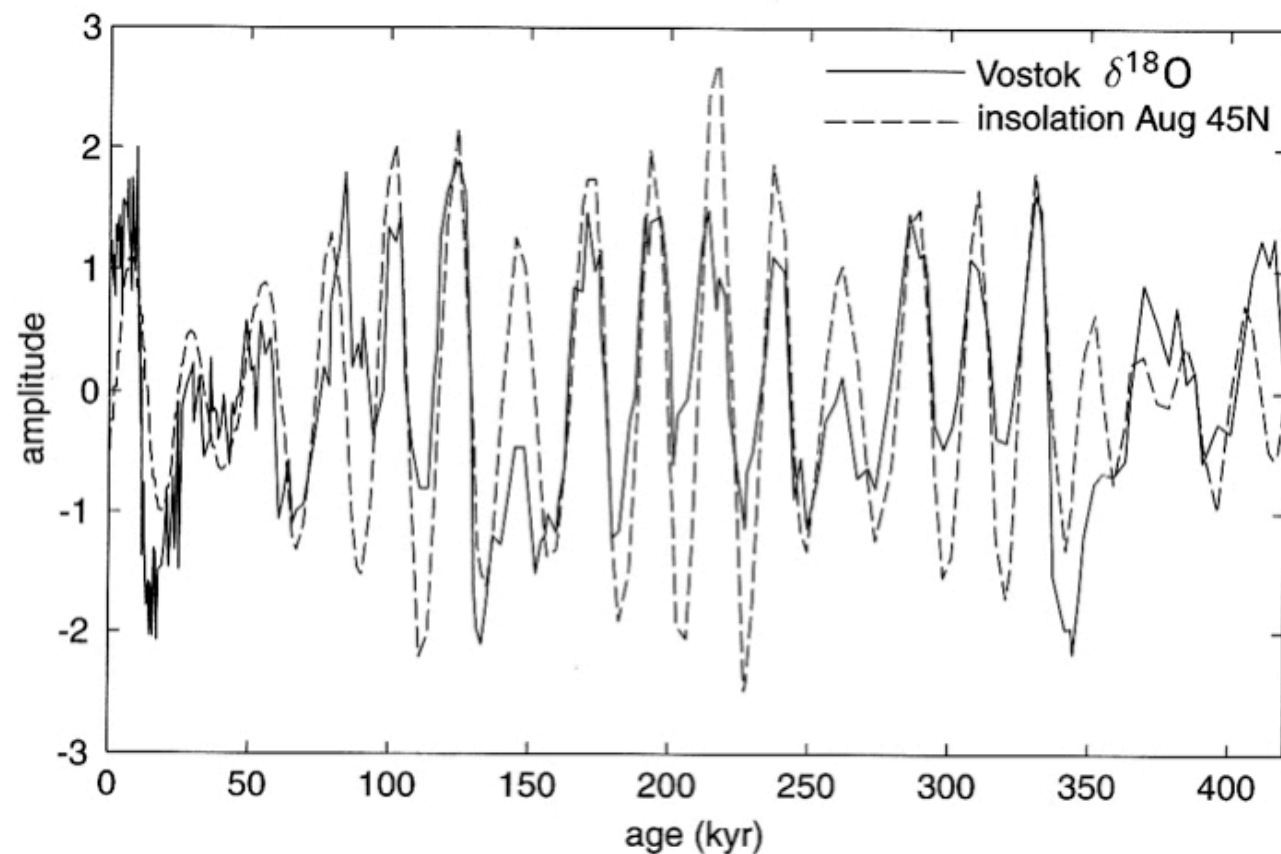
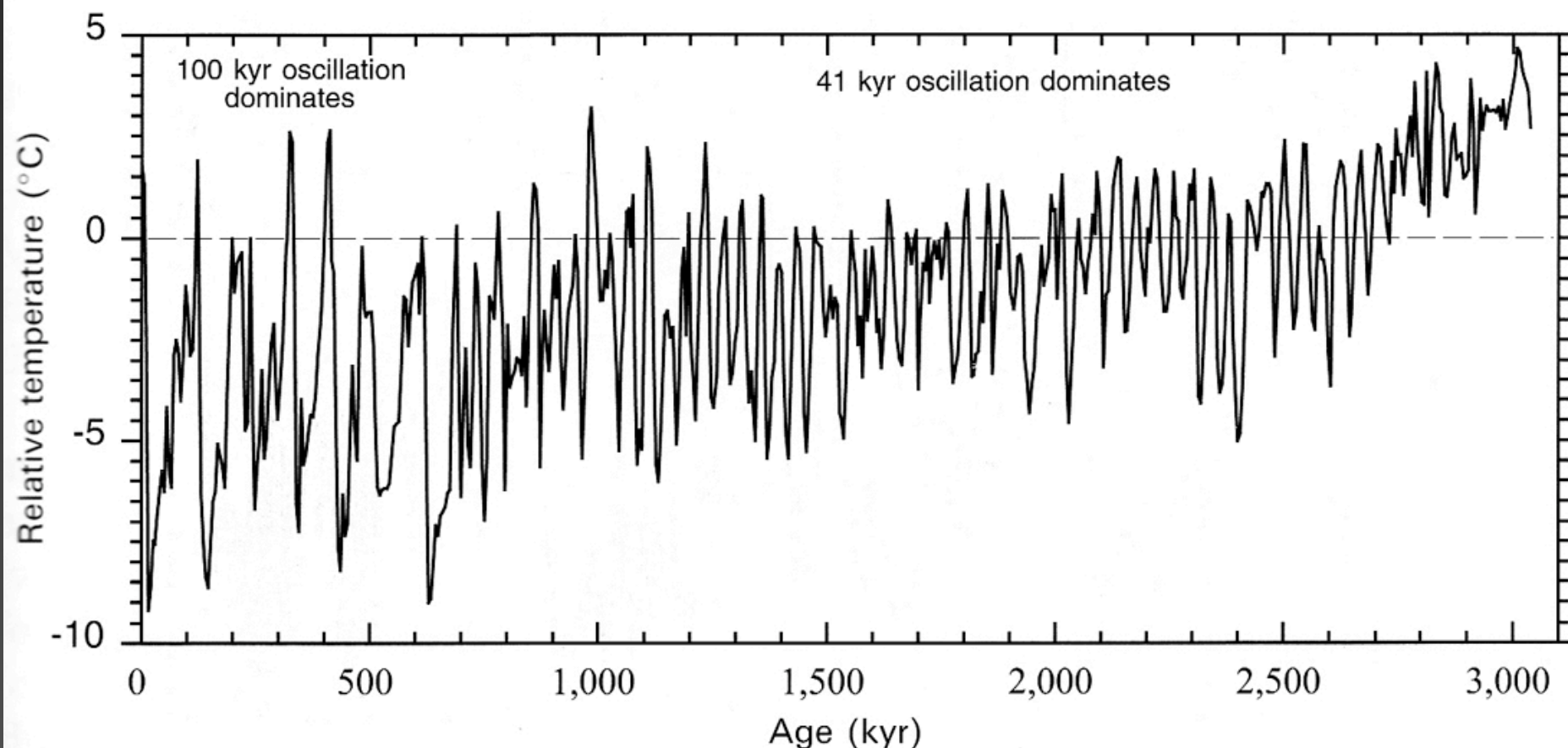


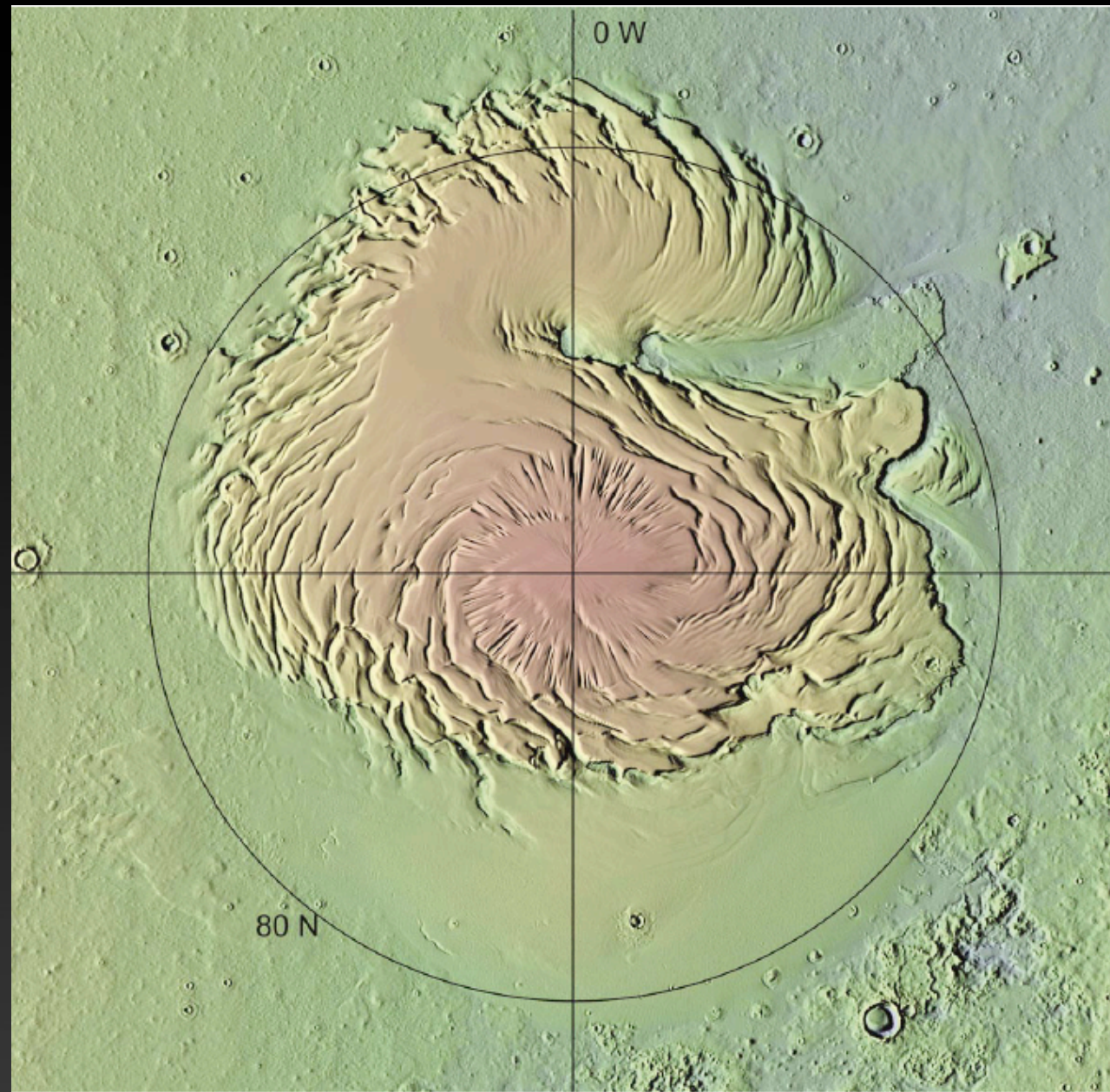
Fig. 4.40. Vostok oxygen and August 45N insolation. No phase lag used.

What amplifies orbital forcing to produce ice ages?

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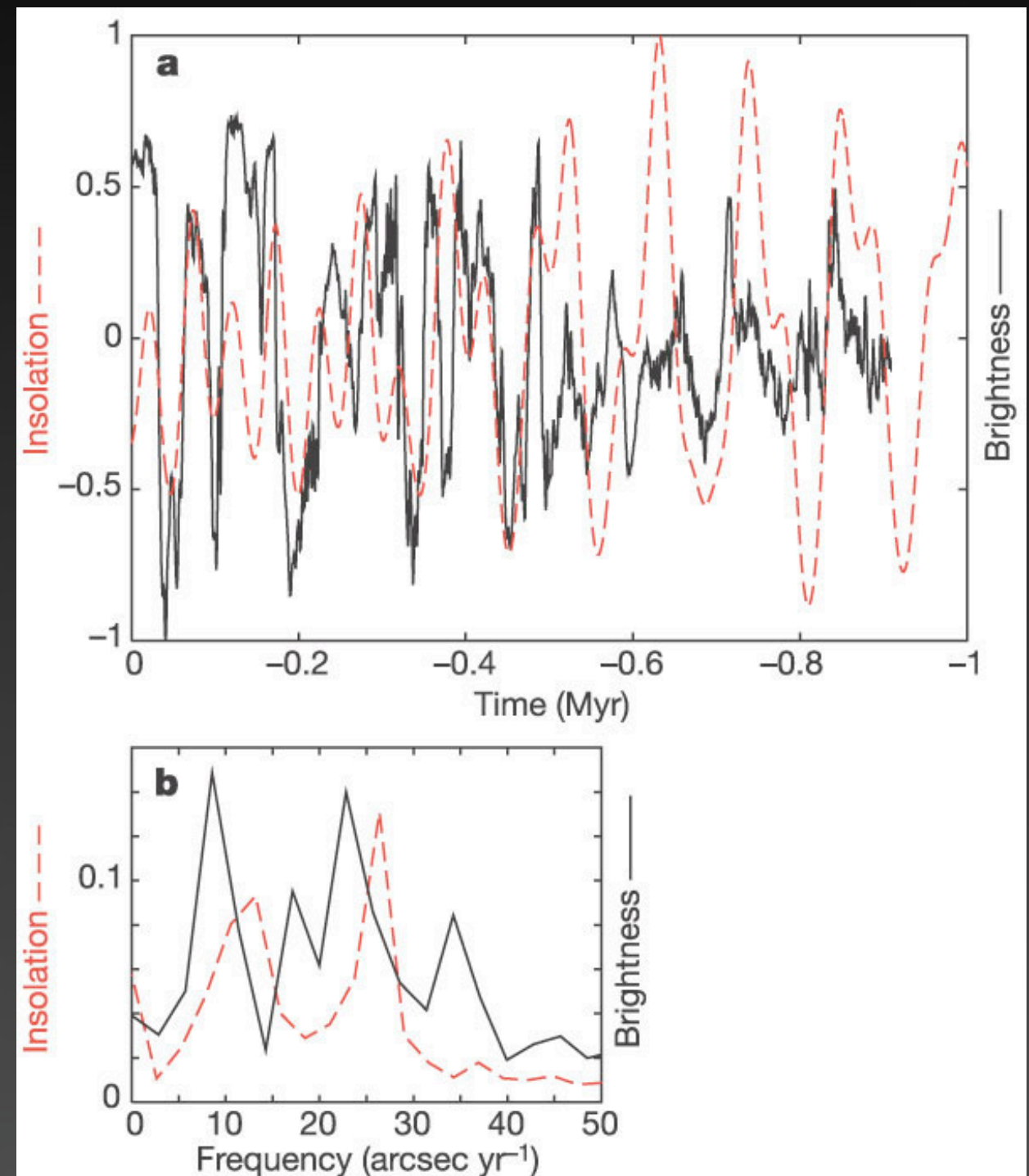
Why did the 41 kyr period dominate 1.5 million years ago?

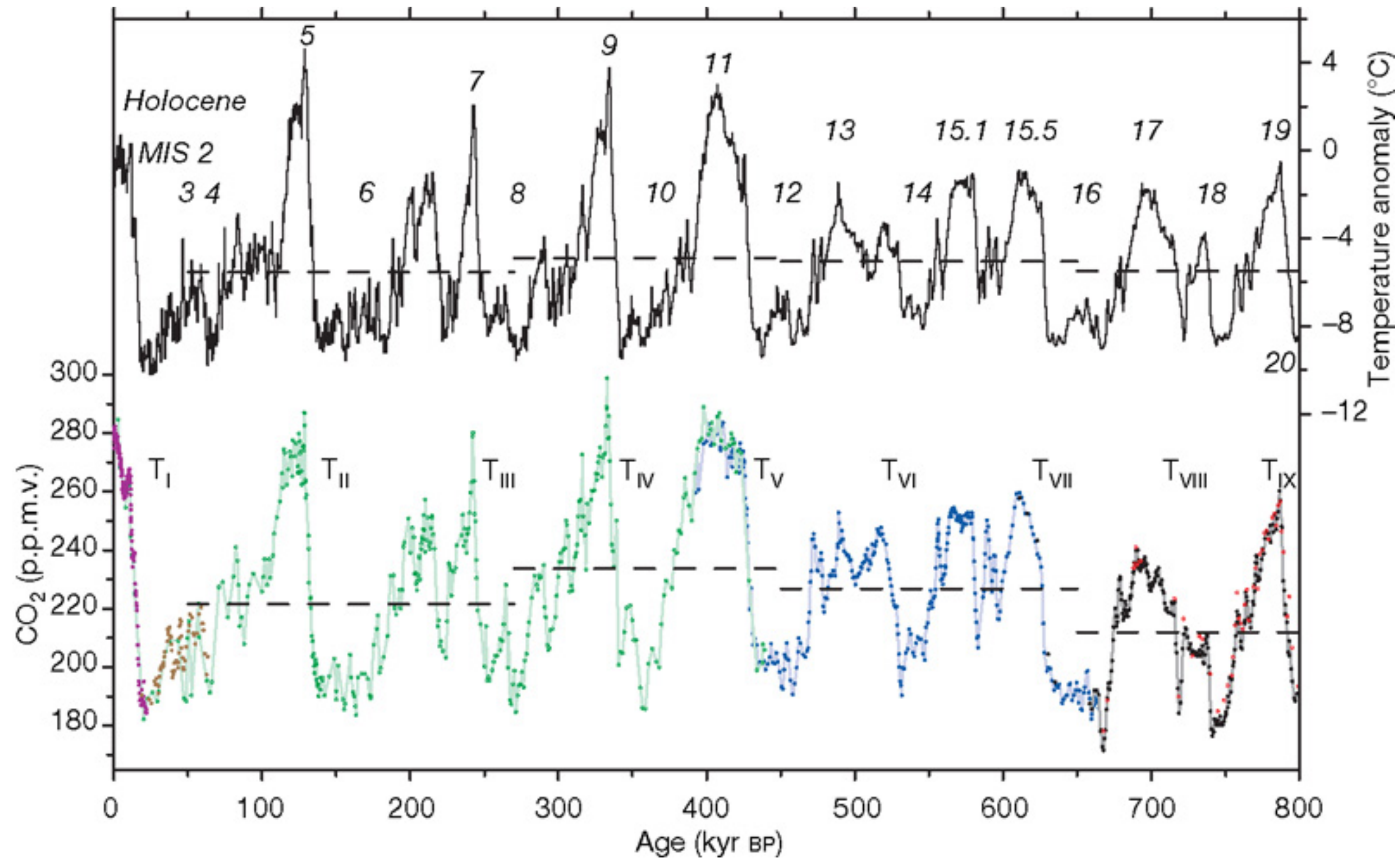


North Polar Cap of Mars

Laskar, Levrard, and Mustard,
Nature **419**, 375 (2002); Head
et al. *Nature* **426**, 797 (2003).

Martian Climate May Also Show Orbital Forcing





Ice Age Climate Forcings (W/m^2)

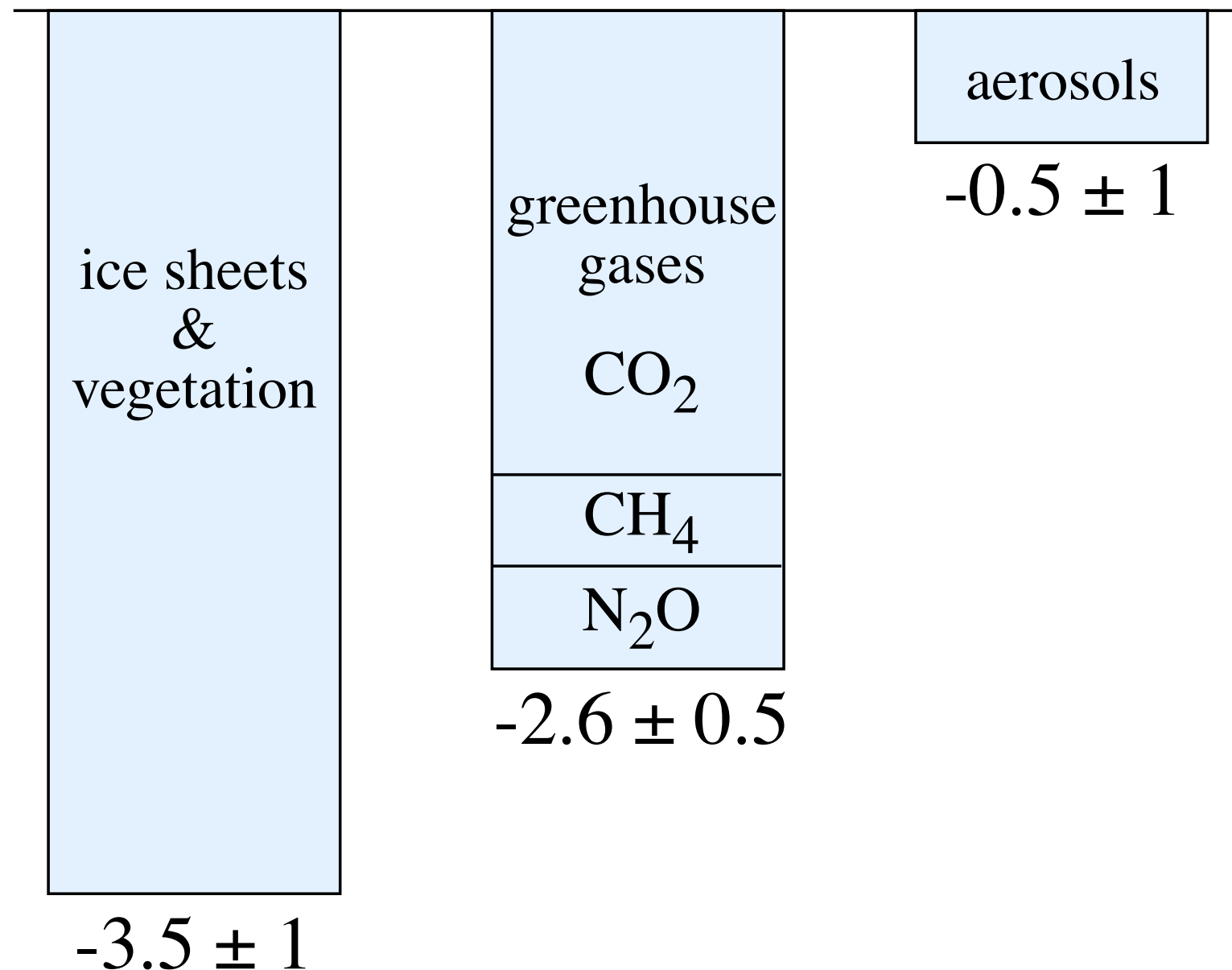
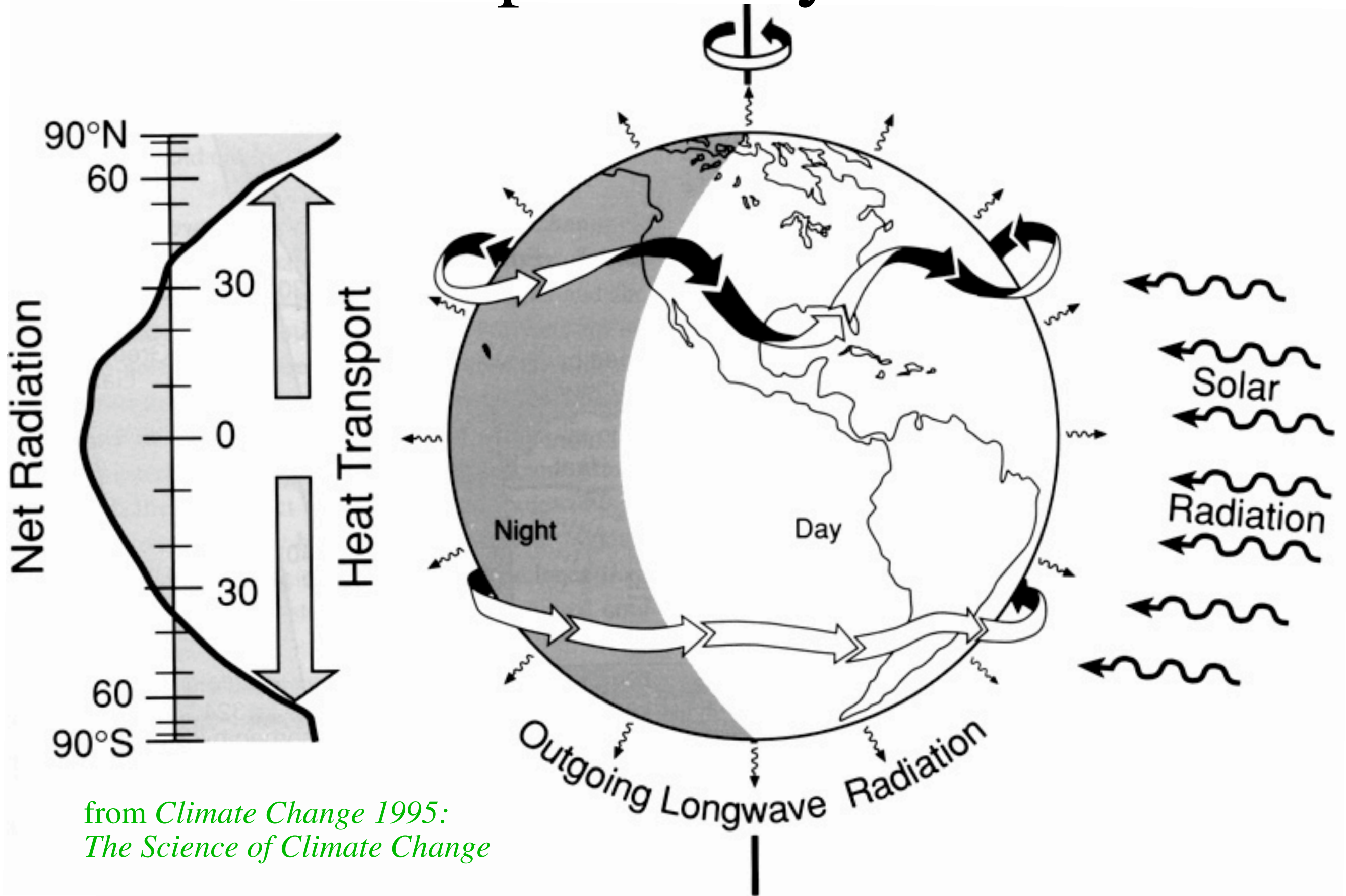


Fig 2. Global radiative forcings during the last ice age relative to the current interglacial period. The total forcing is $-6.6 \pm 1.5 \text{ W/m}^2$. Thus, the 5°C cooling of the ice age implies a climate sensitivity of 0.75°C per 1 W/m^2 forcing.

Hansen, J. et al., The missing climate forcing, Phil. Trans. R. Soc. London. B, 352, 231-240, 1997.

Atmospheric Dynamics




Single Layer Models

Single Layer Models

$$\frac{D\omega}{Dt} = 0$$


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Vorticity  $\omega = \hat{r} \cdot (\vec{\nabla} \times \vec{v})$

Single Layer Models

$$\frac{D\omega}{Dt} = 0$$

Vorticity  $\omega = \hat{r} \cdot (\vec{\nabla} \times \vec{v})$

$$\frac{\partial \omega}{\partial t} + \vec{v} \cdot \vec{\nabla} \omega = 0$$


$$\vec{v} = \hat{r} \times \vec{\nabla} \psi$$

$$\vec{\nabla} \cdot \vec{v} = 0$$

$$\omega = \nabla^2 \psi$$

Single Layer Models

$$\frac{D\omega}{Dt} = 0$$

Vorticity  $\omega = \hat{r} \cdot (\vec{\nabla} \times \vec{v})$

$$\frac{\partial \omega}{\partial t} + \vec{v} \cdot \vec{\nabla} \omega = 0$$

$$\frac{\partial \omega}{\partial t} + J(\psi, \omega) = 0$$

$$\vec{v} = \hat{r} \times \vec{\nabla} \psi$$

$$\vec{\nabla} \cdot \vec{v} = 0$$

$$\omega = \nabla^2 \psi$$

$$J(\psi, \omega) \equiv \frac{\partial \psi}{\partial x} \frac{\partial \omega}{\partial y} - \frac{\partial \psi}{\partial y} \frac{\partial \omega}{\partial x}$$

Freely Decaying Turbulence on Sphere

Coriolis Force

Coriolis Force

$$\frac{\partial q}{\partial t} + J(\psi, q) = 0$$

Coriolis Force

$$\frac{\partial q}{\partial t} + J(\psi, q) = 0$$

Relative vorticity

Absolute vorticity

$$\begin{aligned} q &= \omega + f \\ &= \nabla^2 \psi + f \end{aligned}$$

Coriolis term

The diagram illustrates the relationship between absolute vorticity (q), relative vorticity (ω), and the Coriolis term (f). The equations shown are $q = \omega + f$ and $q = \nabla^2 \psi + f$. A yellow arrow points from the label 'Absolute vorticity' to the variable q . Another yellow arrow points from the label 'Relative vorticity' to the variable ω . A third yellow arrow points from the label 'Coriolis term' to the variable f .

Coriolis Force

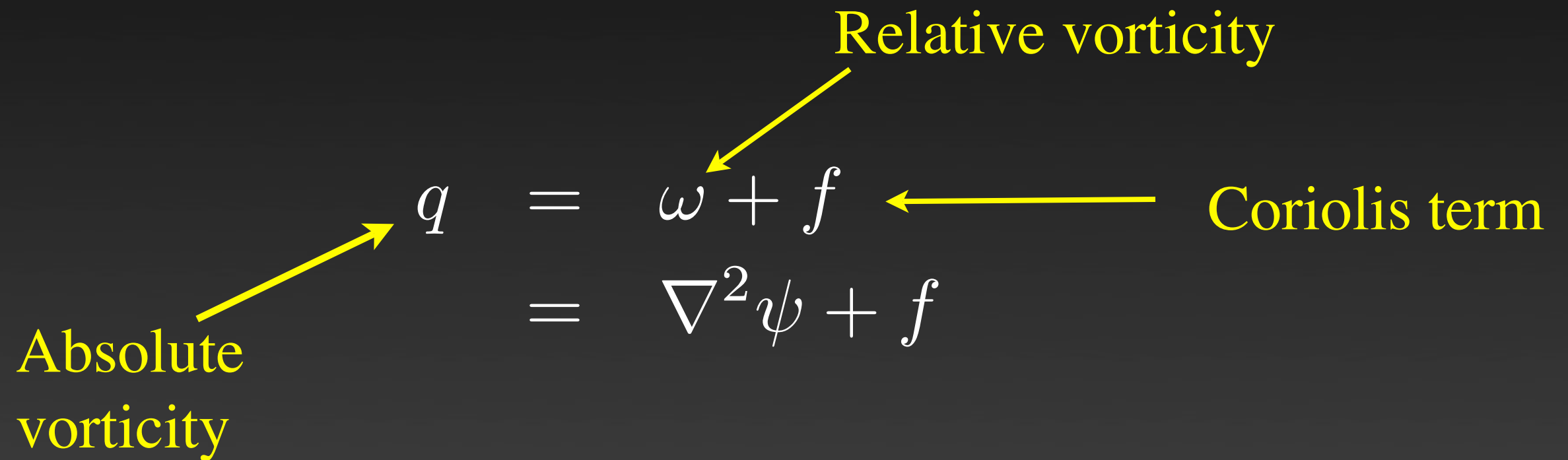
$$\frac{\partial q}{\partial t} + J(\psi, q) = 0$$

Relative vorticity

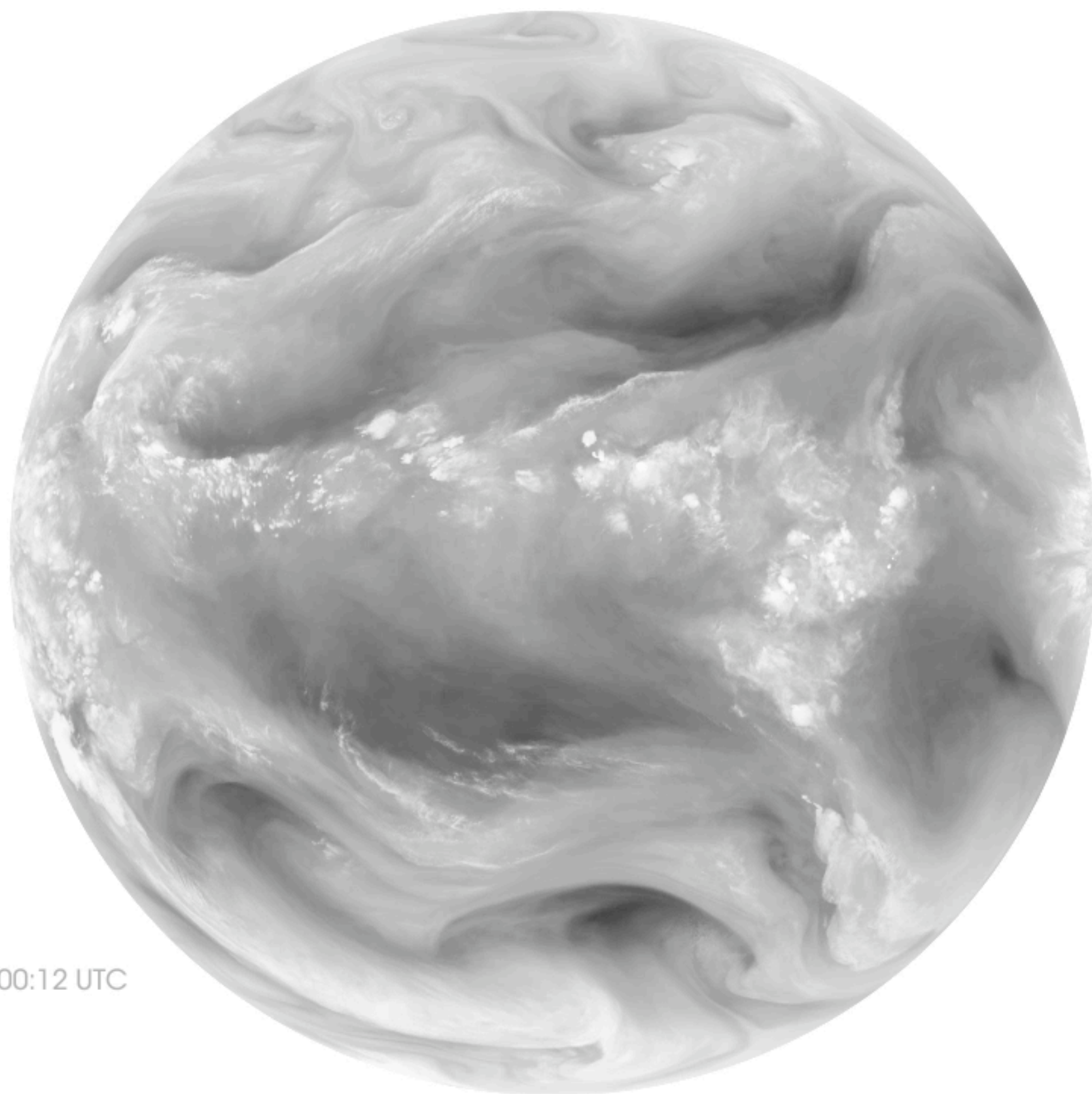
Absolute vorticity

$$\begin{aligned} q &= \omega + f \\ &= \nabla^2 \psi + f \end{aligned}$$

Coriolis term

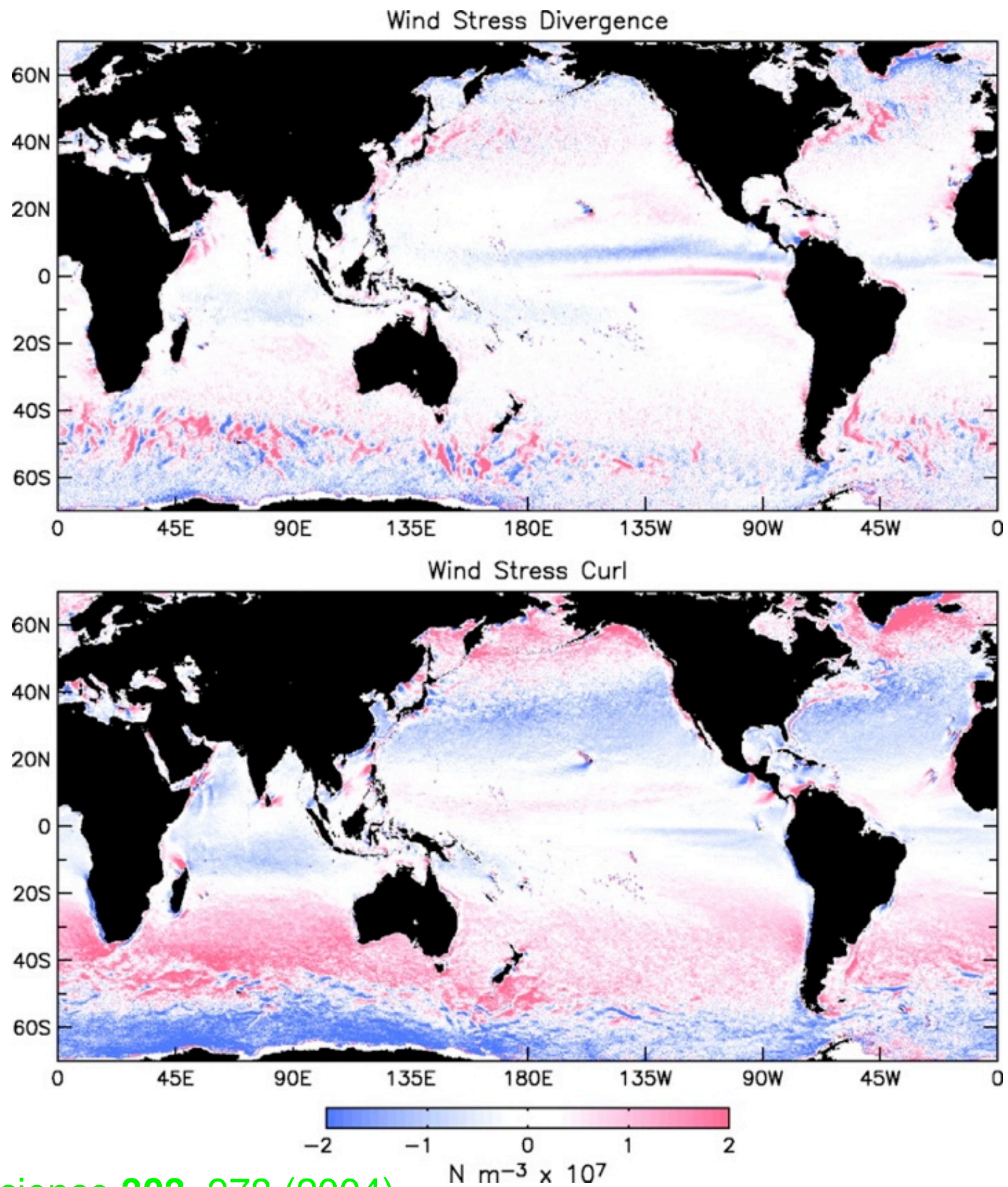


$$f = 2\Omega \sin(\phi)$$



October 7, 2007 00:12 UTC

Coriolis Force



Chelton *et al.*, Science **303**, 978 (2004)

Stratification

Stratification

$$q = \nabla^2 \psi + f - \frac{\psi}{\ell_R^2}$$

Stratification

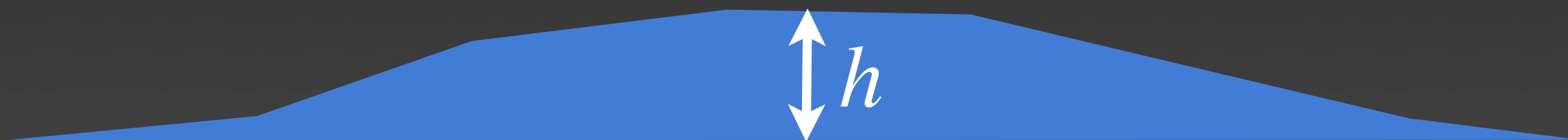
$$q = \nabla^2 \psi + f - \frac{\psi}{\ell_R^2}$$

$$\ell_R^2 = \frac{gh}{f^2}$$

Stratification

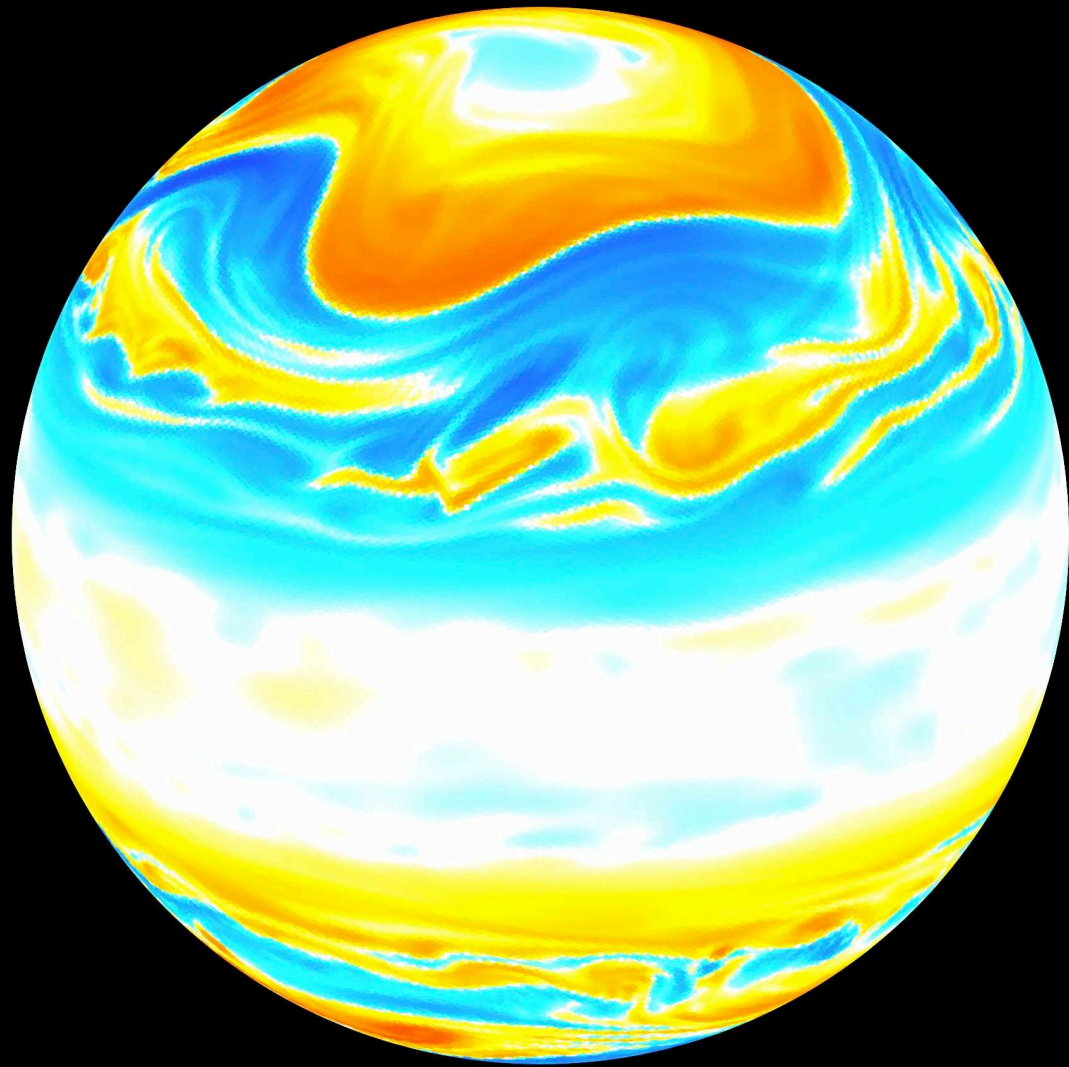
$$q = \nabla^2 \psi + f - \frac{\psi}{\ell_R^2}$$

$$\ell_R^2 = \frac{gh}{f^2}$$

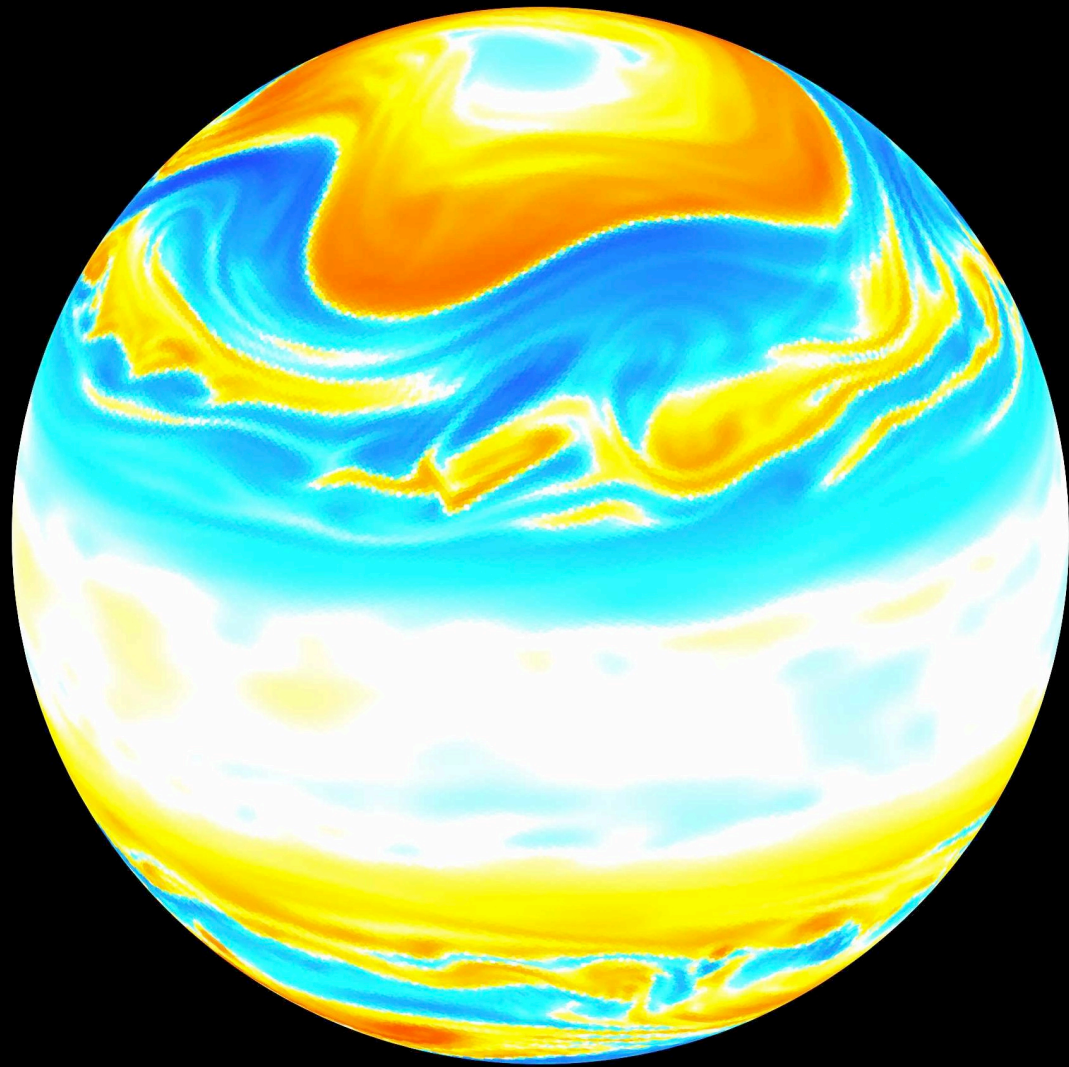


$$\ell_R = \mathcal{O}(1,000 \text{ km})$$

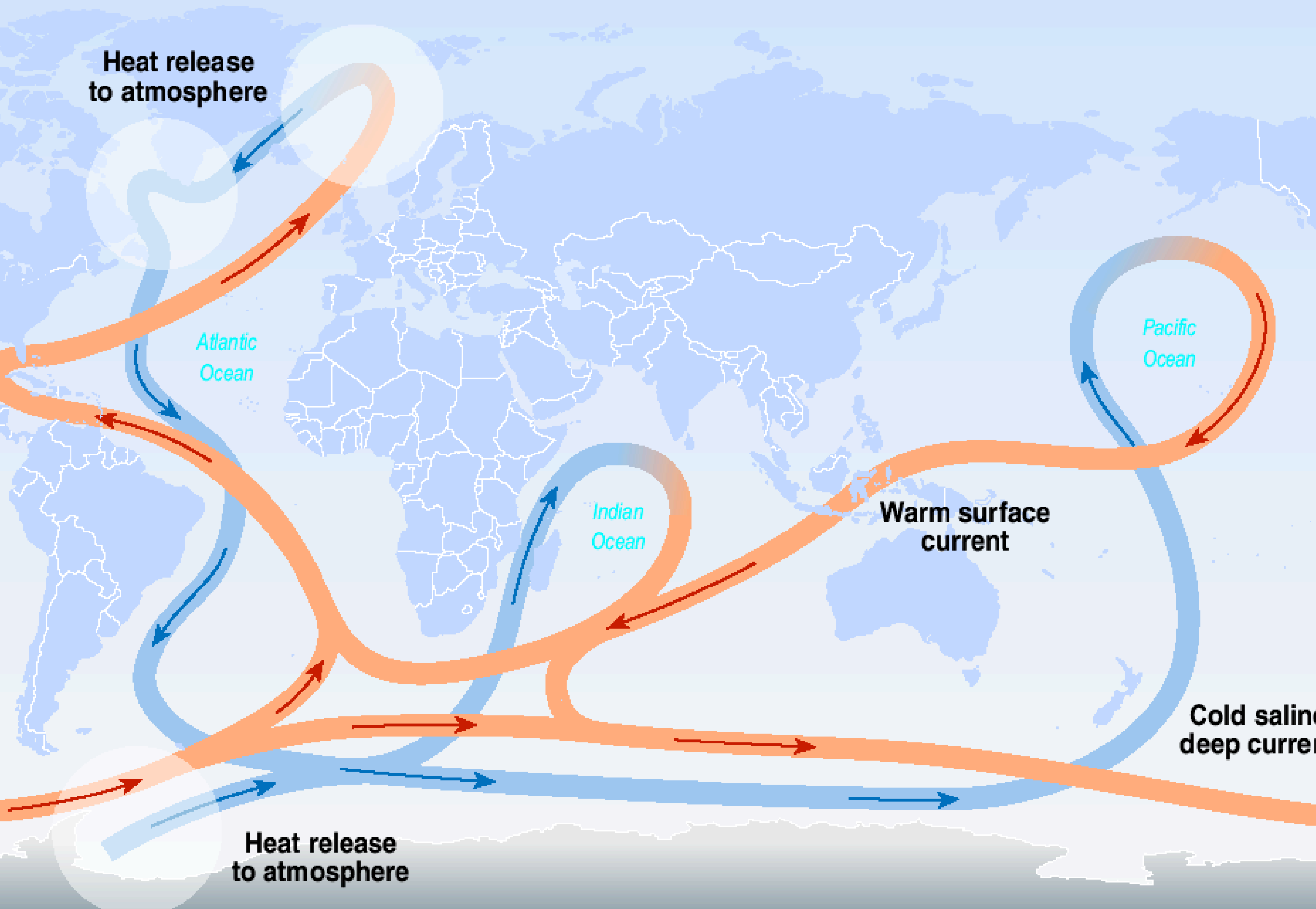
Stratification Sets Synoptic Length Scale



Stratification Sets Synoptic Length Scale



Great ocean conveyor belt



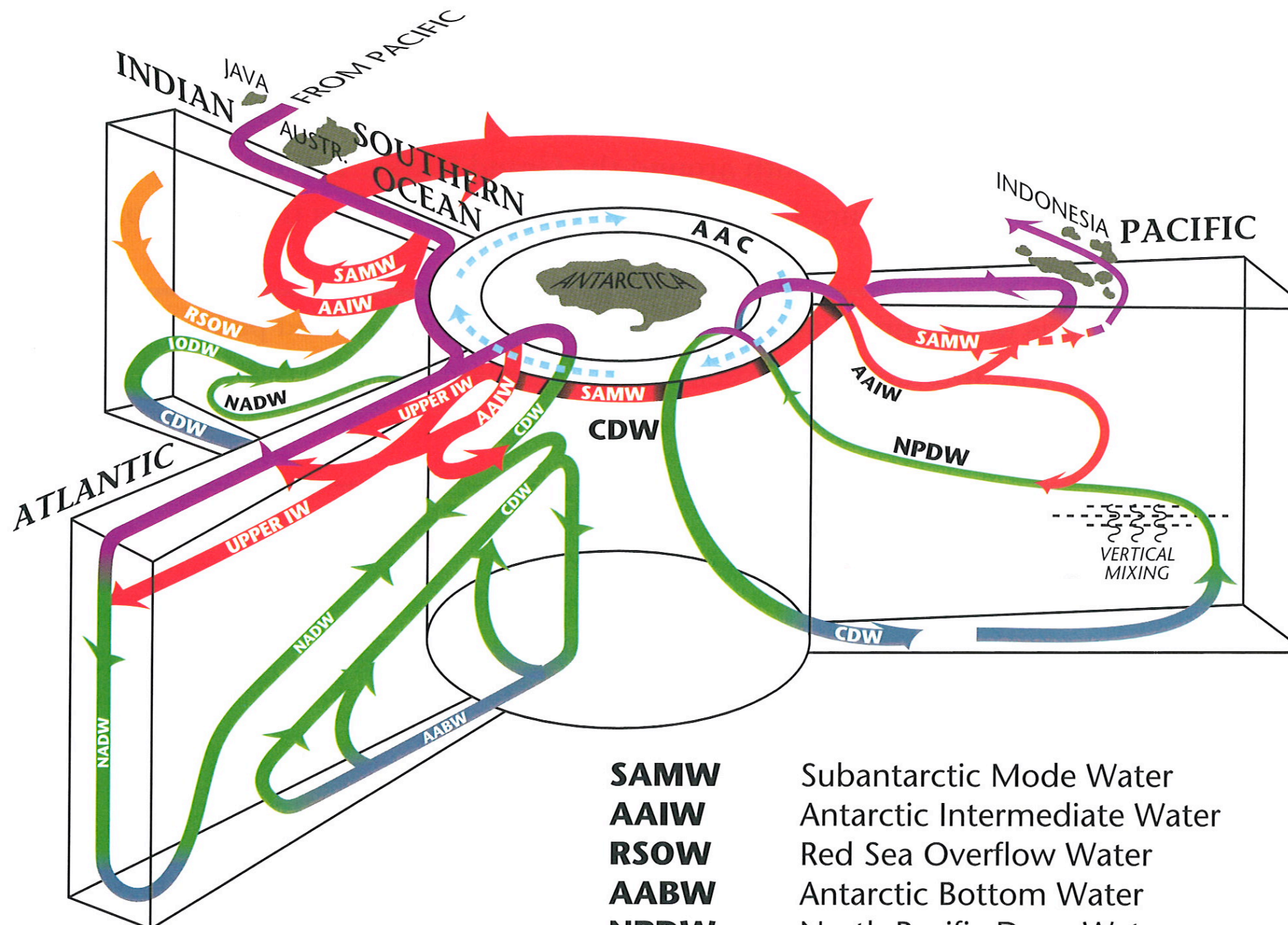
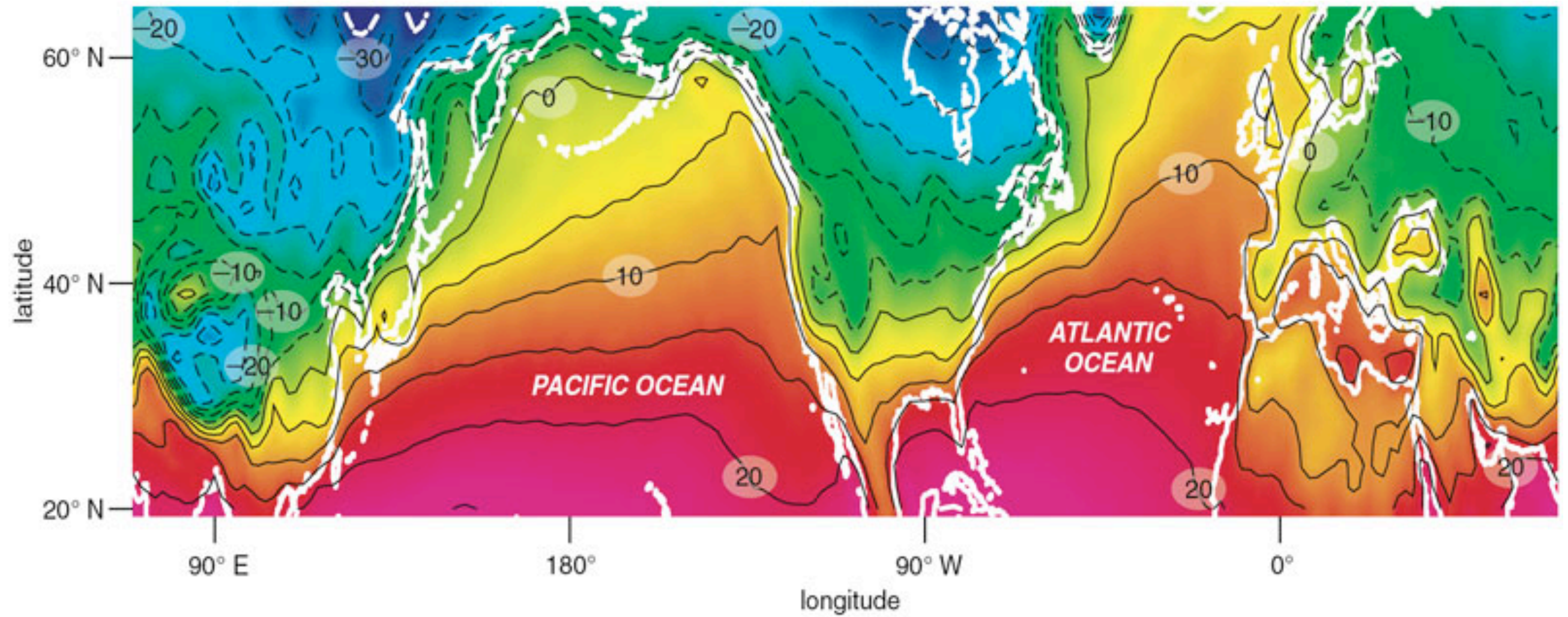


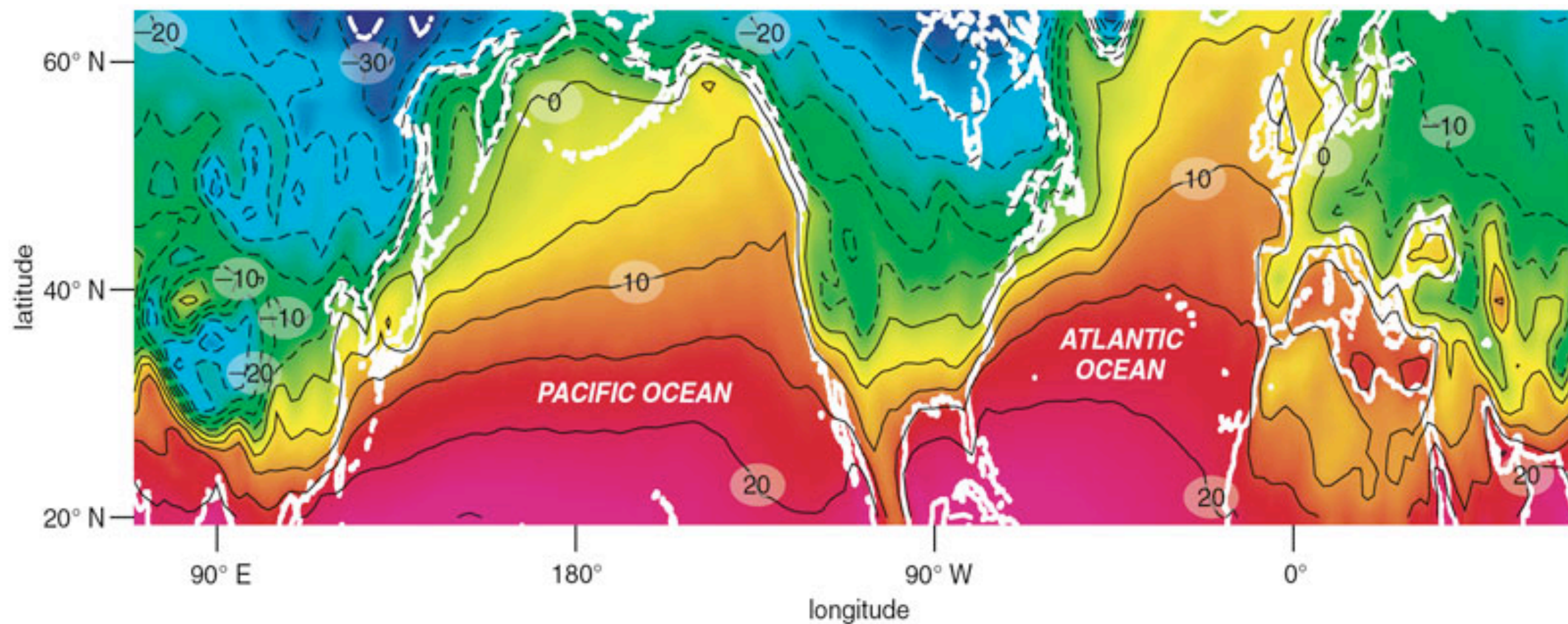
Figure I-91: A new version of Figure I-90 with schematic meridional sections of interbasin flow for each ocean with their global linkages.

SAMW
AAIW
RSOW
AABW
NPDW
AAC
CDW
NADW
UPPER IW
IODW

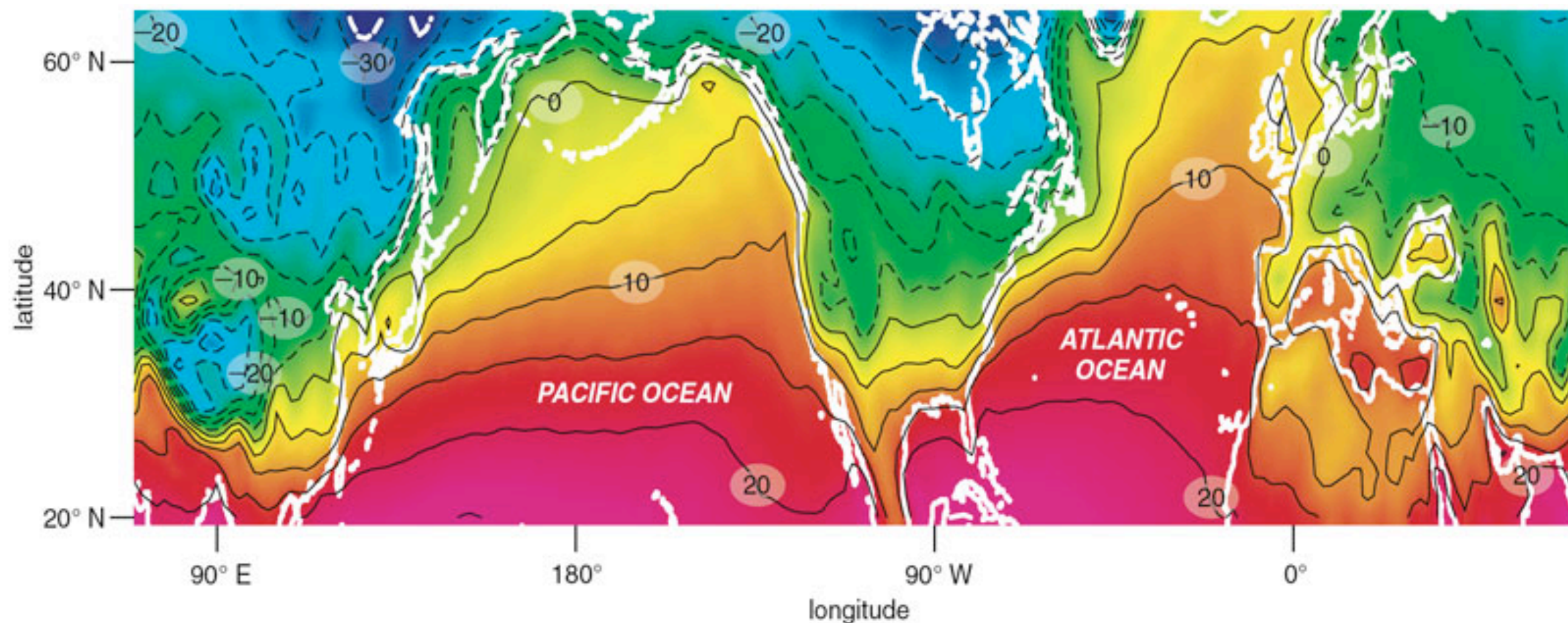
Subantarctic Mode Water
 Antarctic Intermediate Water
 Red Sea Overflow Water
 Antarctic Bottom Water
 North Pacific Deep Water
 Antarctic Circumpolar Current
 Circumpolar Deep Water
 North Atlantic Deep Water
 $26.8 \leq \sigma_\theta \leq 27.25$
 Indian Ocean Deep Water



City	Latitude	January (°F)	August (°F)
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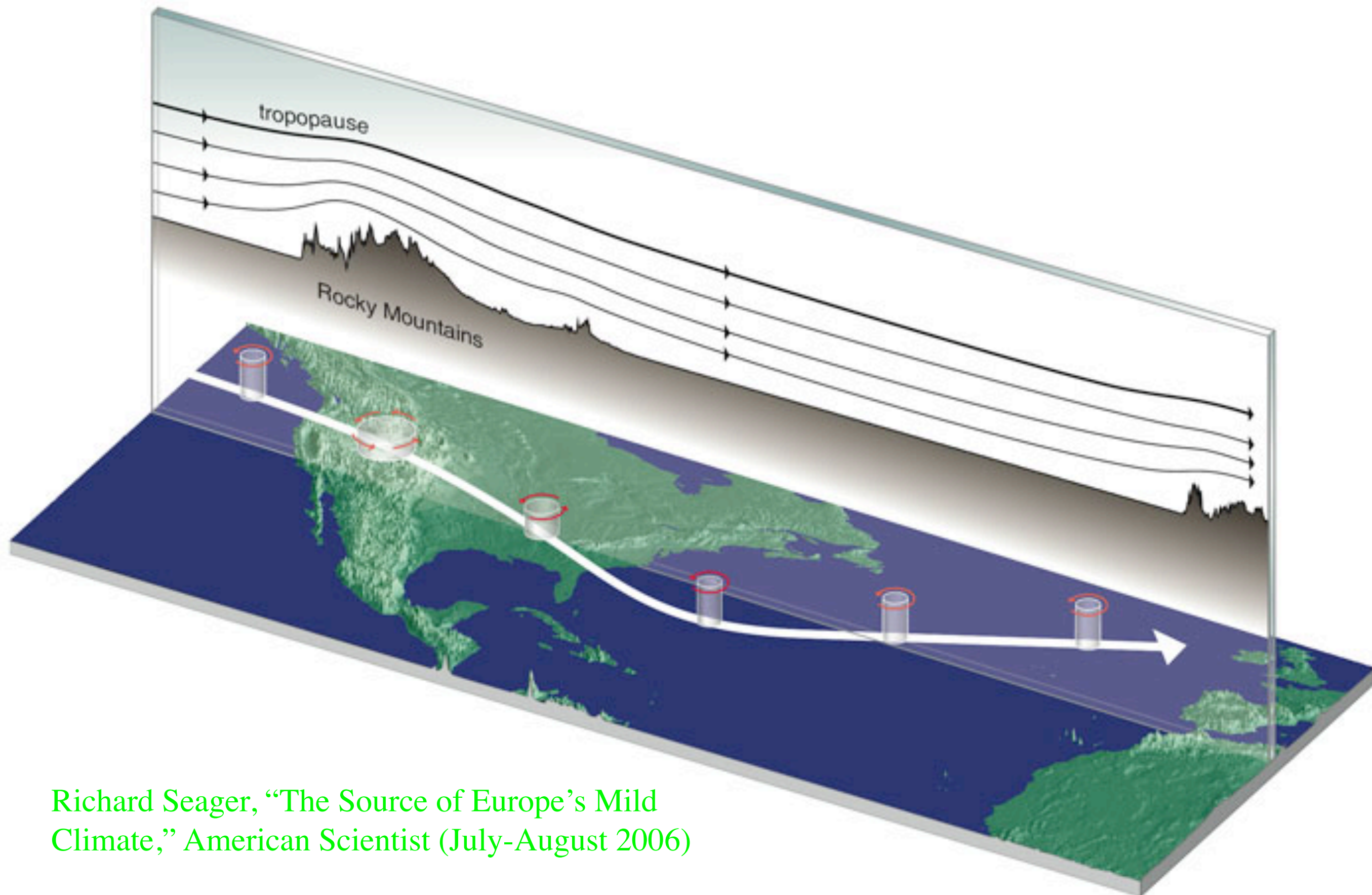


City	Latitude	January (°F)	August (°F)
Glasgow	56°	34 to 45	52 to 64



City	Latitude	January (°F)	August (°F)
Glasgow	56°	34 to 45	52 to 64
Sitka	57°	30 to 38	52 to 62

Topography & Angular Momentum

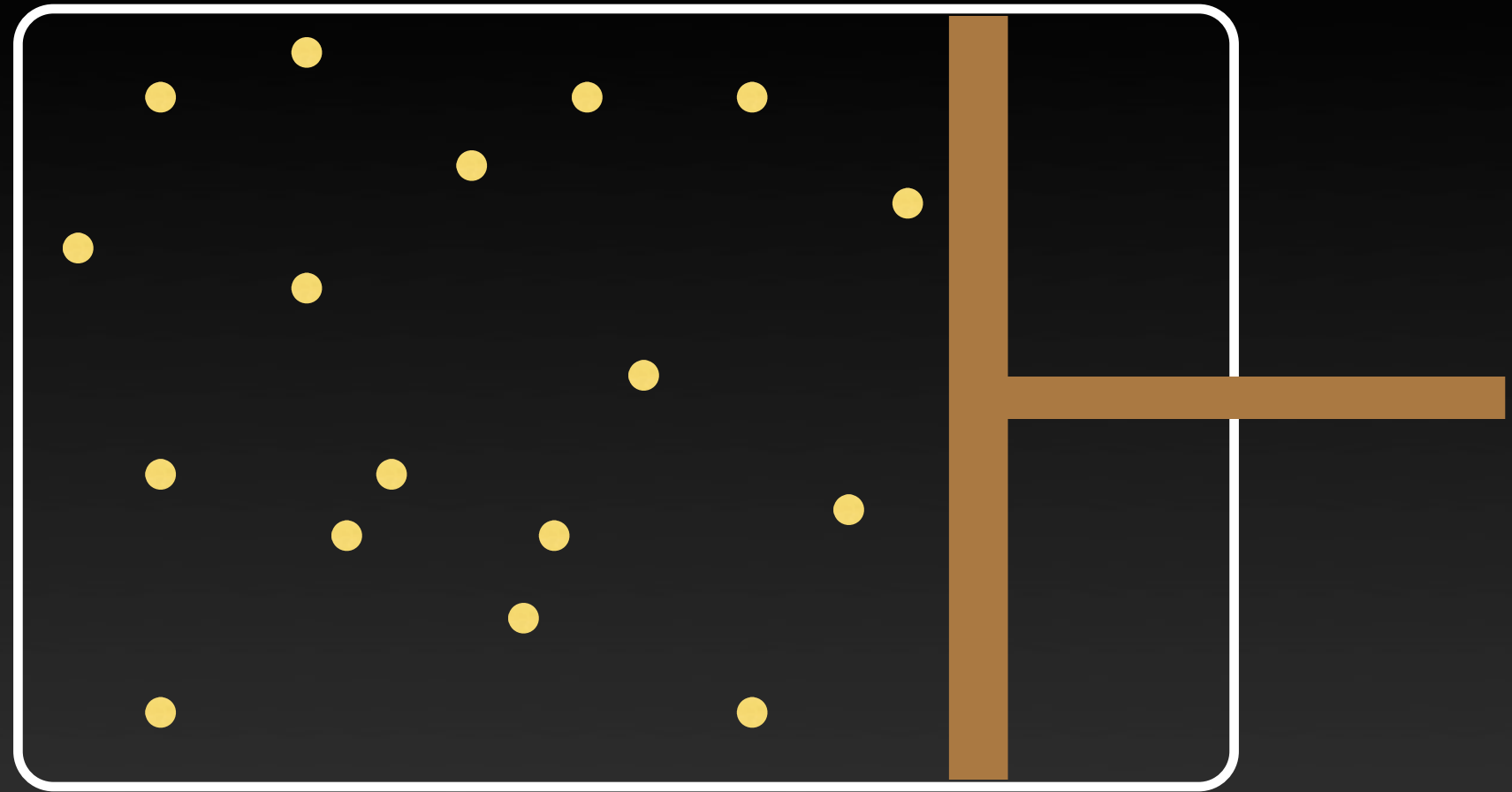


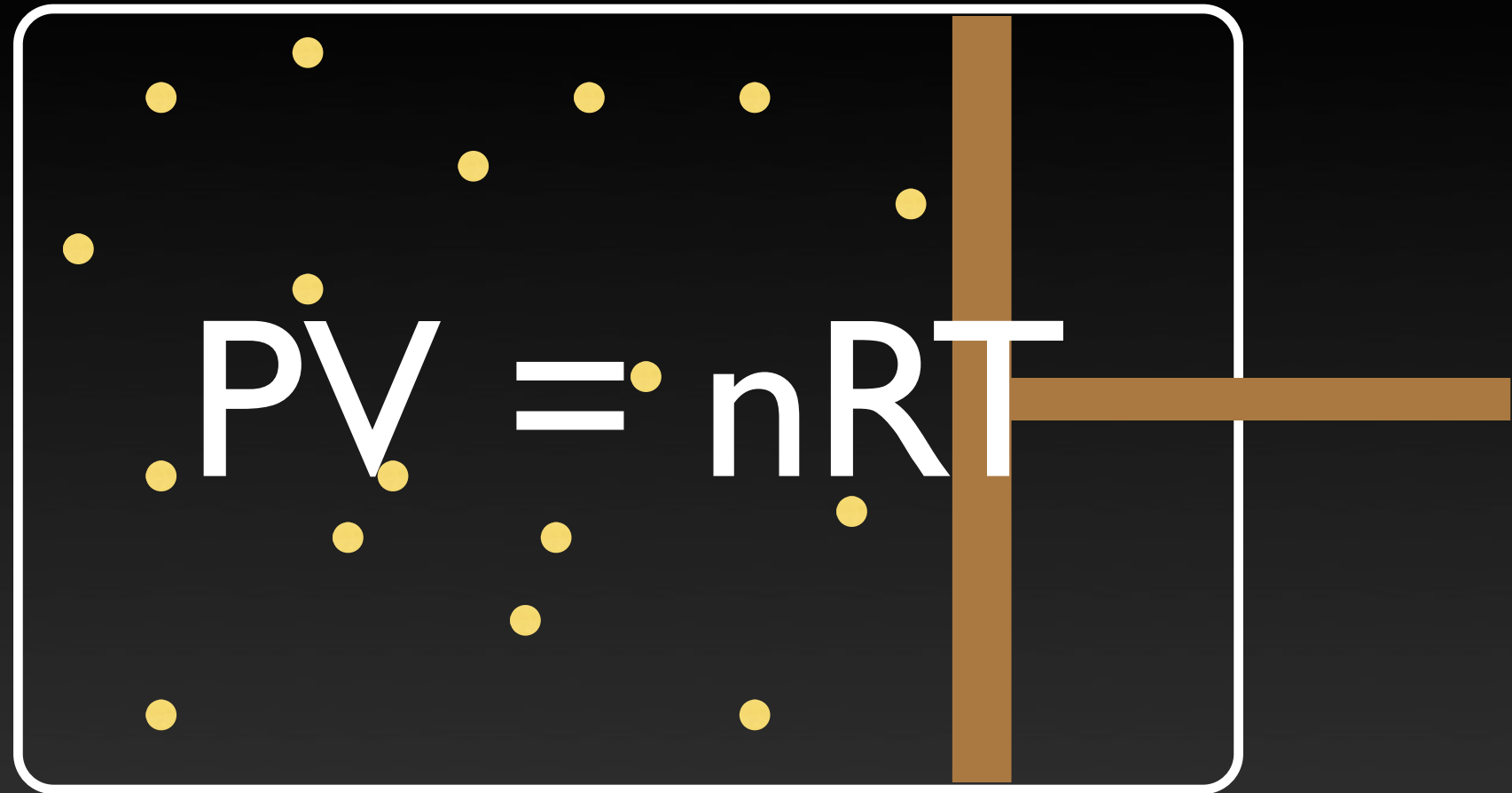
Richard Seager, "The Source of Europe's Mild Climate," *American Scientist* (July-August 2006)

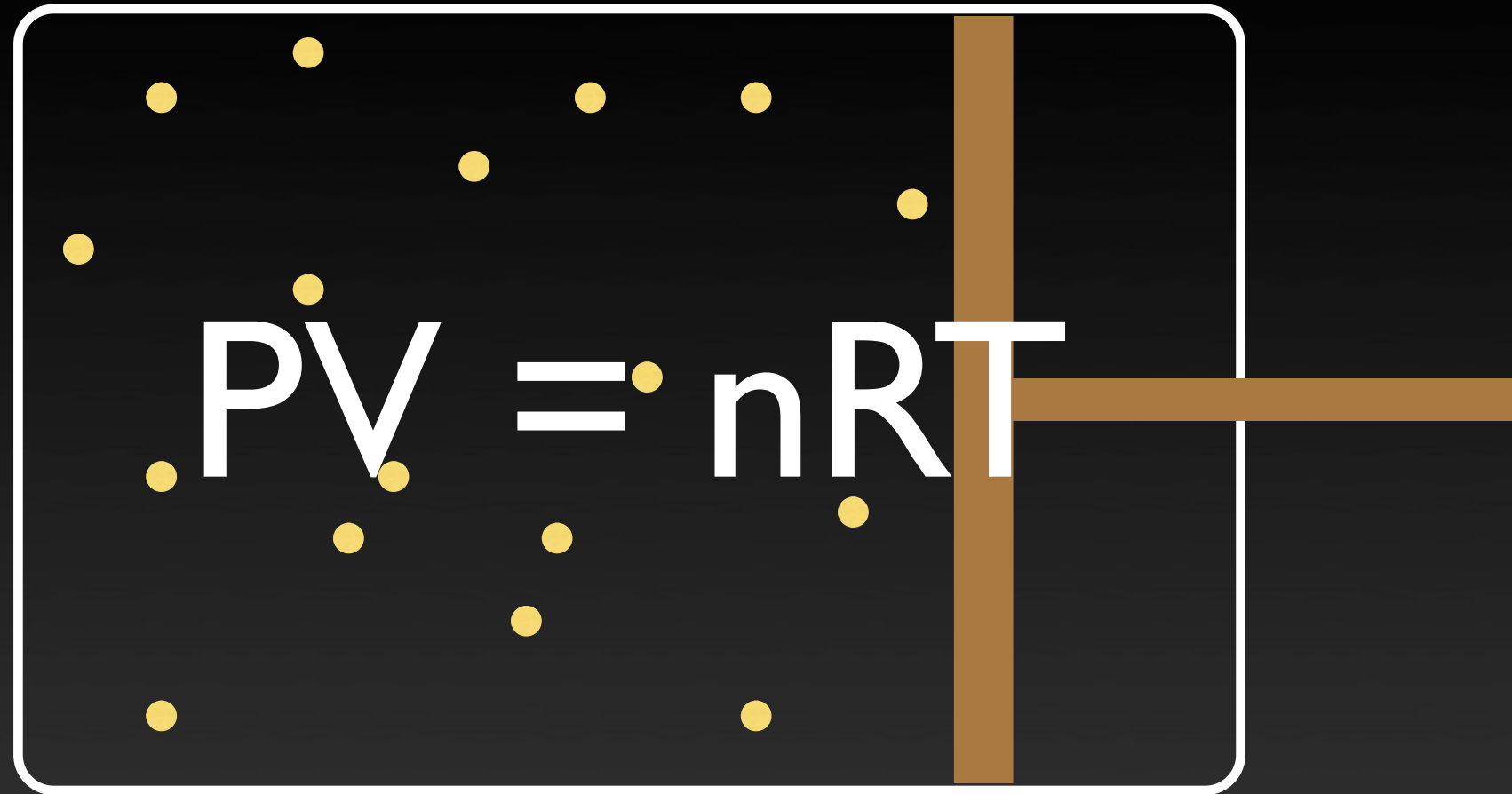
Quantum Field Theory of Global Warming?

"More than any other theoretical procedure, numerical integration is also subject to the criticism that it yields little insight into the problem. The computed numbers are not only processed like data but they look like data, and a study of them may be no more enlightening than a study of real meteorological observations. An alternative procedure which does not suffer this disadvantage consists of deriving a new system of equations whose unknowns are the statistics themselves."

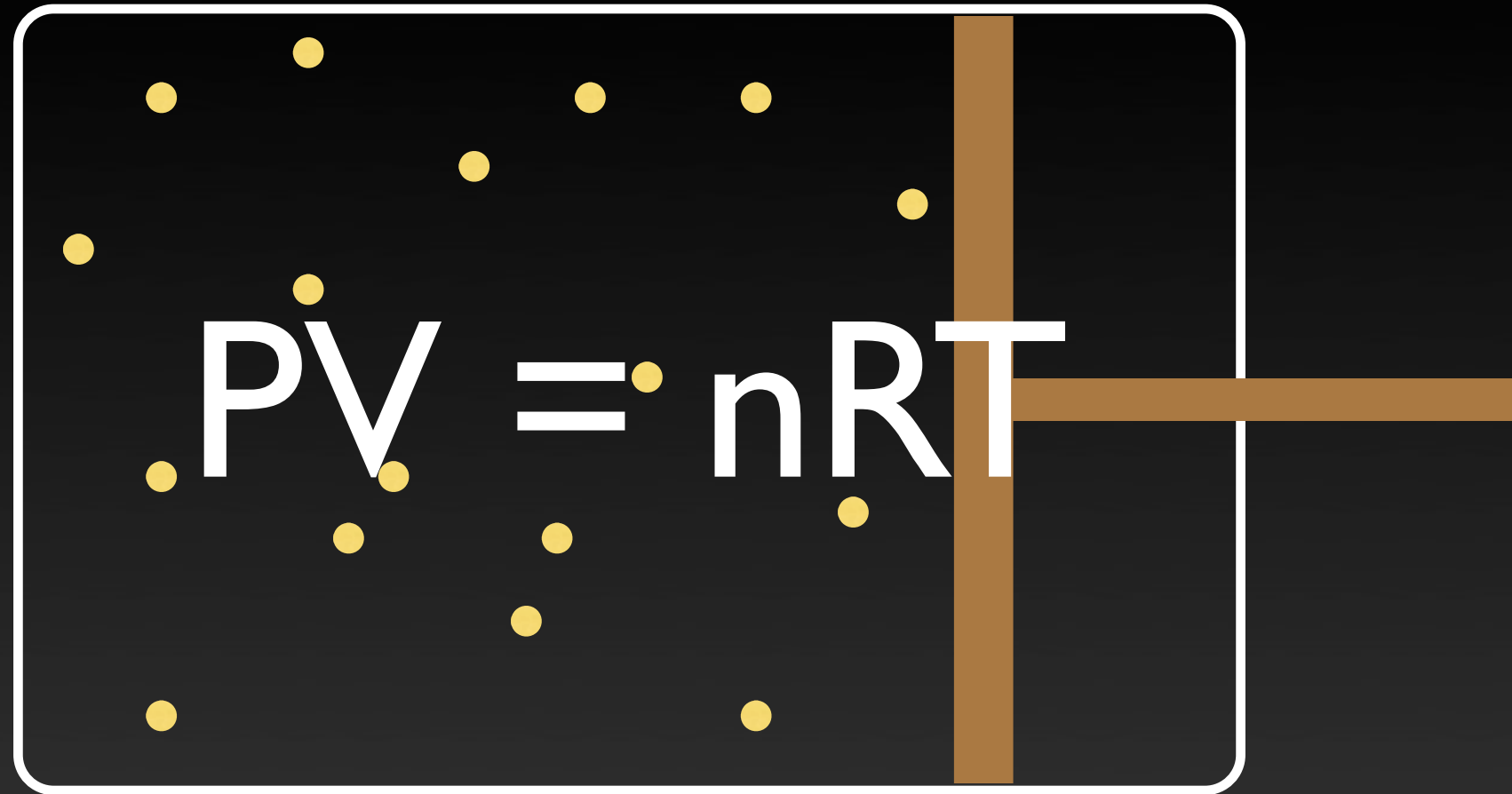
Edward Lorenz, The Nature and Theory of the General Circulation (1967)





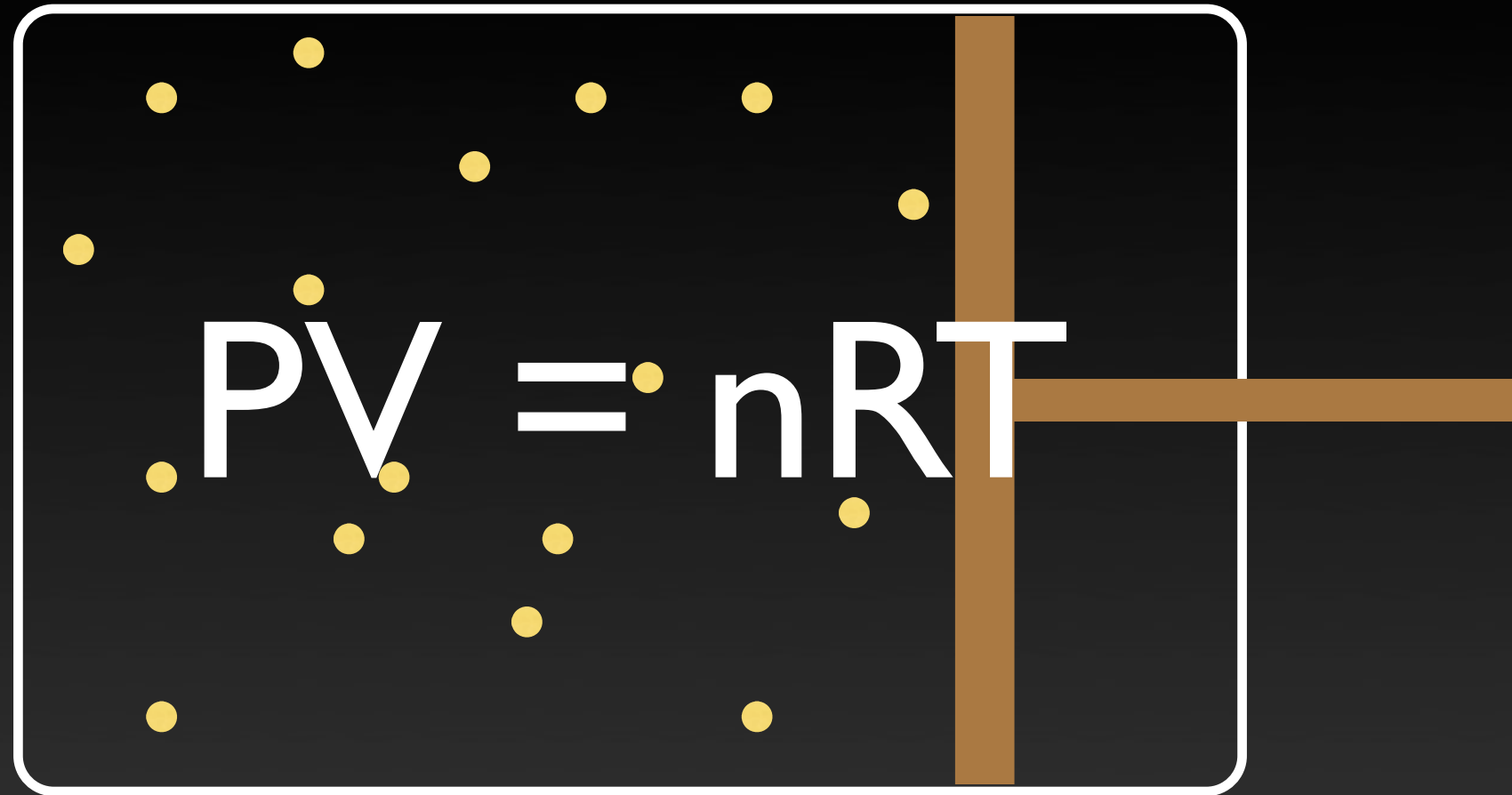


Thermodynamics vs. Statistical Mechanics



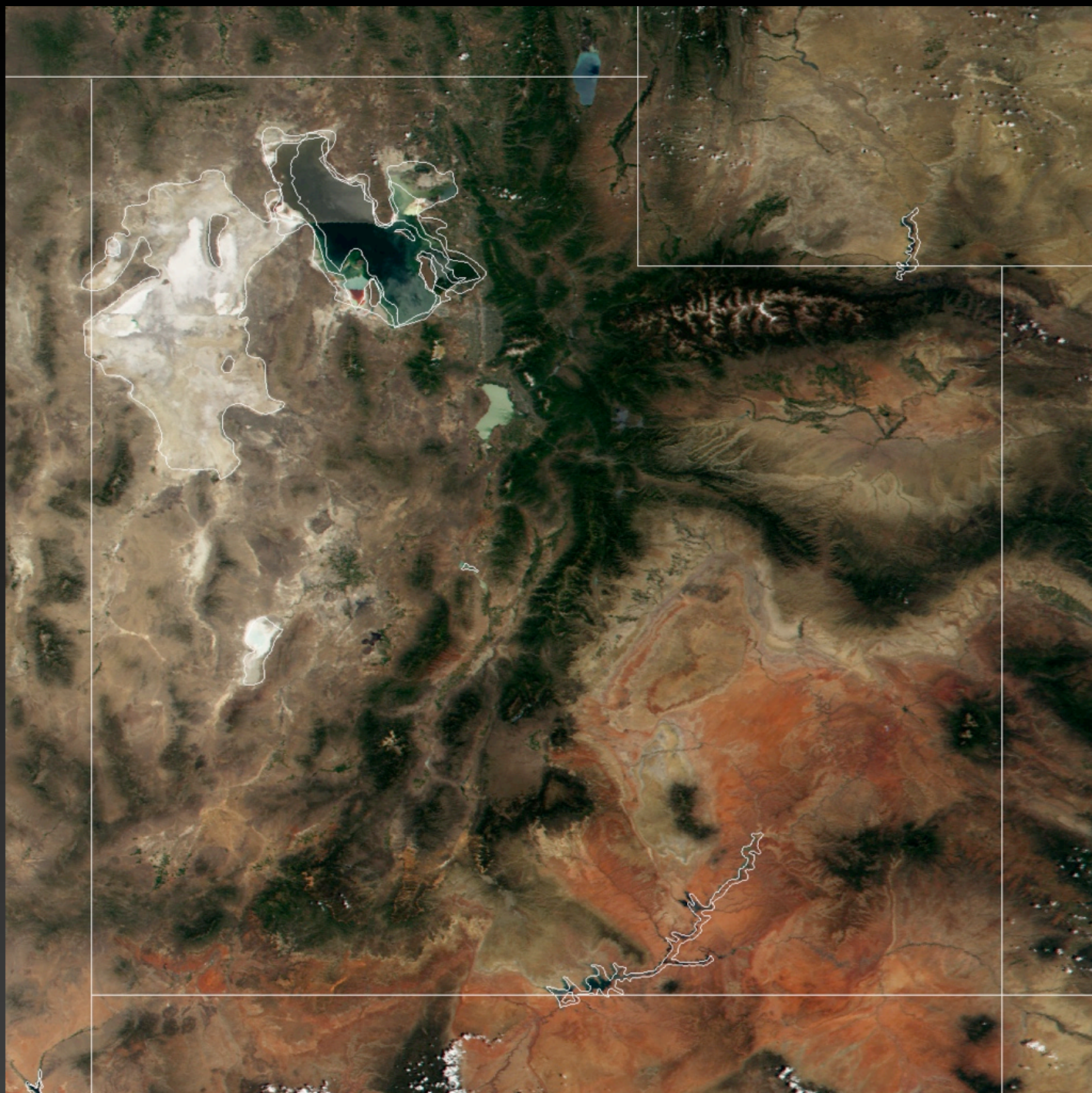
Thermodynamics vs. Statistical Mechanics

Equilibrium vs. Out-of-Equilibrium



Thermodynamics vs. Statistical Mechanics

Equilibrium vs. Out-of-Equilibrium





Hopf Functional Approach

Hopf Functional Approach

$$\frac{dx}{dt} = x^2$$

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$$\Psi(t, u) \equiv e^{iux(t)}$$

Hopf Functional Approach

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$$i \frac{\partial}{\partial t} \Psi = u \frac{\partial^2}{\partial u^2} \Psi$$

Hopf Functional Approach

$$\frac{dx}{dt} = x^2$$

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$$i \frac{\partial}{\partial t} \Psi = u \frac{\partial^2}{\partial u^2} \Psi$$

$$i \frac{\partial}{\partial t} \overline{\Psi} = u \frac{\partial^2}{\partial u^2} \overline{\Psi}$$

Hopf Functional Approach

$$\frac{dx}{dt} = x^2$$

$$\Psi(t, u) \equiv e^{iux(t)}$$

$$i \frac{\partial}{\partial t} \Psi = u \frac{\partial^2}{\partial u^2} \Psi$$

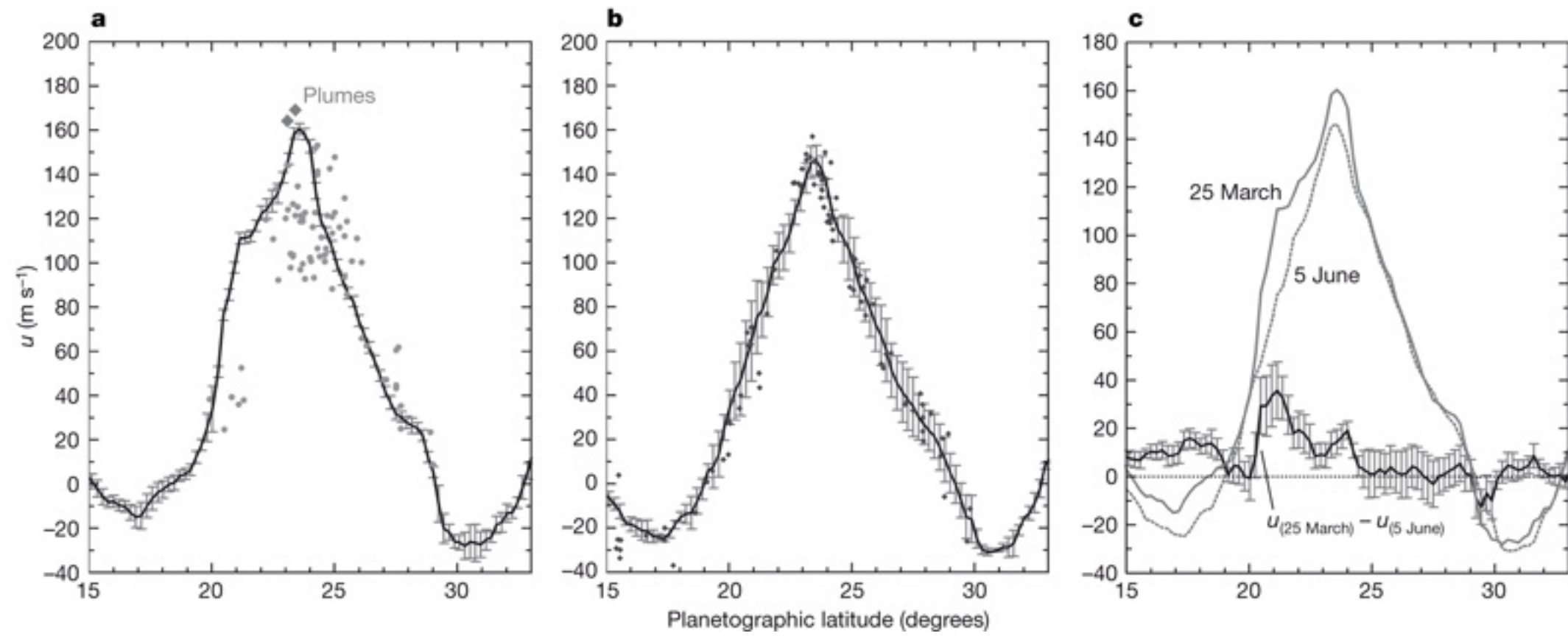
$$i \frac{\partial}{\partial t} \overline{\Psi} = u \frac{\partial^2}{\partial u^2} \overline{\Psi}$$

$$\hat{H} \overline{\Psi}_0 = 0$$

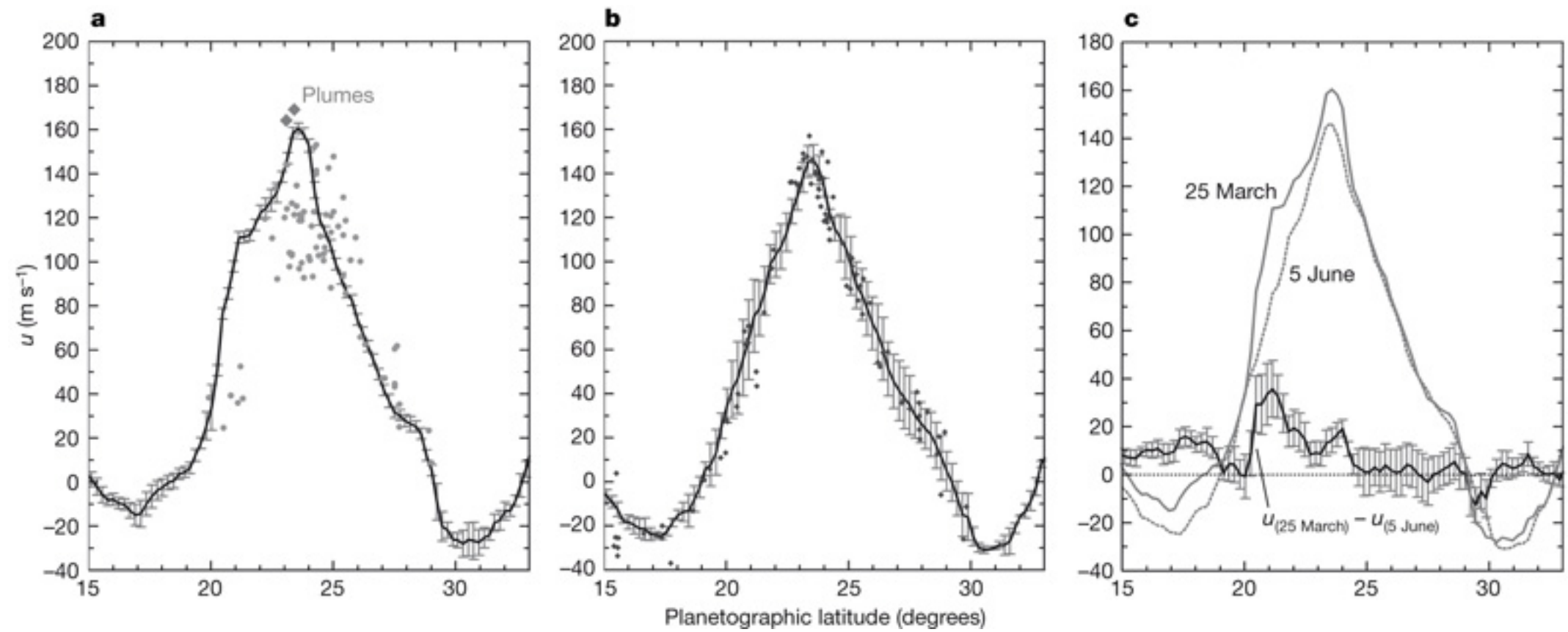
$$\overline{\Psi}_0(u) = \exp\left\{iu\langle x \rangle - \frac{1}{2!}u^2(\langle x^2 \rangle - \langle x \rangle^2) + \dots\right\}$$

$$\langle x \rangle = -i \frac{\partial \overline{\Psi}_0(u)}{\partial u} \Big|_{u=0}$$

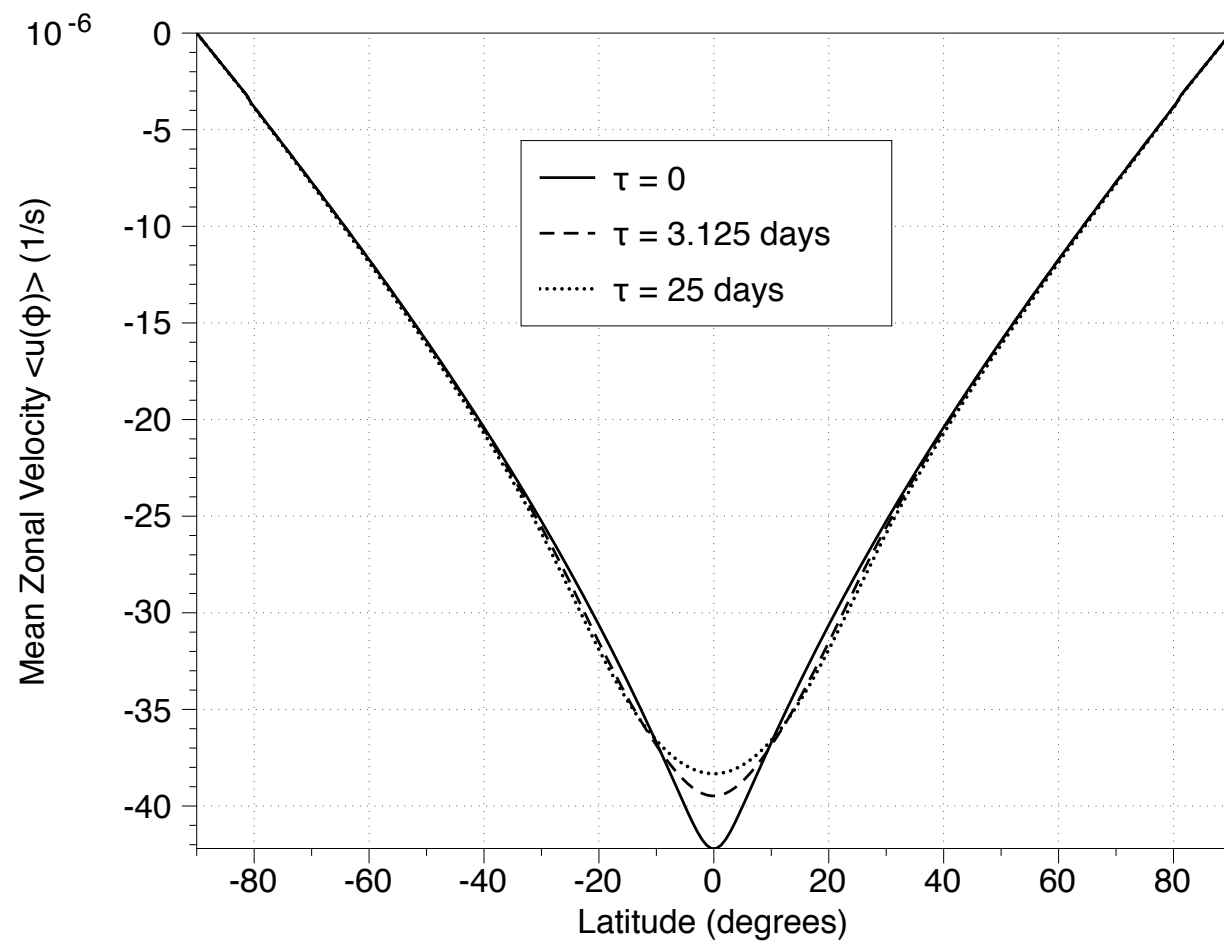


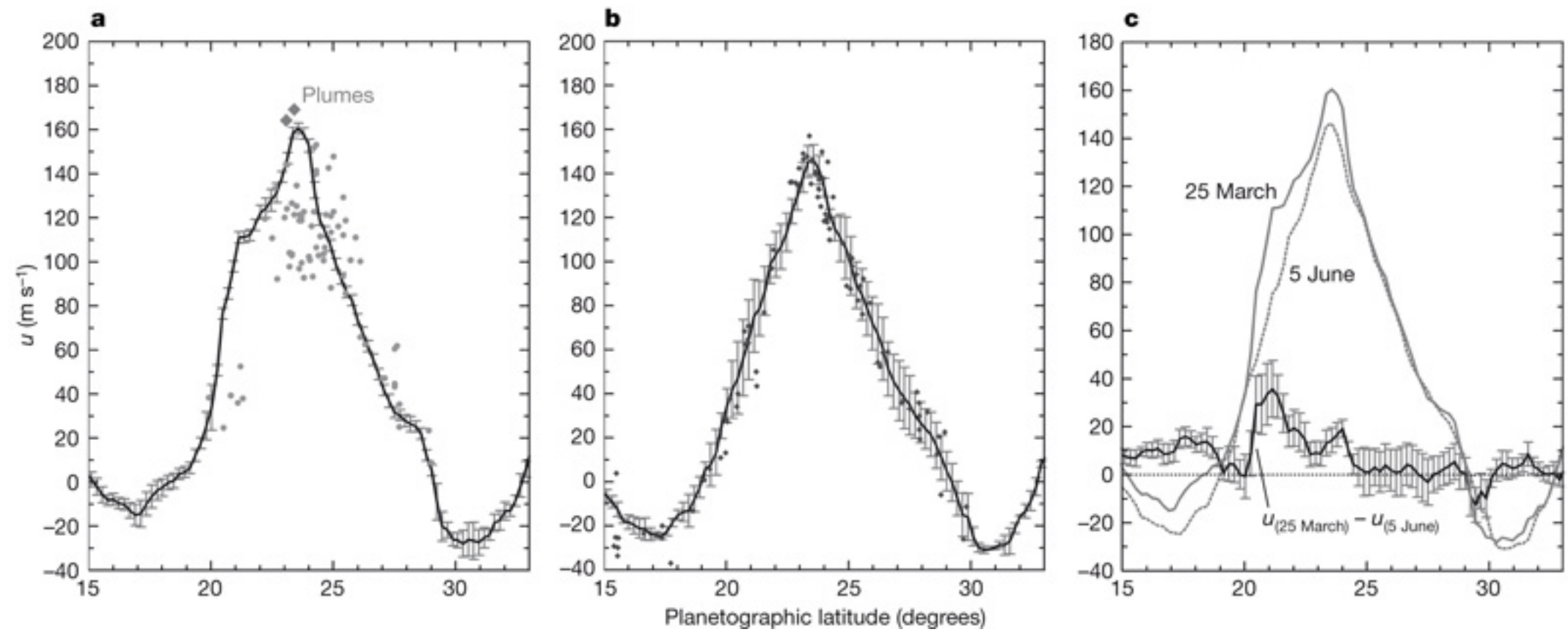


A. Sanchez-Lavega *et al.* Nature **451**, 437 (2008)

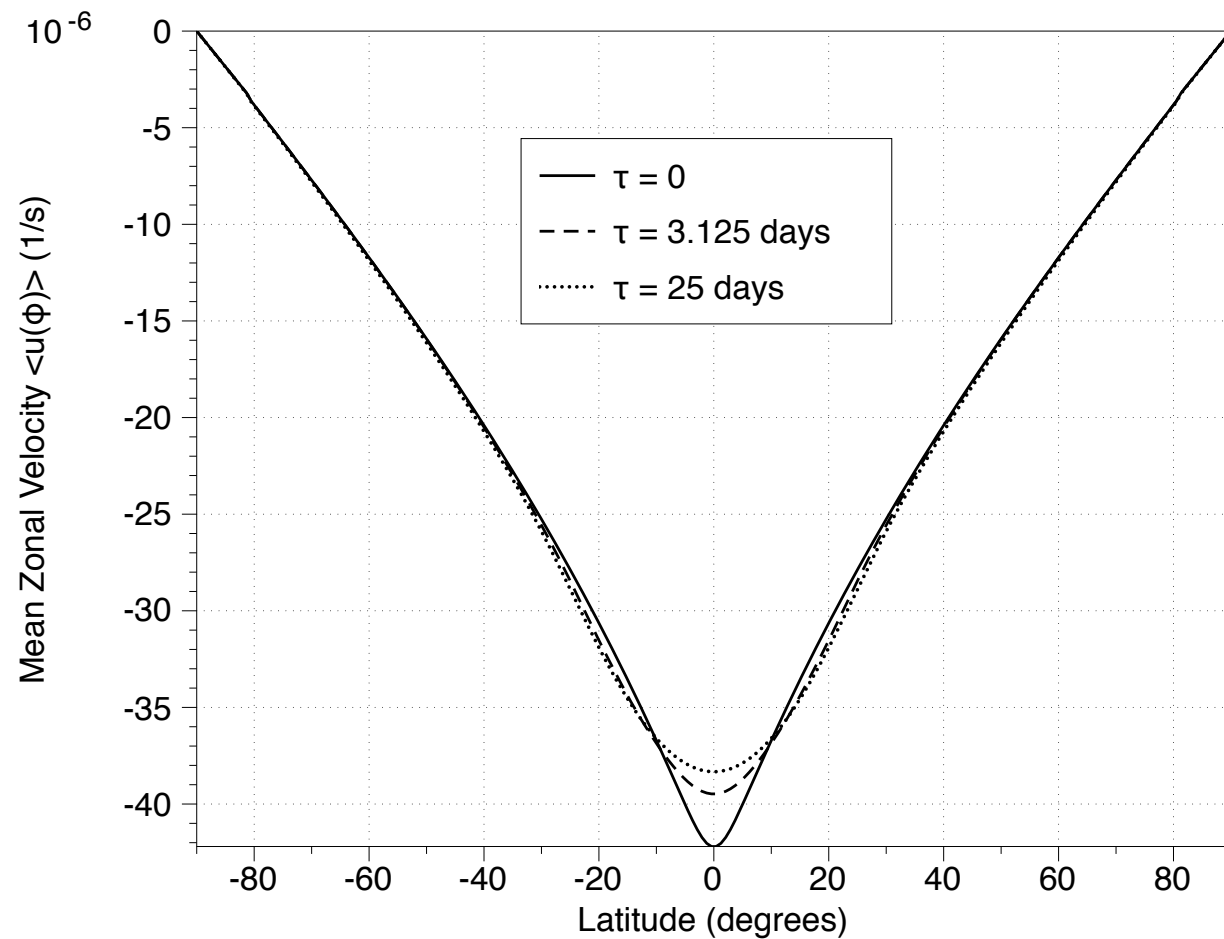


A. Sanchez-Lavega *et al.* Nature **451**, 437 (2008)





A. Sanchez-Lavega *et al.* Nature **451**, 437 (2008)



$$\frac{\partial q}{\partial t} + J[\psi, q] = \frac{q_{\text{jet}} - q}{\tau}$$

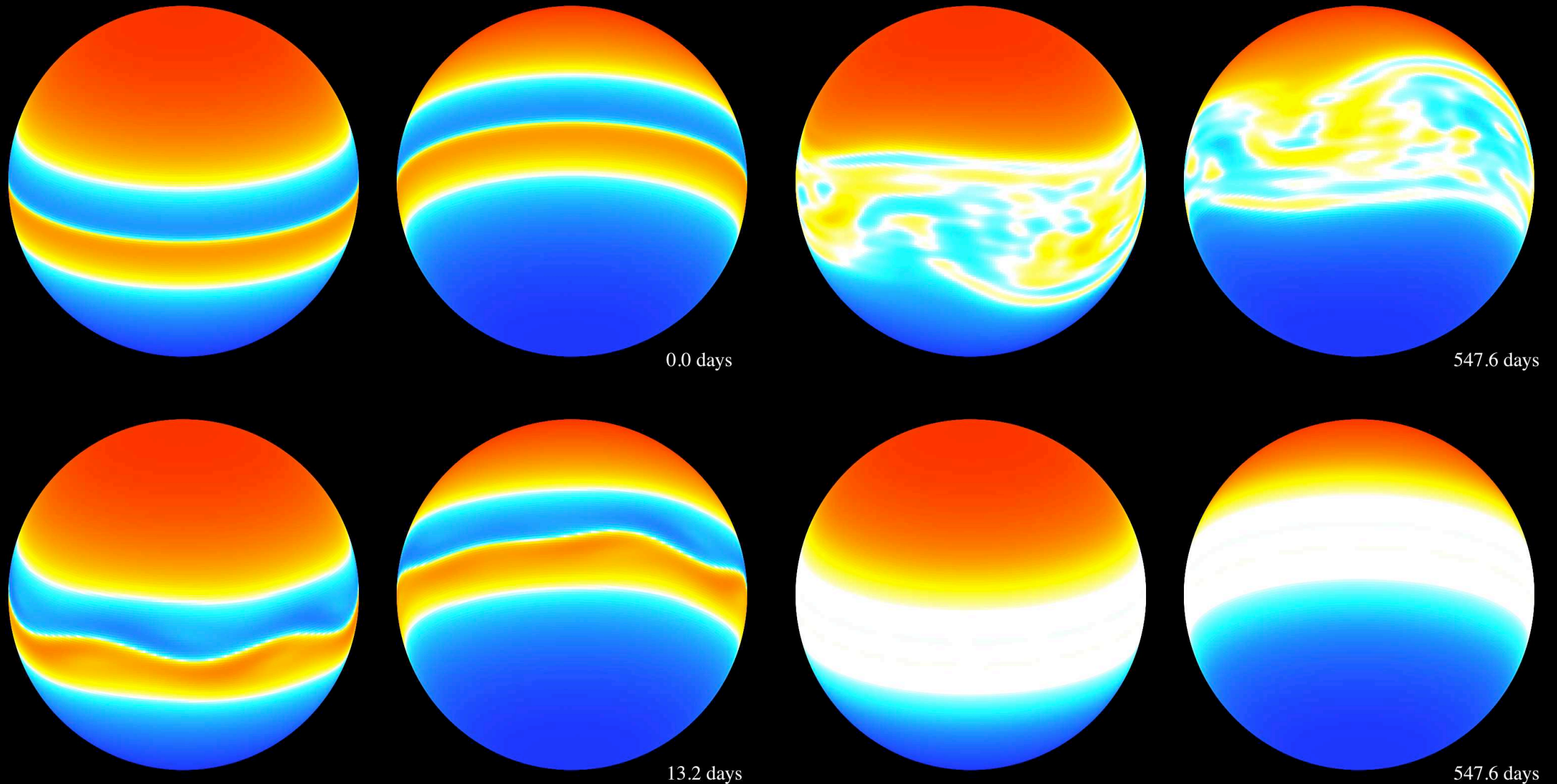
Direct Numerical Simulation of Jet

jet relaxation time = 25 days

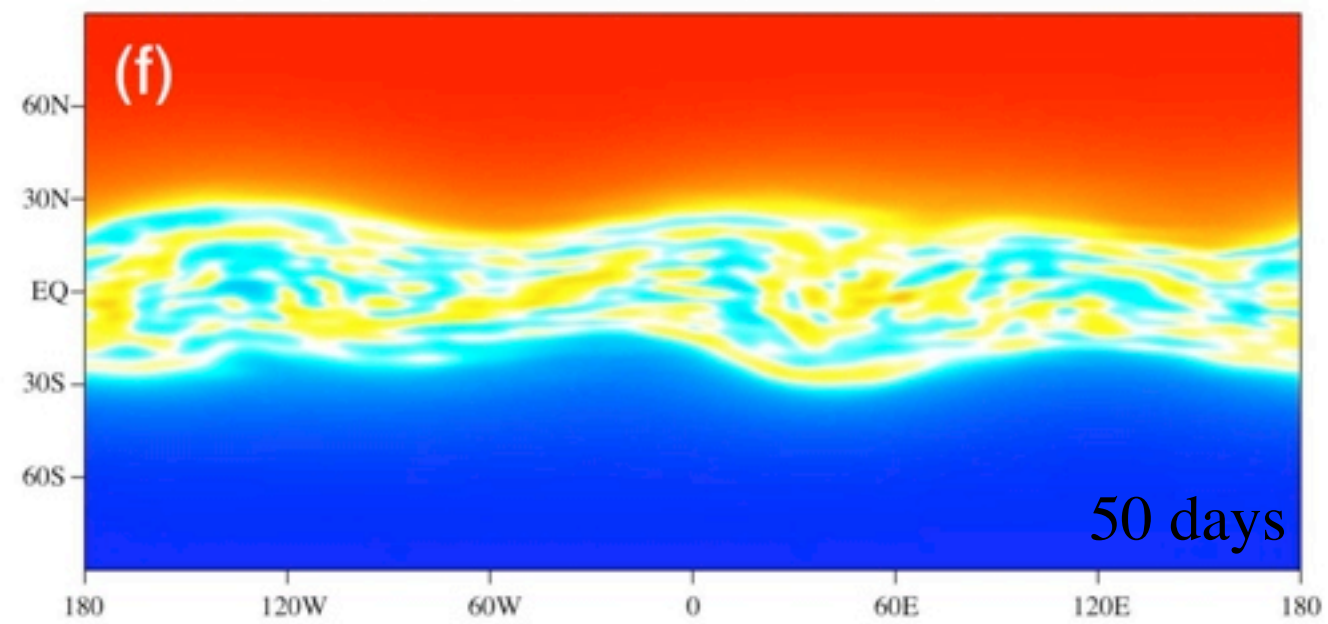
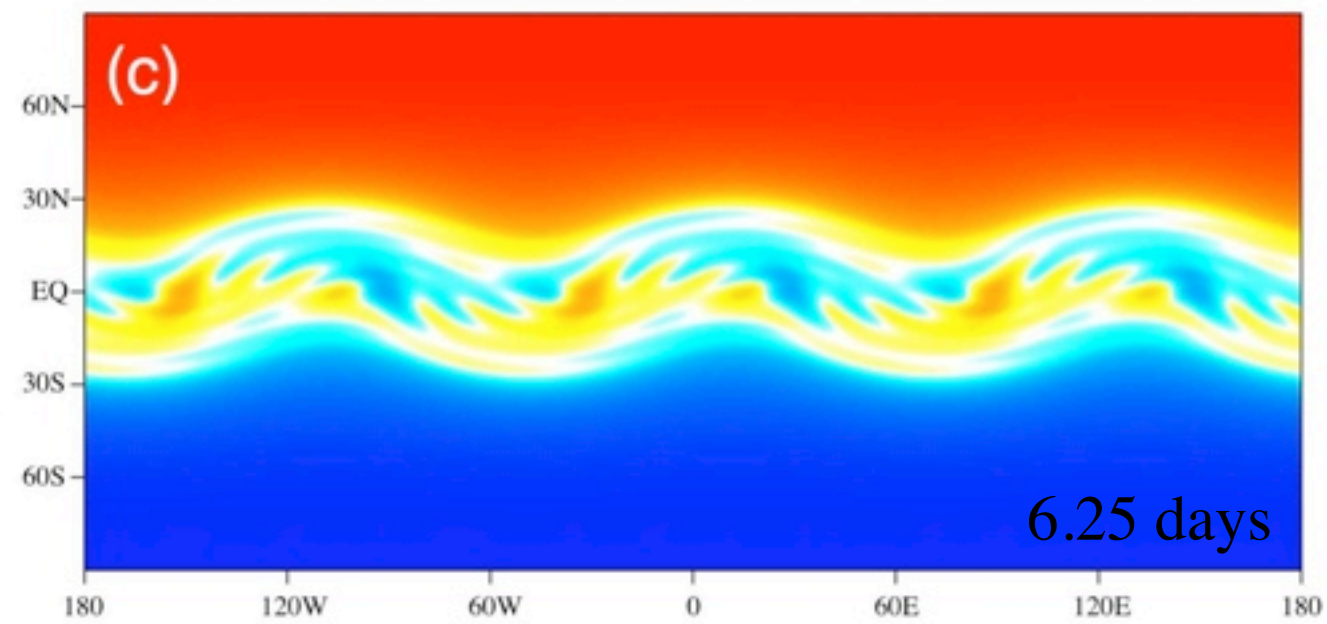
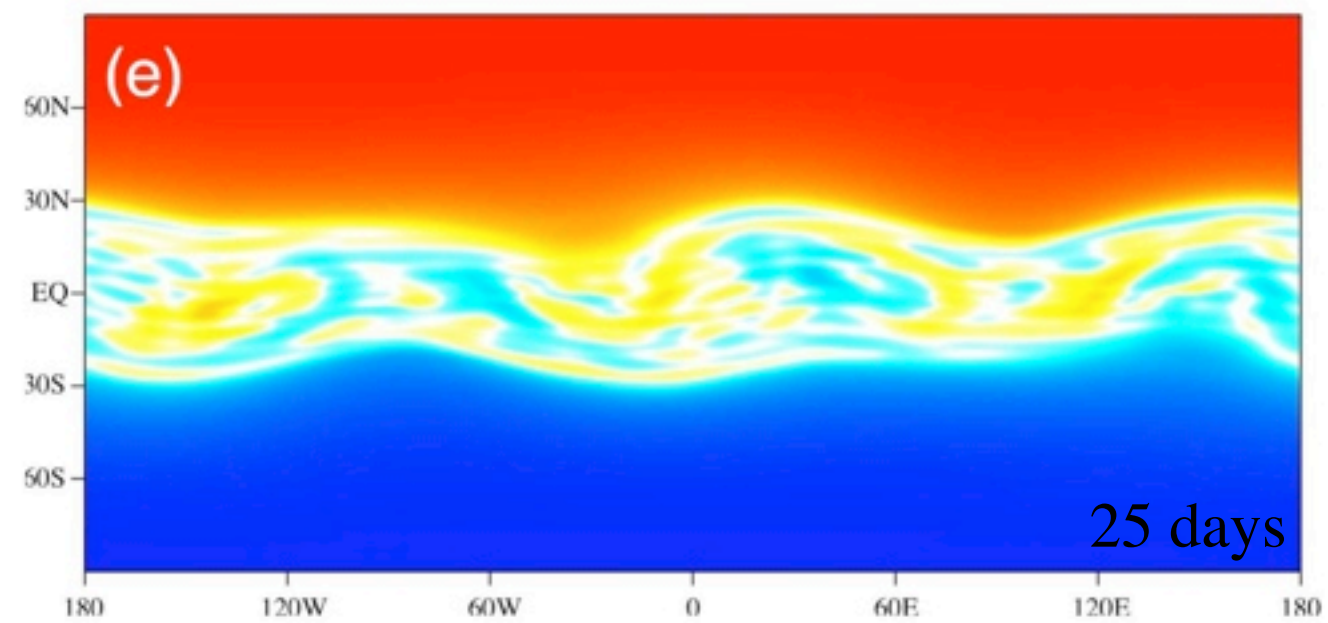
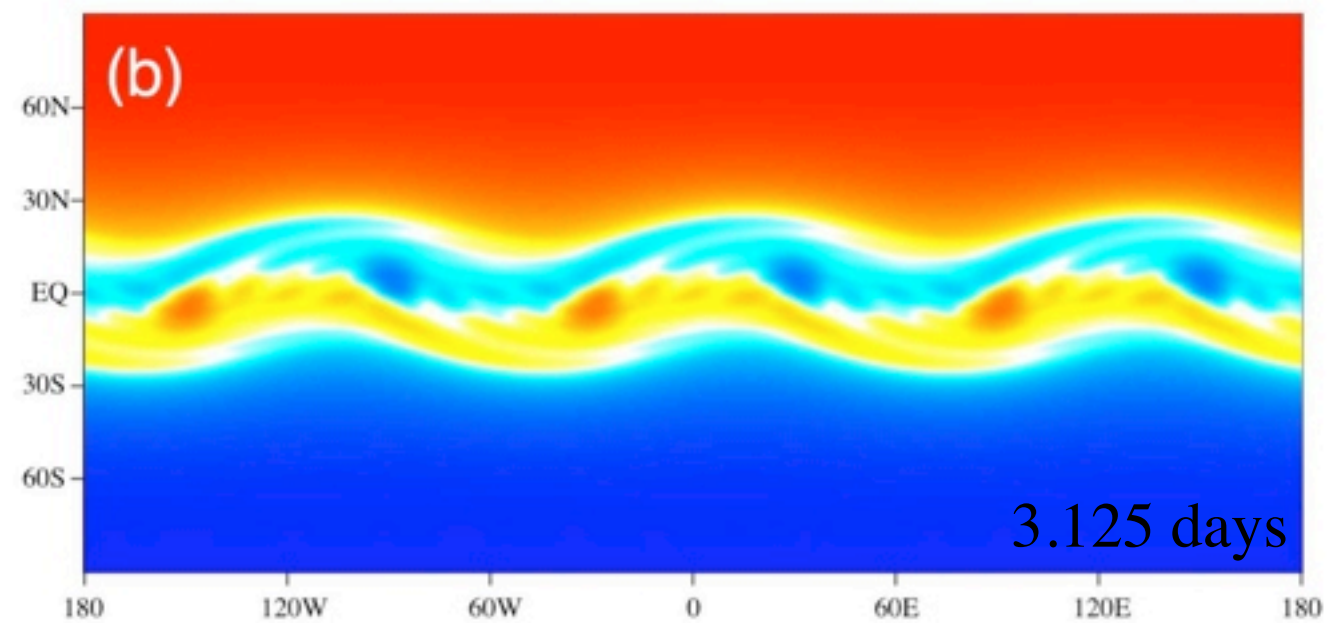
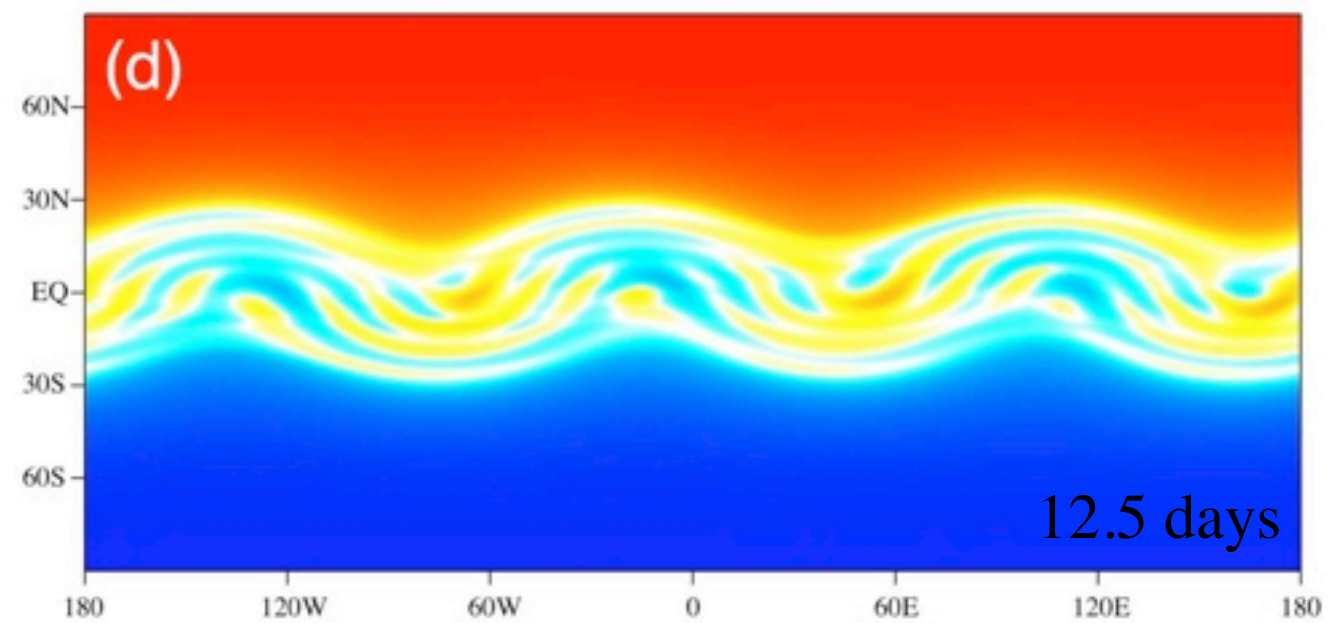
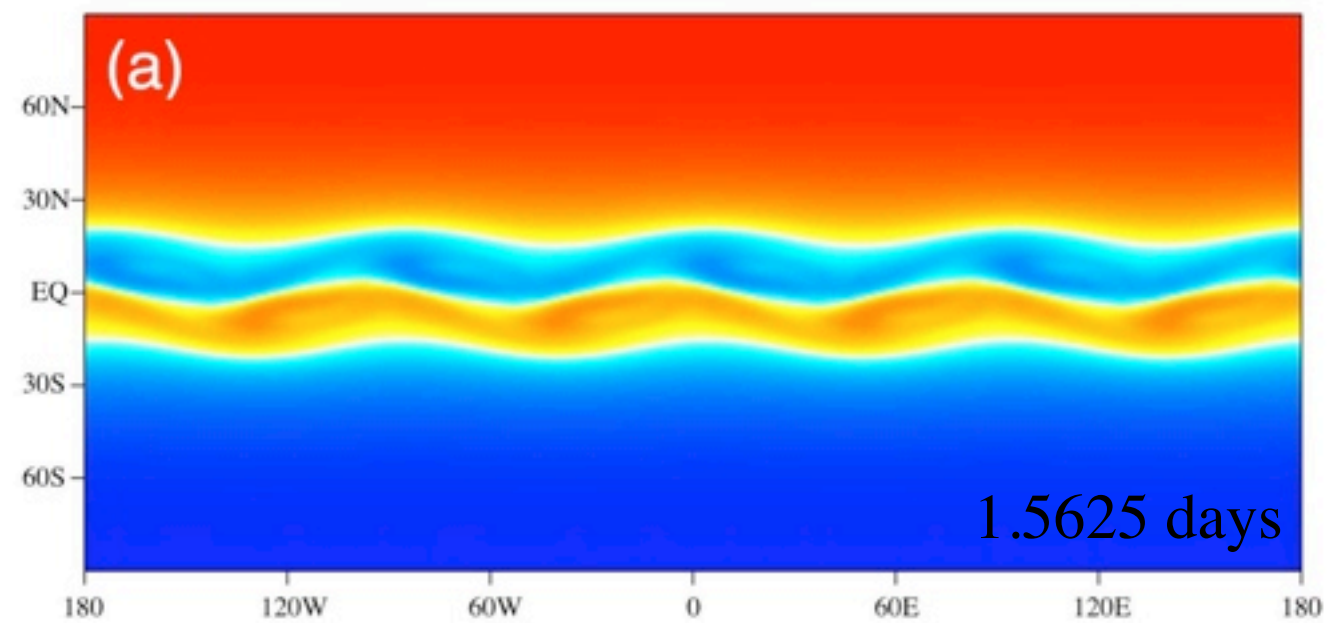
J. B. M, E. Conover, and T. Schneider, J. Atmos. Sci. **65**, 1955 (2008)

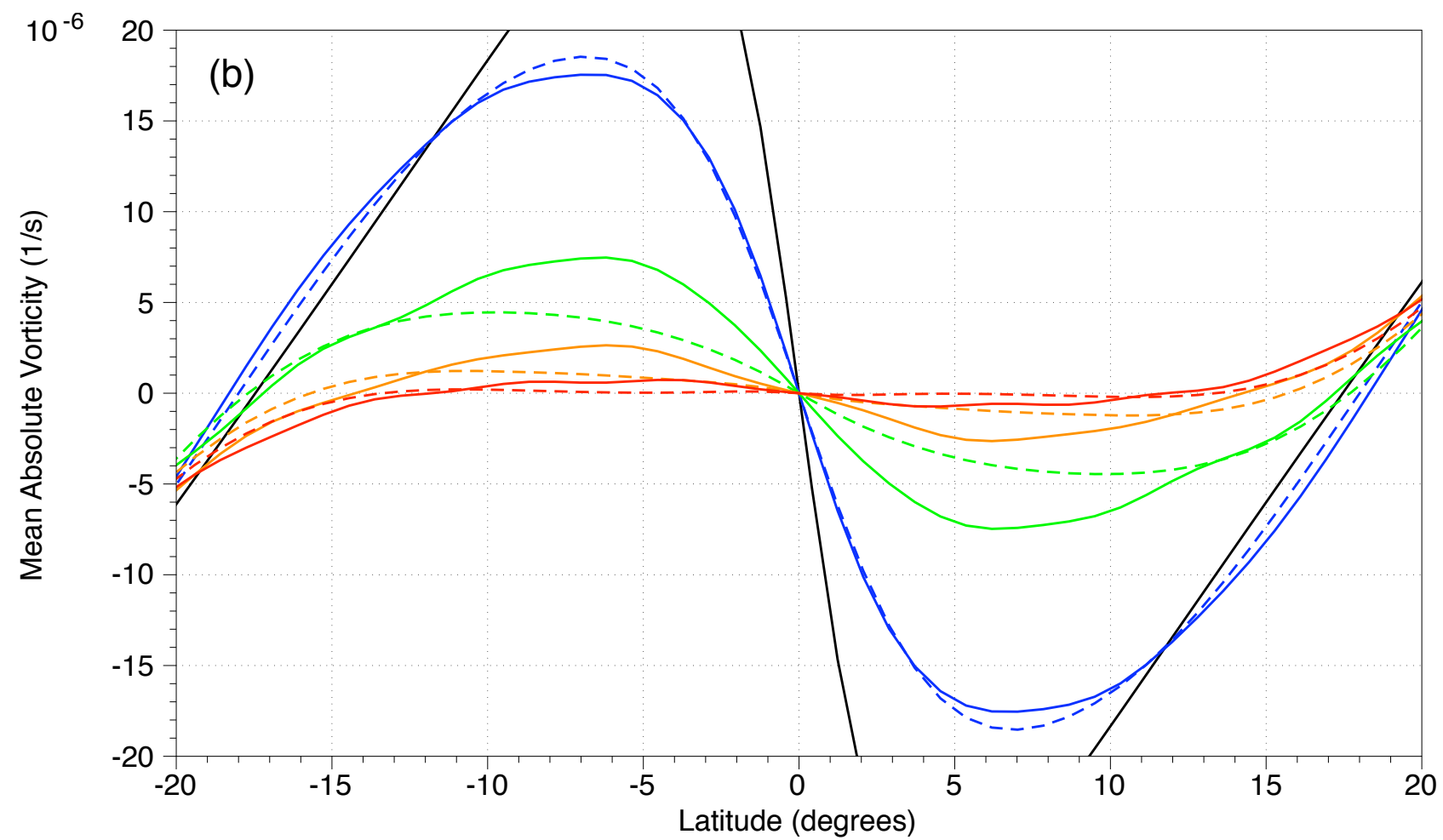
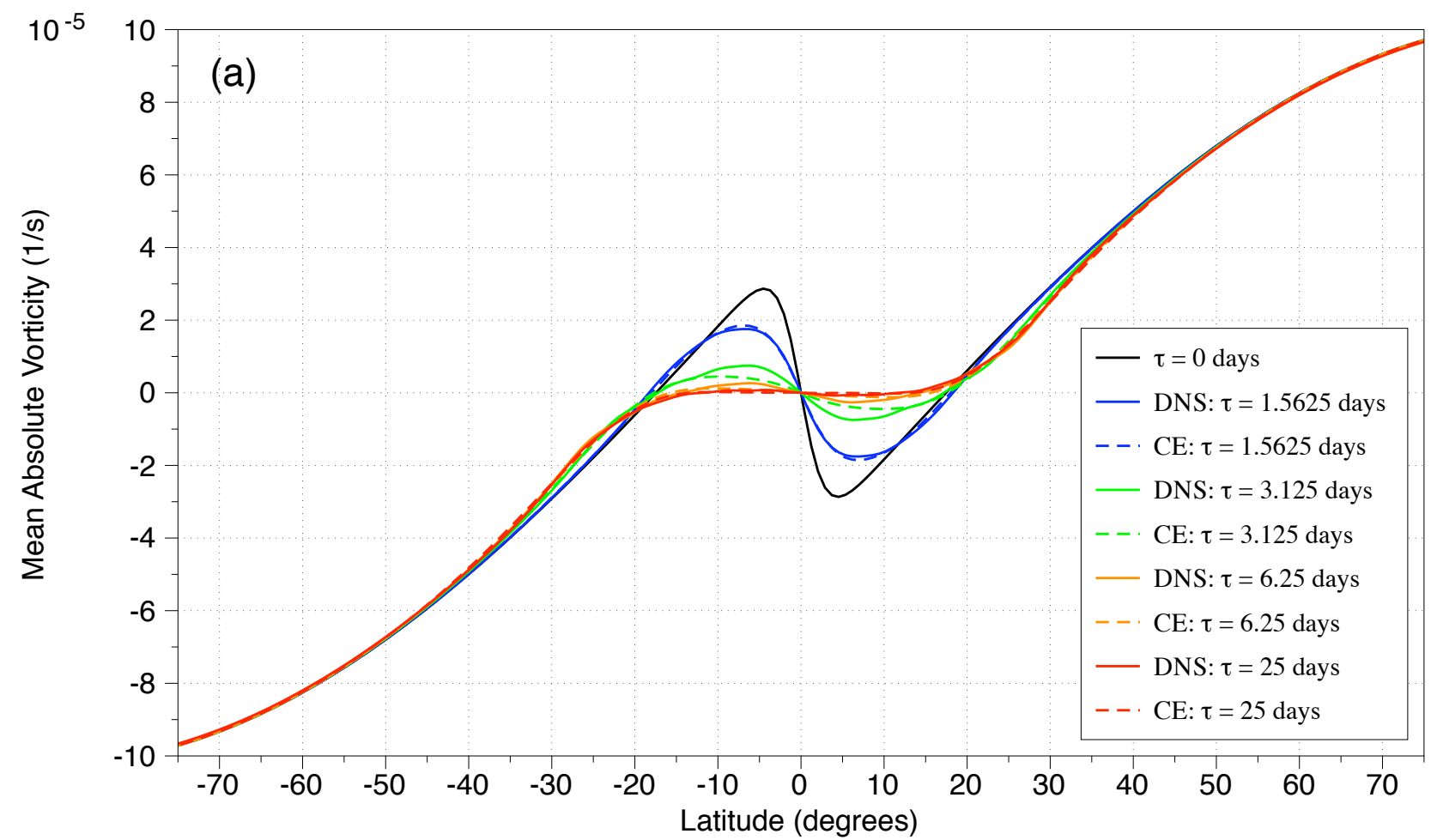
Direct Numerical Simulation of Jet

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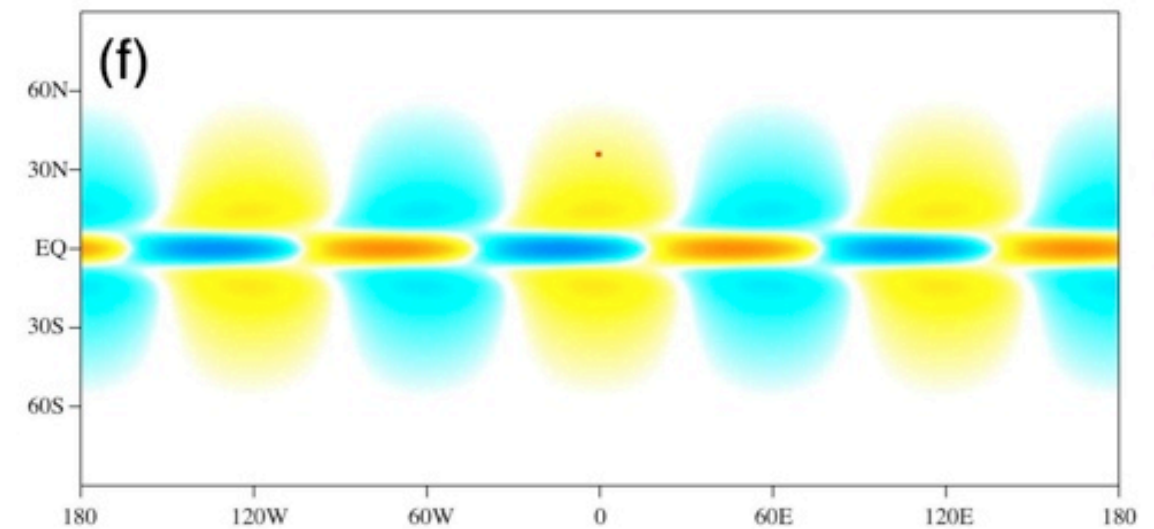
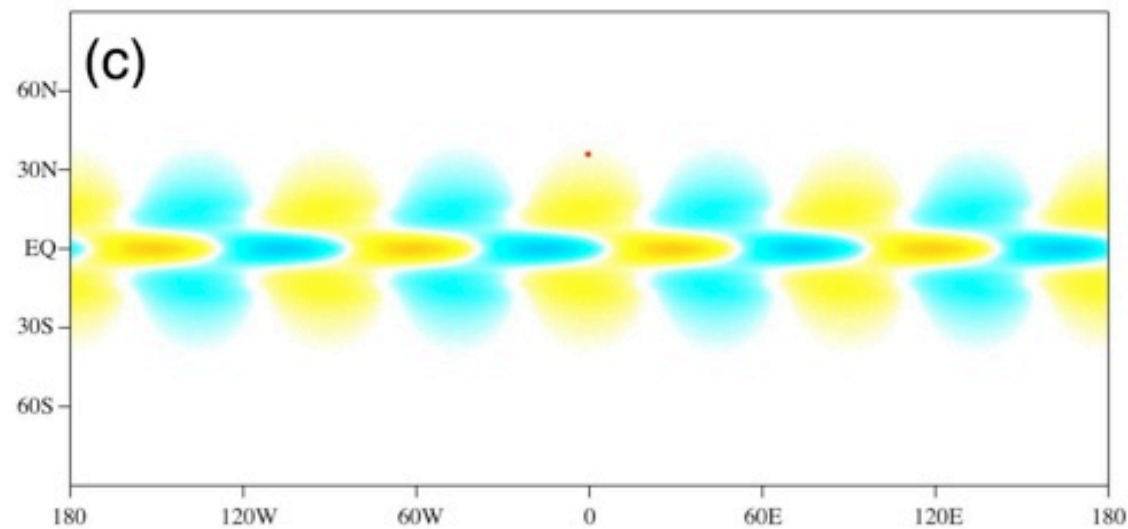
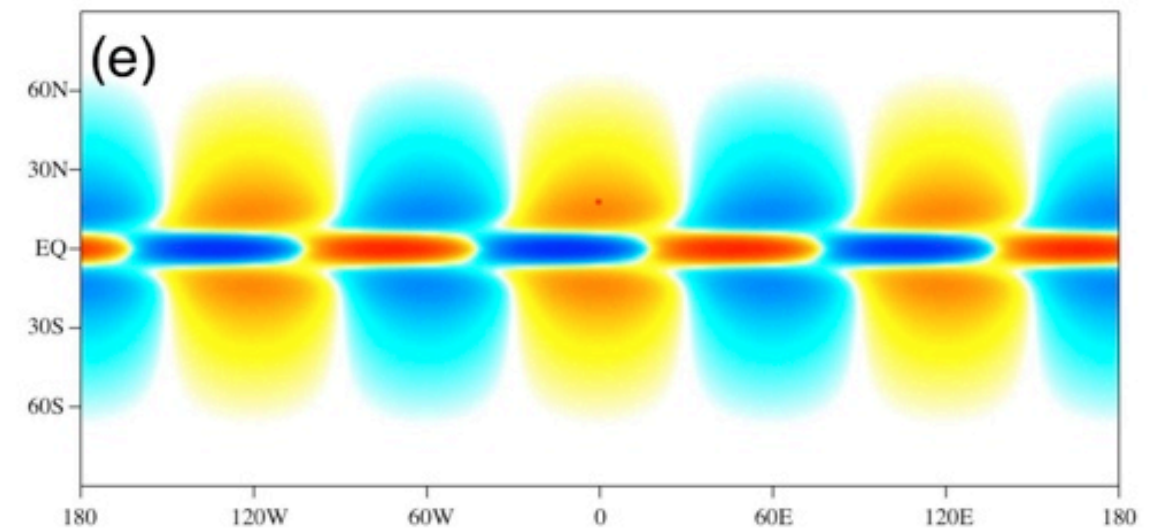
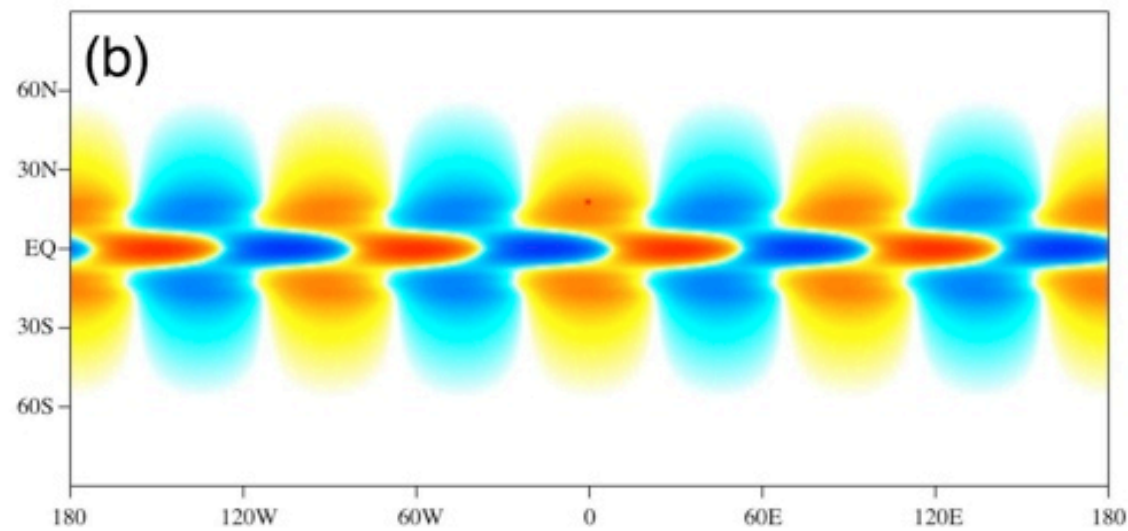
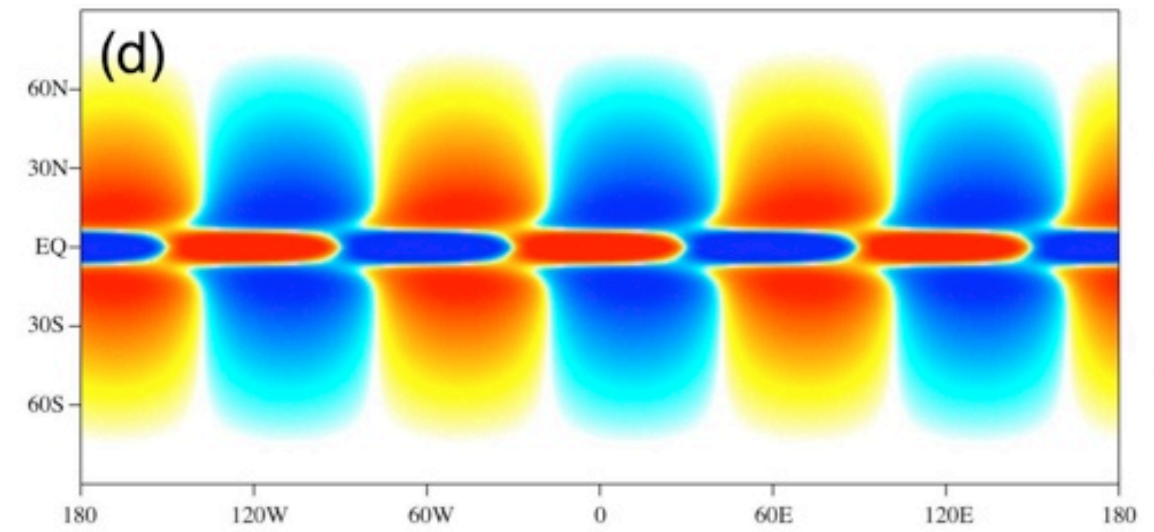
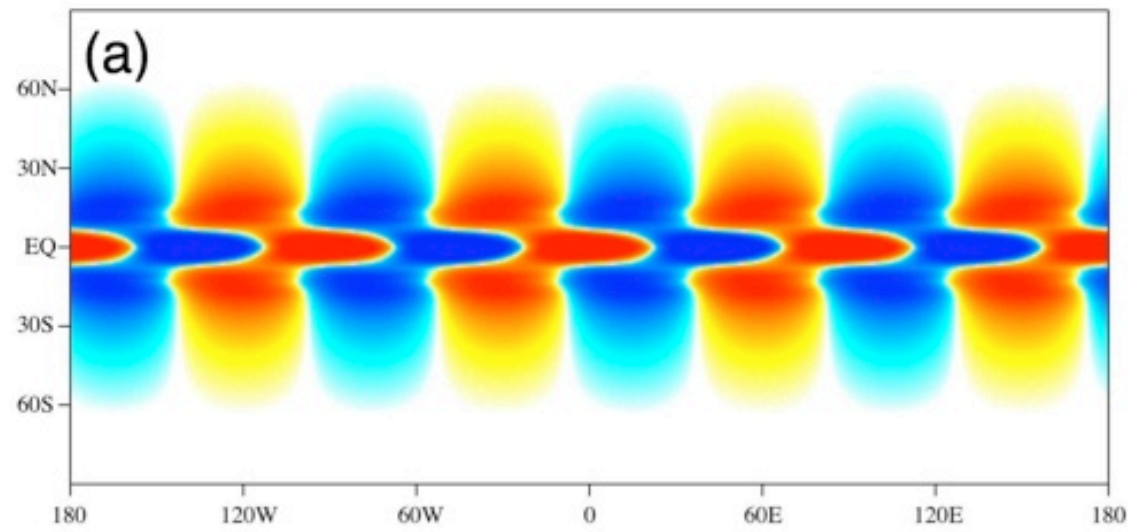


J. B. M, E. Conover, and T. Schneider, J. Atmos. Sci. **65**, 1955 (2008)

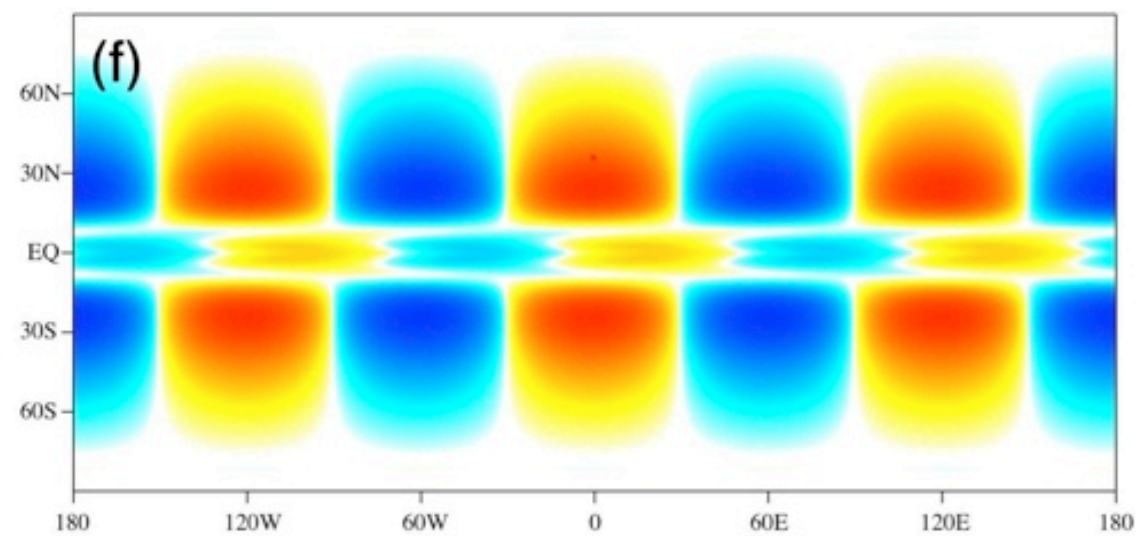
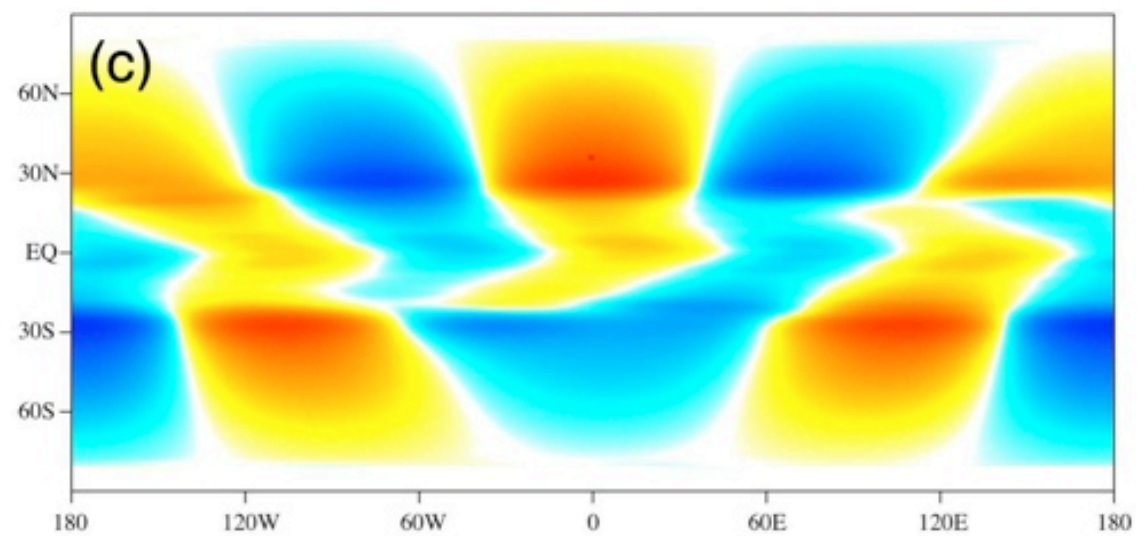
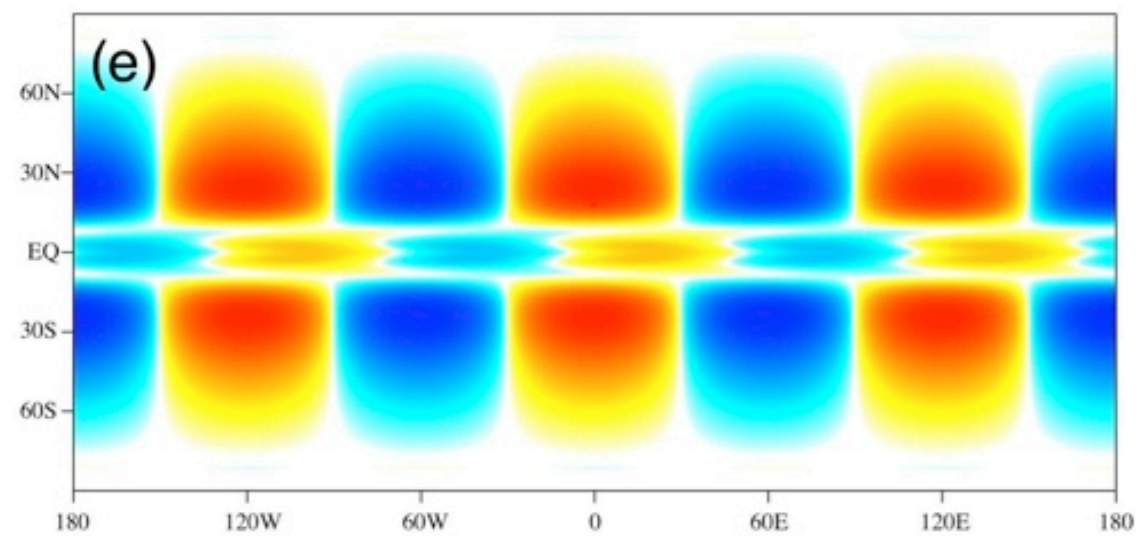
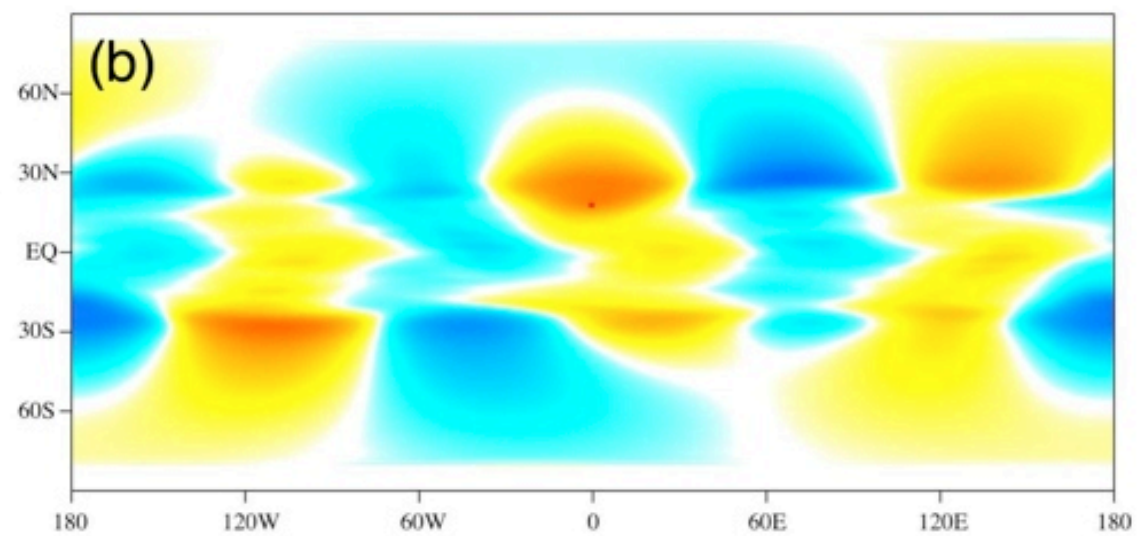
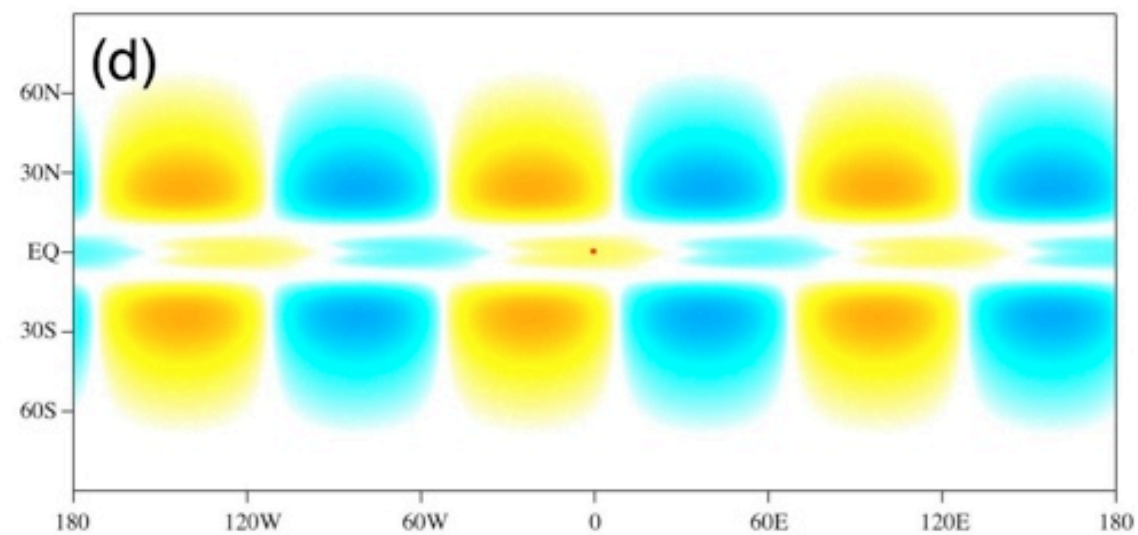
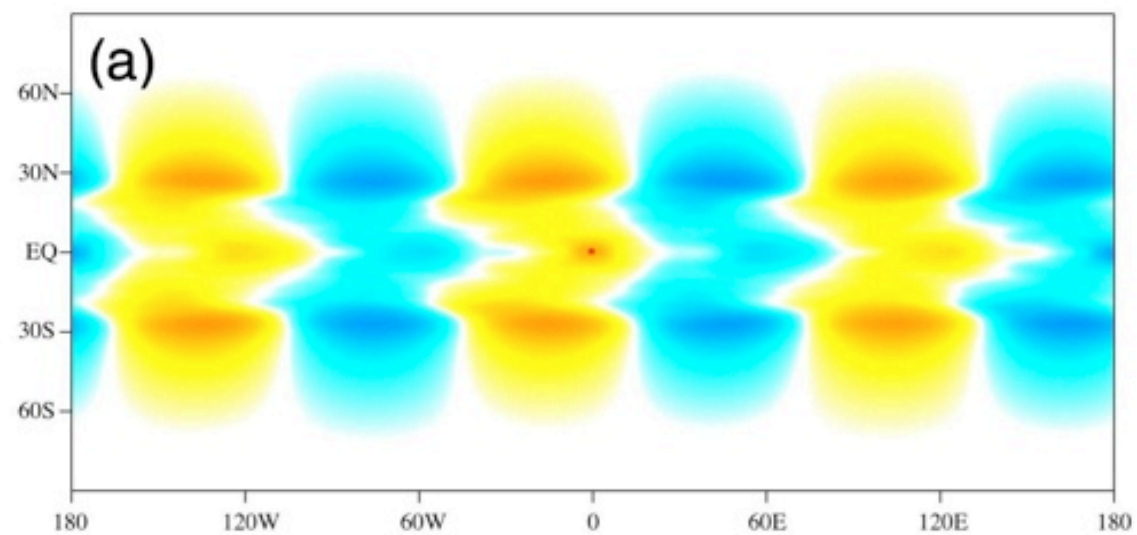




2nd Cumulant = 2-point Correlation Function

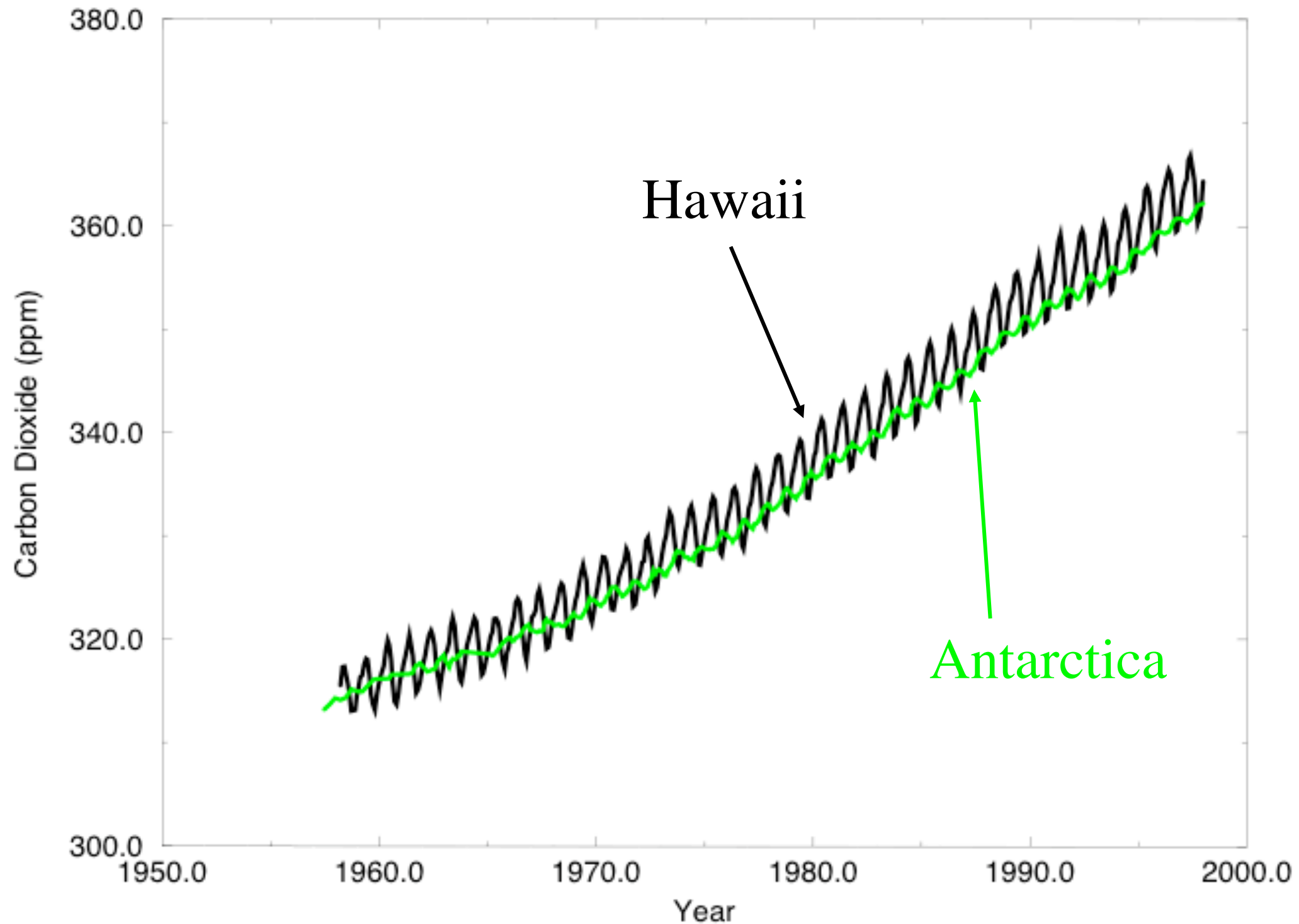


25 days



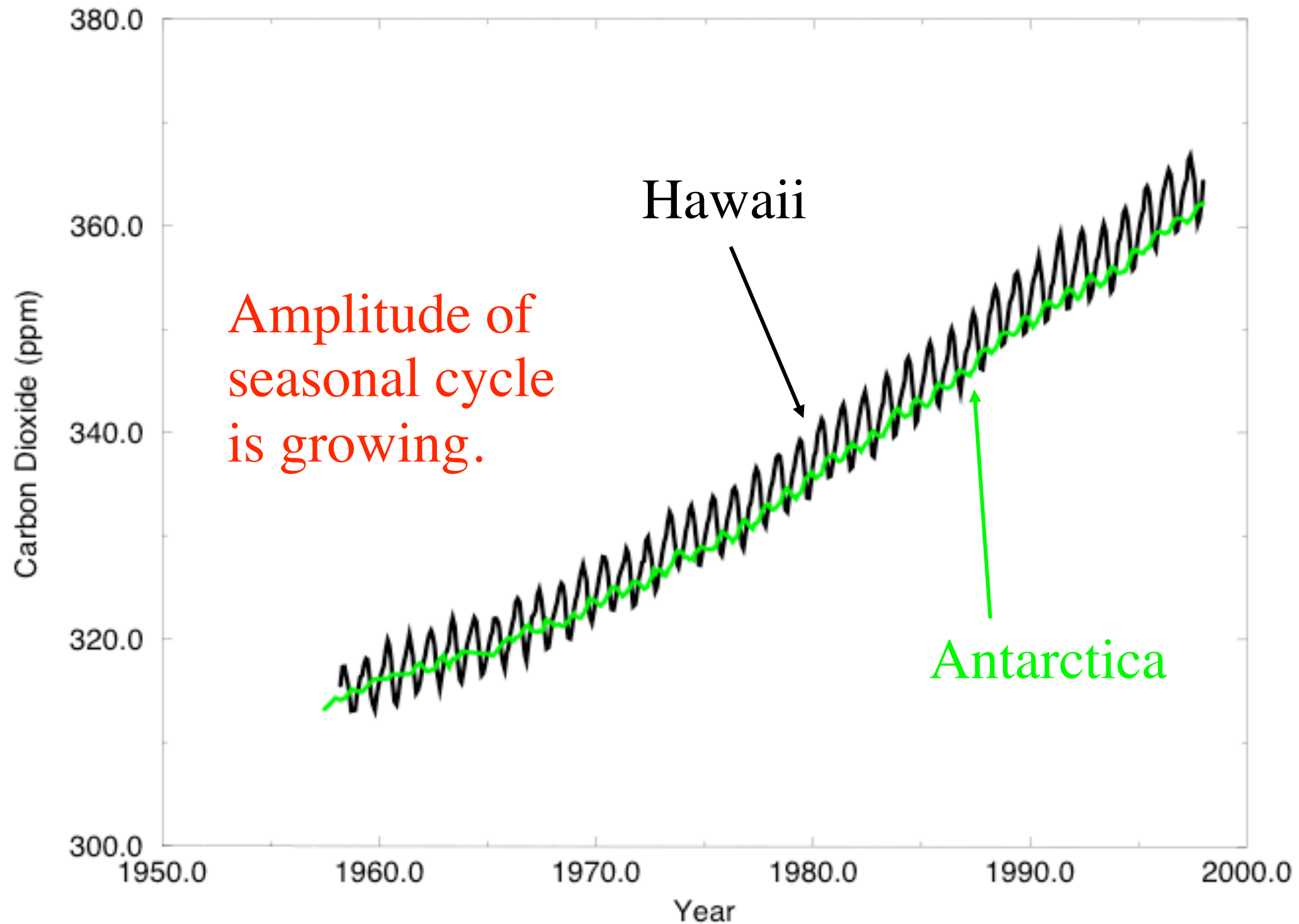
Ecosystems & Feedbacks

Mauna Loa and Antarctic Carbon Dioxide

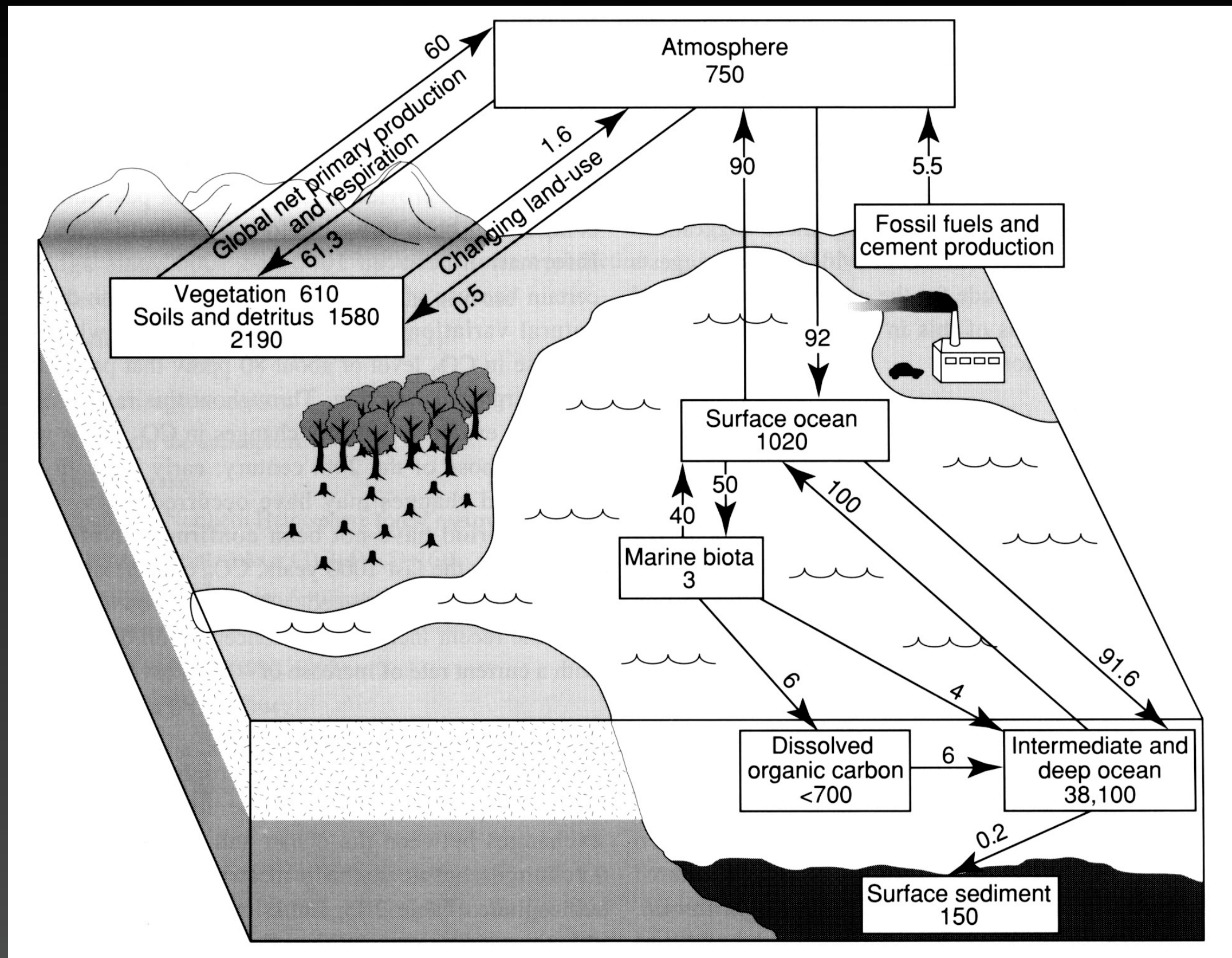


Ecosystems & Feedbacks

Mauna Loa and Antarctic Carbon Dioxide



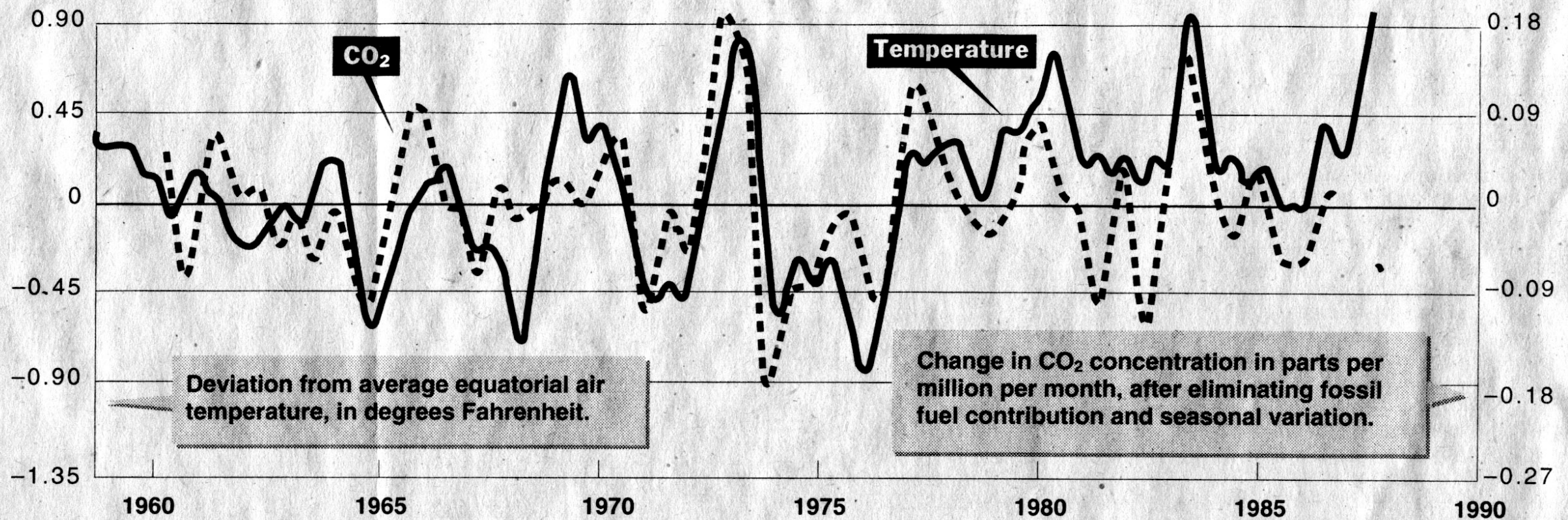
Vast Reservoirs of Carbon & Enormous Fluxes



Source: *Climate Change 1995*

Temperature and CO₂, Moving in Tandem

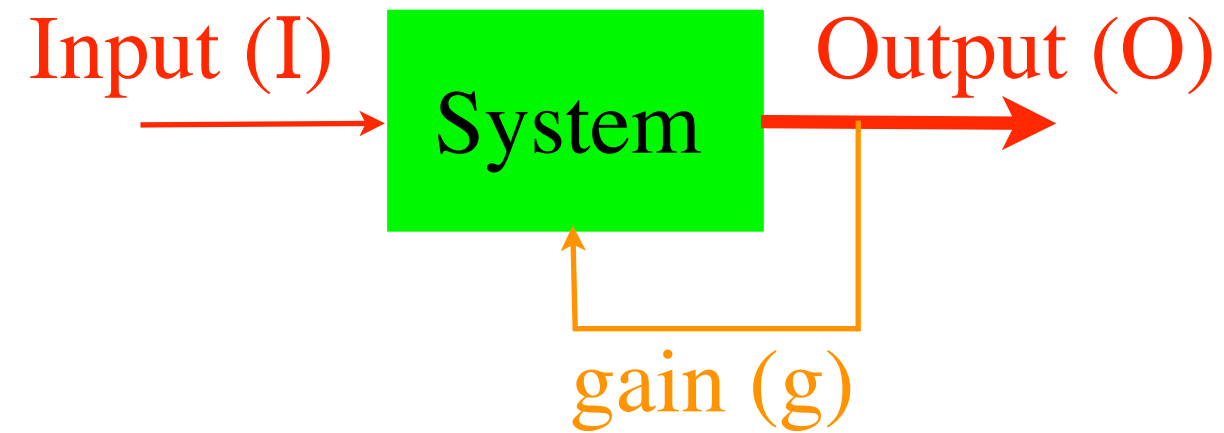
Research results indicate a strong correlation between variations in temperature and variations in atmospheric carbon dioxide concentration. Some scientists say that the temperature increases often precede the carbon dioxide rises, meaning that warming could build on itself to create further warming.



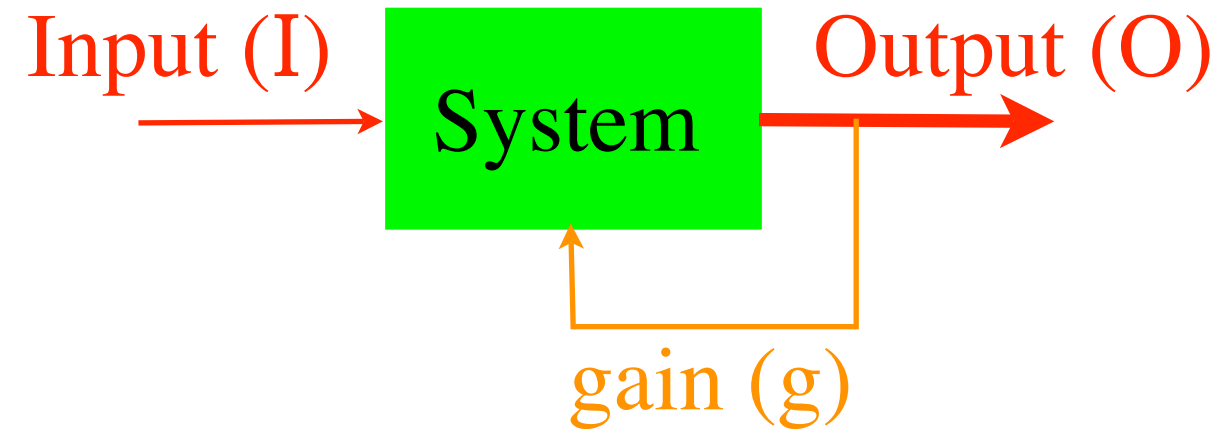
Sources: Dr. Michael Oppenheimer, and Dr. J.B. Marston

J. B. Marston, M. Oppenheimer, R. M. Fujita, and S. R. Gaffin, "CO₂ and temperature" *Nature* **349**, 573 (1991).

Physics of Feedbacks



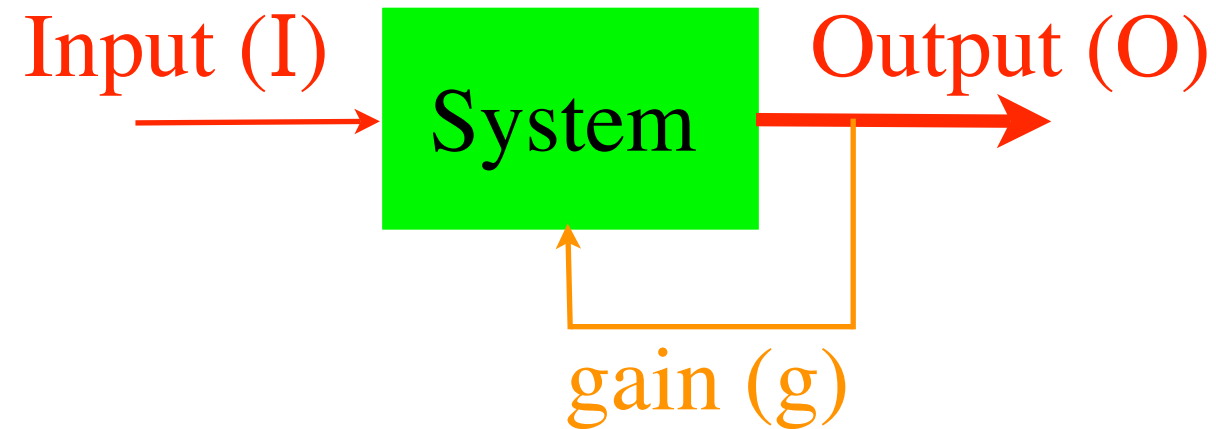
Physics of Feedbacks



$$\begin{aligned}\mathcal{O} &= \mathcal{I} + g\mathcal{I} + gg\mathcal{I} + \dots \\ &= \frac{\mathcal{I}}{1 - g} \quad \text{if } g < 1\end{aligned}$$

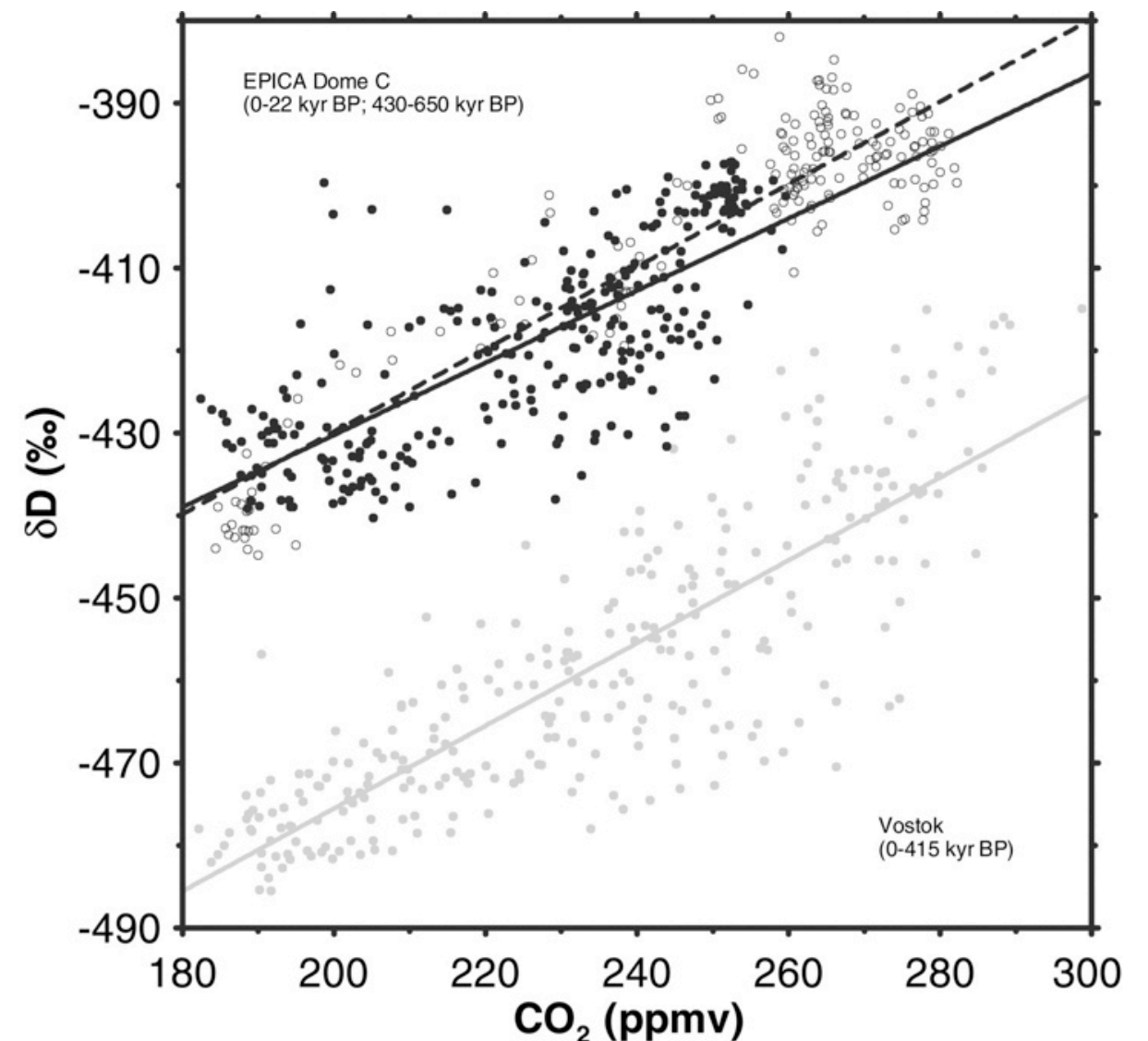
$$g = \sum_i \left(\frac{\partial T}{\partial p_i} \right) \left(\frac{\partial p_i}{\partial T} \right)$$

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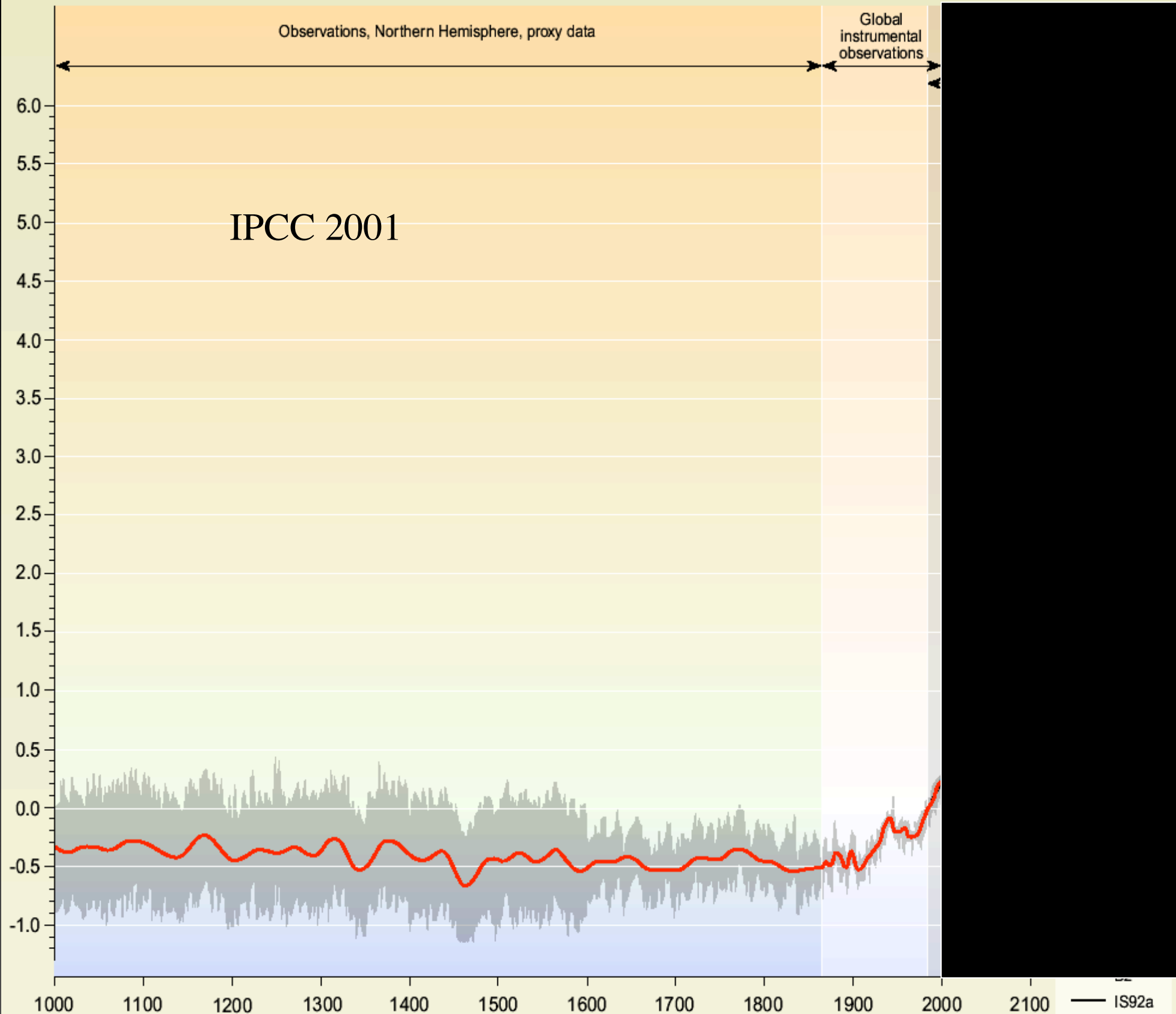
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$$\Delta T \approx 1^{\circ}\text{C} / (1 - 0.71) \approx 3.4^{\circ}\text{C}$$

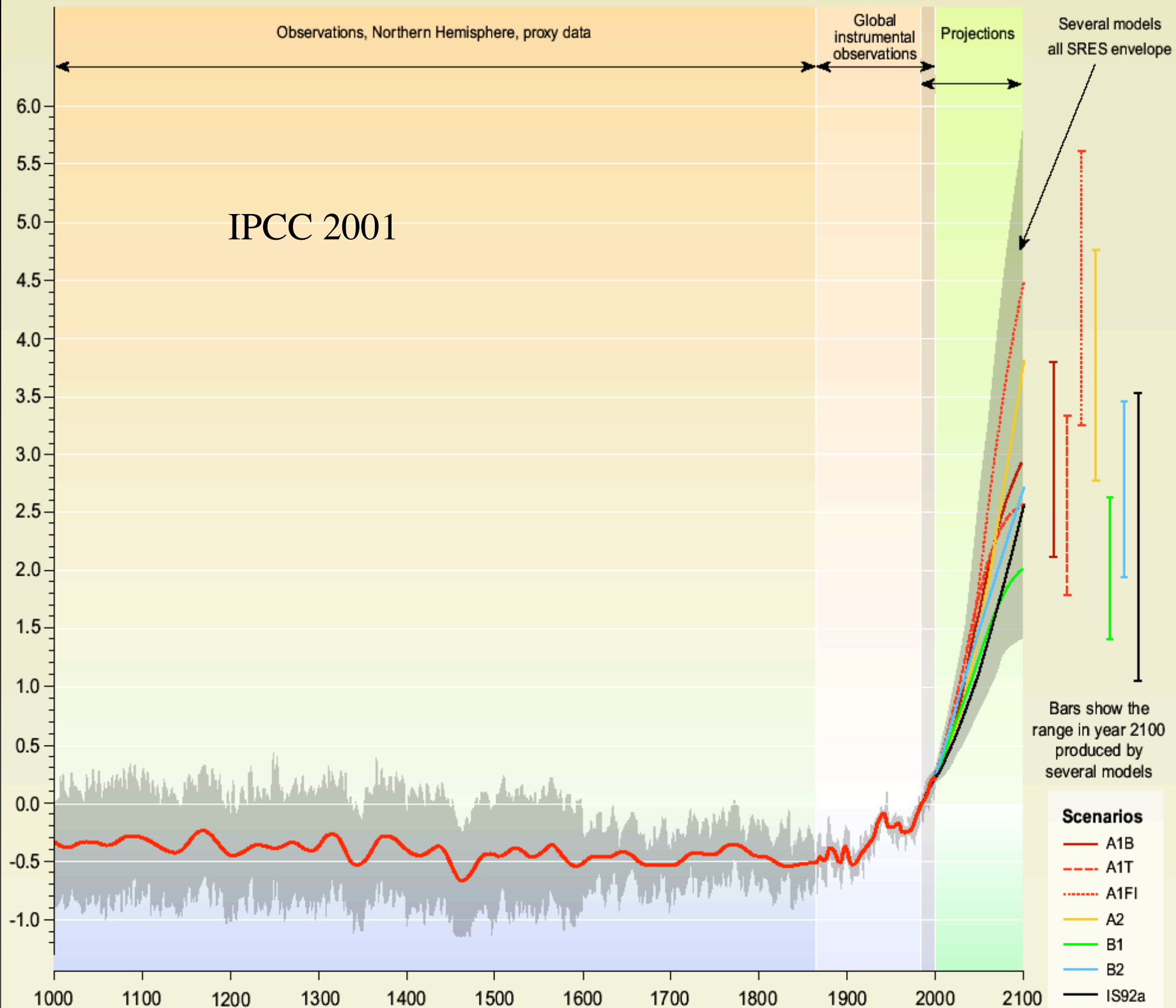
Variations of the Earth's surface temperature: years 1000 to 2100

Departures in temperature in °C (from the 1990 value)



Variations of the Earth's surface temperature: years 1000 to 2100

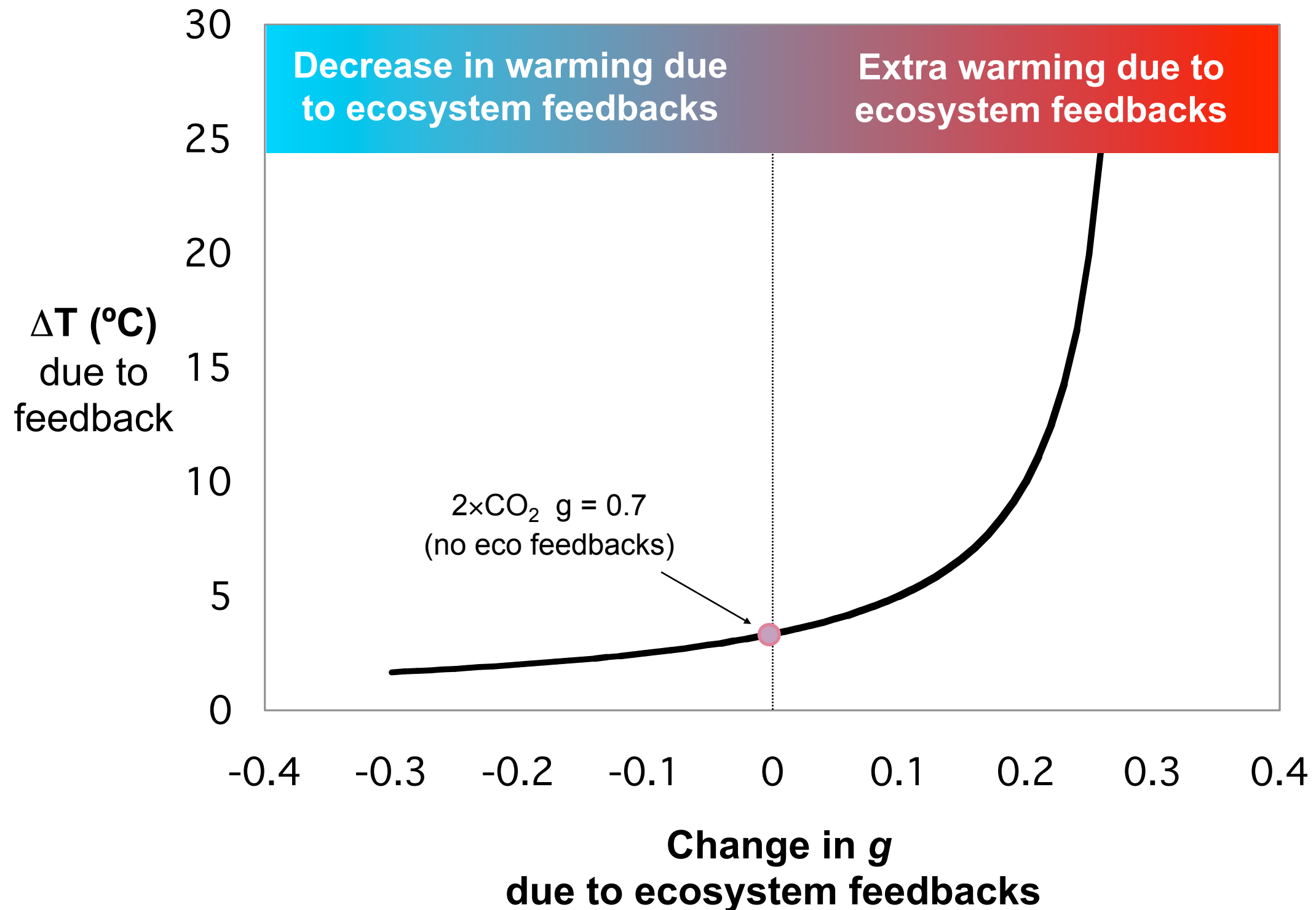
Departures in temperature in °C (from the 1990 value)



Global Carbon Cycle

Small change in g causes large ΔT

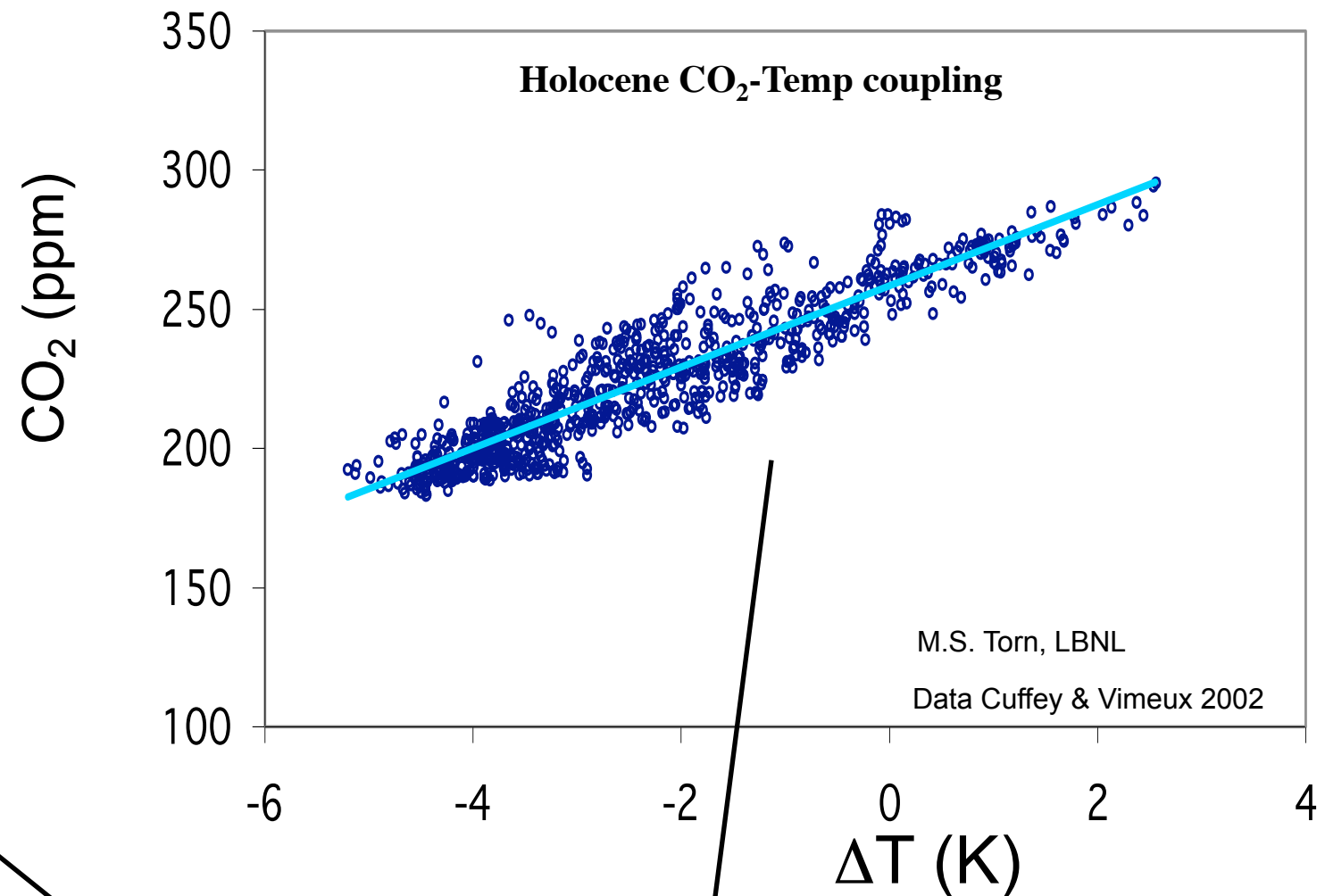
Asymmetries



An estimate of the contribution to g from Vostok core data:

Torn and Harte, GRL33,
L10703 (2006)

General
Circulation
Models

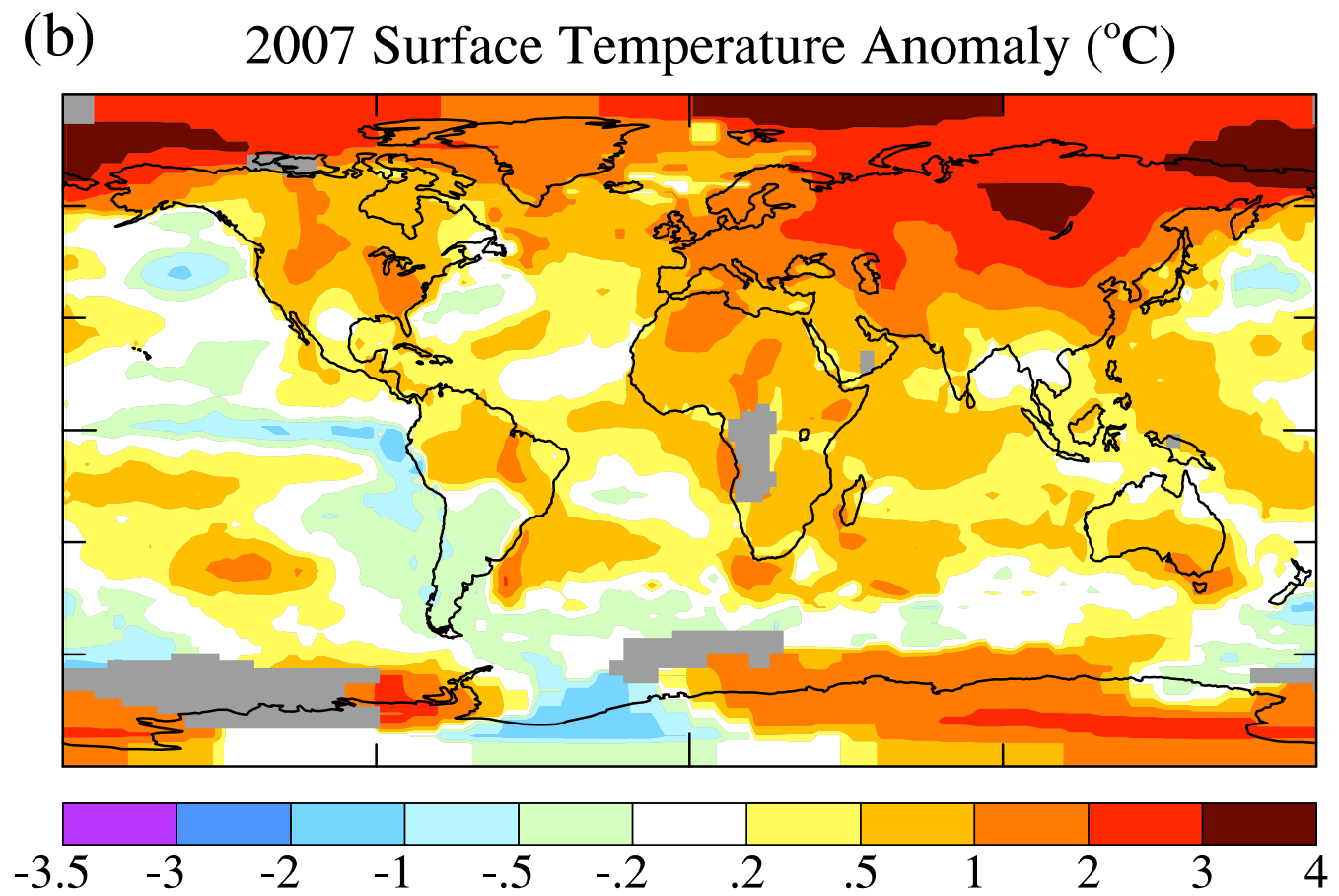
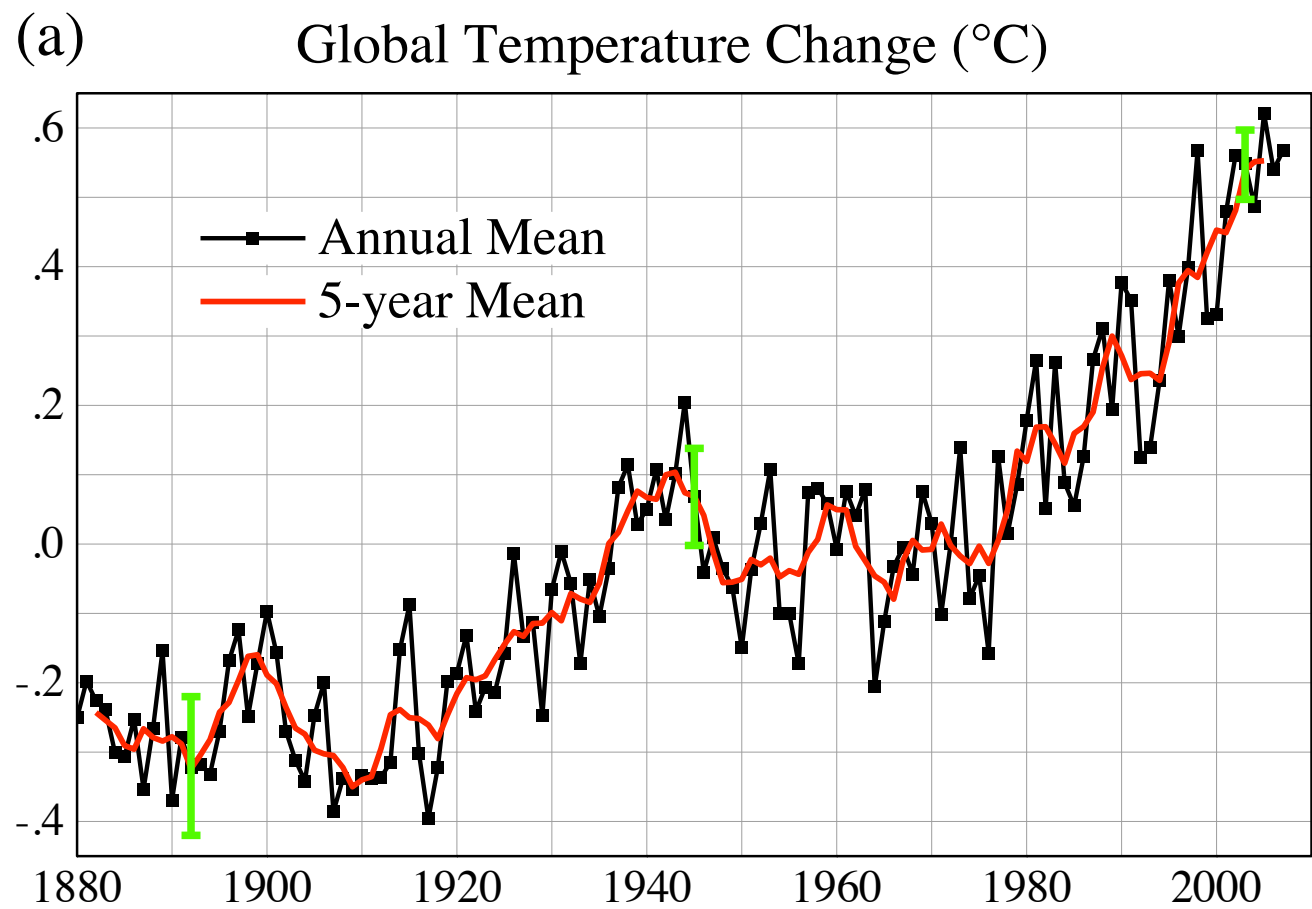


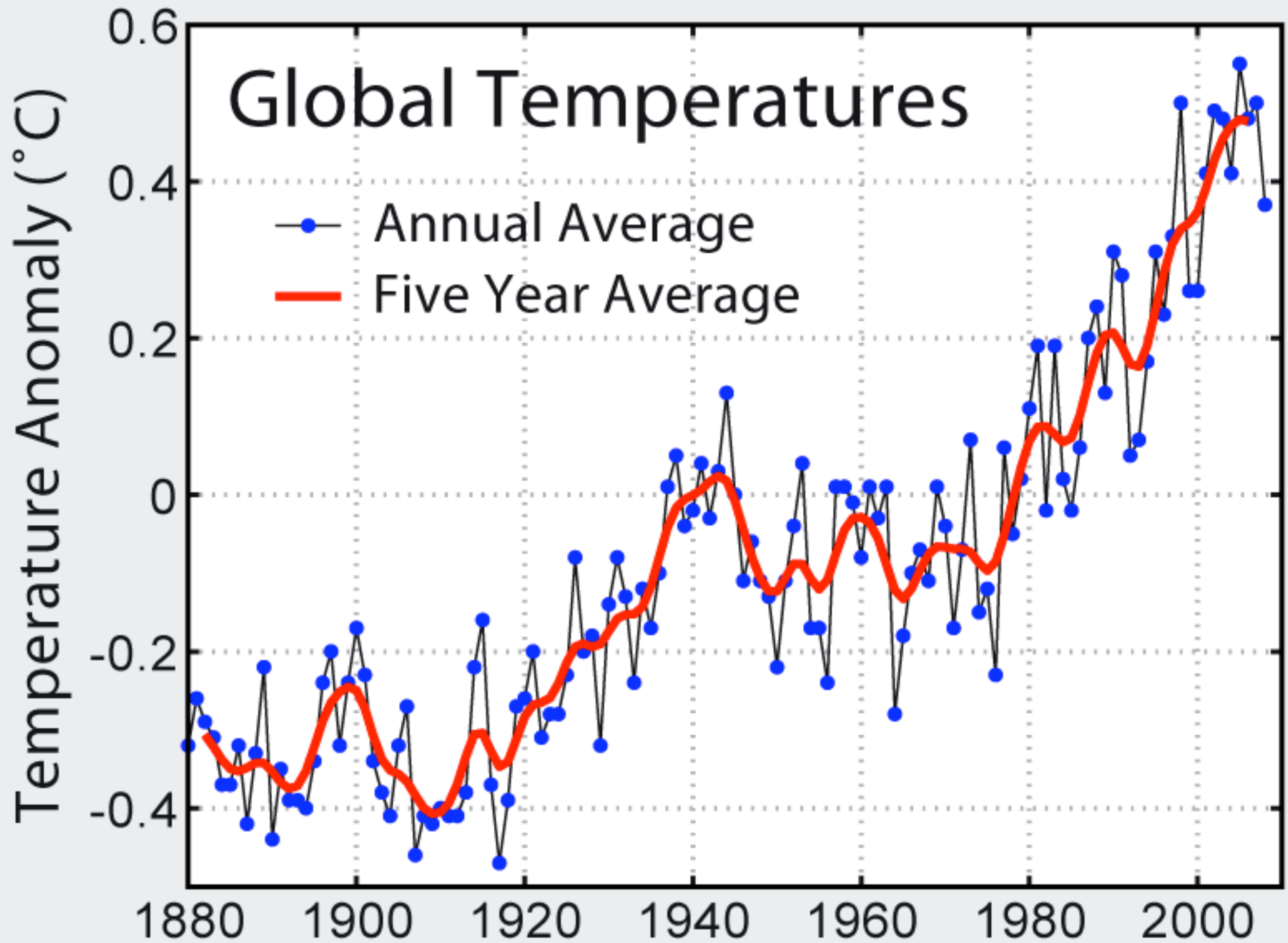
$$g_{\text{CO}_2} = \frac{\partial T}{\partial [\text{CO}_2]} \cdot \frac{\partial [\text{CO}_2]}{\partial T} = \frac{1^\circ\text{C}}{275\text{ppmv}} \cdot \frac{14.6\text{ppmv}}{1^\circ\text{C}} = 0.053$$

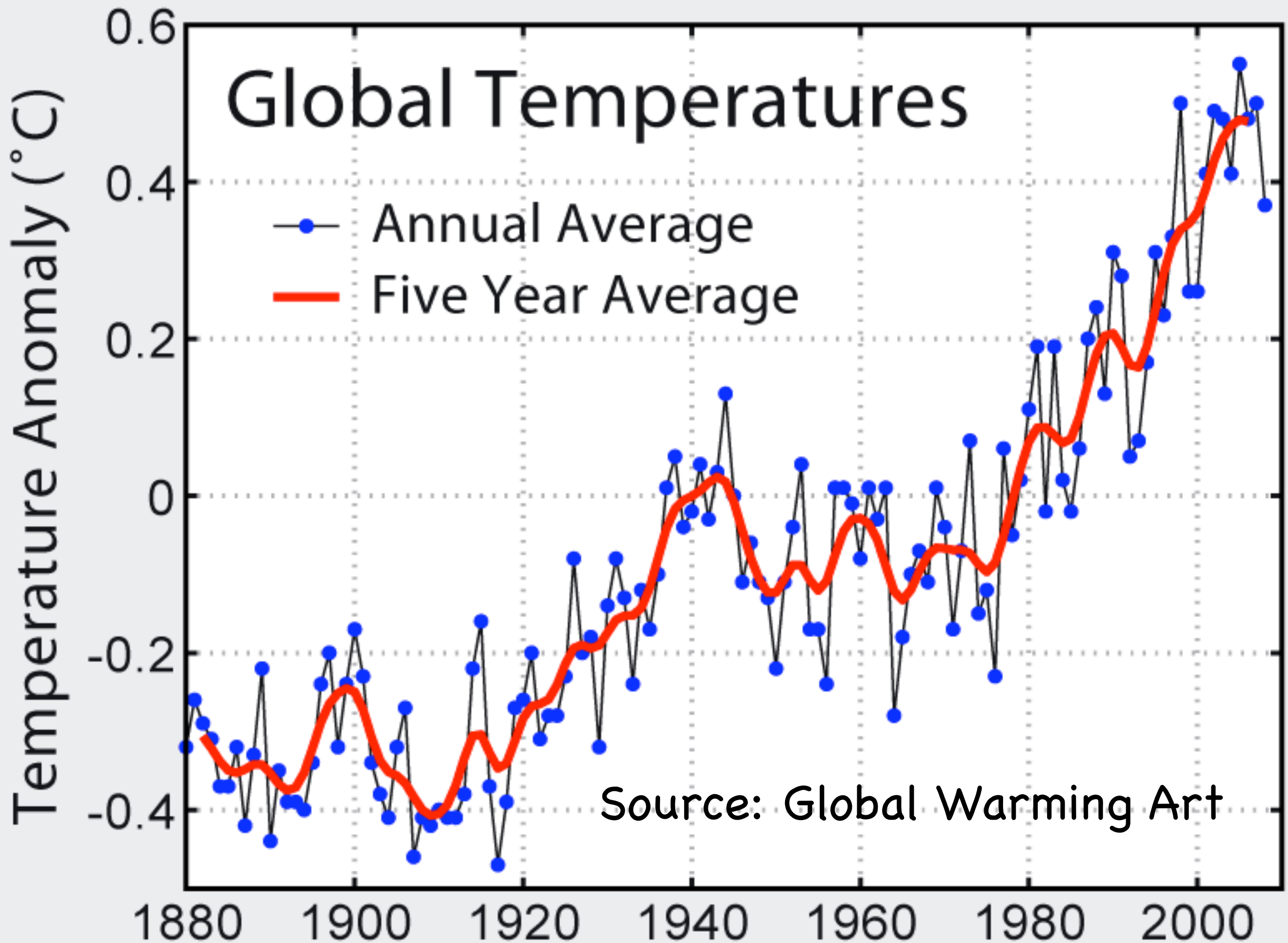
$$1^\circ\text{C}/(1 - .71) = 3.4^\circ\text{C}$$

$$1^\circ\text{C}/(1 - .71 - .05) = 4.2^\circ\text{C}$$

But where is the carbon coming from?









What Can Modern Physics Contribute?

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Summer 2005 Workshop

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John Harte's long-term ecosystem heating experiment at the Rocky Mountain Biological Laboratory near Aspen.

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Kavli Institute for Theoretical Physics

Physics of Climate Change
April 28 -- July 11, 2008
Frontiers of Climate Science
& Engineering the Earth
May 6 -- 10, 2008



Co-organizers:
J. Carlson, G. Falkovich, J. Harte,
J. B. Marston, and R. Pierrehumbert







“Human beings are now carrying out a large scale geophysical experiment of a kind that could not have happened in the past nor be reproduced in the future. Within a few centuries we are returning to the atmosphere and oceans the concentrated organic carbon stored in sedimentary rocks over hundreds of millions of years. (Revelle and Suess, 1957)

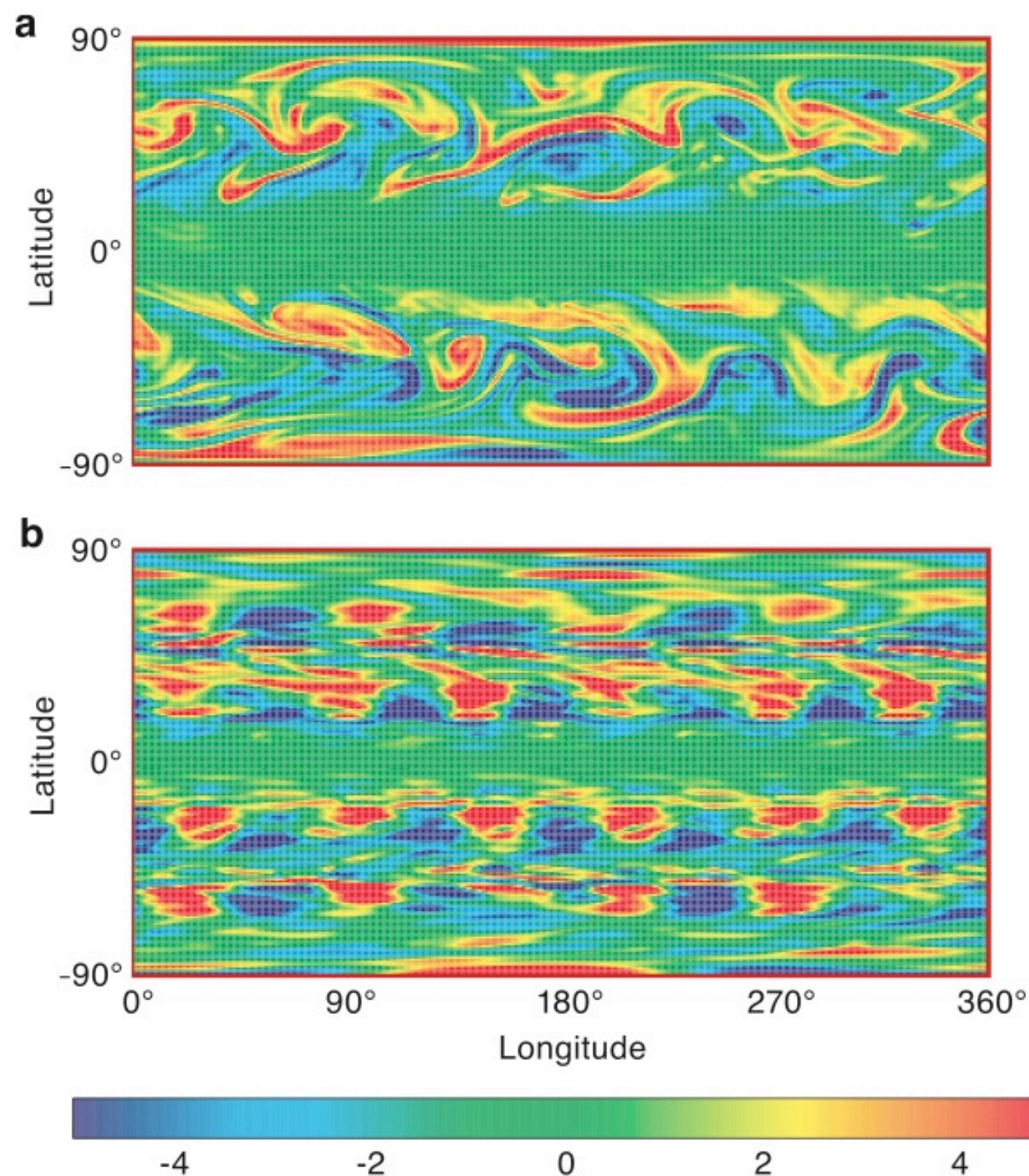


Figure 1. Typical instantaneous vorticity fields (10^{-5} s^{-1}) in (a) the full simulation and (b) the simulation without eddy-eddy interactions. The horizontal surface shown is in the mid-troposphere at $\sigma = 0.5$. The fields are shown at times after the simulations have reached statistically steady states.

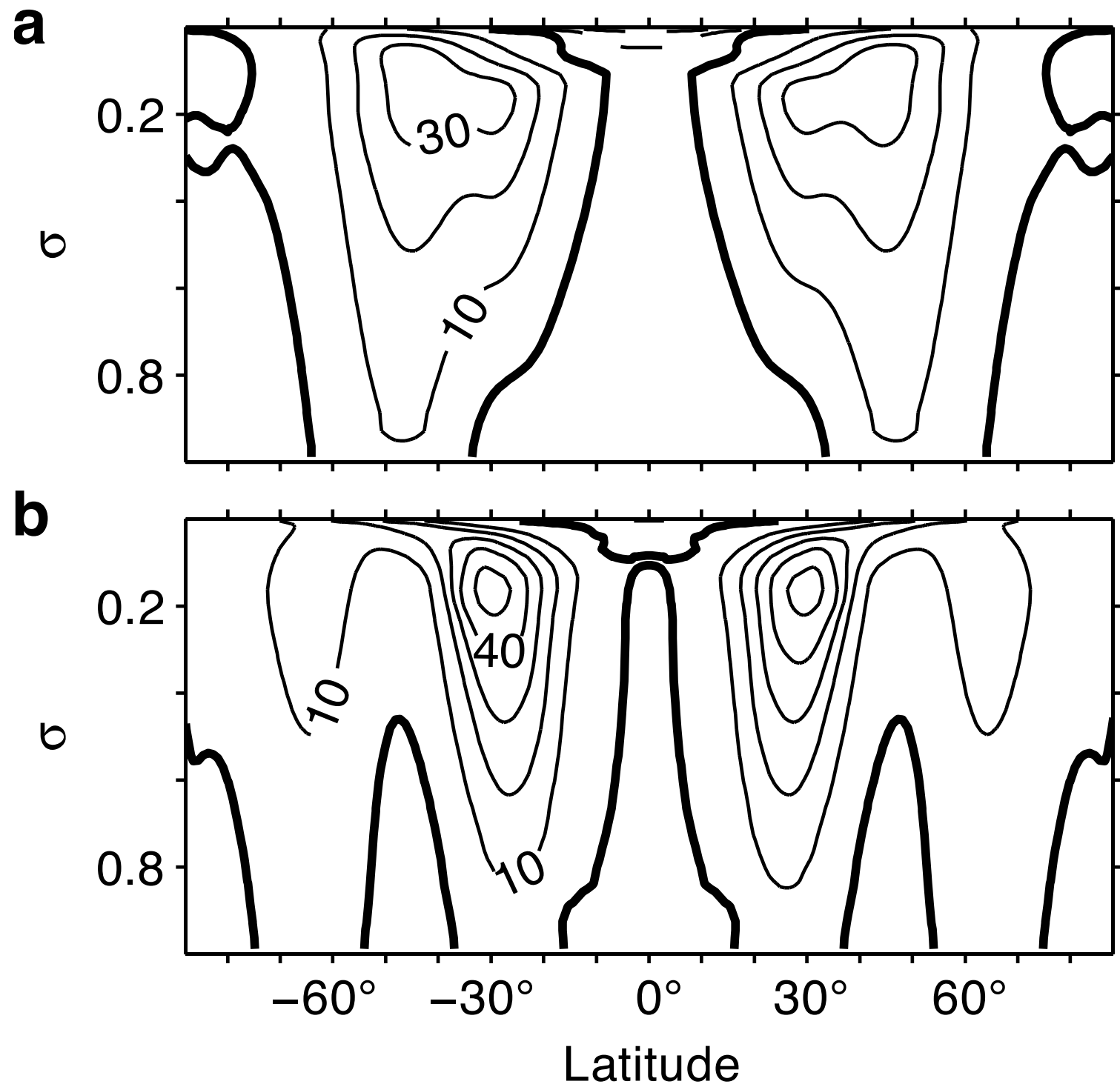
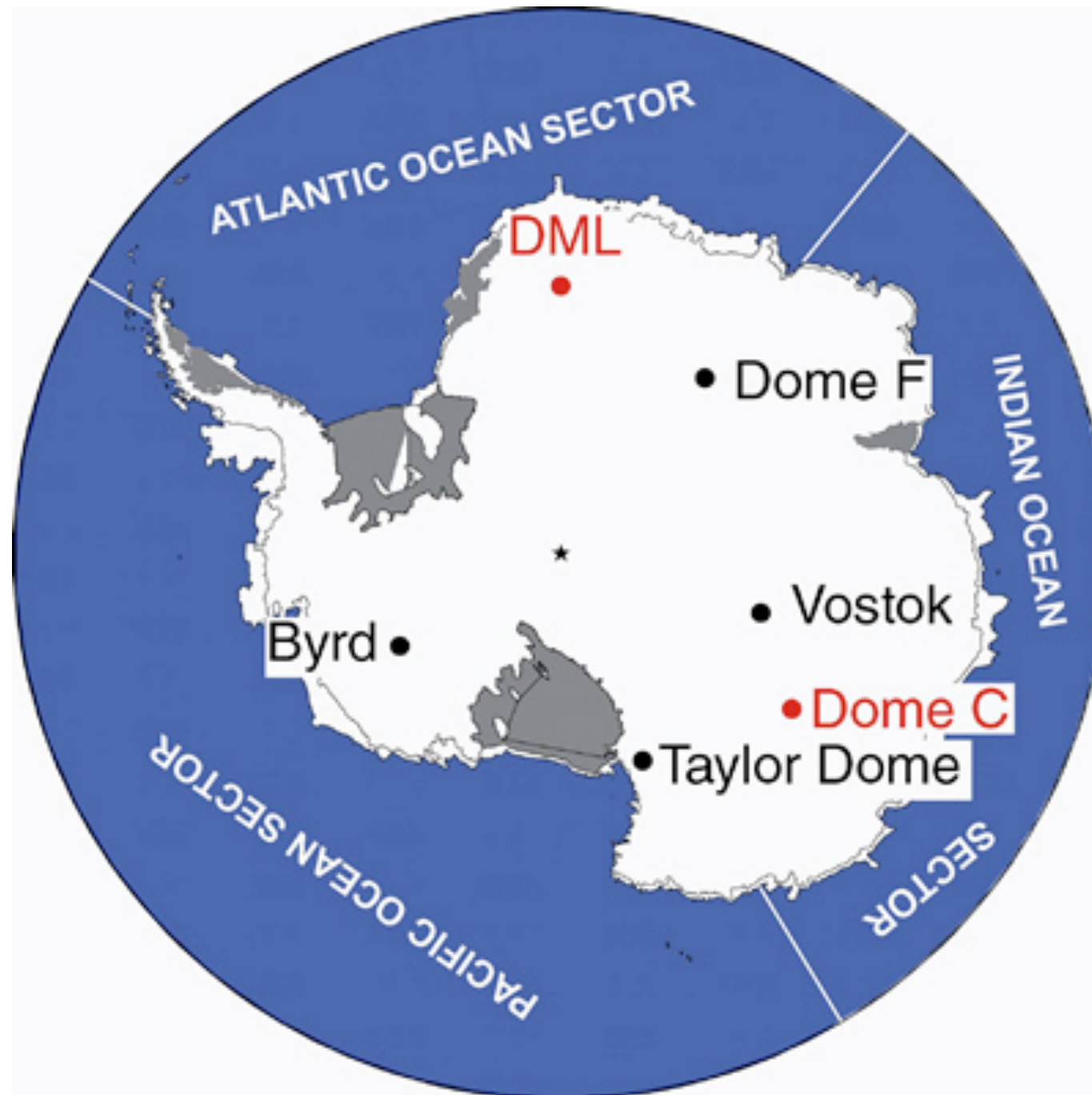


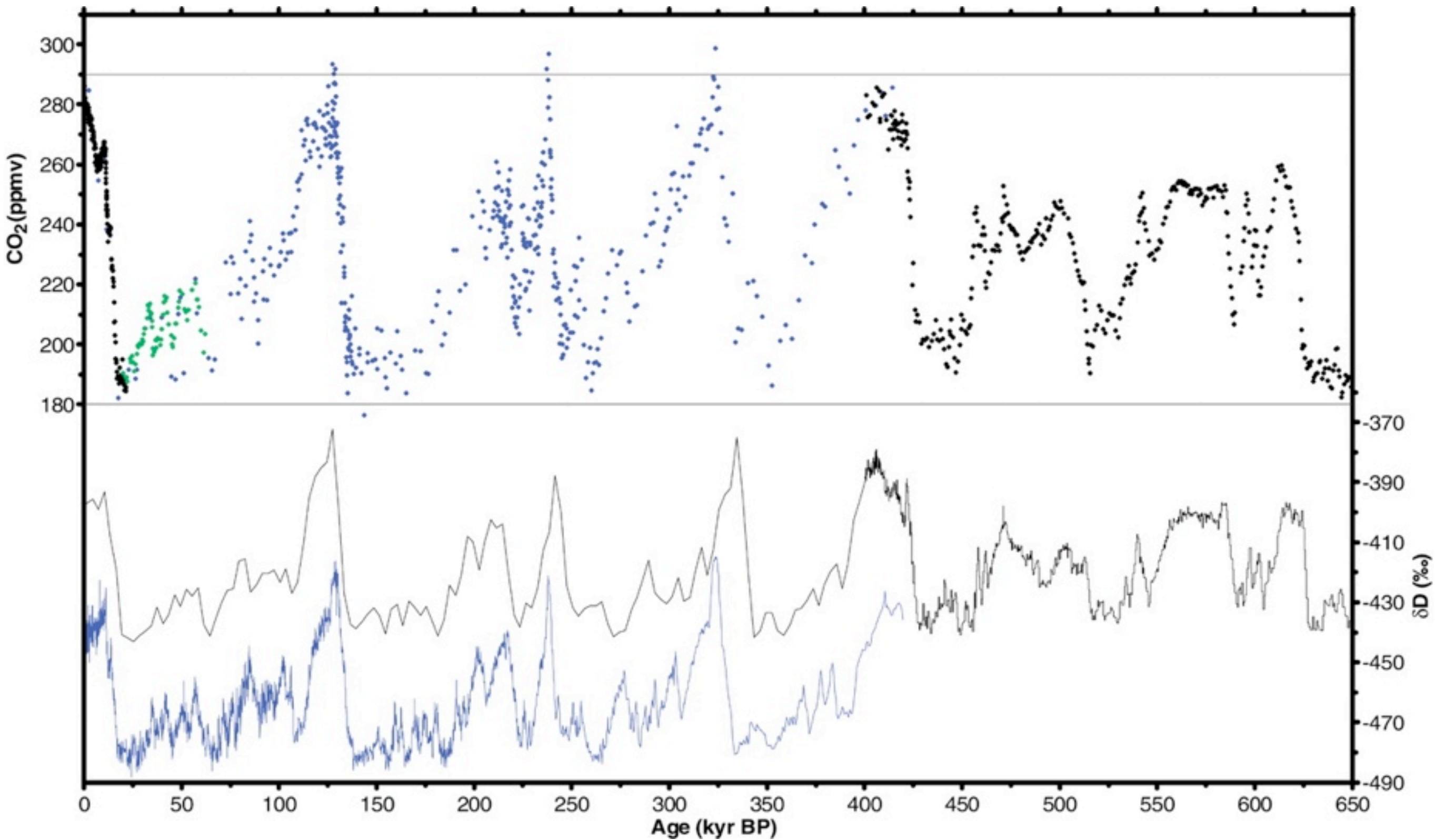
Figure 3. Mean eastward wind (m s^{-1}) in the meridional plane in (a) the full simulation and (b) the simulation without eddy-eddy interactions. The mean is a zonal, time, and interhemispheric average with mass weighting. The thick solid lines are the zero-wind lines.

Antarctic Dome C



Siegenthaler *et al.* Science **310**, 1313 (2005)

Antarctic Dome C



Siegenthaler *et al.* Science **310**, 1313 (2005)



Lake Mead