

# Sterile Neutrinos and Neutrino Interactions

To see or not to see, that is the question

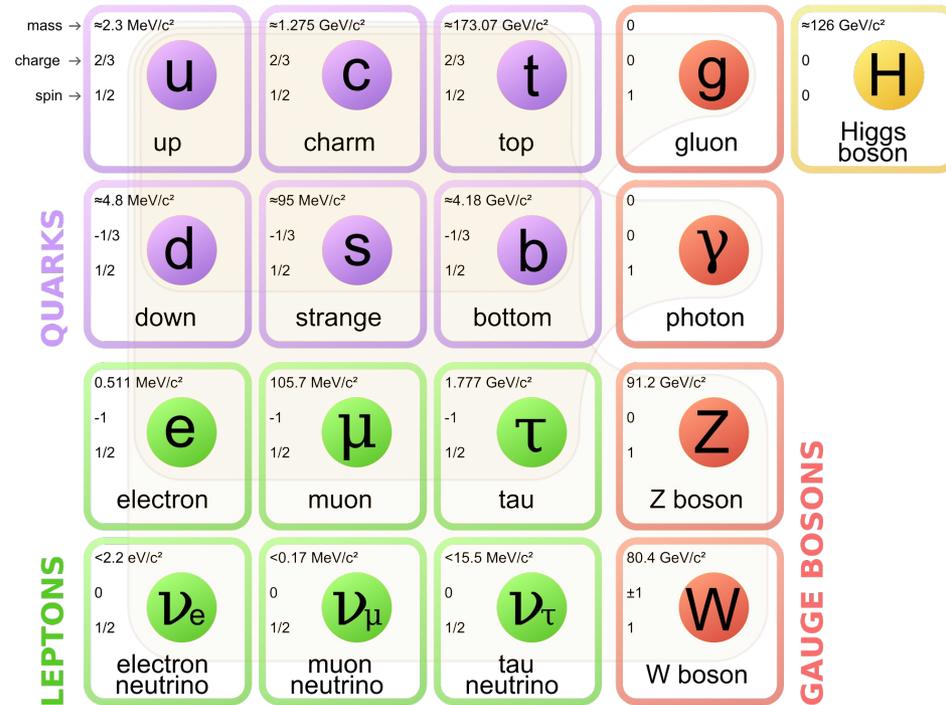
Mike Kordosky

William & Mary

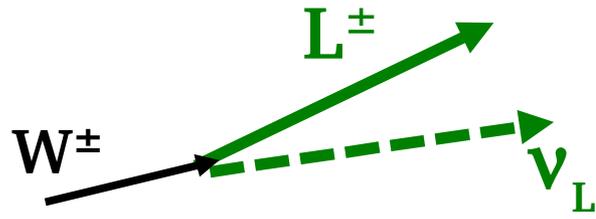
UVa HEP Seminar  
February 4, 2015

# Neutrinos: not just MET!

- Vital but mysterious part of the SM
  - Why  $SU(2)_L$ ?
- Massive, but very light.
  - How do they get their masses?
  - Different from other fermions?
- **Flavor mixing** is large, in contrast to quarks
- May violate CP, perhaps even maximally
- Could be their own anti-particle
- Interesting/complementary probe of nucleons/nuclei



# Oscillation Formalism



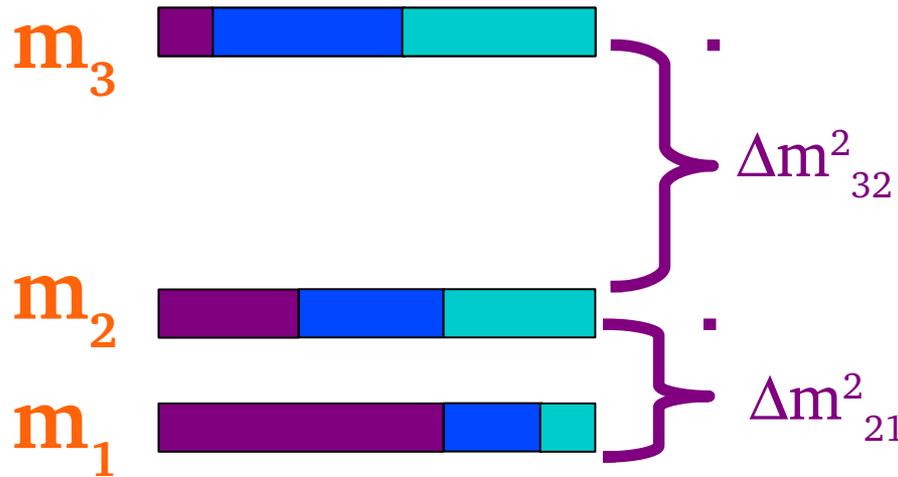
## Flavor

e    μ    τ

## Mass



$$E^2 = p^2 + m_i^2$$



PMNS

Mixing Matrix

$$U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$$

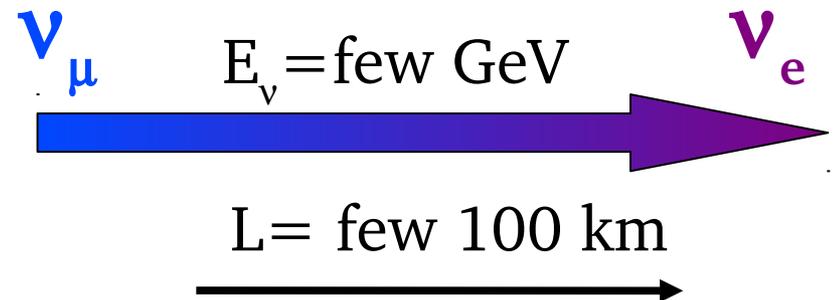
Propagation (vacuum)

flavor                      mass states

$$|\nu_\alpha(L)\rangle = \sum_j U_{\alpha j}^* |\nu_j\rangle \exp(-i L m_j^2 / 2p)$$

(L=distance)

Flavor change



# Three flavor mixing matrix

## PMNS Mixing Matrix

$$U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{bmatrix}$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

# Muon neutrino disappearance

## PMNS Mixing Matrix

$$U = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix}$$

## Propagation (vacuum)

flavor mass states

$$|\nu_{\alpha}(L)\rangle = \sum_j U_{\alpha j}^* |\nu_j\rangle \exp(-i L m_j^2 / 2p)$$

(L=distance)

$$P(\nu_{\mu} \rightarrow \nu_{\mu}) = 1 - 4|U_{\mu 3}|^2 |U_{\mu 1}|^2 \sin^2 \Delta_{31} \\ - 4|U_{\mu 3}|^2 |U_{\mu 2}|^2 \sin^2 \Delta_{32} \\ - 4|U_{\mu 2}|^2 |U_{\mu 1}|^2 \sin^2 \Delta_{21}$$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

Characteristic oscillatory behavior depends on  $\Delta m^2$  and  $L/E$

“Survival Probability”

For a neutrino of energy  $E$  a distance  $L$  from the source

# Muon neutrino disappearance

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

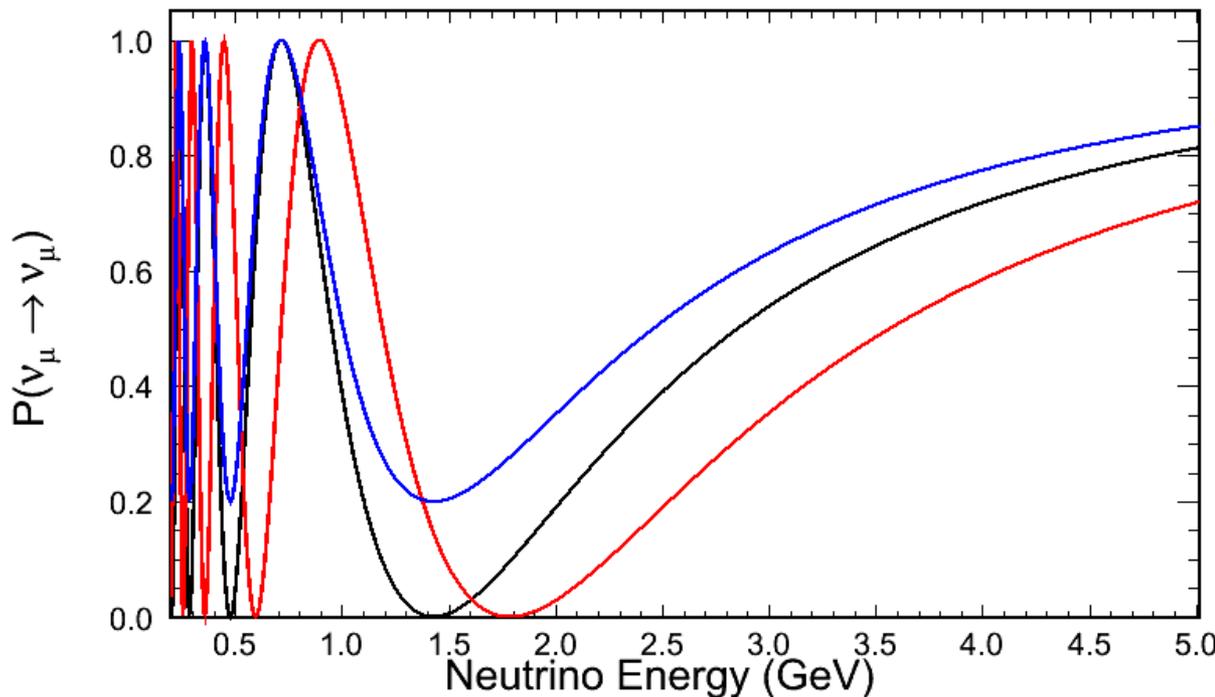
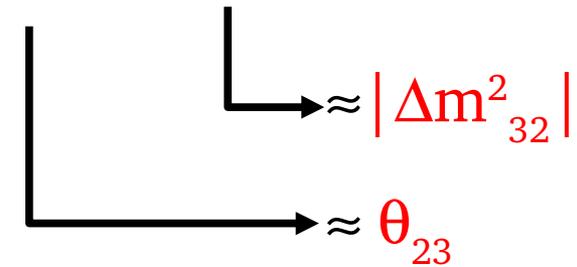
“Atmospheric oscillations”  
 $L/E \sim 500 \text{ km/GeV}$

Limiting Case

$$\theta_{13} = 0$$

$$|\Delta_{21}| \ll |\Delta_{31}| \approx |\Delta_{32}|$$

$$P(\nu_\mu \rightarrow \nu_\mu) = 1 - 4 \left\{ \begin{array}{l} |U_{\mu 3}|^2 |U_{\mu 1}|^2 \sin^2 \Delta_{31} \\ |U_{\mu 3}|^2 |U_{\mu 2}|^2 \sin^2 \Delta_{32} \\ |U_{\mu 2}|^2 |U_{\mu 1}|^2 \sin^2 \Delta_{21} \end{array} \right\} \approx 1 - \sin^2 2\theta \sin^2(|\Delta m^2| L / 4E)$$



$$|\Delta m^2| = 2.5 \times 10^{-3} \text{ eV}^2, \sin^2 2\theta = 0.8$$

$$|\Delta m^2| = 2.5 \times 10^{-3} \text{ eV}^2, \sin^2 2\theta = 1.0$$

$$|\Delta m^2| = 3.0 \times 10^{-3} \text{ eV}^2, \sin^2 2\theta = 1.0$$

# Electron Neutrino Appearance

“Atmospheric oscillations”

$L/E \sim 500 \text{ km/GeV}$

$$P(\nu_\mu \rightarrow \nu_e) \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} + \delta)} + \sqrt{P_{sol}} \right|^2$$

“Atmospheric” Term



$$\sqrt{P_{atm}} = \sin(\theta_{23}) \sin(2\theta_{13}) \frac{\sin(\Delta_{31} - aL)}{(\Delta_{31} - aL)} \Delta_{31}$$

depends on  $\Delta m_{31}^2$  and  $\theta_{13}$

“Solar” Term



$$\sqrt{P_{sol}} = \cos(\theta_{23}) \sin(2\theta_{12}) \frac{\sin(aL)}{(aL)} \Delta_{21}$$

<1% effect for current  
accelerator experiments

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$L/E$  oscillatory behavior  
embedded in  $\Delta_{ij}$  terms

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

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$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

Positive for neutrinos

Negative for anti-neutrinos

“Solar” Term

$$\sqrt{P_{sol}} = \cos(\theta_{23}) \sin(2\theta_{12}) \frac{\sin(aL)}{aL} \Delta_{21}$$

< 1% effect for current  
accelerator experiments

Matter Effect

Additional term in Hamiltonian  
introduced by  $\nu_e + e$  and  $\bar{\nu}_e + e$

CC scattering modifies oscillations

$$a = \frac{\pm G_F N_e}{\sqrt{2}} \approx \frac{1}{4000 \text{ km}}$$

# Electron Neutrino Appearance

“Atmospheric oscillations”

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depends on  $\Delta m_{31}^2$

and  $\theta_{13}$

< 1% effect for current  
accelerator experiments

CP Violating Phase

+ $\delta$  for neutrinos

- $\delta$  for anti-neutrinos

# Electron Neutrino Appearance

“Atmospheric oscillations”

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depends on  $\Delta m_{31}^2$   
and  $\theta_{13}$

< 1% effect for current  
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Mass Hierarchy

Unknown sign of

$\Delta m_{31}^2$  &  $\Delta m_{32}^2$

modifies probabilities

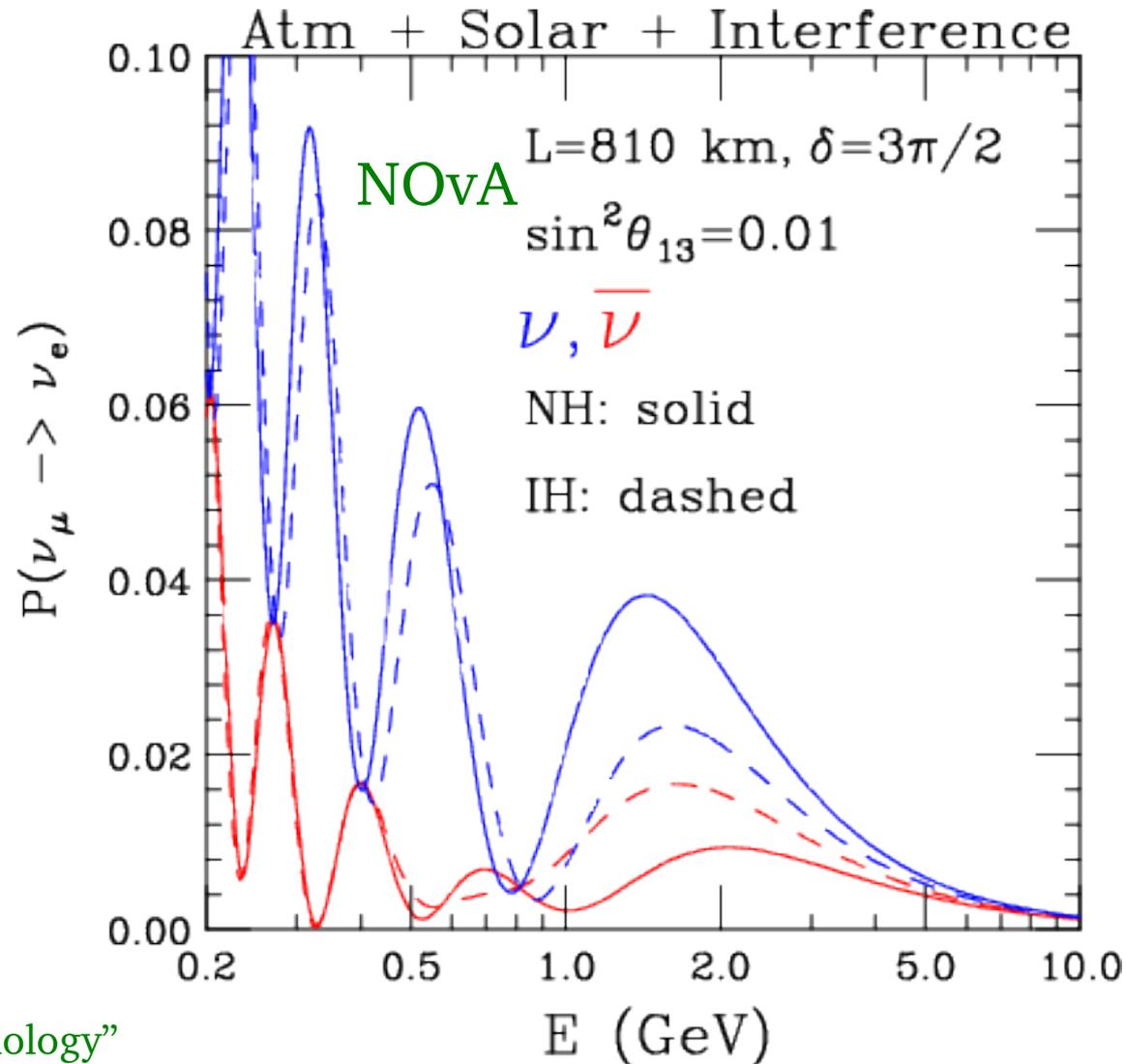
# Electron Neutrino Appearance

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$$a = \frac{\pm G_F N_e}{\sqrt{2}} \approx \frac{1}{4000 \text{ km}}$$



S. Parke, "Neutrino Oscillation Phenomenology"  
 in *Neutrino Oscillations: Present Status and  
 Future Plans*, Ed. J. Thomas, P. Vahle

# What do we know?

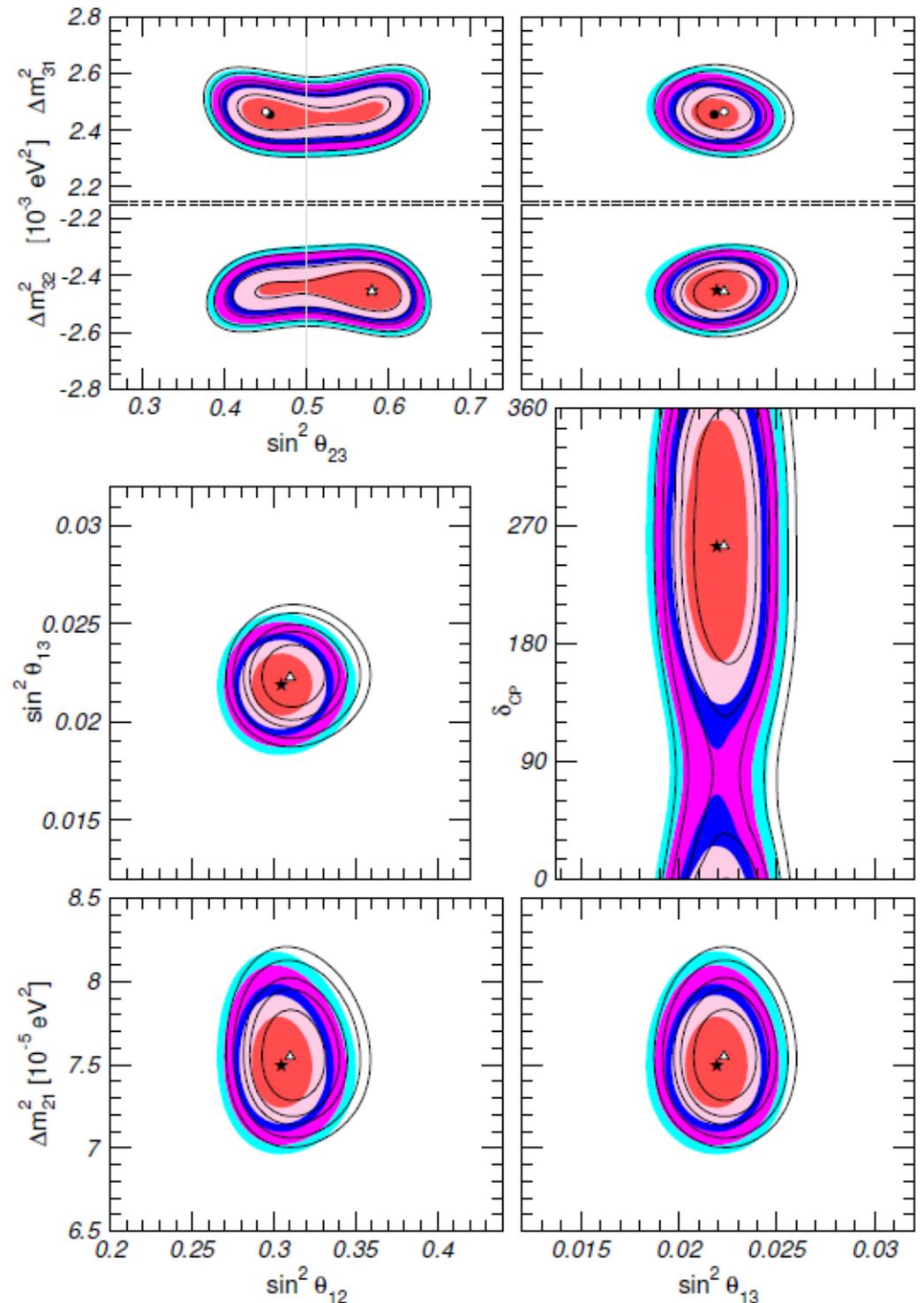
$$\mathbf{U} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Three active flavors ( LEP  $Z \rightarrow l\bar{l}, q\bar{q}$ )
- $\sin^2 \theta_{12}$  and  $\Delta m_{21}^2$  from  $\nu_e \rightarrow \nu_\mu$  in the Sun  
and from  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  at reactors (SuperK/SNO/KAMLAND)
- $\sin^2 \theta_{23}$  and  $|\Delta m_{31}^2| \approx |\Delta m_{32}^2|$  from  $\nu_\mu \rightarrow \nu_\mu$  in the atmosphere  
and long baseline accelerators (SuperK, MINOS, T2K)
- $\sin^2 \theta_{13}$  from  $\bar{\nu}_e \rightarrow \bar{\nu}_e$  at reactors (Daya Bay, RENO, D-CHOOZ)

# What do we know?

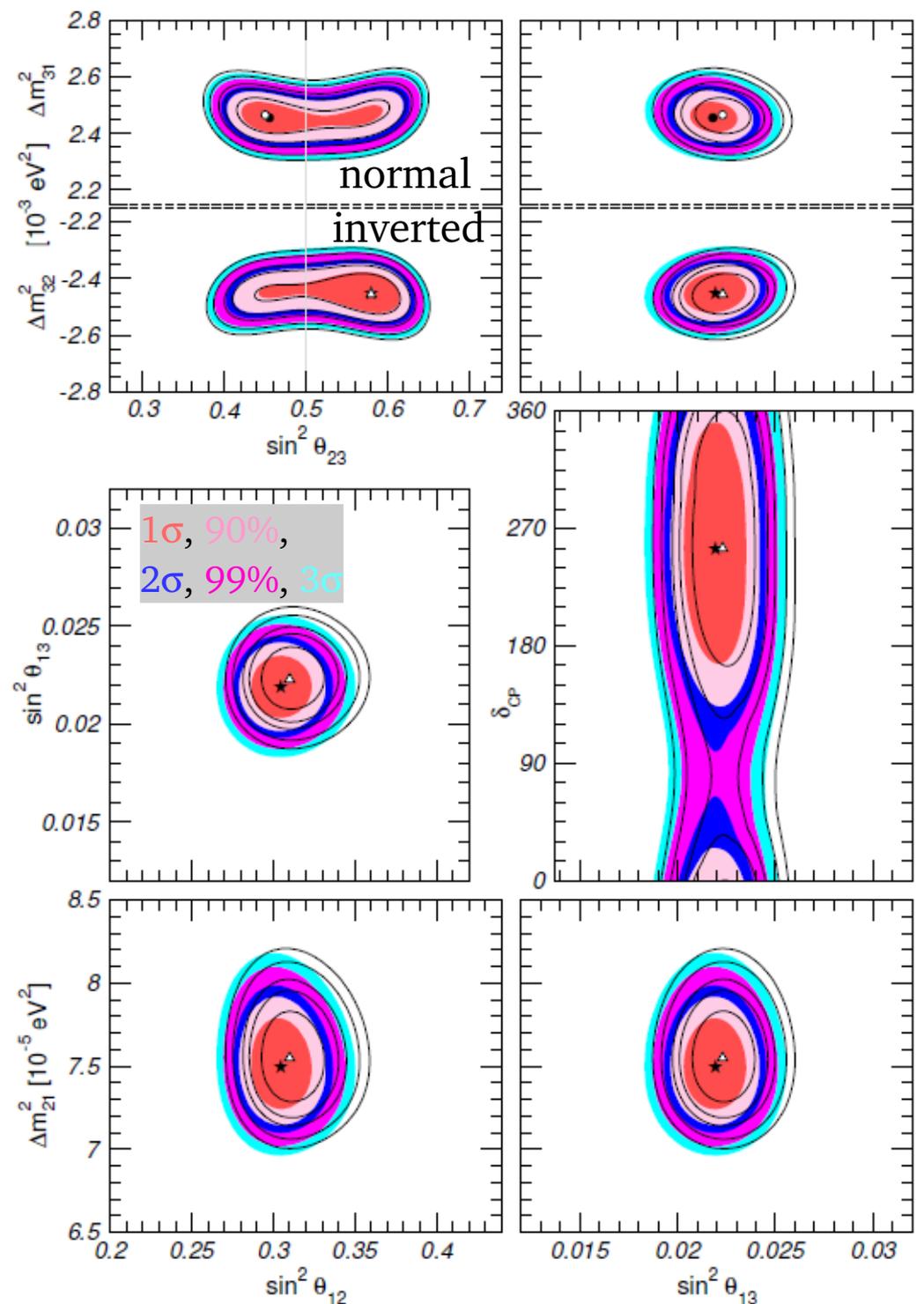
*Updated fit to three neutrino mixing: status of leptonic CP violation*

Gonzalez-Garcia, Maltoni, Schwetz arXiv-1409.5439

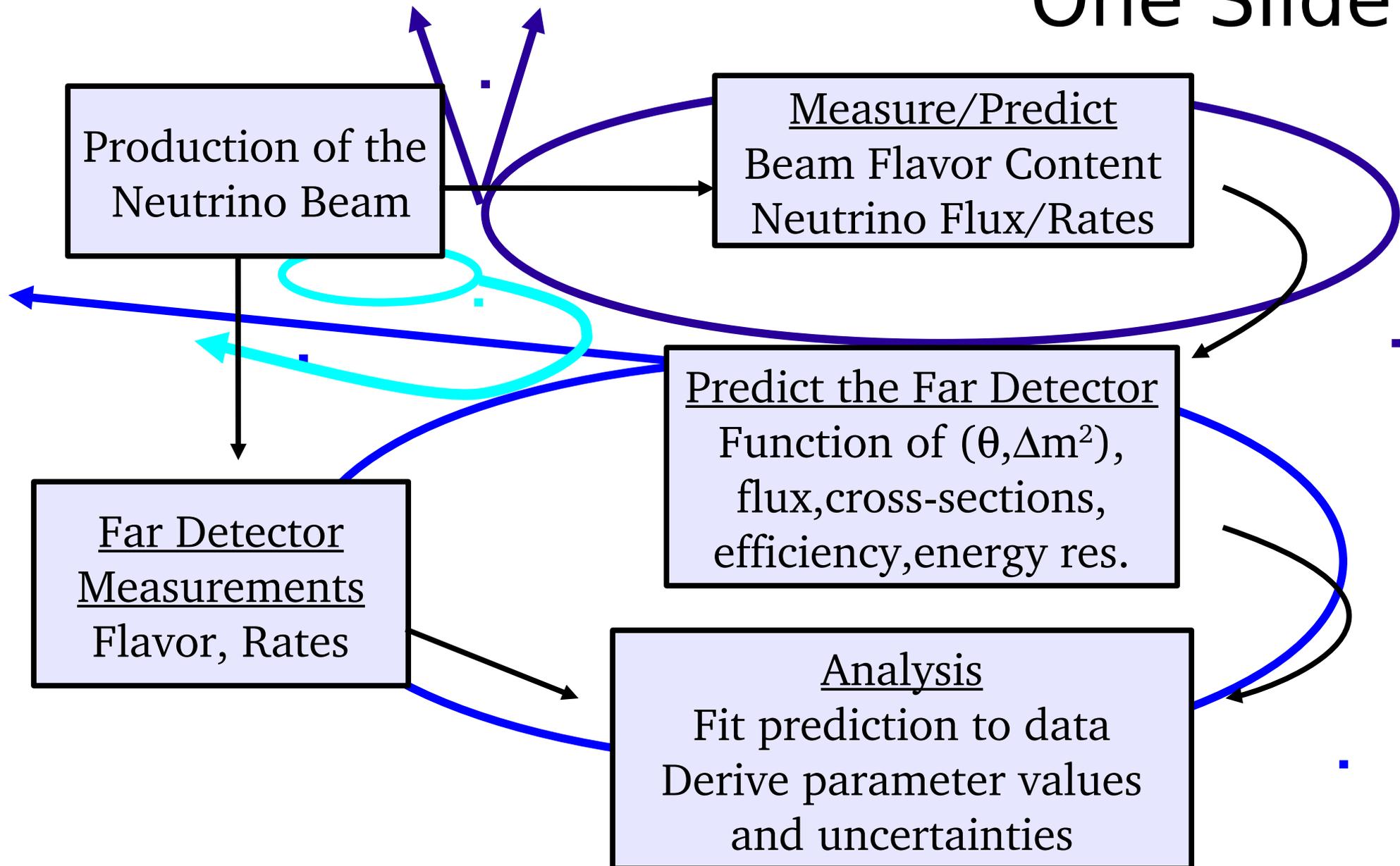


# What we can learn?

- $\delta_{CP}$  from  $\nu_\mu \rightarrow \nu_e$  and  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  (NOvA, LBNF)
- Mass ordering  
 $m_3 > m_2, m_1$  “normal”  
 $m_3 < m_2, m_1$  “inverted”  
 (NOvA, JUNO, PINGU)
- Octant of  $\theta_{23}$
- Are there sterile neutrinos?

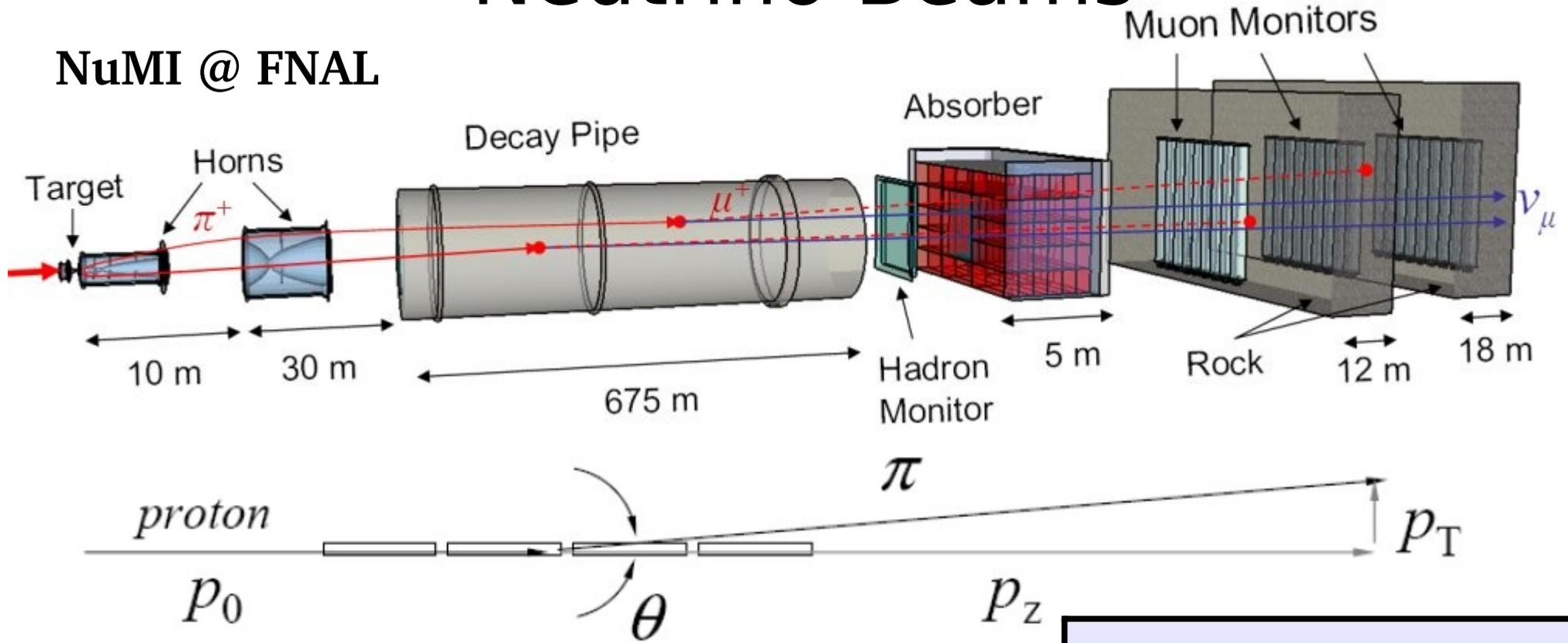


# An Oscillation Experiment In One Slide



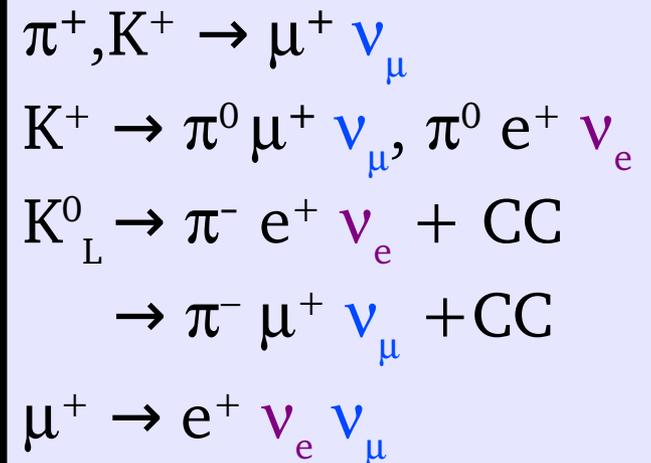
# Neutrino Beams

## NuMI @ FNAL



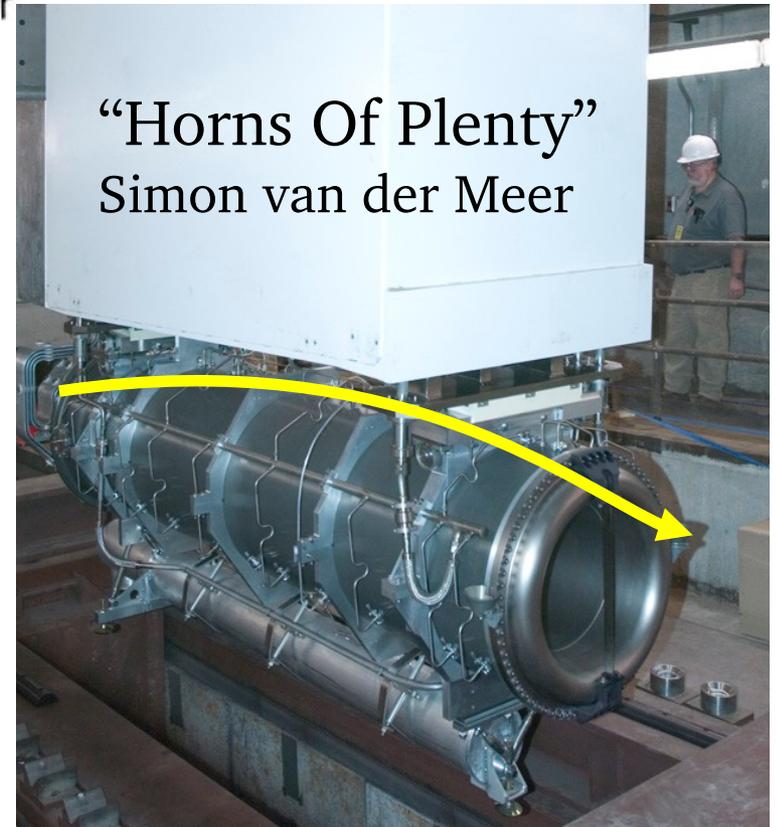
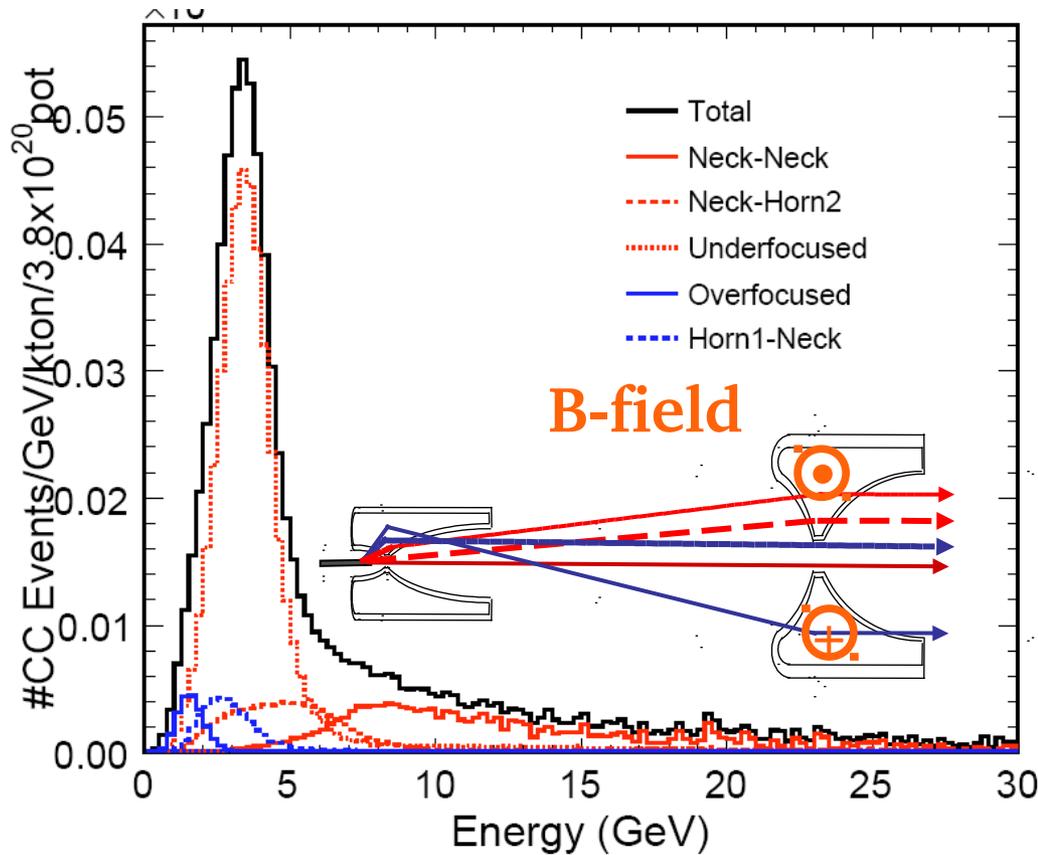
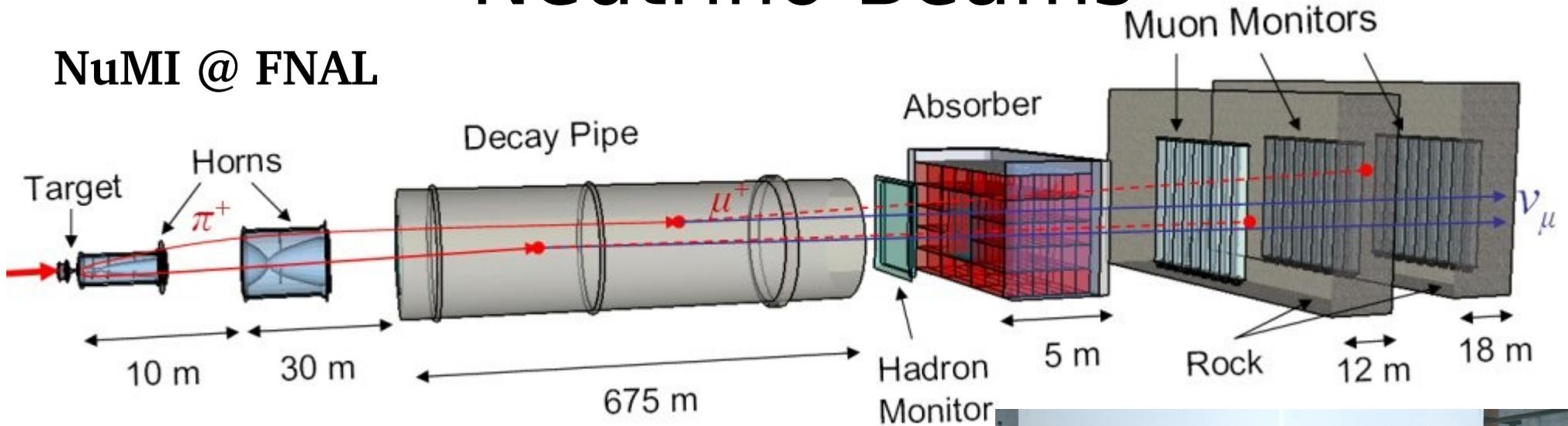
- $\pi, K$  production off a solid target
- Wide range of  $p_t, p_z$
- Cross-sections not well known

### Important decay modes

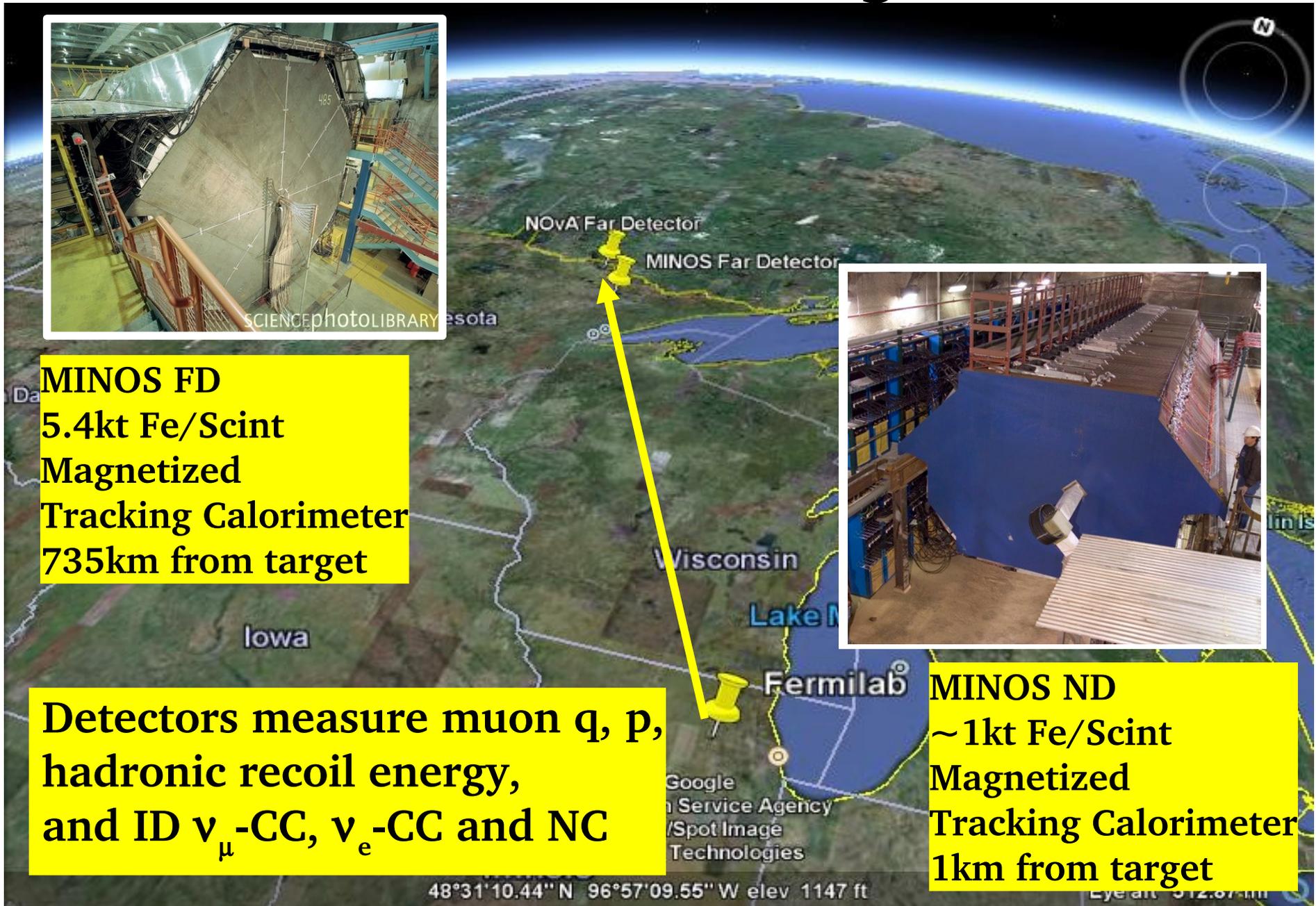


# Neutrino Beams

## NuMI @ FNAL



# Weak interaction = Big Detectors



**MINOS FD**  
5.4kt Fe/Scint  
Magnetized  
Tracking Calorimeter  
735km from target

**Detectors measure muon  $q$ ,  $p$ ,  
hadronic recoil energy,  
and ID  $\nu_{\mu}$ -CC,  $\nu_e$ -CC and NC**

**MINOS ND**  
~1kt Fe/Scint  
Magnetized  
Tracking Calorimeter  
1km from target

# One event at the FD

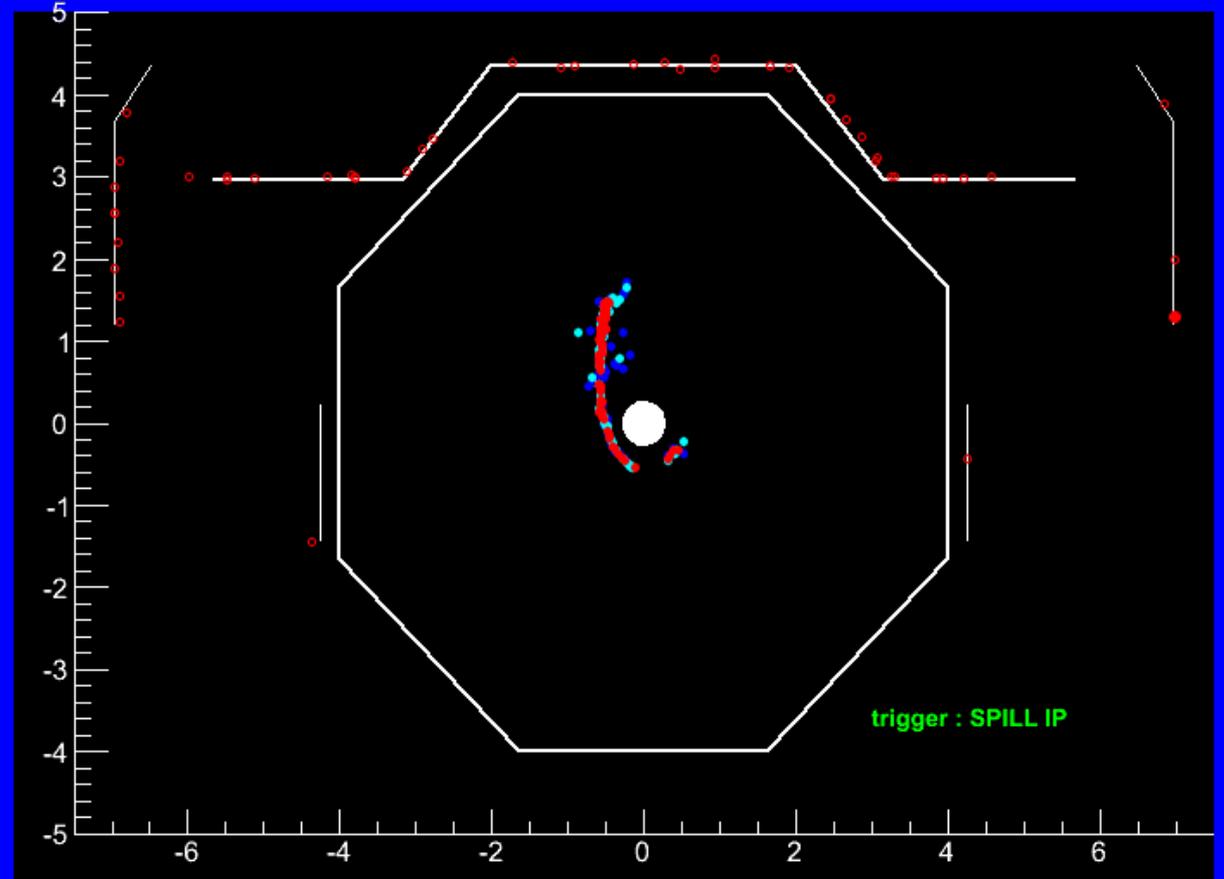
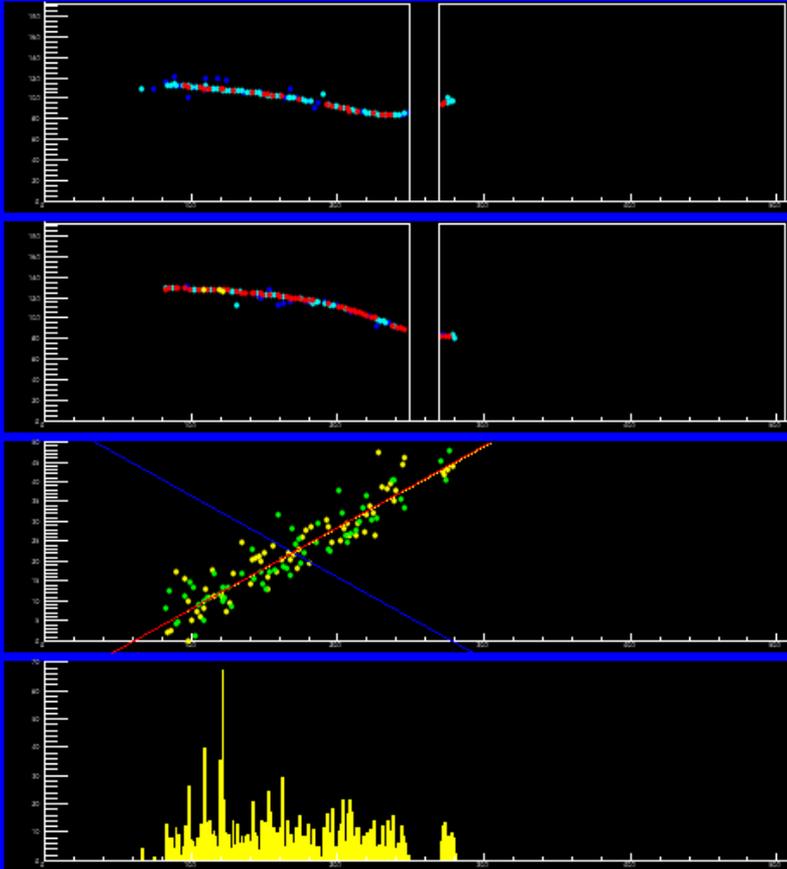
Date : 3 Feb 2015

Time : 20:48:31

Run : 62201\_23

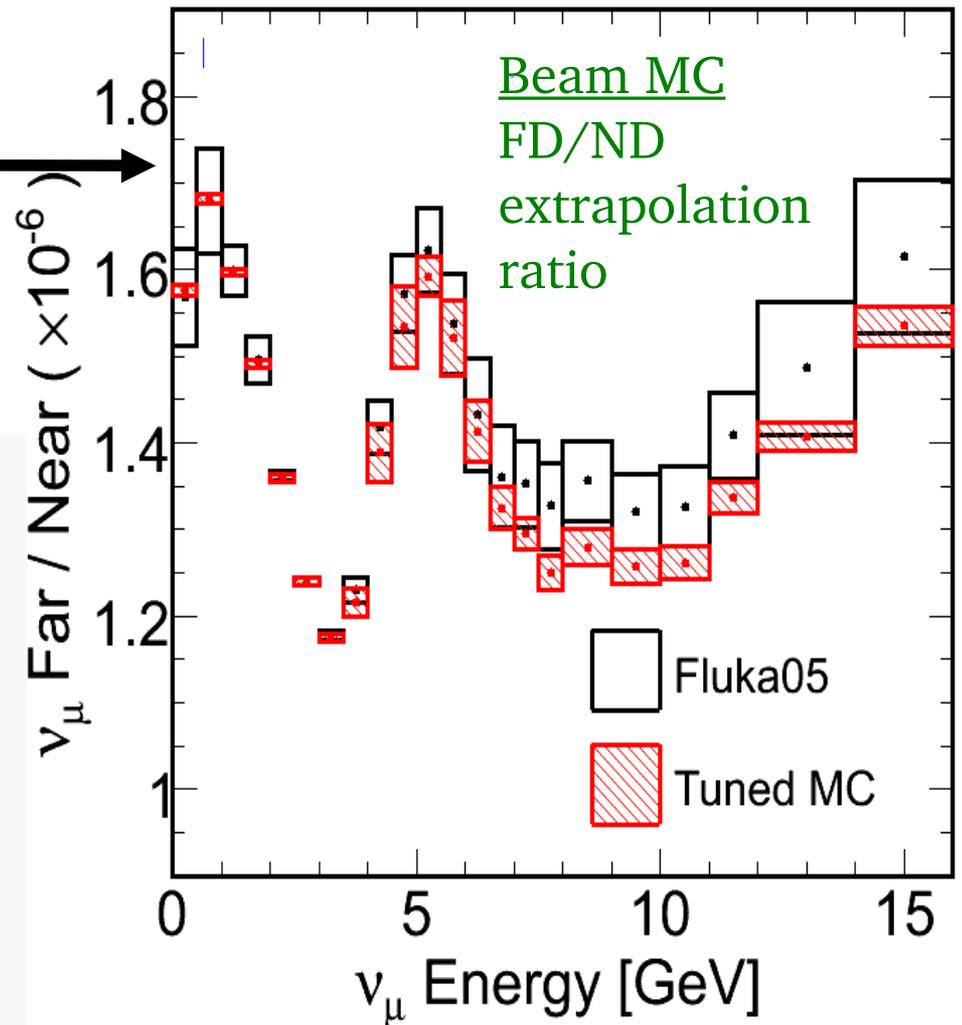
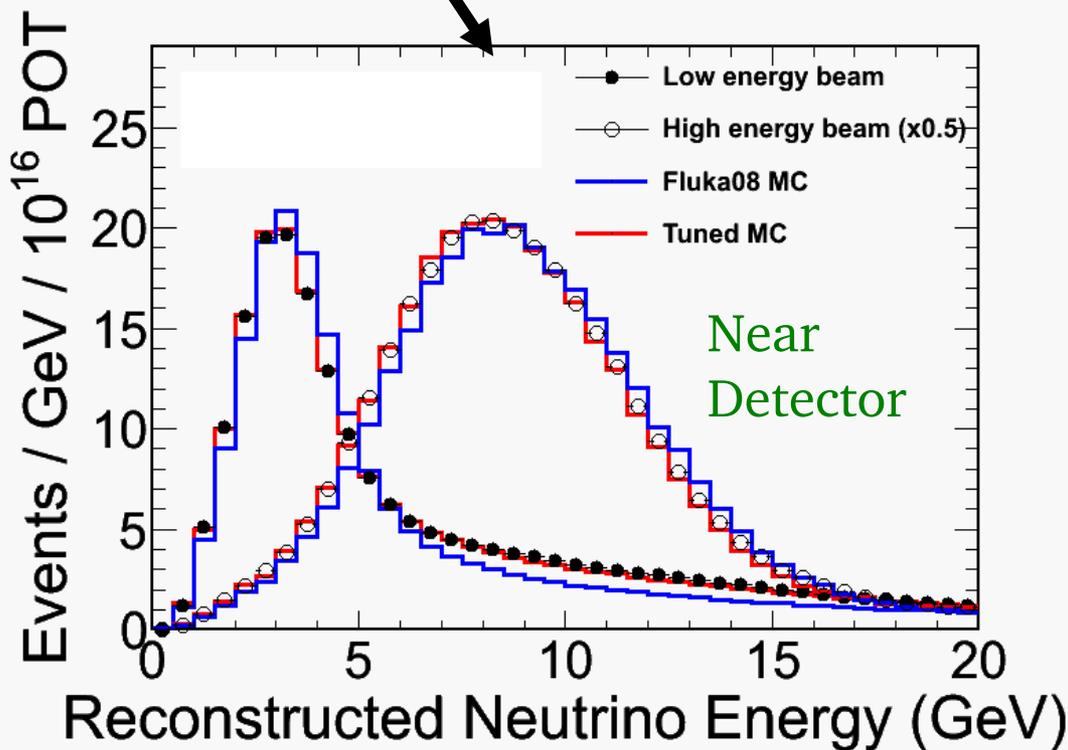
Snarl : 206193

EventType : Beam Neutrino Candidate



# Predicting the FD $\nu_\mu \rightarrow \nu_\mu$

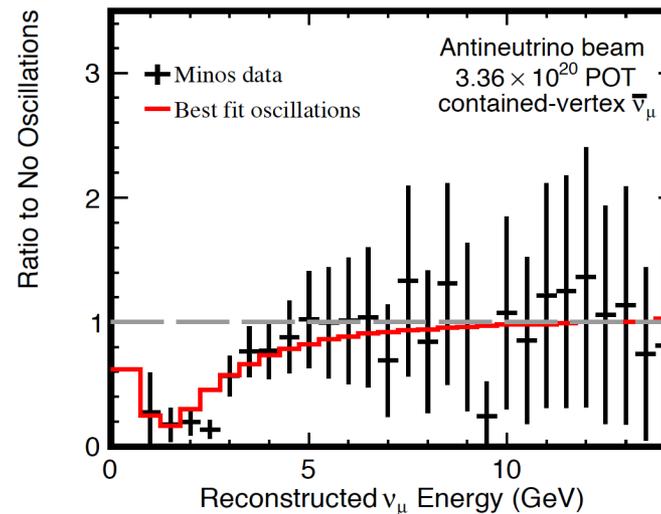
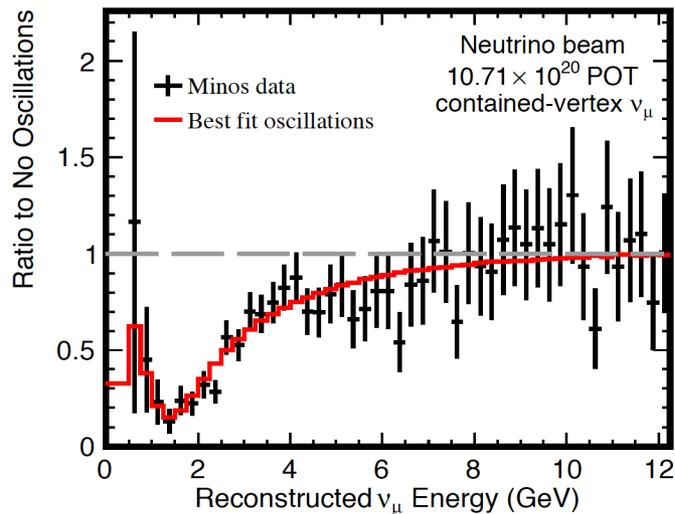
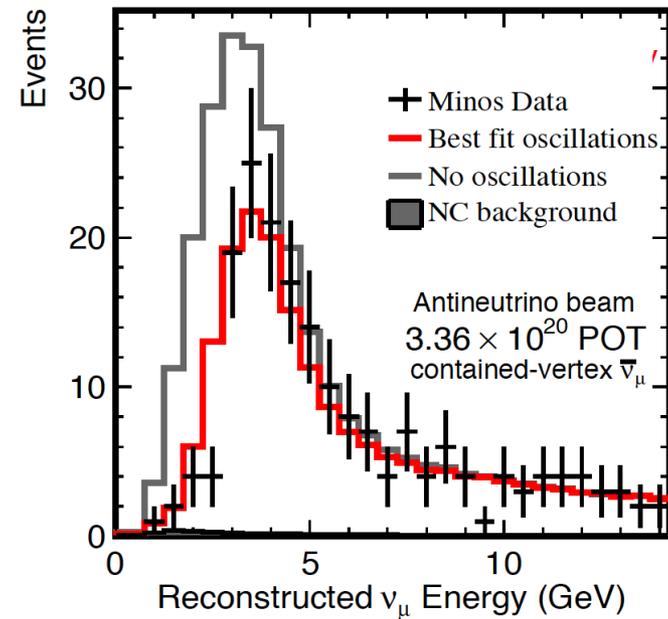
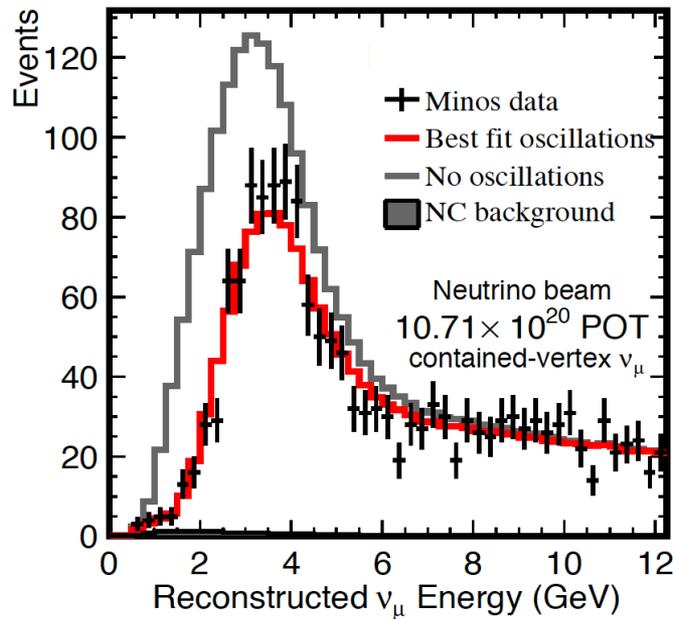
- Extrapolation improved by tuning beam MC to data in multiple focusing configurations



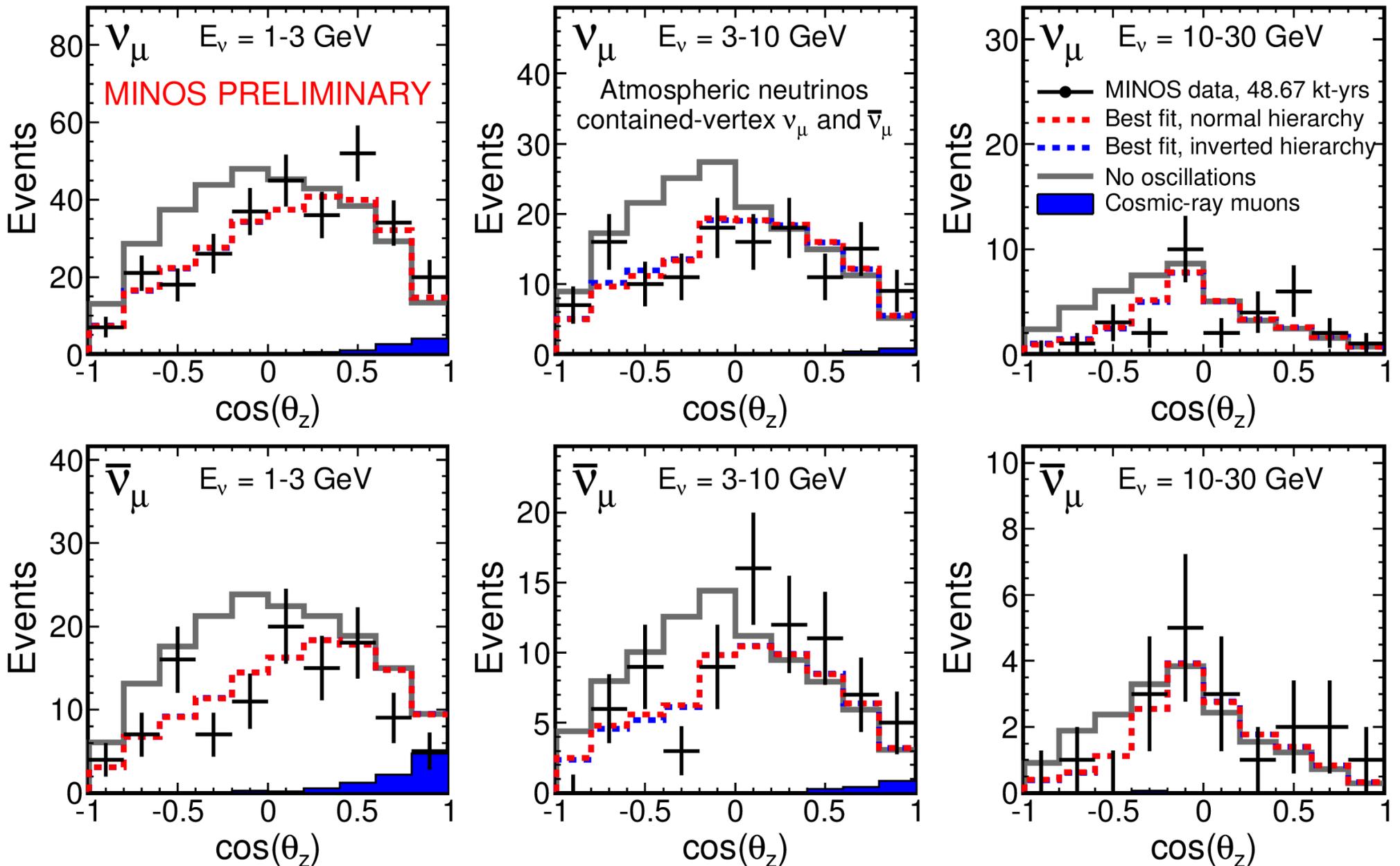
# Full 3 flavor oscillation analysis

- Multi-parameter likelihood fit, with systematics handled as nuisance parameters
- Beam  $\nu_\mu$ - and  $\bar{\nu}_\mu$ -CC events from the entire “low energy” dataset
  - $10.7e20 + 3.4e20$  protons on target
  - constrain  $\sin^2 2\theta_{23}$ ,  $\Delta m^2_{32}$
- Atmospheric  $\nu_\mu$ - and  $\bar{\nu}_\mu$  -47.6 kiloton-years
  - mass ordering (a.k.a. hierarchy),  $\theta_{23}$  octant
- Beam  $\nu_e$ -CC:
  - $\theta_{13}$ ,  $\delta_{CP}$ , mass ordering
  - $\theta_{13}$  fit with penalty term using measurements from reactor experiments.

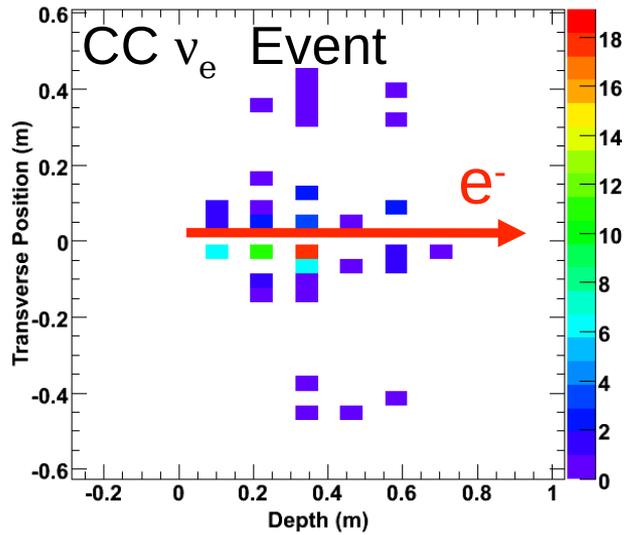
# Beam $\nu_\mu$ at the FD



# Atmospheric neutrinos



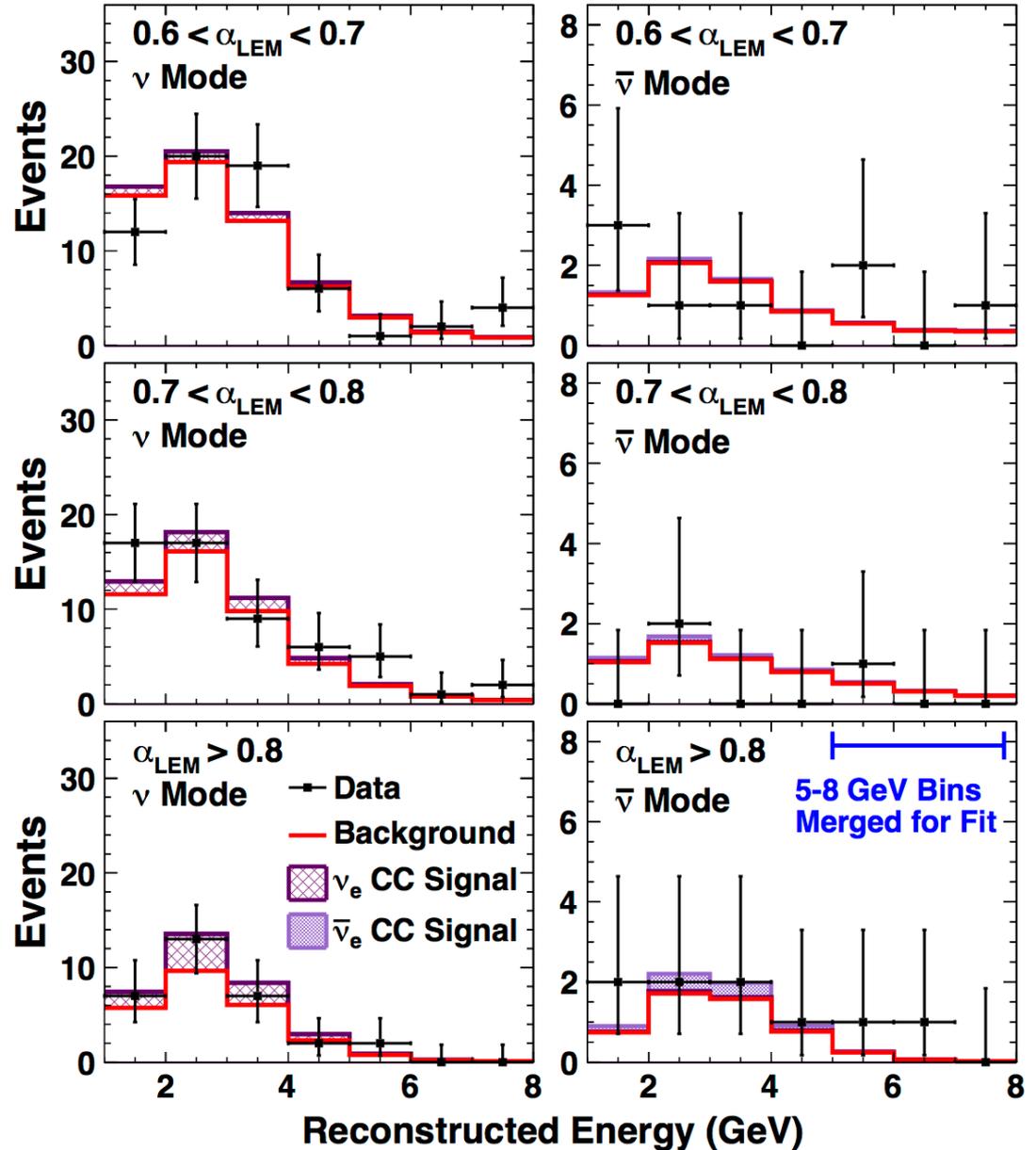
$$\nu_{\mu} \rightarrow \nu_e$$



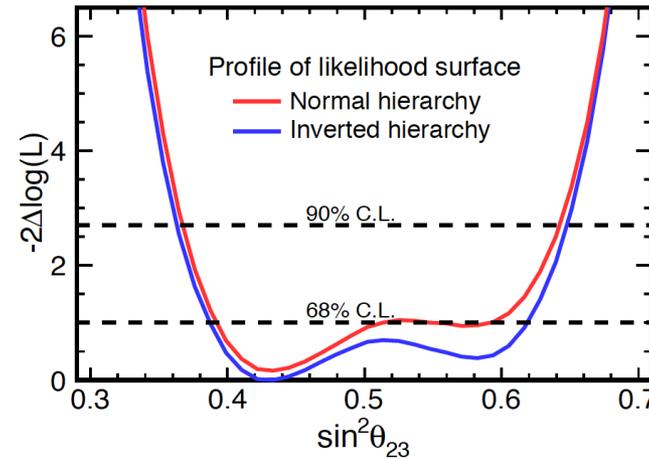
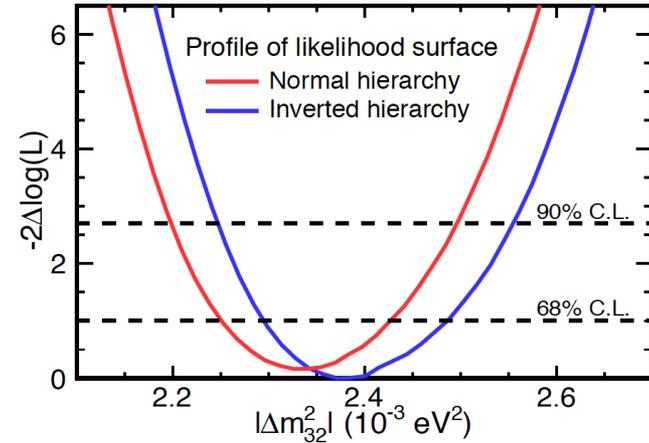
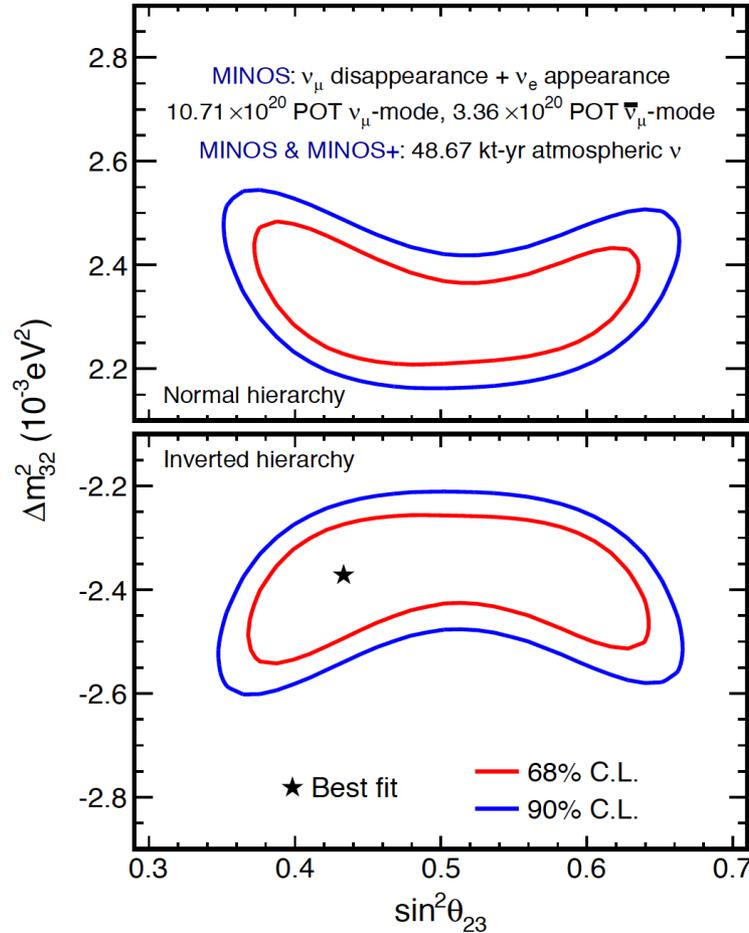
FD event yields for normal mass hierarchy,  $\delta_{CP}=0$ ,  $\theta_{23}=\pi/4$

	$\nu$ -beam	$\bar{\nu}$ -beam
$\theta_{13} = 0$	69.1	10.5
$\theta_{13} = 0.1$	+26.0	+3.1
Obs.	88	12

### MINOS Far Detector Data



# Three Flavor Results

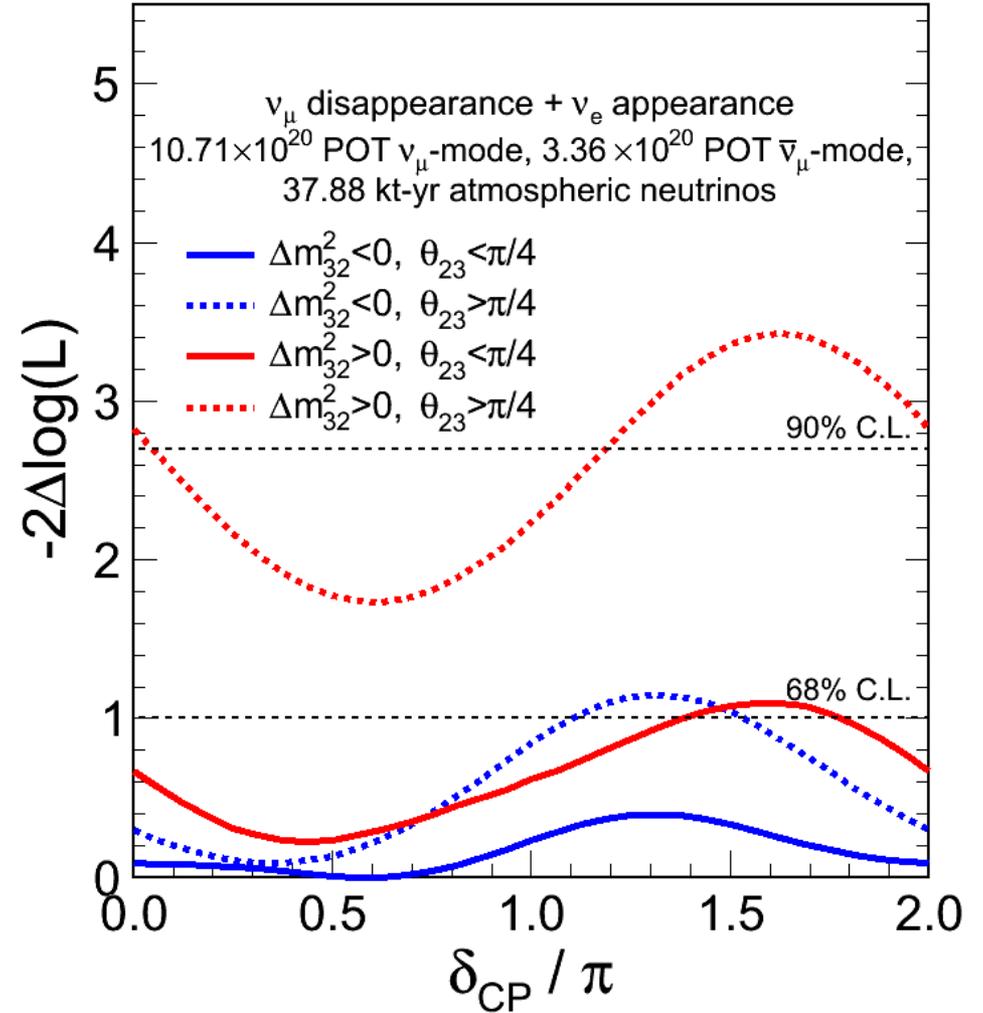
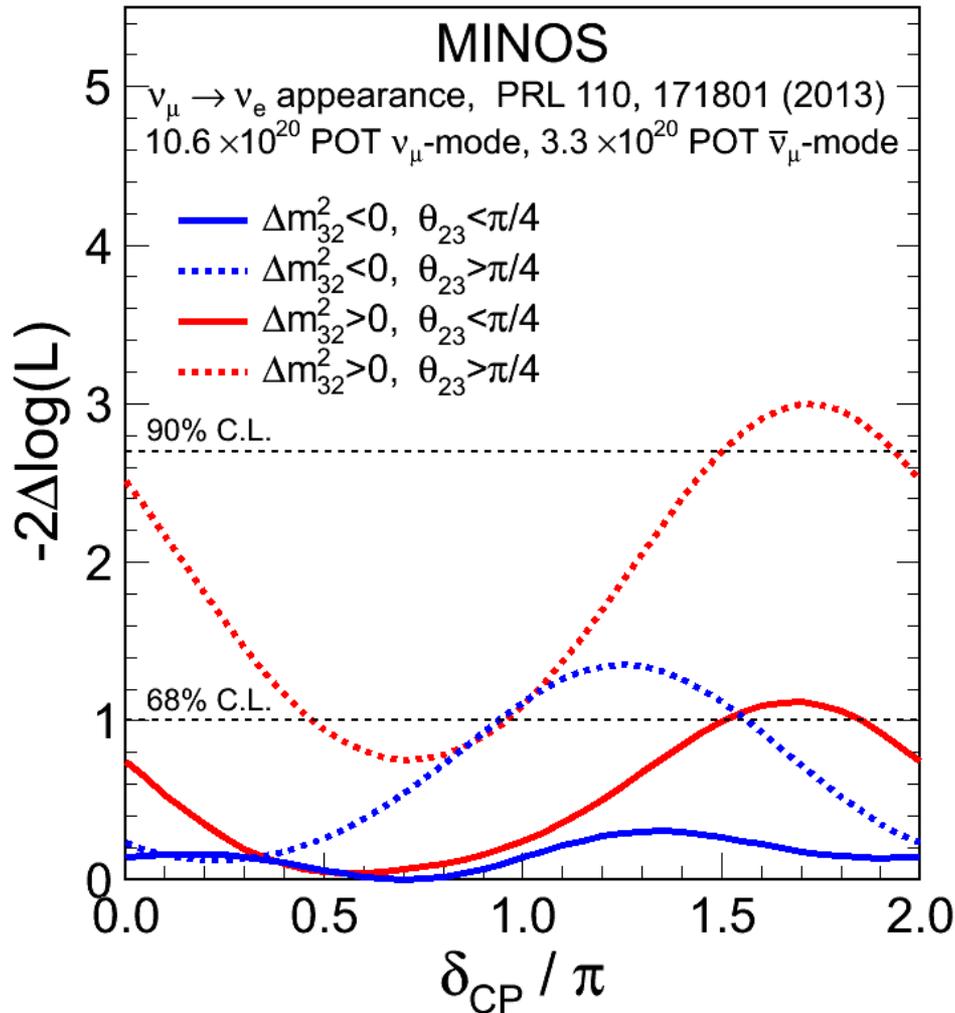


- Solar mixing parameters fixed to  $\Delta m_{21}^2 = 7.54 \times 10^{-5} \text{eV}^2$  and  $\sin^2 \theta_{12} = 0.307$  *Fogli et al., PRD **86**, 013012 (2012)*
- $\theta_{13}$  fit as nuisance parameter, constrained by reactor results:  $\sin^2 \theta_{13} = 0.0242 \pm 0.0025$  ( $\theta_{13} = 8.95^\circ$ )
- $\delta_{CP}$ ,  $\theta_{23}$ ,  $\Delta m_{32}^2$  unconstrained
- 19 systematic uncertainties (4 for beam+15 for atmospheric) included as nuisance parameters

# Three flavor results

Appearance only

Disappearance + Appearance

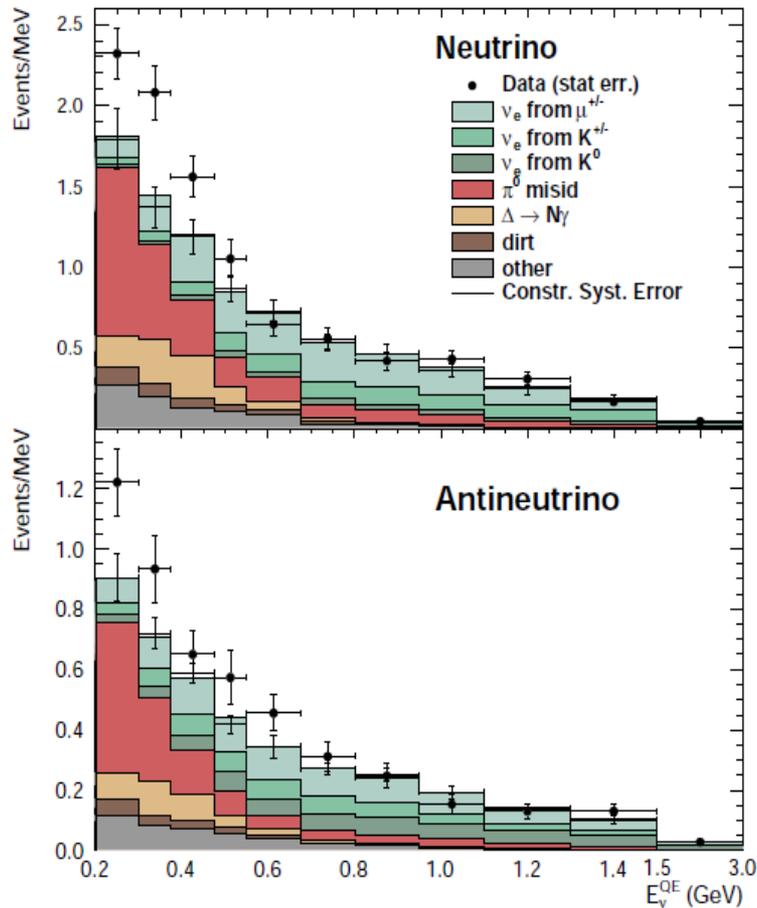
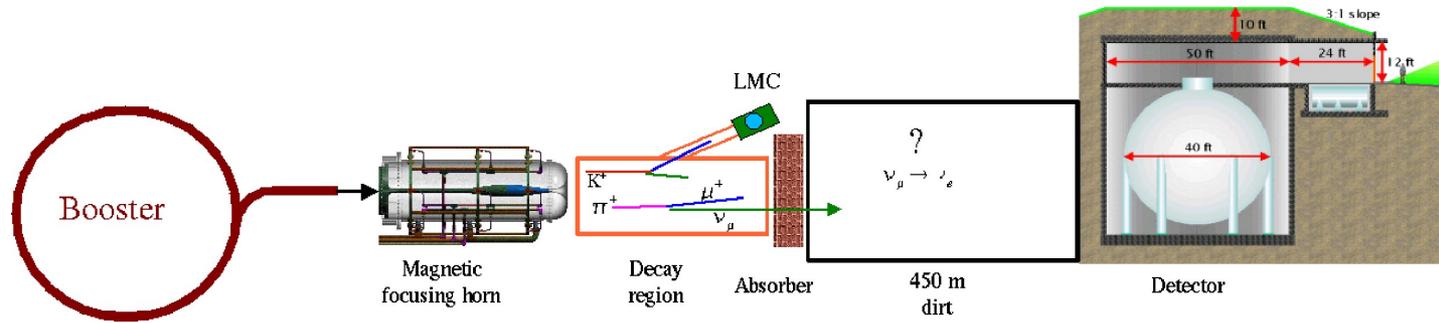


*Phys. Rev. Lett.* **112**, 191801 (2014)

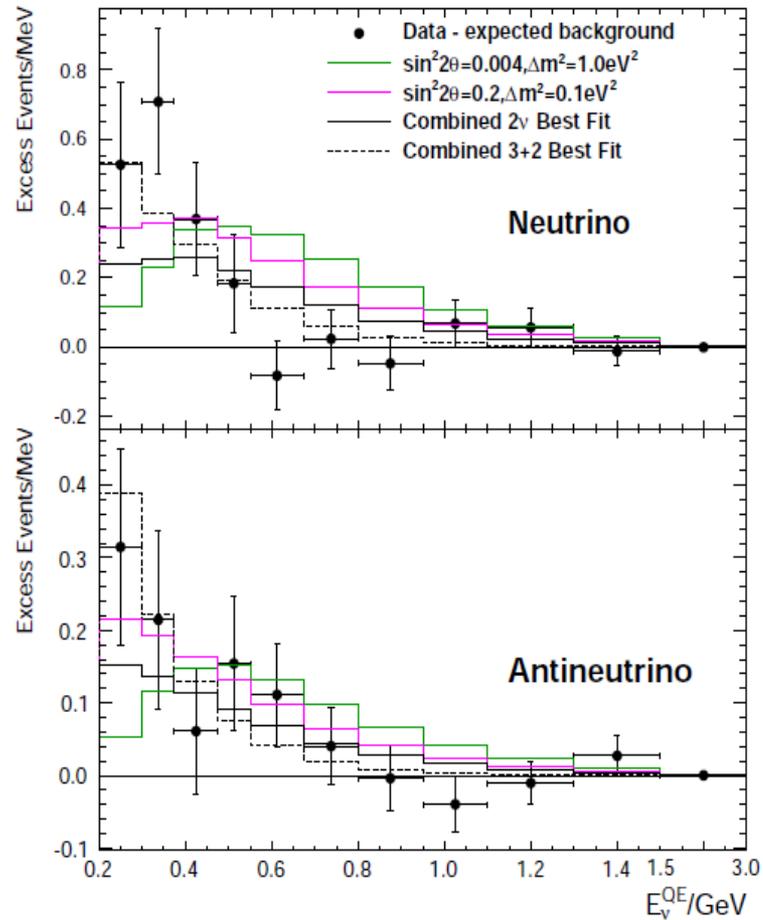
# A fourth neutrino?

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Anomalies in:  
accelerator  $\nu_\mu \rightarrow \nu_e$



MiniBooNE, PRL 110, 161801(2013)

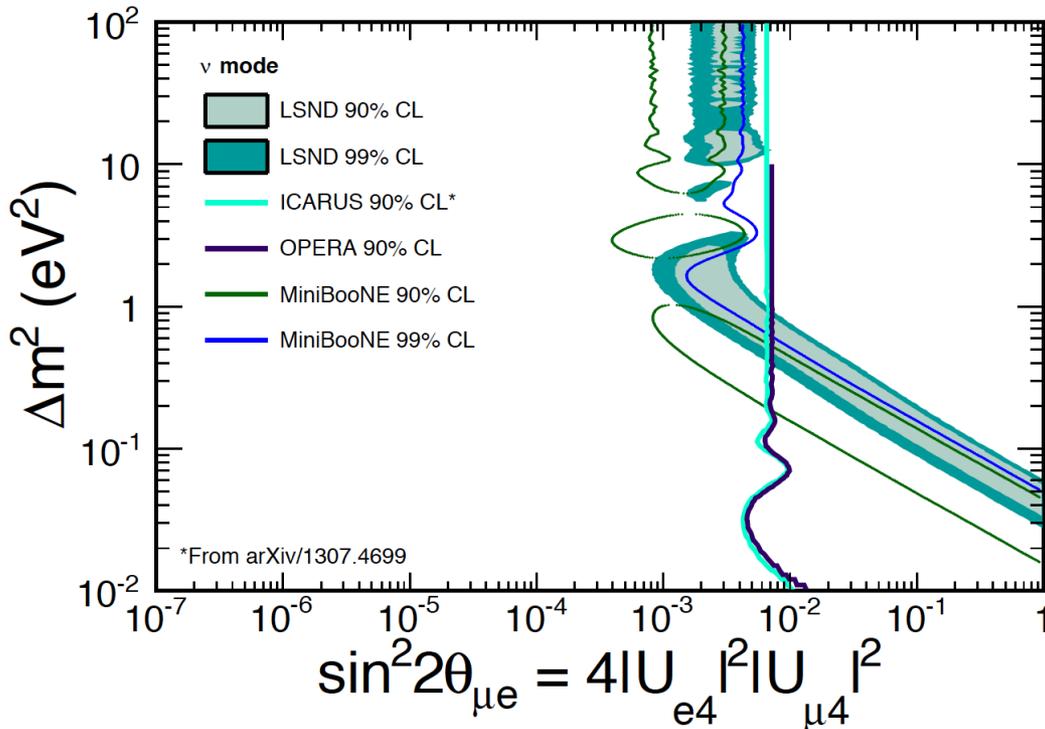


# A fourth neutrino state?

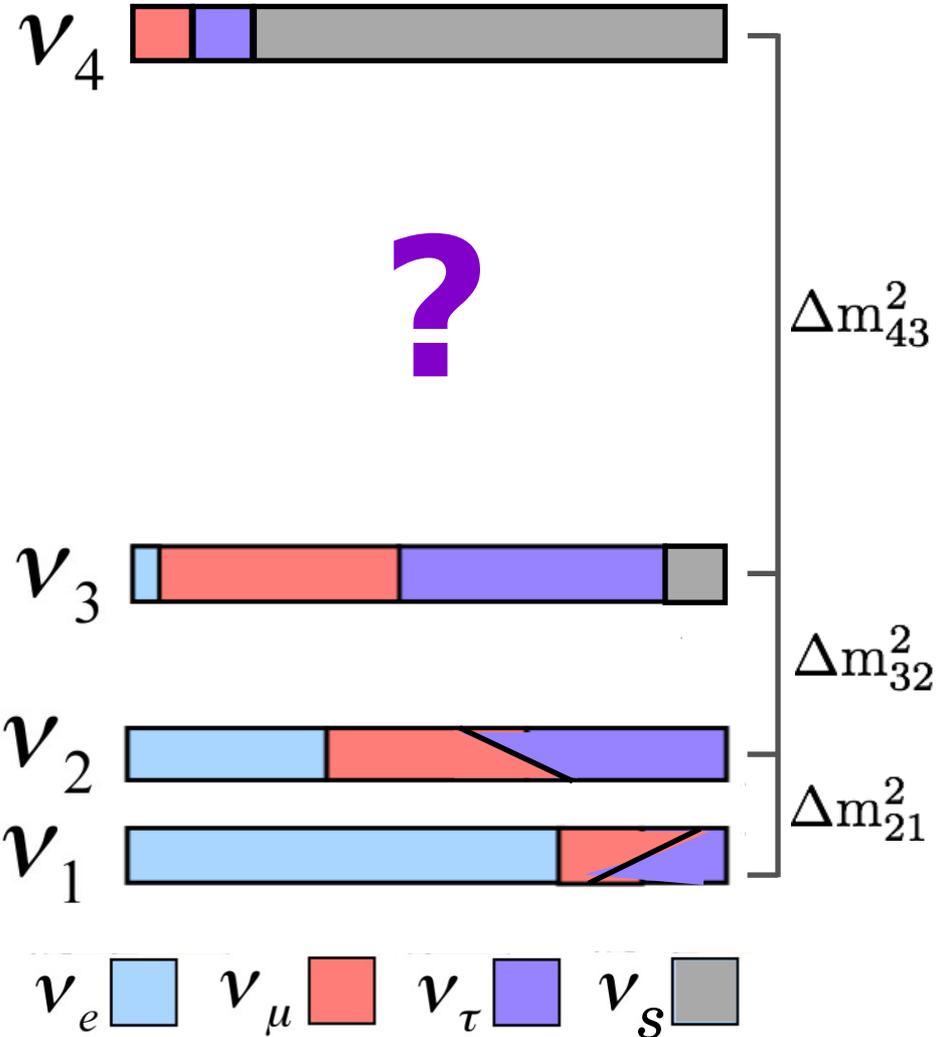
**Anomalies** in: **accelerator**  $\nu_\mu \rightarrow \nu_e$

and **reactor**  $\bar{\nu}_e \rightarrow \bar{\nu}_e$

If oscillations, requires  $\Delta m^2 \gg \Delta m^2_{32}$

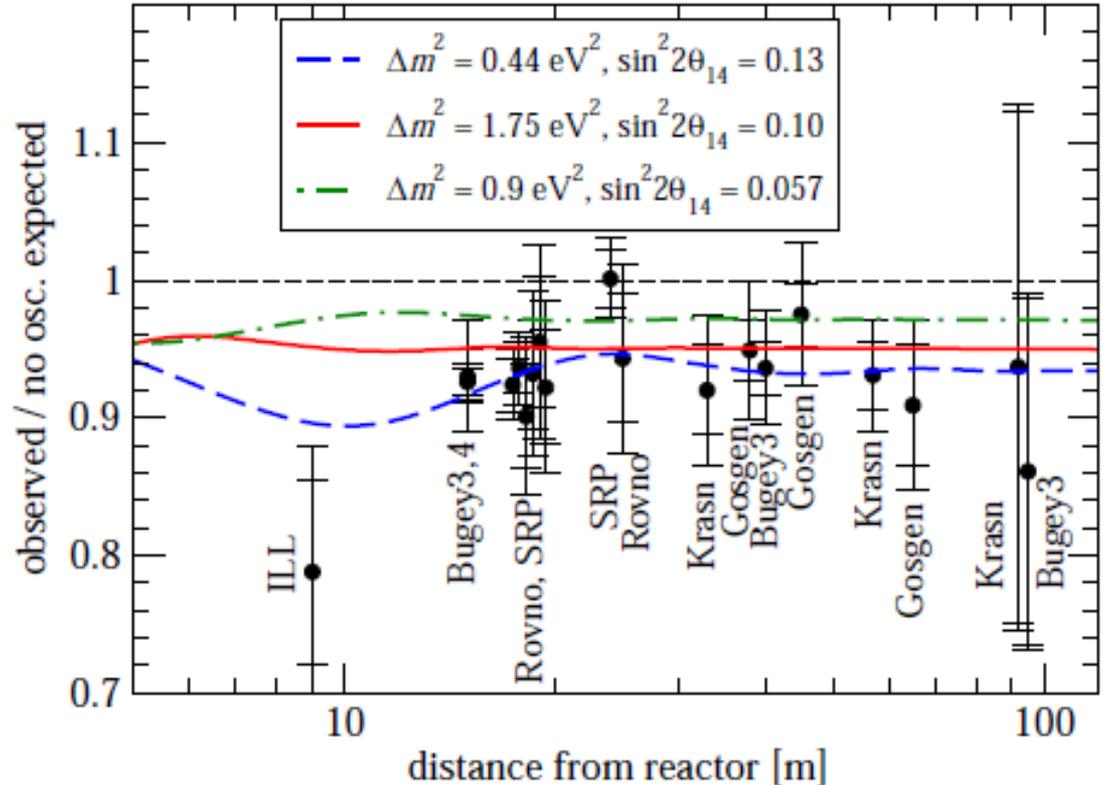
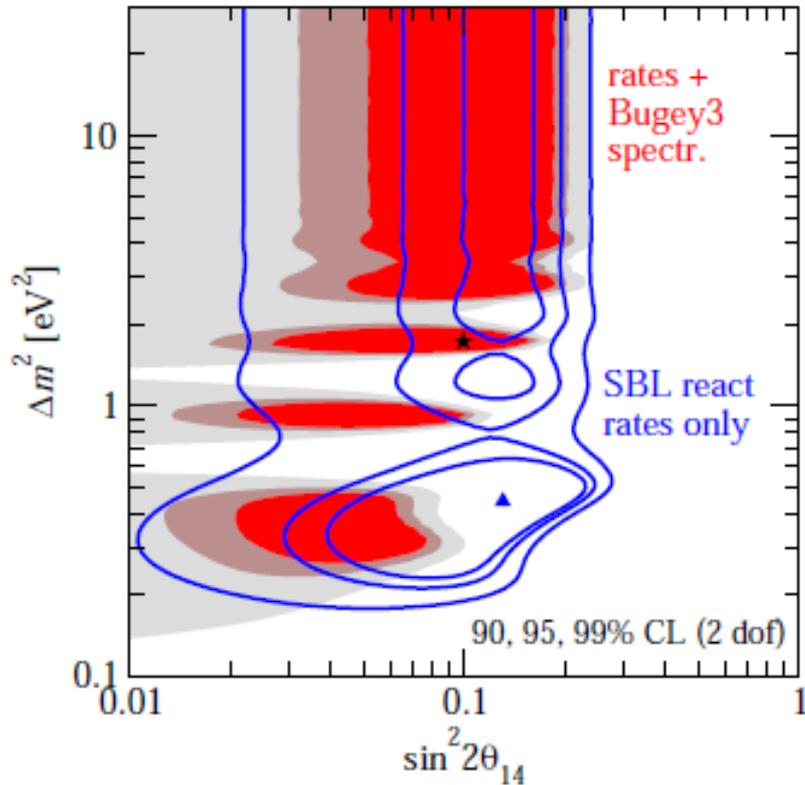


*MiniBooNE, PRL 110, 161801(2013)*



# A fourth neutrino state?

Anomalies in: reactor  $\nu_e \rightarrow \nu_e$



*MiniBooNE, PRL 110, 161801(2013)*

# Adding a 4<sup>th</sup> neutrino

$$U_{3+1} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{bmatrix}$$

Example:  
 $U_{\mu4} = \cos \theta_{14} \sin \theta_{24}$   
 $= c_{14} s_{24}$

Three new mixing angles

$$\theta_{14}, \theta_{24}, \theta_{34}$$

Two new phases

$$\delta_{14}, \delta_{24}$$

Phases come packaged with angles  $\sin \theta_{24} e^{i\delta_{24}}$

# Phenomenology: $\nu_\mu \rightarrow \nu_\mu$

$$\Delta_{ij} = \frac{\Delta m_{ij}^2 L}{4E}$$

General form for survival probability

$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - 4 \sum_{i=1}^4 \sum_{j < i} |U_{\alpha i}|^2 |U_{\alpha j}|^2 \sin^2 \Delta_{ji}$$

Look at  $\nu_\mu$  disappearance for the case  $\Delta m_{43}^2 \gg \Delta m_{31}^2$  and expand to second order in  $s_{13}$ ,  $s_{14}$  and  $s_{24}$ :

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - \sin^2 2\theta_{23} \cos 2\theta_{24} \sin^2 \Delta_{32} - \sin^2 2\theta_{24} \sin^2 \Delta_{43}$$

Therefore,  $\theta_{24}$  controls disappearance driven by the sterile state

# Phenomenology: $\nu_\mu \rightarrow \nu_s$

Disappearance of NC events = sterile appearance

$$P(\nu_\mu \rightarrow \nu_s) \approx c_{14}^4 c_{34}^2 \sin^2 2\theta_{24} \sin^2 \Delta_{43} \\ + A \sin^2 \Delta_{32} + B \sin 2\Delta_{32}$$

A and B are a big mess, but to first order:

$$A = s_{34}^2 \sin^2 2\theta_{23}$$

$$B = \frac{1}{2} \sin \delta_{24} s_{24} \sin 2\theta_{34} \sin 2\theta_{23}$$

The oscillation probability also gets modified at the L/E where standard 3 flavor oscillations occur

# Oscillation Regimes

A)  $10^{-3} < \Delta m_{43}^2 < 10^{-1} \text{ eV}^2$

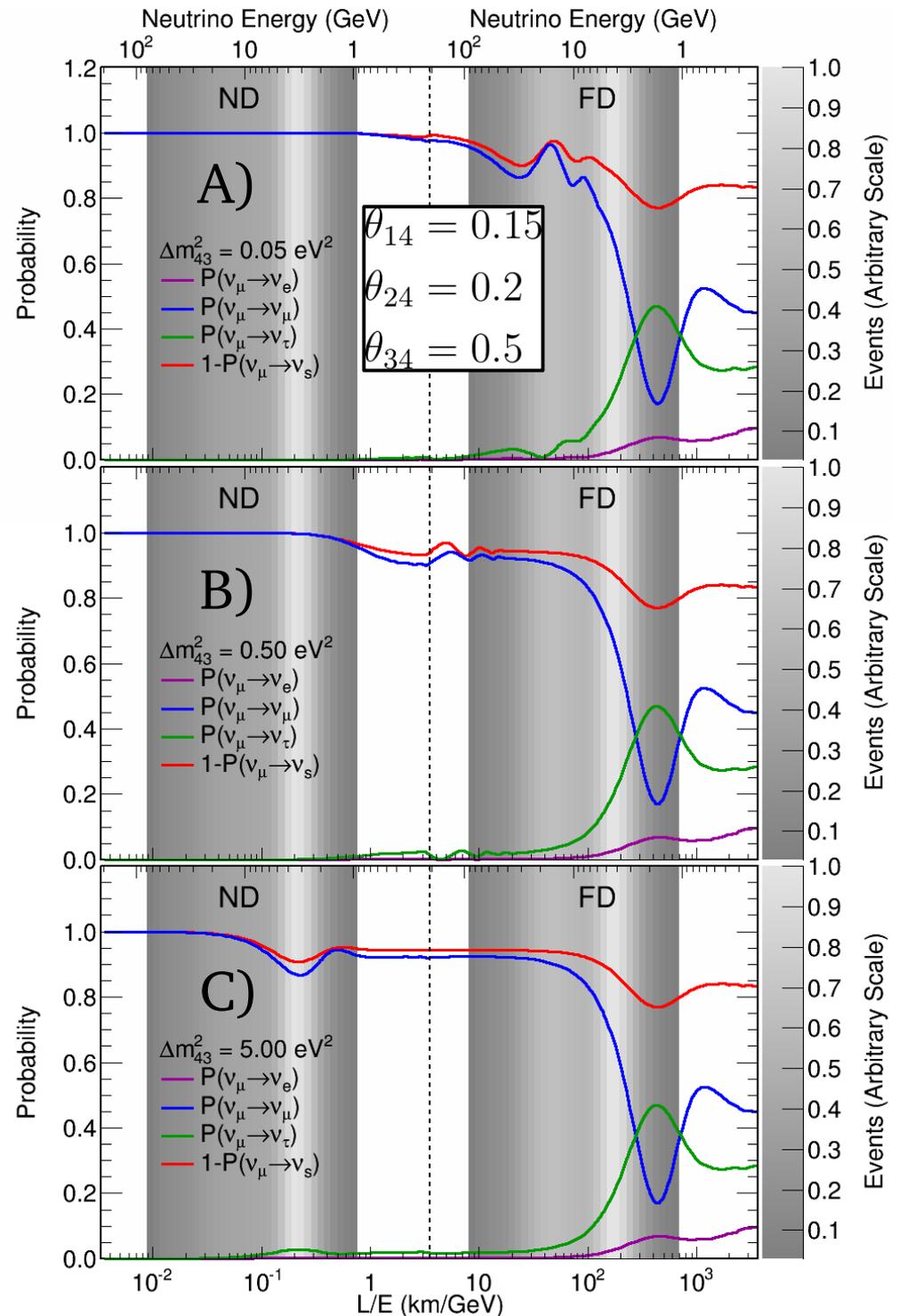
- i) Energy dependent depletion at high energy in FD but ND unaffected
- ii) Use ND to predict FD as usual

B)  $10^{-1} < \Delta m_{43}^2 < 1 \text{ eV}^2$

- i) Fast oscillations at the FD. Energy independent depletion.
- ii) No effect at the ND
- iii) “counting experiment”

C)  $\Delta m_{43}^2 > 1 \text{ eV}^2$

- i) Oscillations begin to occur at the ND
- ii) Fast oscillations at the FD.
- iii) Cannot use ND to predict FD.



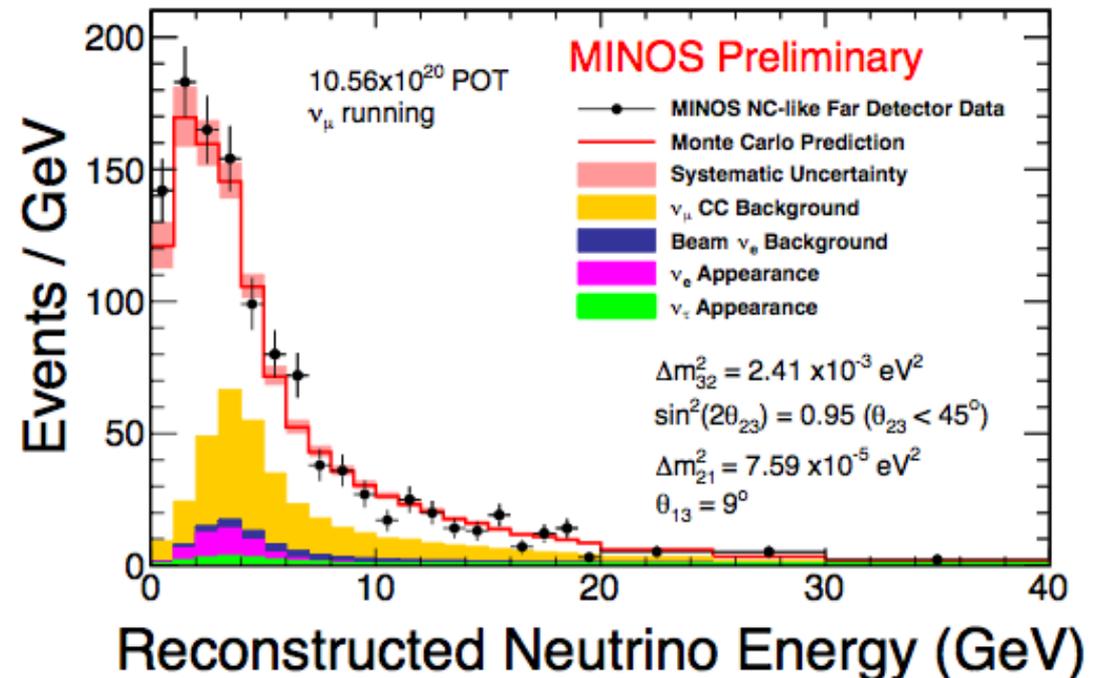
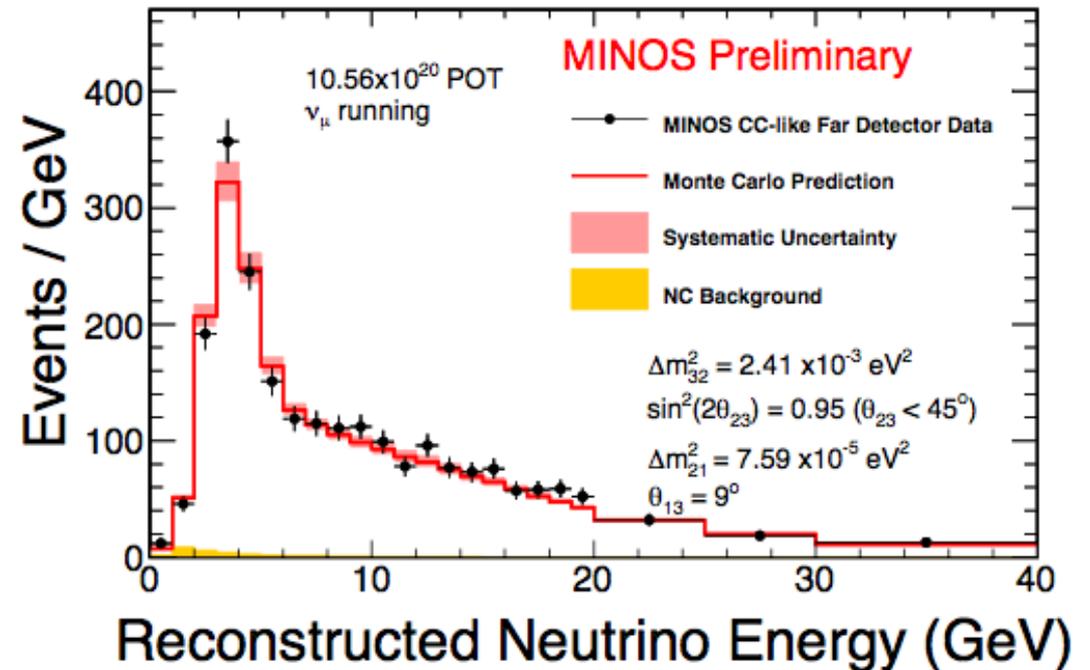
# FD energy spectra

Comparison with the null hypothesis: 3 flavors only

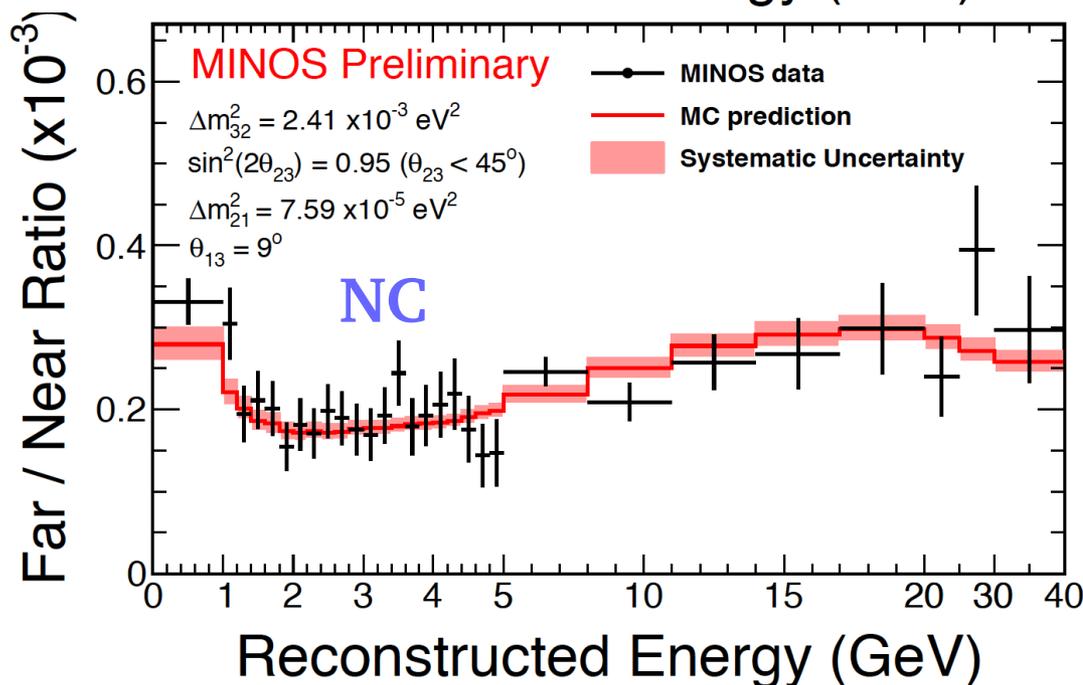
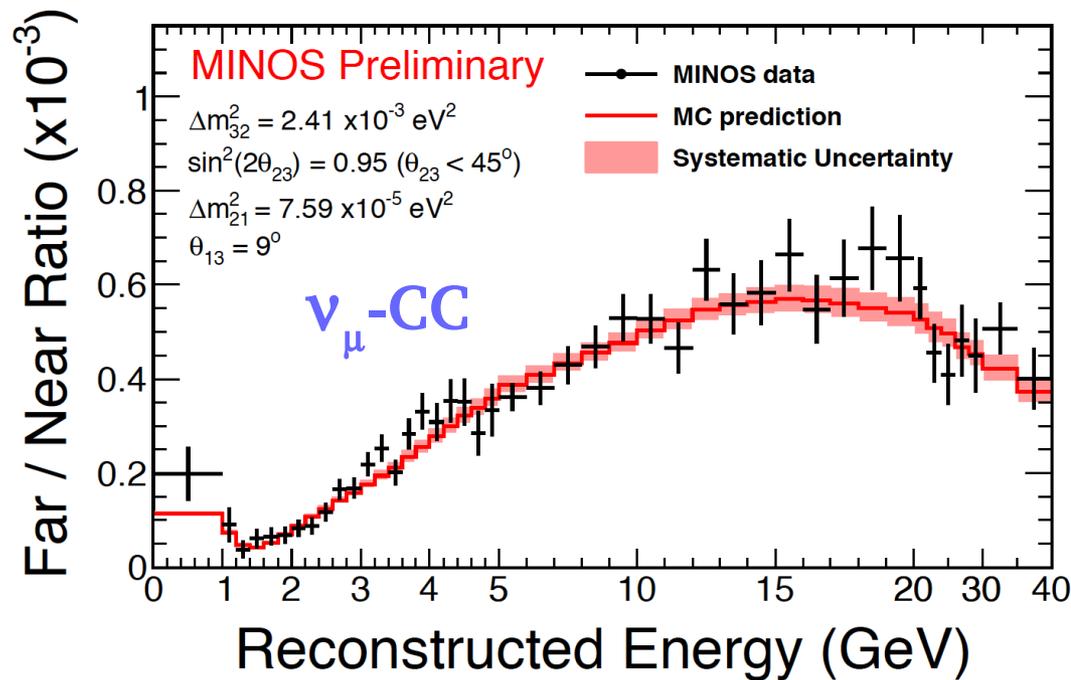
2721 CC events  
1221 NC events

Slight excess of NC in the FD.

Important: FD prediction tuned to ND here.



# Analysis Strategy



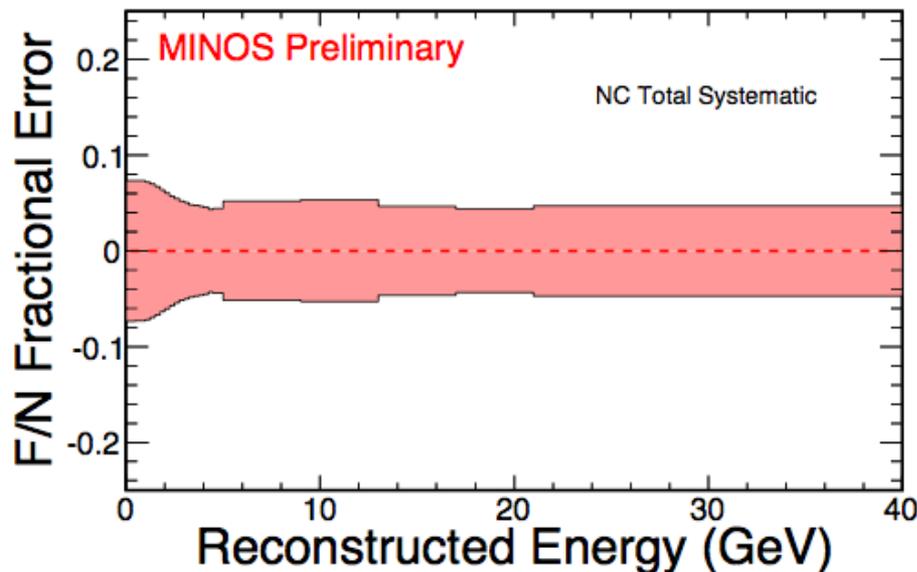
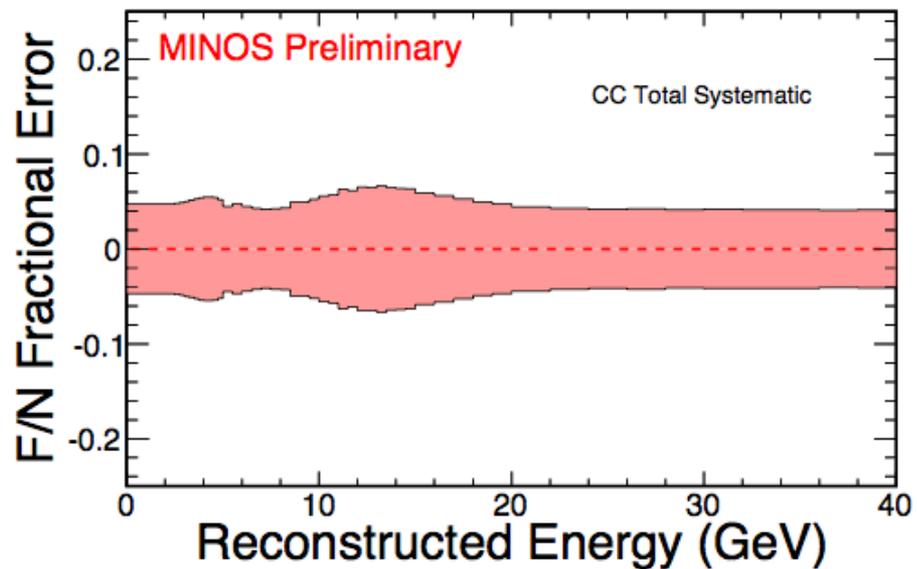
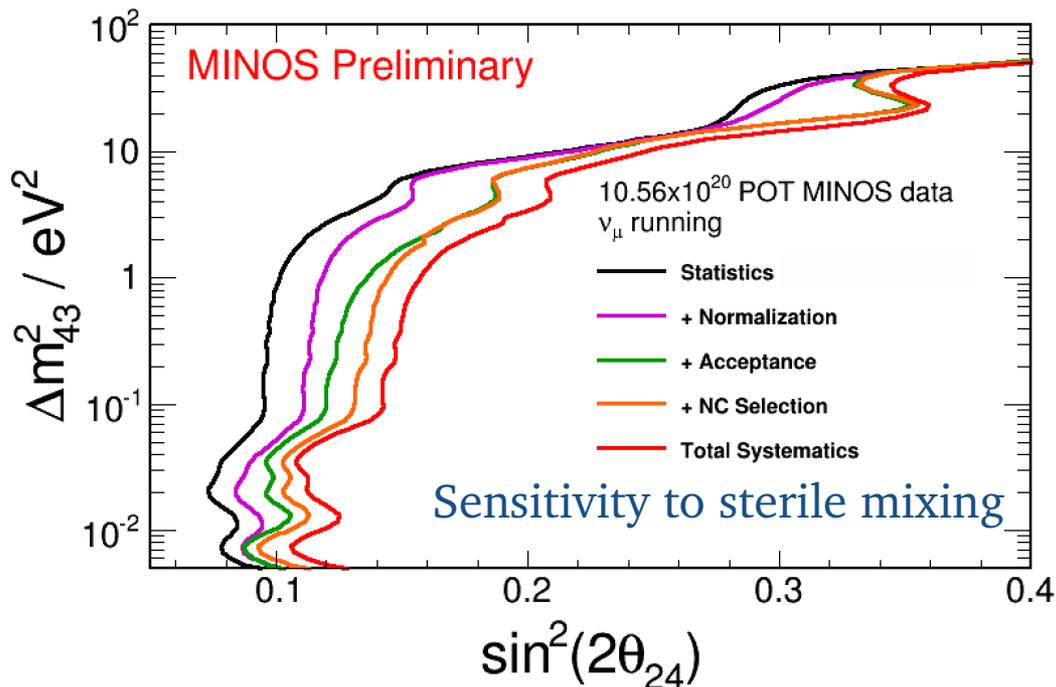
- Key observable is the ratio Far/Near
  - Sensitive to wiggles in either detector
  - Insensitive to fast oscillations in both detectors
- Strategy:
  - fit Far/Near for CC and NC samples to extract  $\theta_{24}$  and  $\Delta m_{43}^2$  as well as  $\theta_{23}$ ,  $\Delta m_{32}^2$ , and  $\theta_{34}$
  - Penalty terms for  $\theta_{13}$ ,  $\theta_{12}$  and  $\Delta m_{21}^2$  informed by global fits
  - Set  $\theta_{14}$  and CP phases to zero
  - Assign an uncertainty of 40% to the overall rate in the ND

# Systematics

Worries:

- 1) anything that causes a “wobble” in E
- 2) overall normalization effects

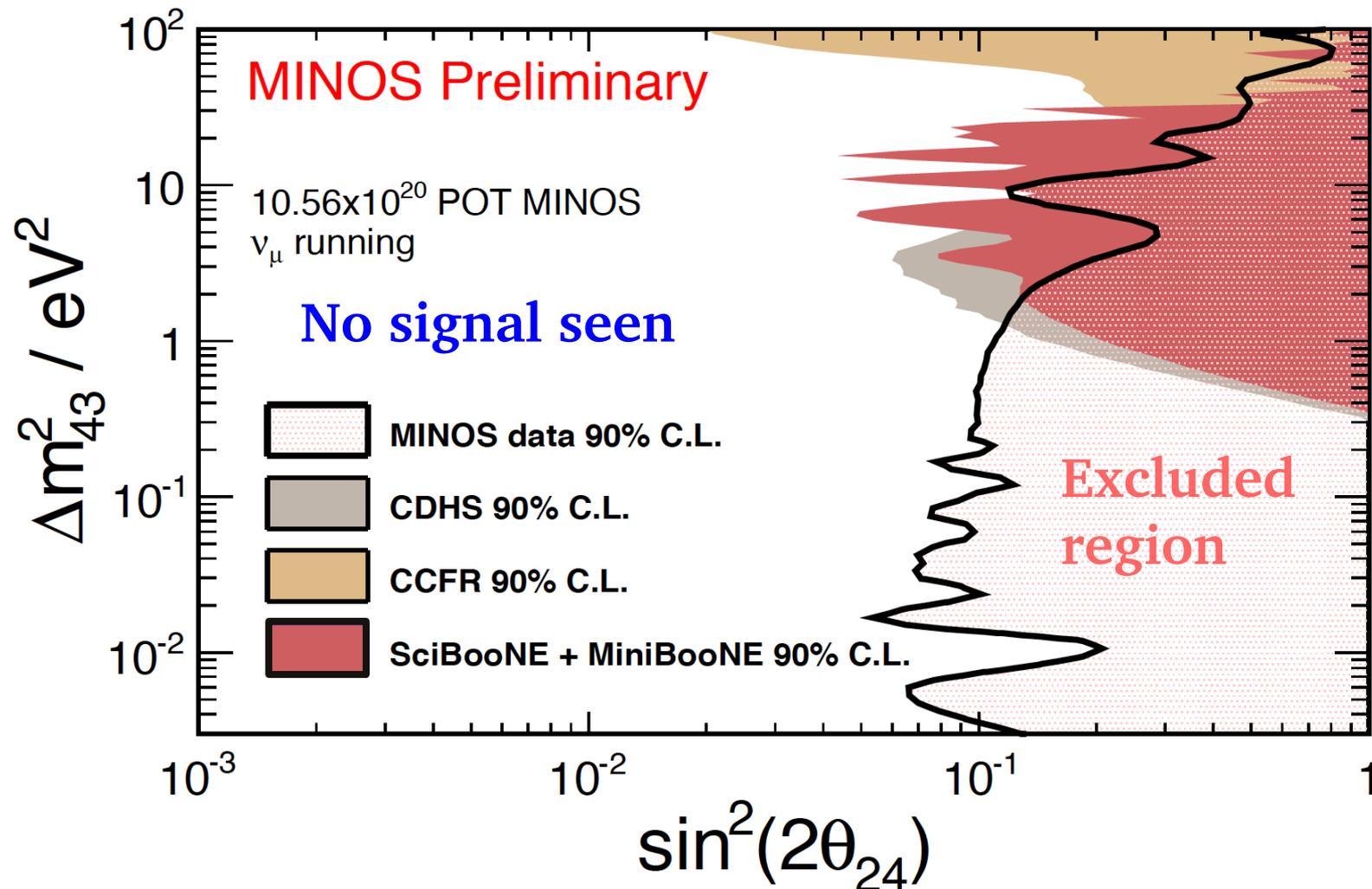
Assessed 26 different systematics.



# Results

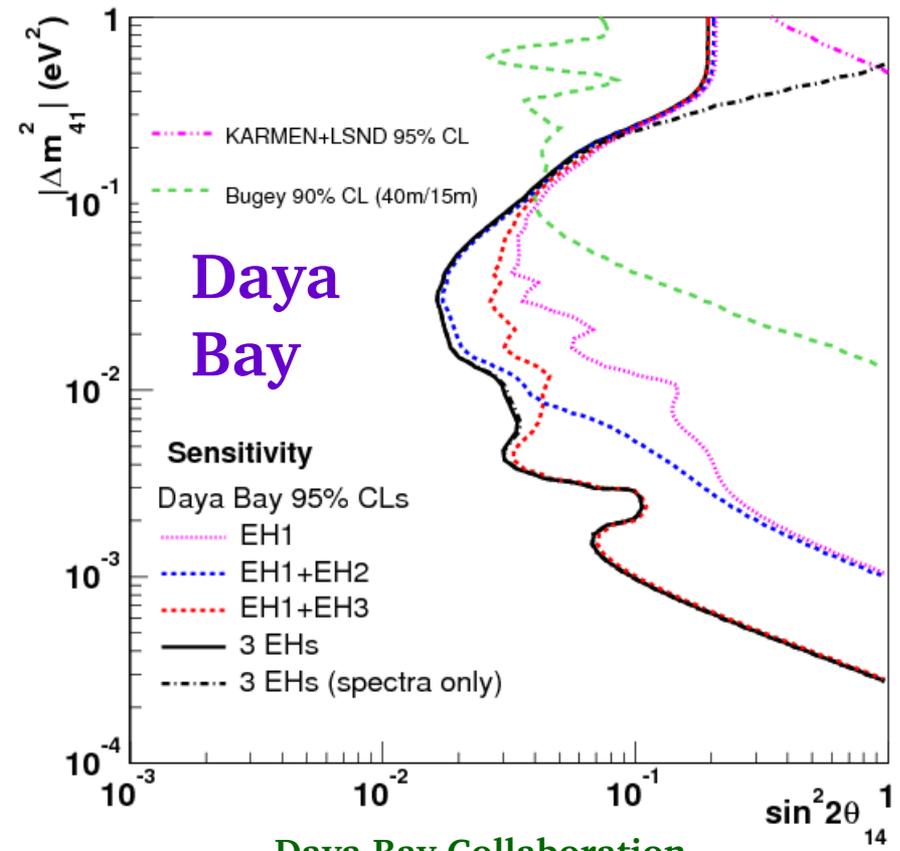
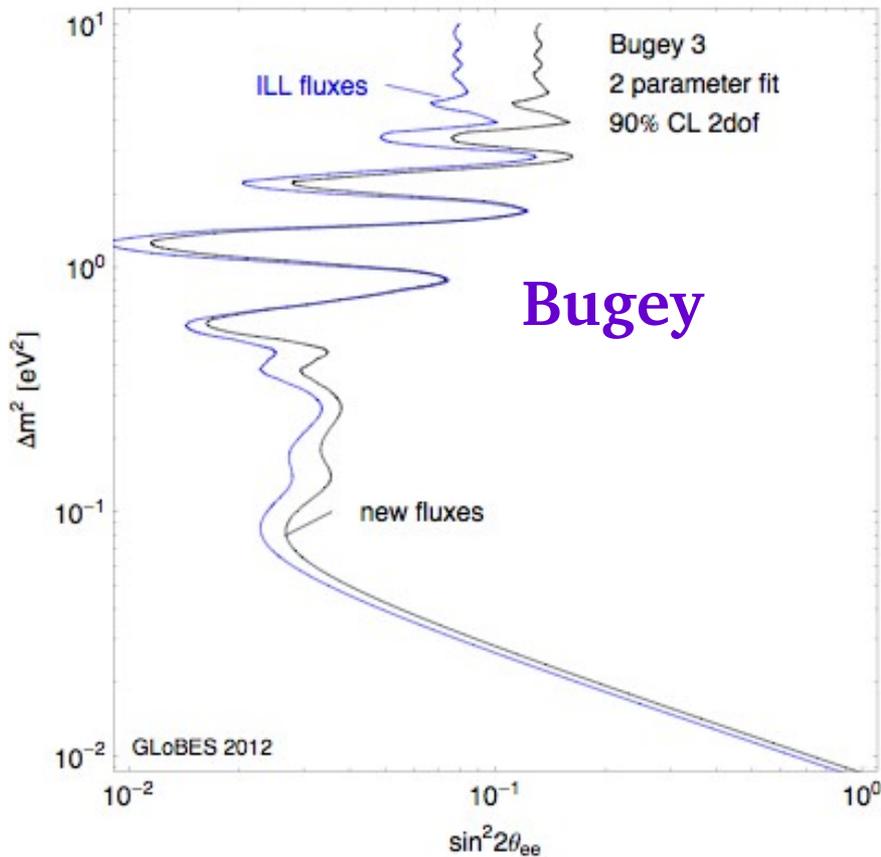
Fit with a bin-by-bin stats + systematics covariance matrix.

Fit is “global” with confidence intervals set by pseudo experiments (Feldman-Cousins “modified frequentist procedure”).



# Reactor neutrino constraints

Reactor  $\nu_e$  disappearance is similar to accelerator  $\nu_\mu$  disappearance, but constrains  $\theta_{14}$  instead of  $\theta_{24}$



Daya Bay Collaboration

Phys.Rev.Lett. 113 (2014) 141802

# Combining $\nu_e \rightarrow \nu_e$ and $\nu_\mu \rightarrow \nu_\mu$

## Major takeaway

$\nu_\mu \rightarrow \nu_e$  requires both

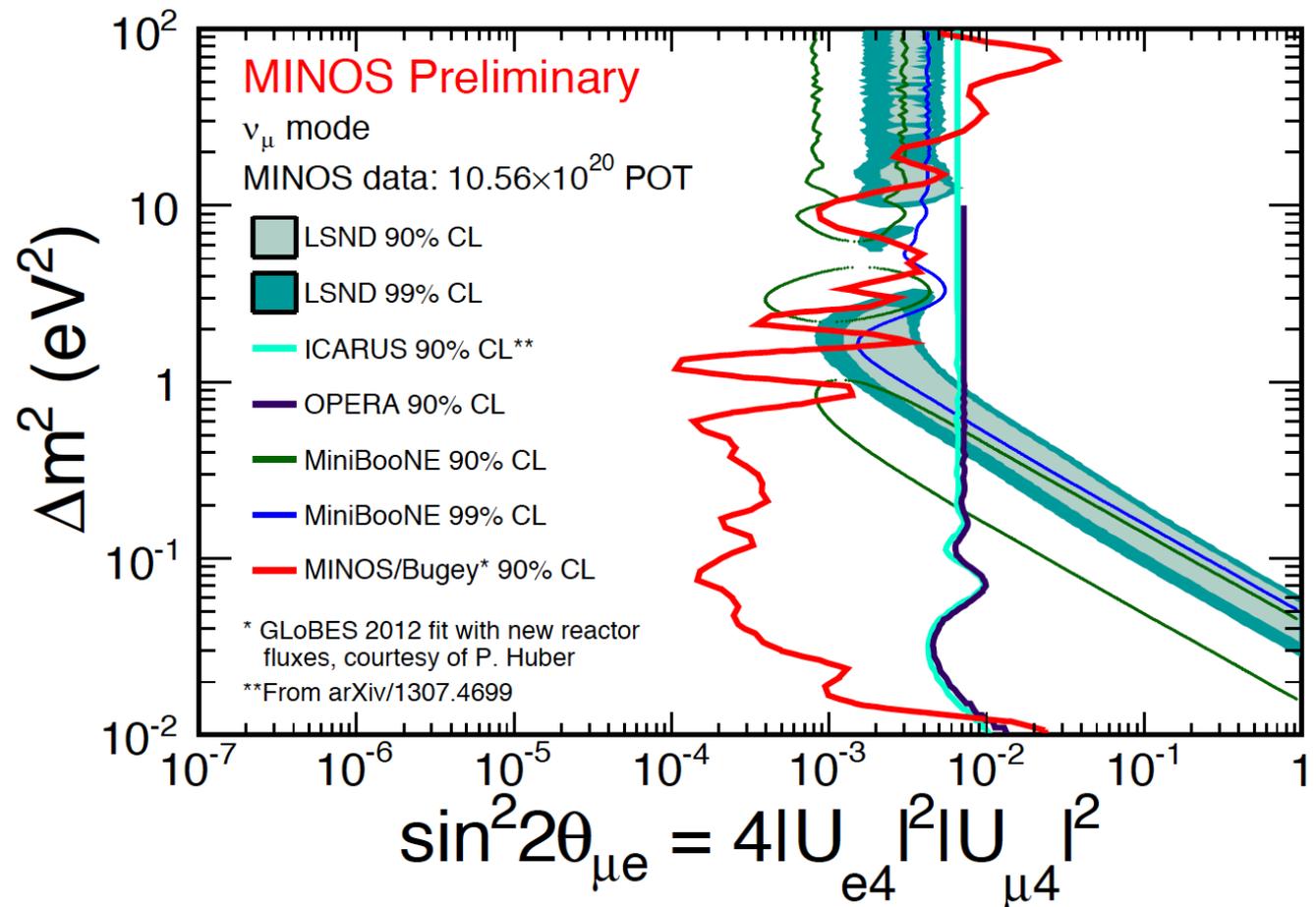
$\nu_\mu \rightarrow \nu_\mu$  and  $\nu_e \rightarrow \nu_e$

- Combine MINOS and Bugey results to constrain MiniBooNE and LSND
- MINOS + Daya Bay combination in the works

*Oscillation probability for MiniBooNE and LSND*

$$P(\nu_\mu \rightarrow \nu_e) \approx 4|U_{\mu 4}|^2|U_{e 4}|^2 \sin^2 \Delta_{41}$$

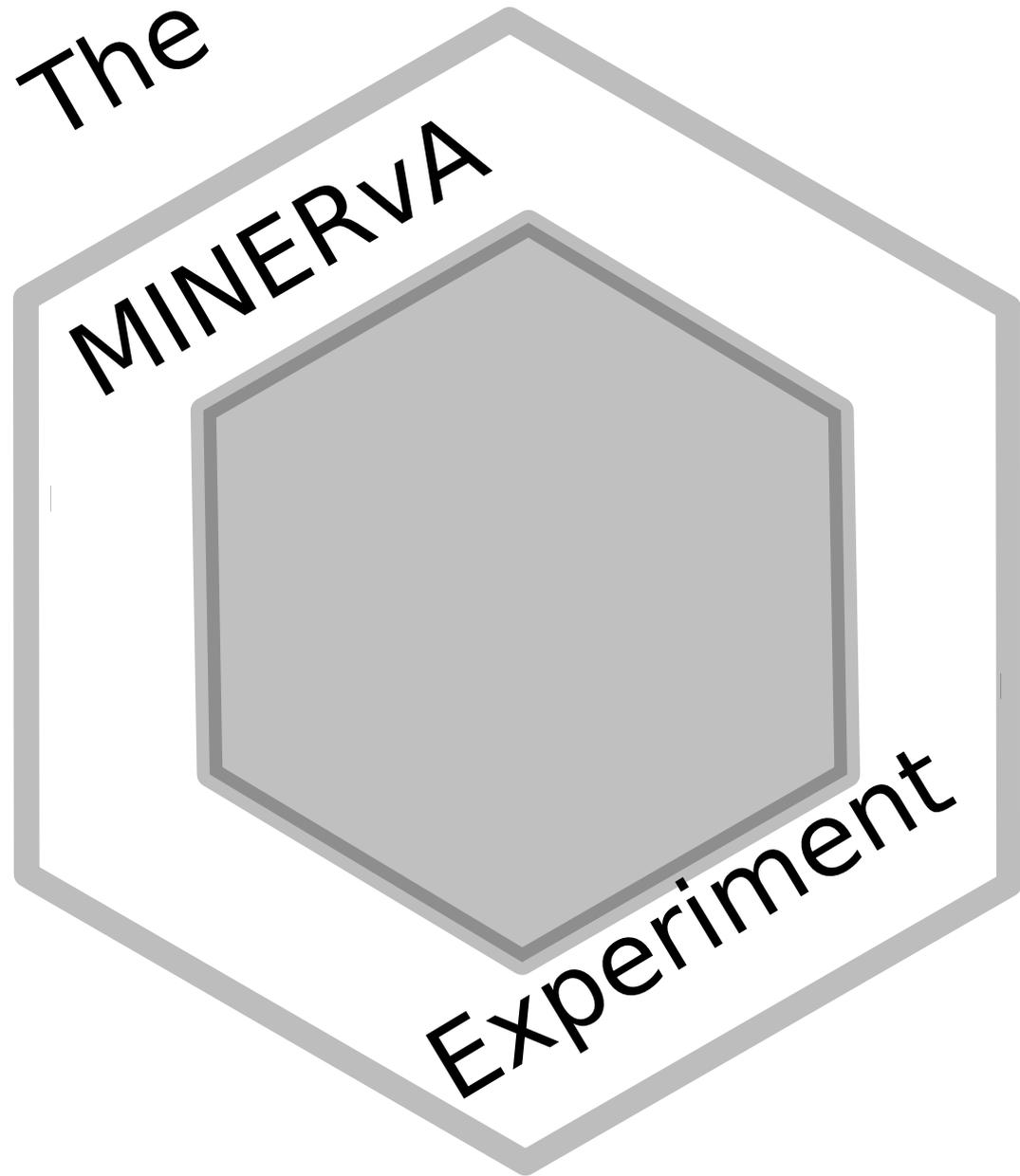
$$= 4s_{14}^2 c_{14}^2 s_{24}^2 \sin^2 \Delta_{41}$$



# Oscillations Summary

- Three flavor oscillations appear to describe world's data very well.
  - Entering era of precision tests, exploration of mass ordering and CP violation.
- Disappearance measurements combine to exclude much of the MiniBooNE / LSND allowed region.
  - In general, sterile driven  $\nu_\mu \rightarrow \nu_e$  requires  $\nu_\mu$  and  $\nu_e$  disappearance.
  - Robust two detector experiments set limits that will be hard to beat, even in the next generation of experiments at FNAL.
  - Possible x2 factor on sensitivity with additional data taking by MINOS +

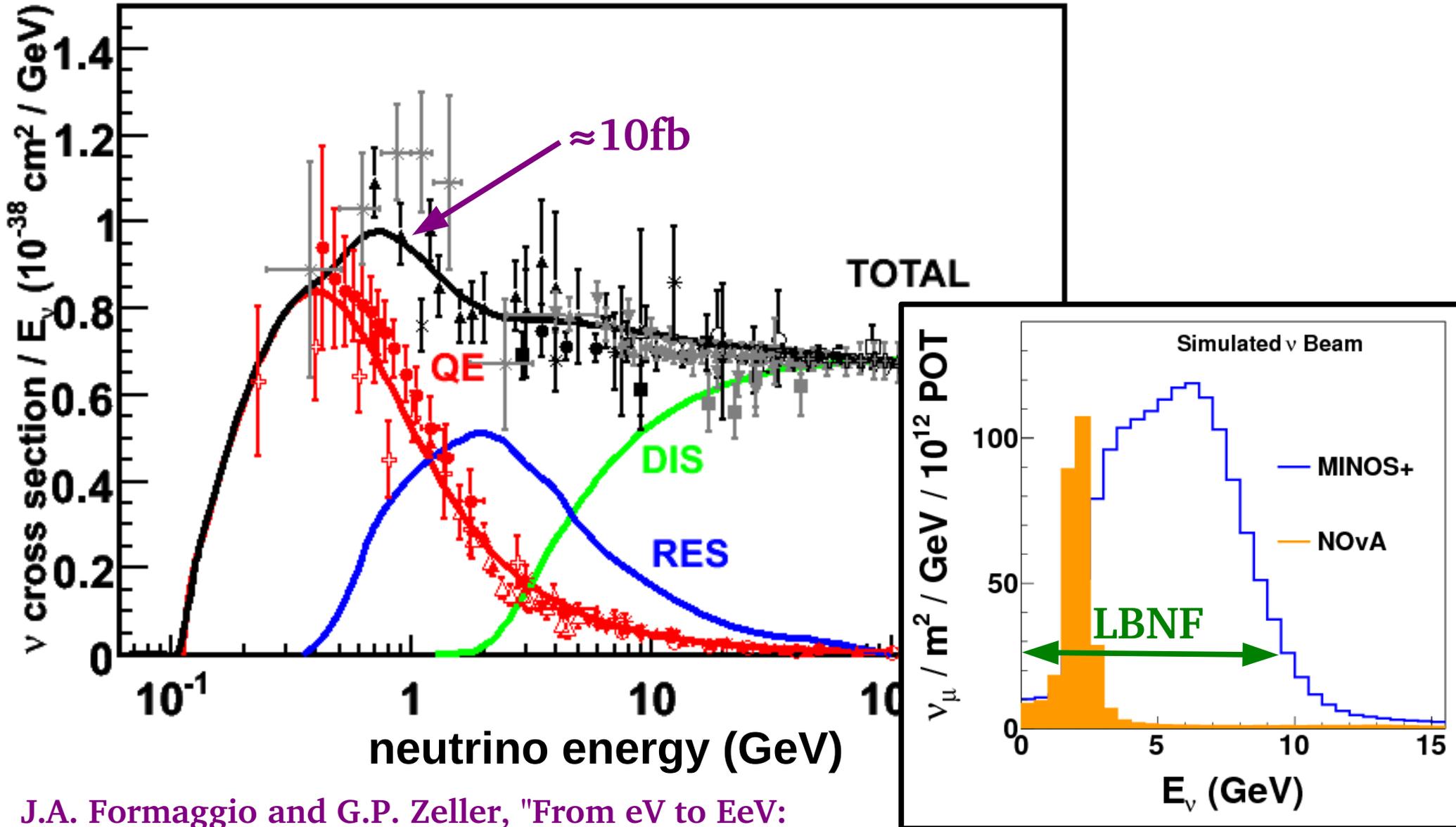
# Cross-sections and



Why are we interested?

# World $\nu_\mu$ cross-section

G. Zeller



J.A. Formaggio and G.P. Zeller, "From eV to EeV: Neutrino Cross Sections Across Energy Scales", Rev. Mod. Phys. 2012

Feb 4, 2015

Mike Kordosky, W<sup>m</sup> & Mary

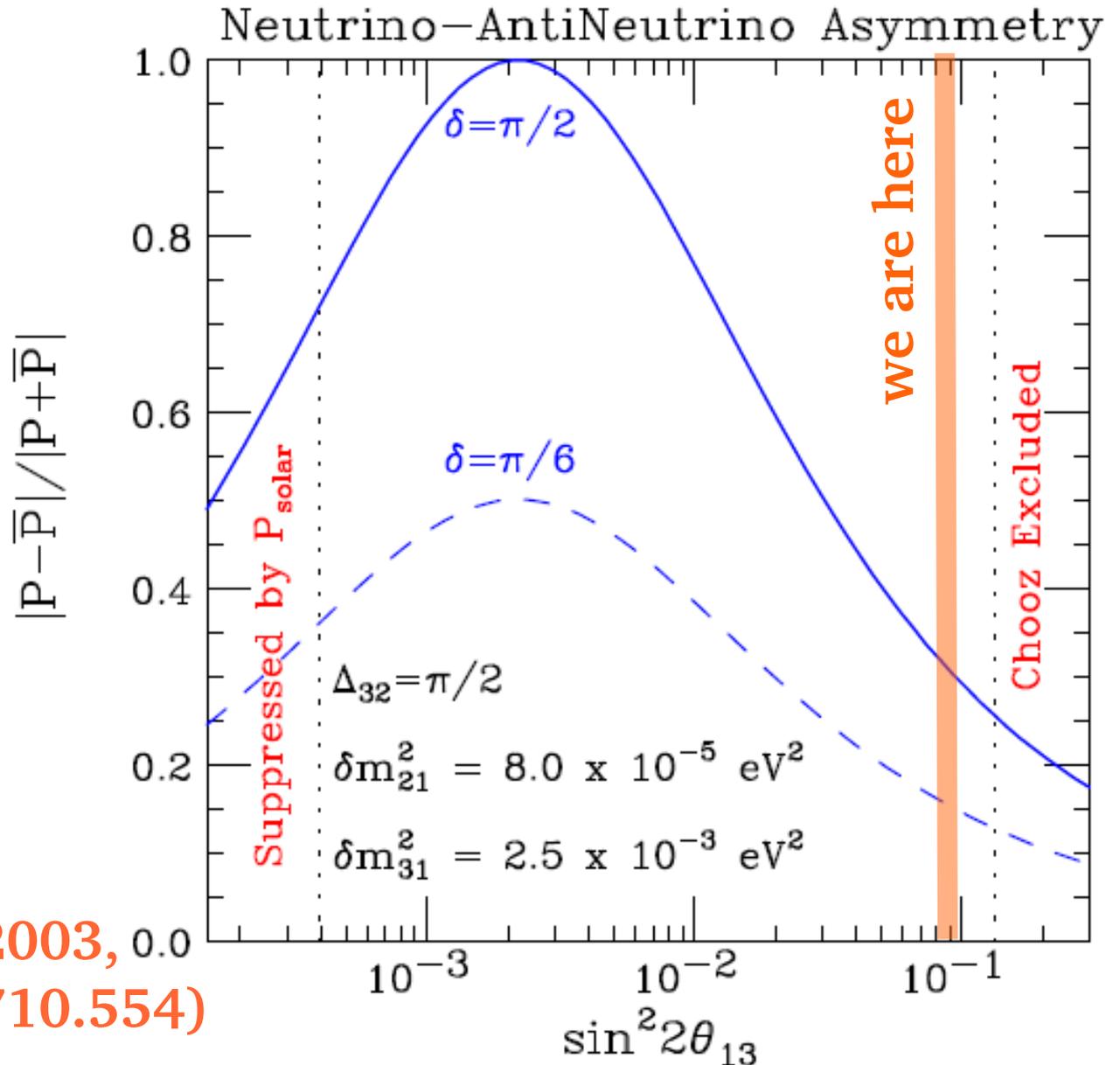
Why are we interested?

# implications of large $\theta_{13}$

Rate of  $\nu_{\mu} \rightarrow \nu_e$   
increases

but  $\nu - \bar{\nu}$   
asymmetry  
decreases

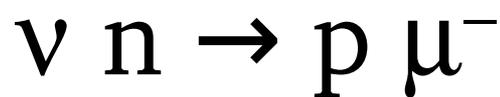
(Parke 2003,  
arXiv:0710.554)



## Why are we interested?

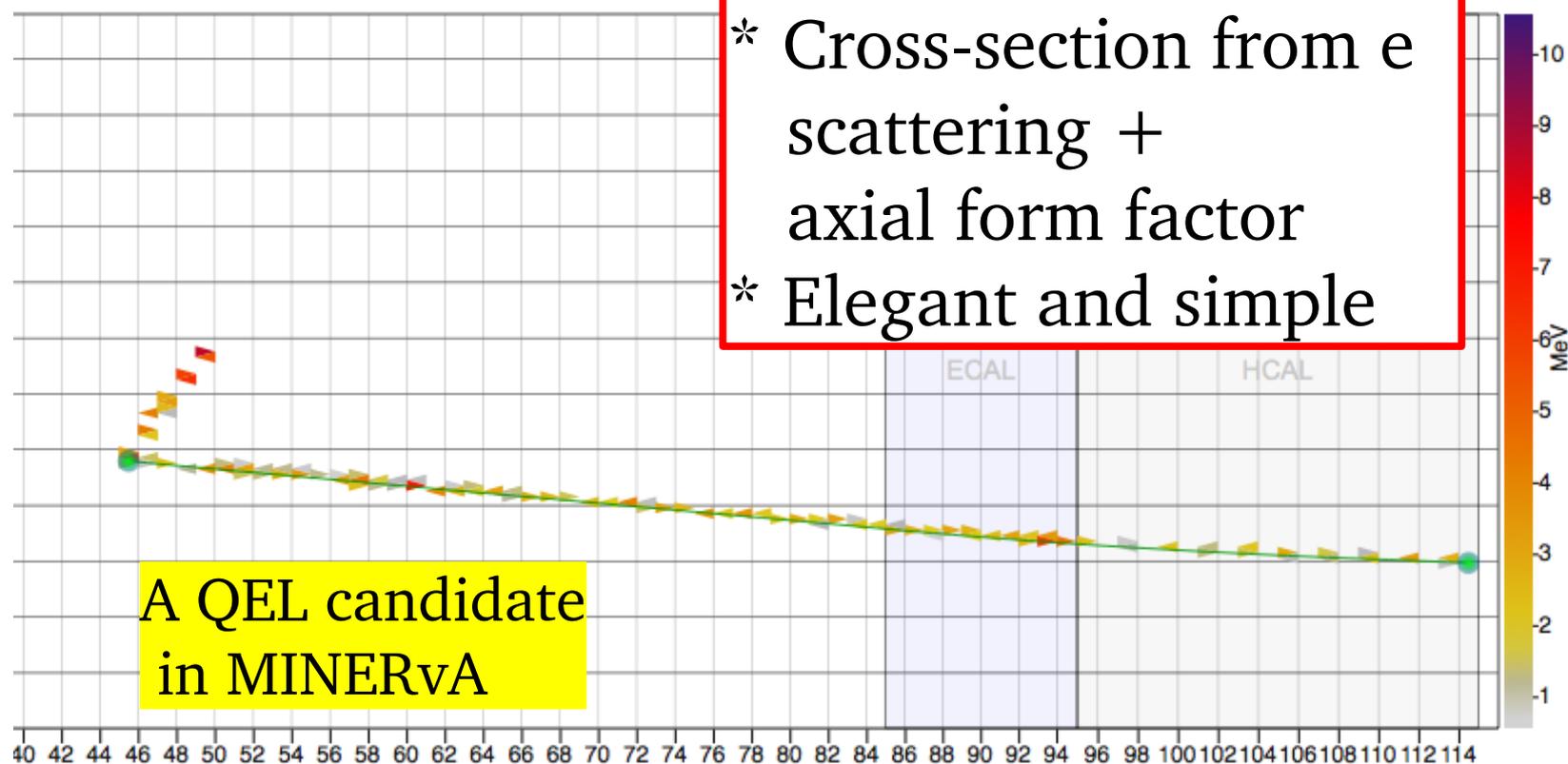
# In search of a standard candle

Quasi-elastic  
scattering



Pros:

- \* Low energy threshold
- \* No messy pions
- \* Energy from 2 of 3  
 $p_\mu$ ,  $\theta_\mu$  or  $p_{\text{proton}}$
- \* Cross-section from e  
scattering +  
axial form factor
- \* Elegant and simple

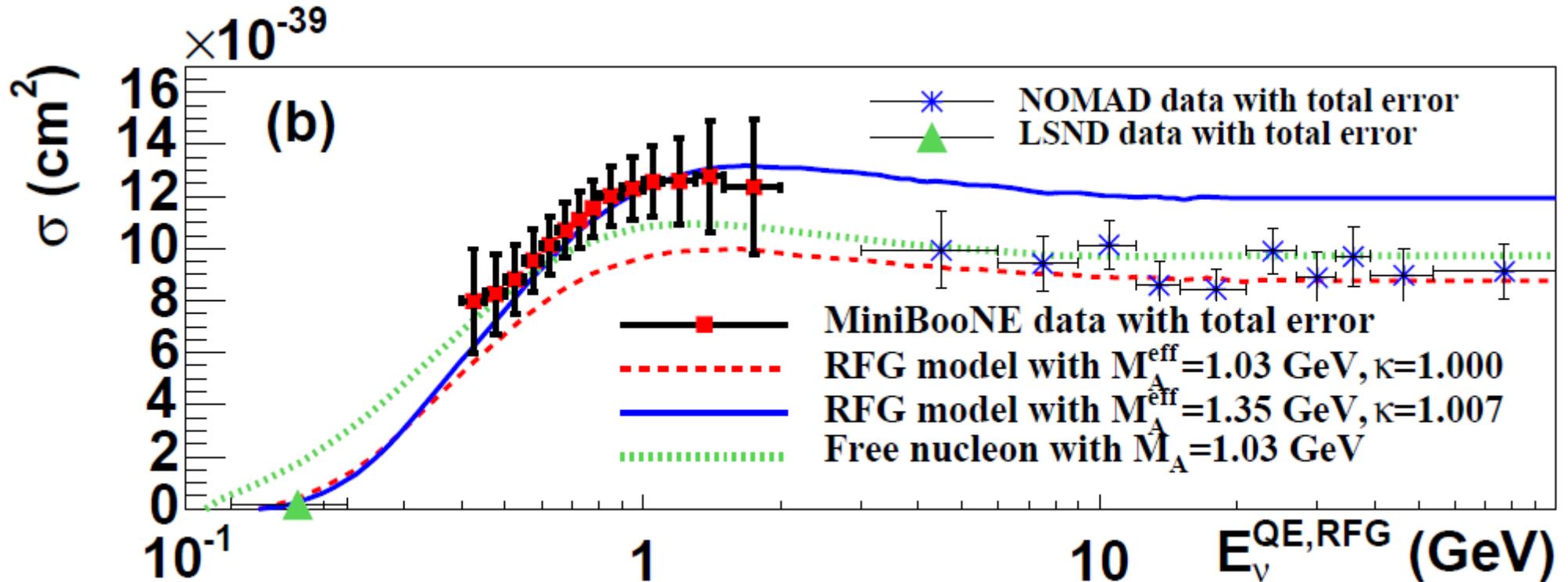


# Why are we interested?

## In search of a standard candle

Quasi-elastic  
scattering

Cons: \* We don't fully understand the energy dependence

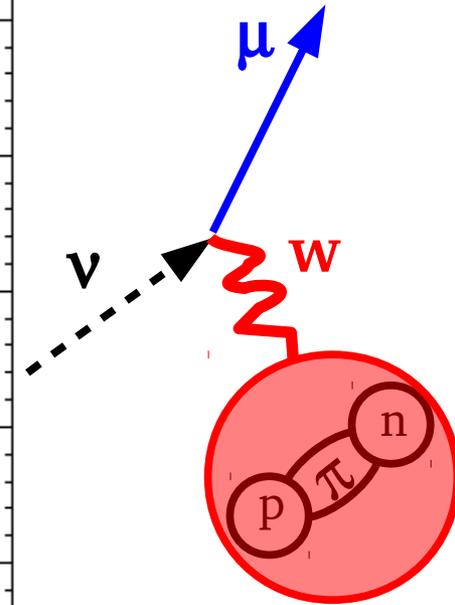
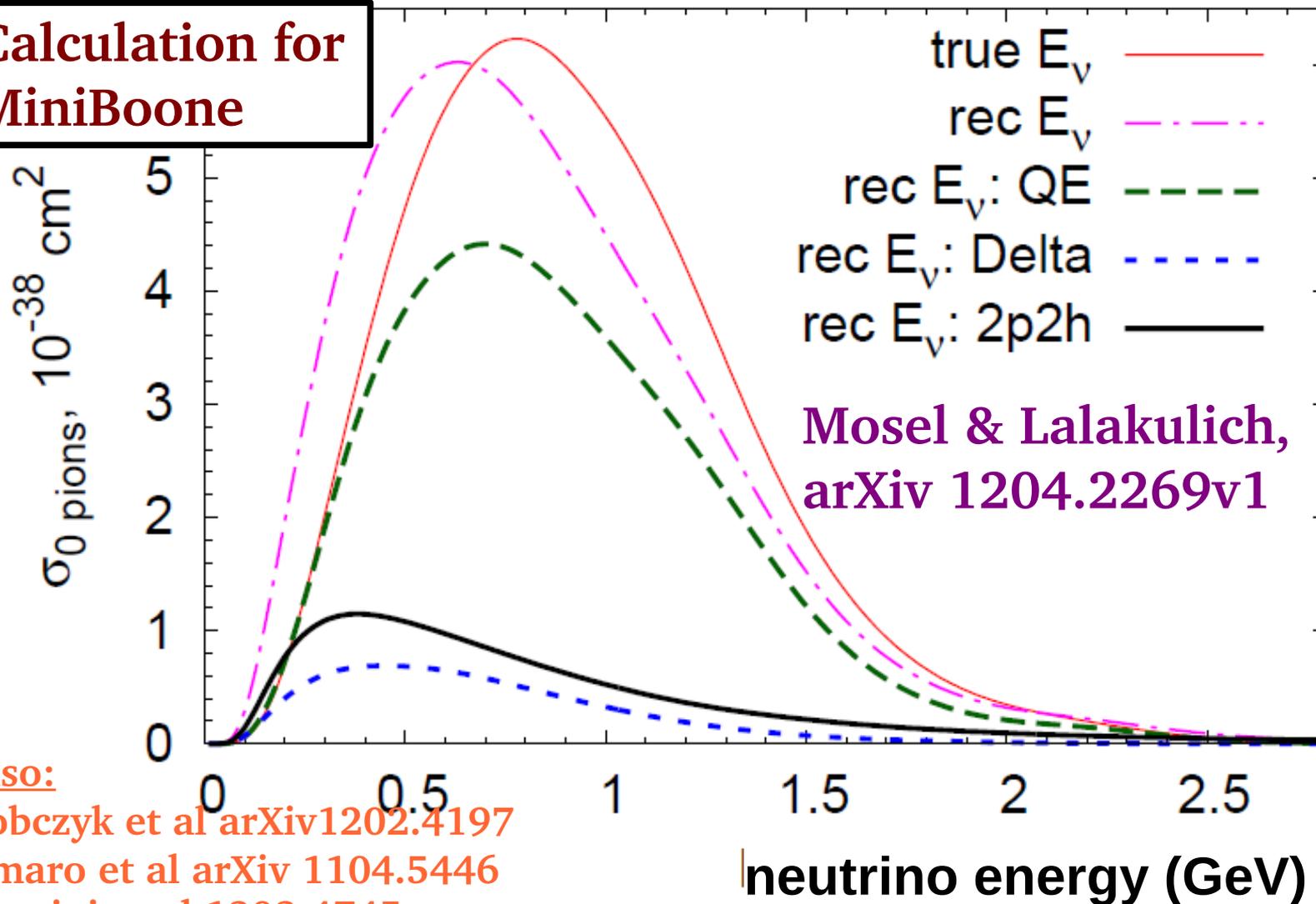


Why are we interested?

# In search of a standard candle

**Cons:** We don't fully understand energy reconstruction

Calculation for  
MiniBoone



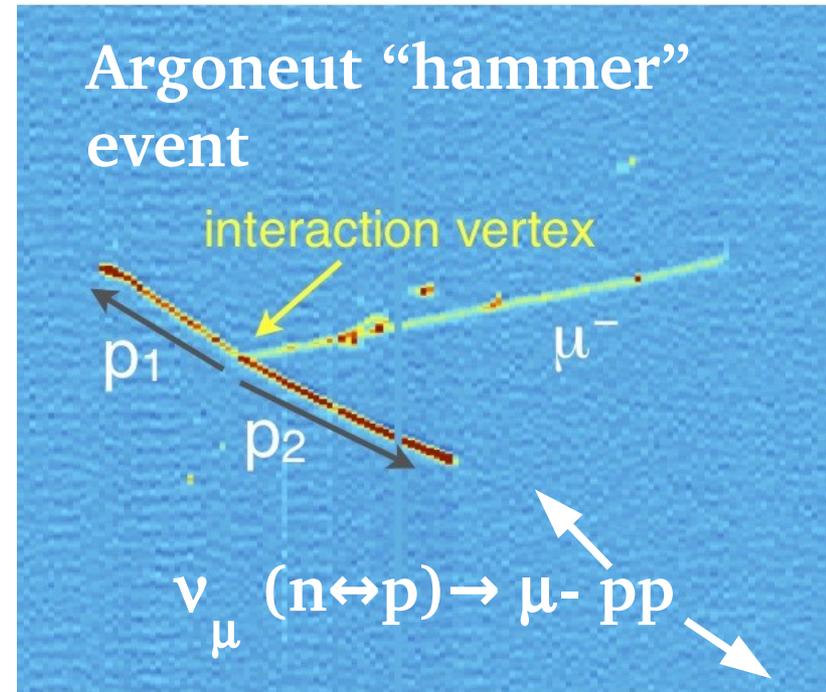
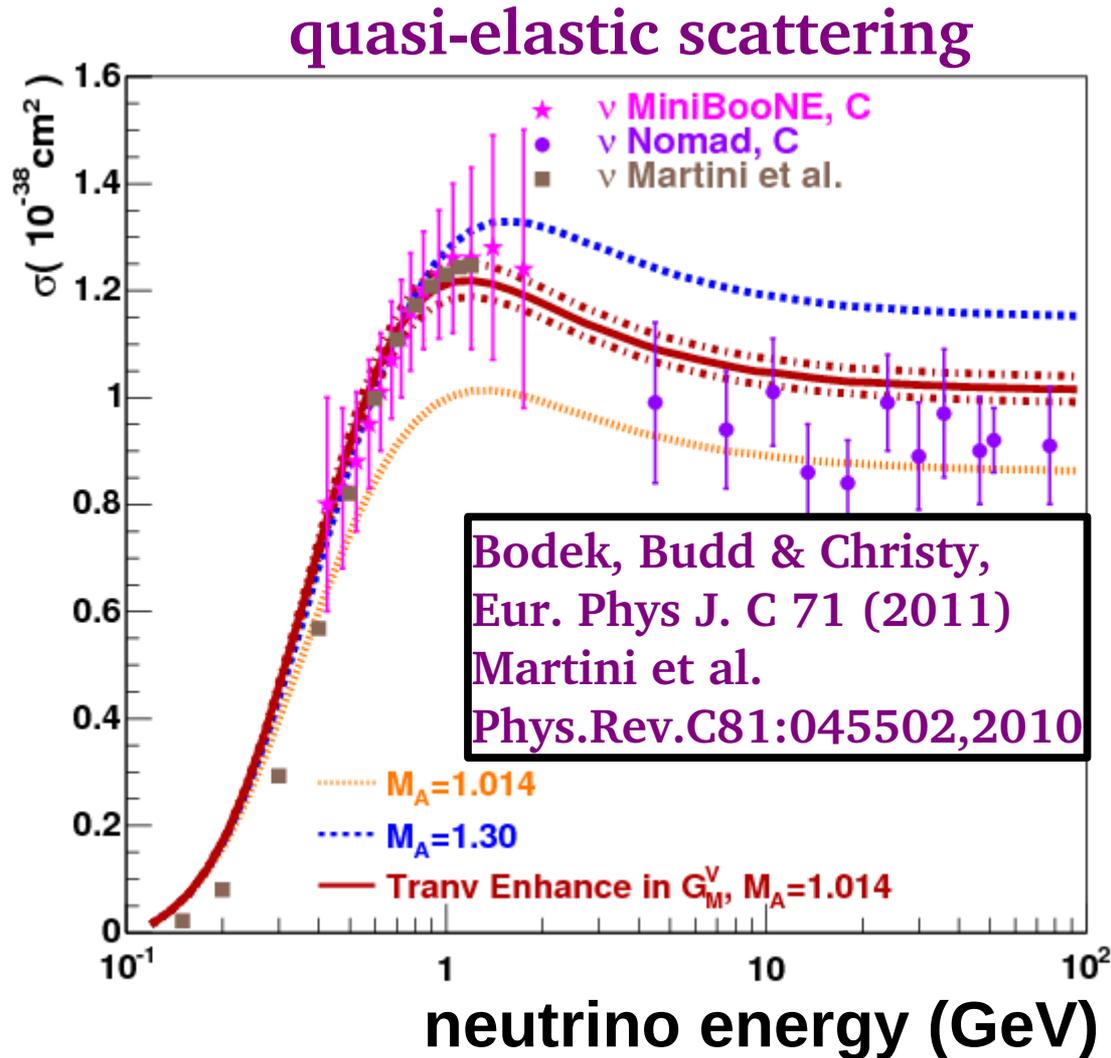
“meson exchange currents”  
also  
“short range correlations”  
“2p2h” 48

Also:  
Sobczyk et al arXiv1202.4197  
Amaro et al arXiv 1104.5446  
Martini et al 1202.4745  
Mosel et al arXiv 1402.0297

Why are we interested?

# In search of a standard candle

Cons: initial nuclear state, multi-body dynamics matter



No pions!  
Looks like QEL if you can't see the protons.

Why are we interested?

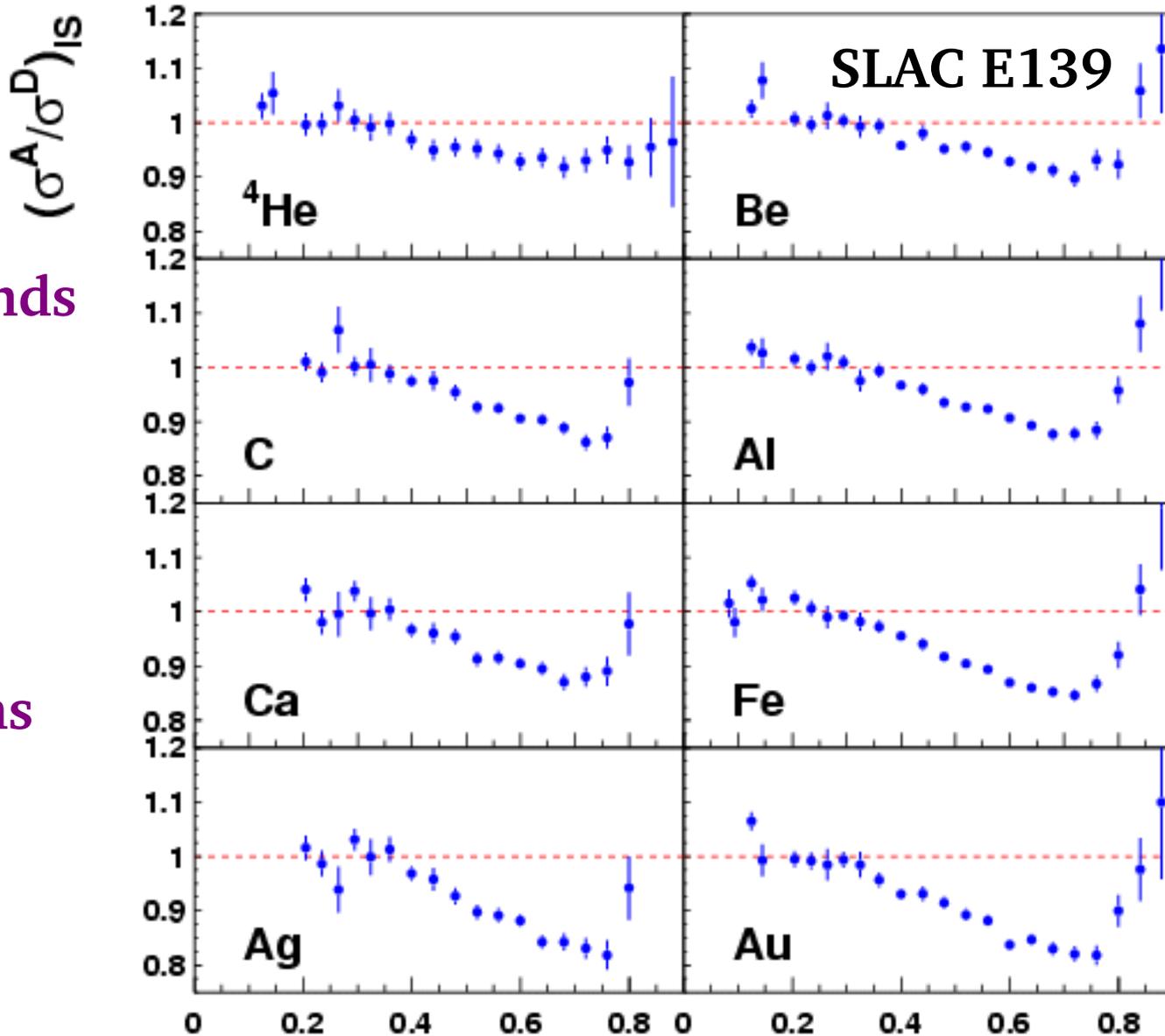
# An old mystery

## “EMC Effect”

x dependence of eA  
DIS cross-section depends  
on A → why?

Some evidence that  $\nu A$   
has different behavior

Short range correlations  
/ multi-body dynamics  
↔ EMC ?

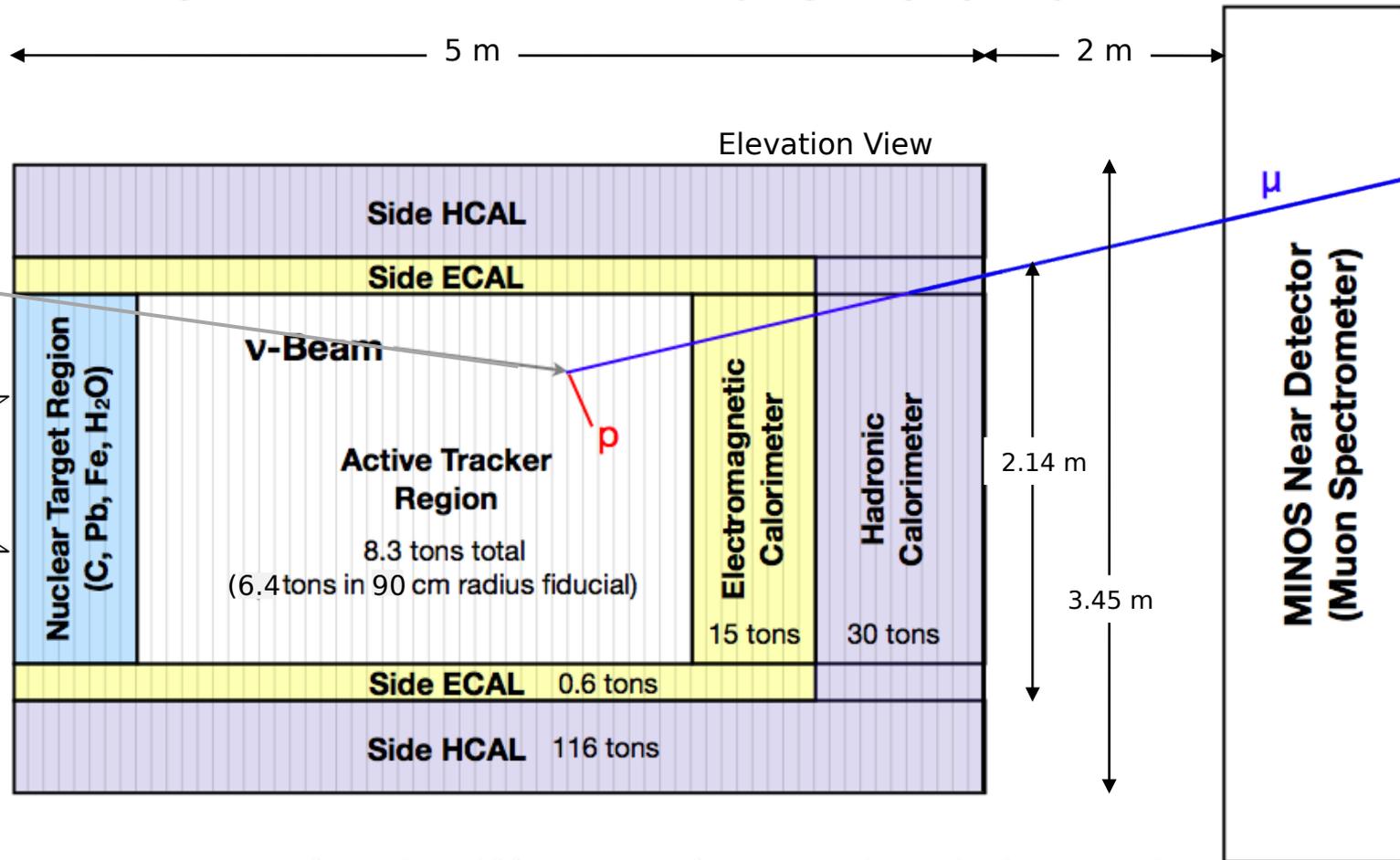


Nice review talk

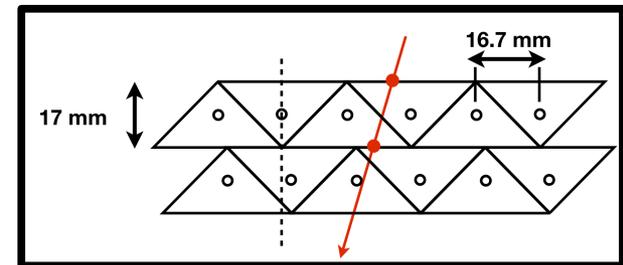
D. Gaskell ECT\*, Trento 2012

<http://www.physics.sc.edu/~strauch/ect2012/index.html>

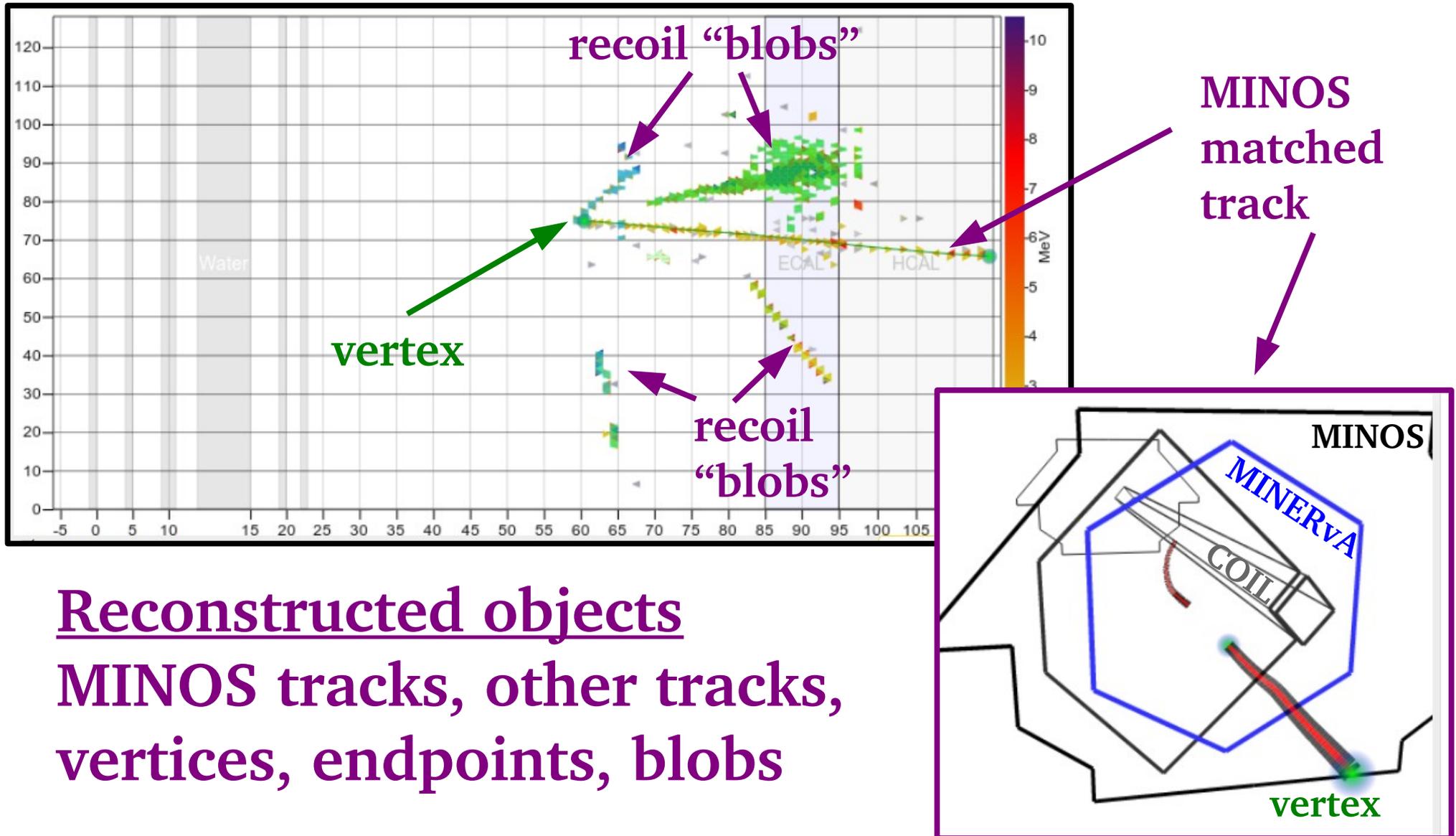
# The MINERvA detector



- \* 200 finely segmented scintillator planes (CH) in 3 views
- \* Calib: FEB bench tests, source mapper, LI, rock  $\mu$ , Michel electrons, test-beam
- \* 4% channel to channel variations after calibration

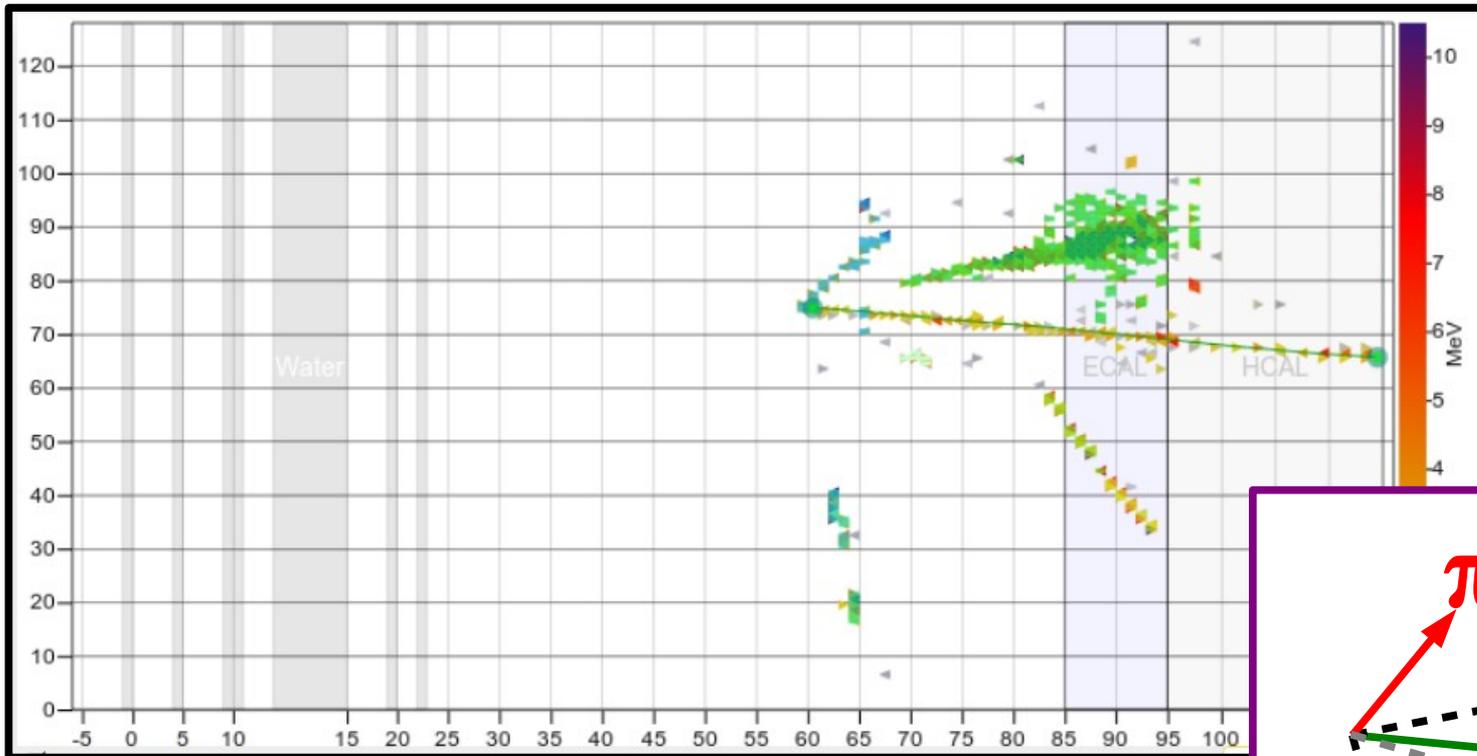


# Event reconstruction



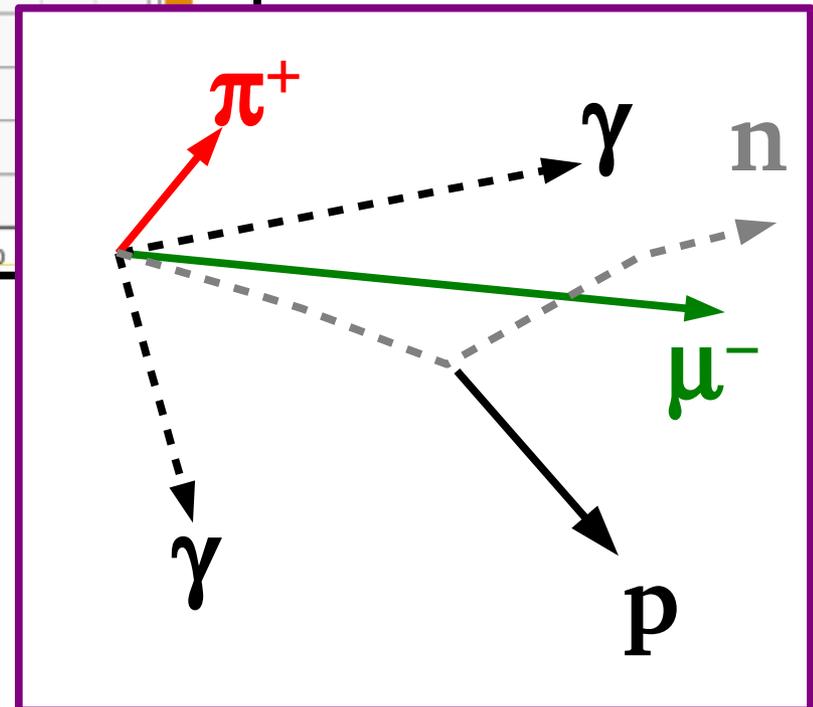
Reconstructed objects  
MINOS tracks, other tracks,  
vertices, endpoints, blobs

# Event reconstruction

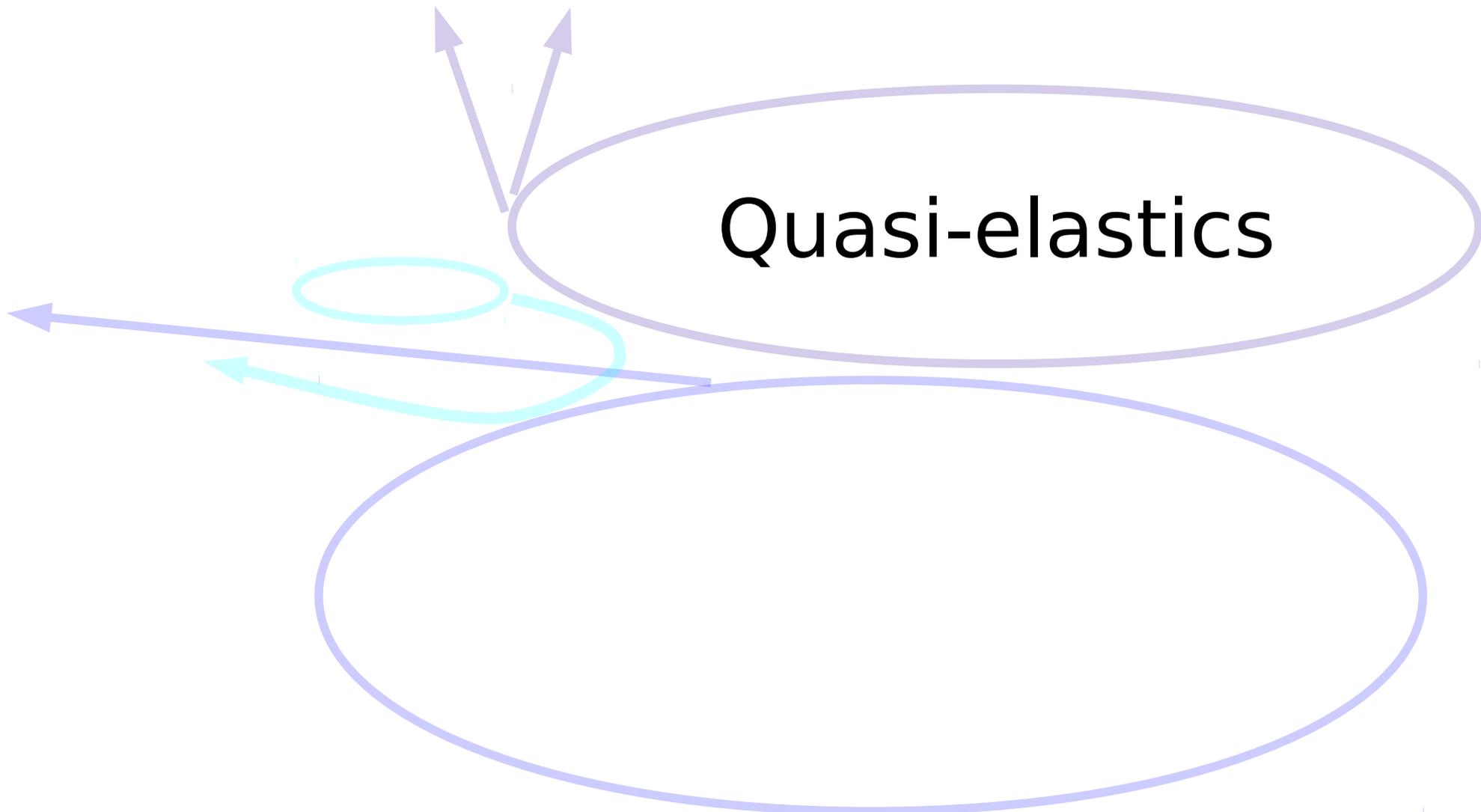


My guess,  
just for fun

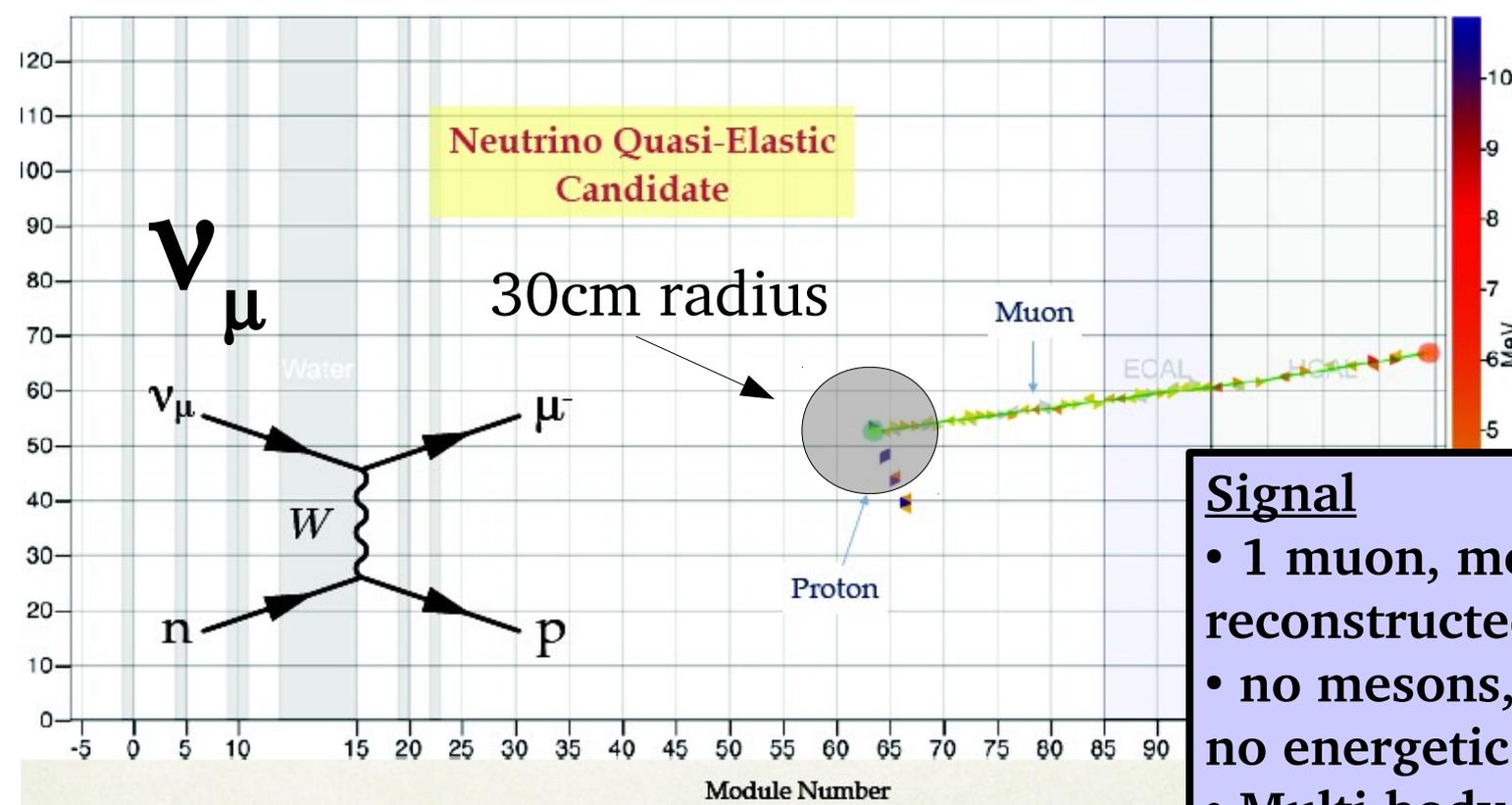
Most important quantities:  
muon energy and angle  
recoil energy  
secondary tracks/blobs



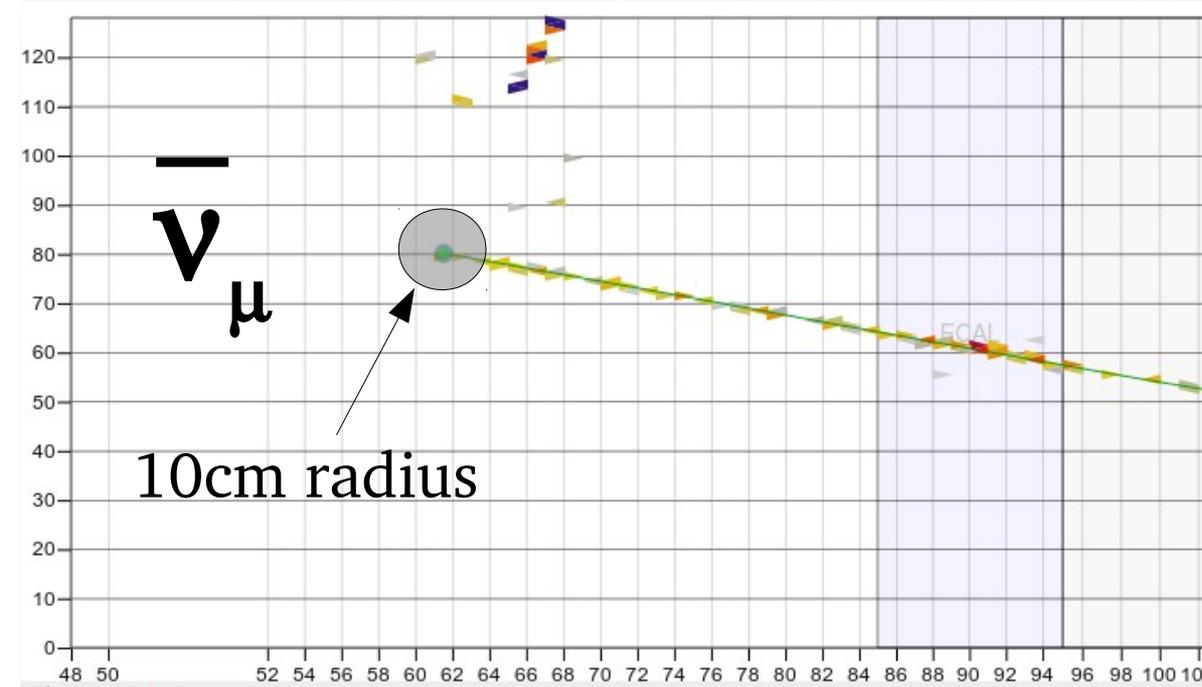
# Quasi-elastics



# QEL event selection



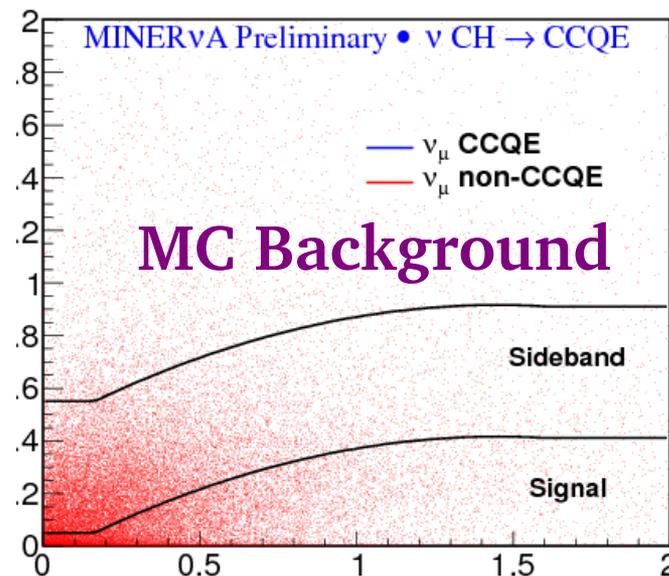
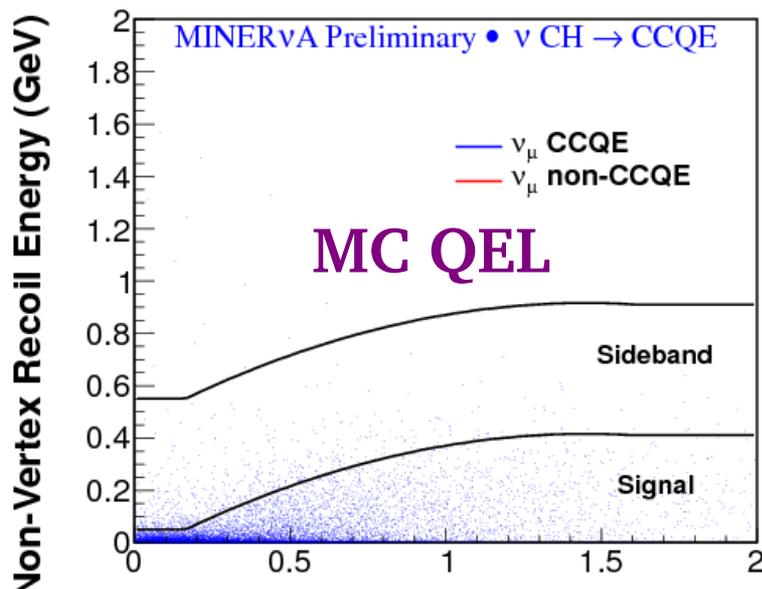
- Signal**
- 1 muon, momentum and charge reconstructed in MINOS
  - no mesons, no heavy baryons, no energetic photons
  - Multi-body effects may result in multiple nucleons – allow those
- Background**
- Pions deposit energy away from the vertex → use calorimetry
  - “Black out” region around the vertex
    - poorly modeled in MC
    - sensitive to multi-nucleon effects



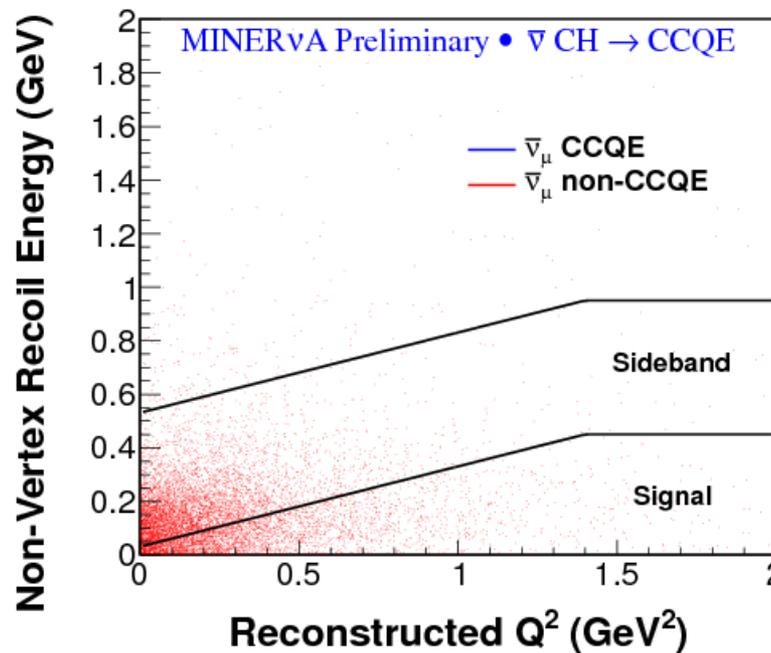
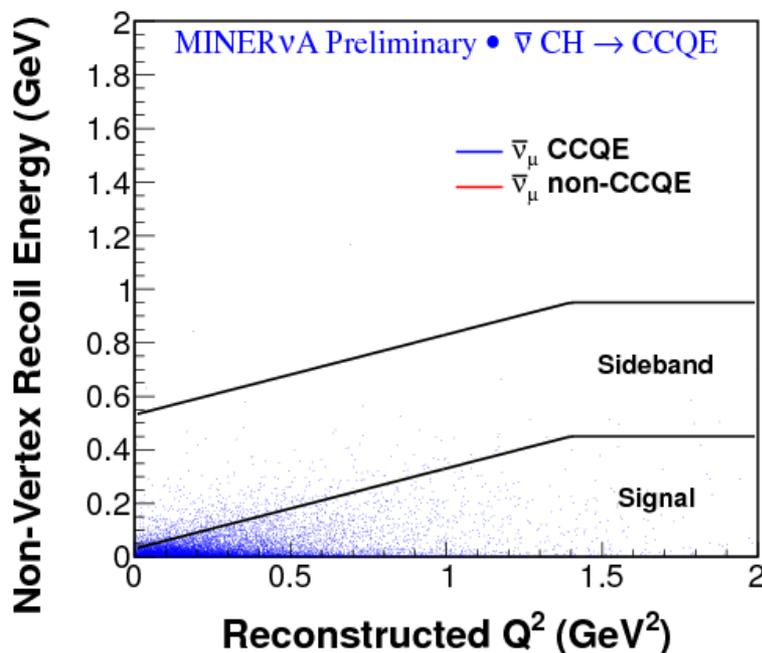
# Recoil vs. $Q^2$

For  $x_{Bj}=1$  expect  $E_{\text{recoil}} = Q^2/2M_N$

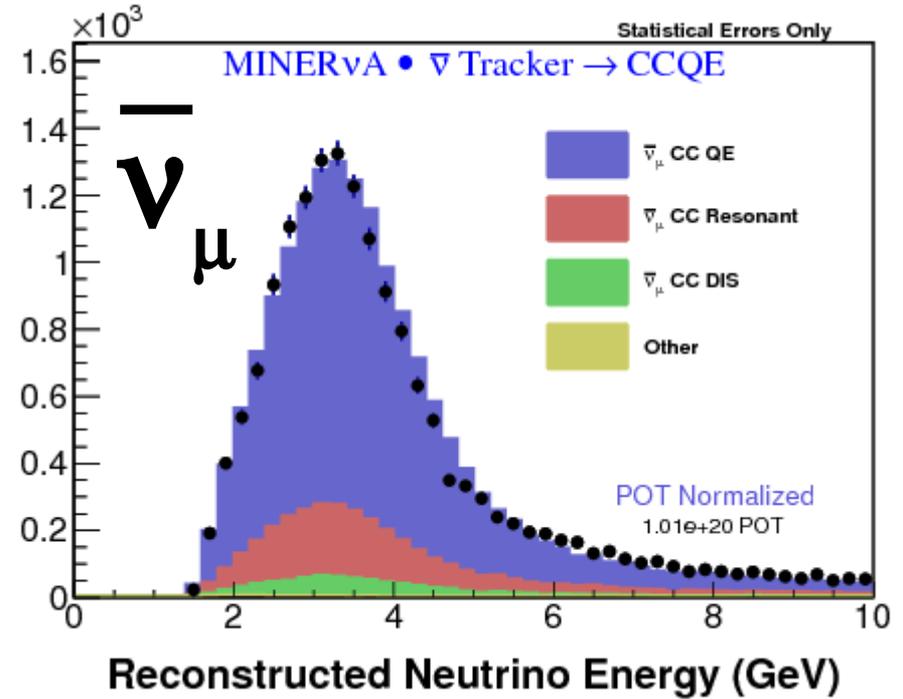
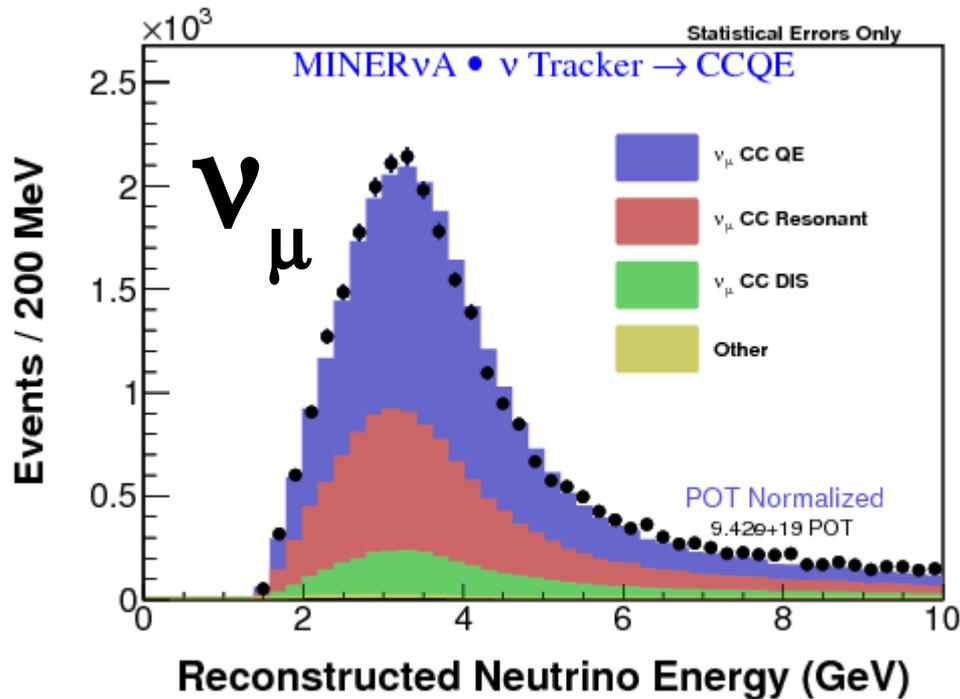
$\nu_{\mu}$



$\bar{\nu}_{\mu}$

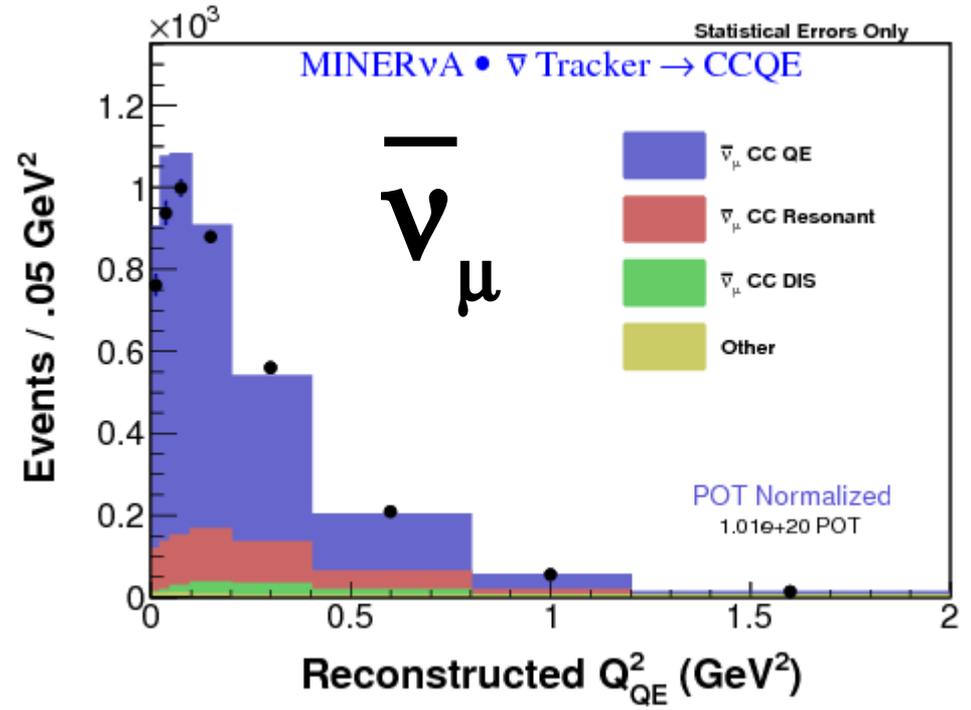
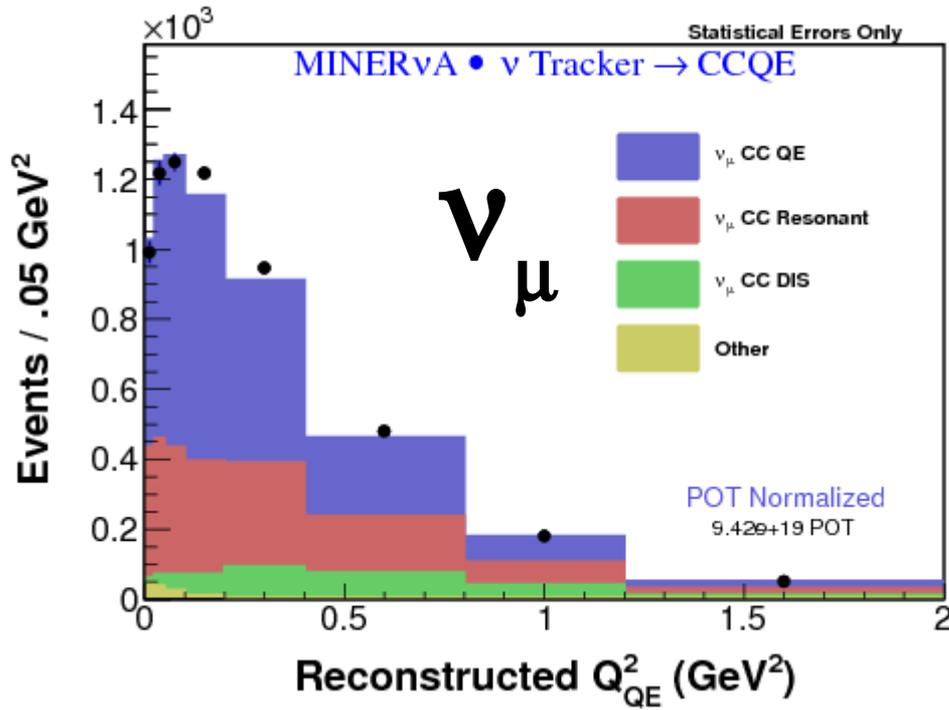


# Selected samples



$$E_\nu = \frac{m_\mu^2 - (m_p - E_b)^2 - m_\mu^2 + 2(m_p - E_b)E_\mu}{2(m_p - E_b - E_\mu + p_\mu \cos \theta_\mu)}$$

# Selected Samples

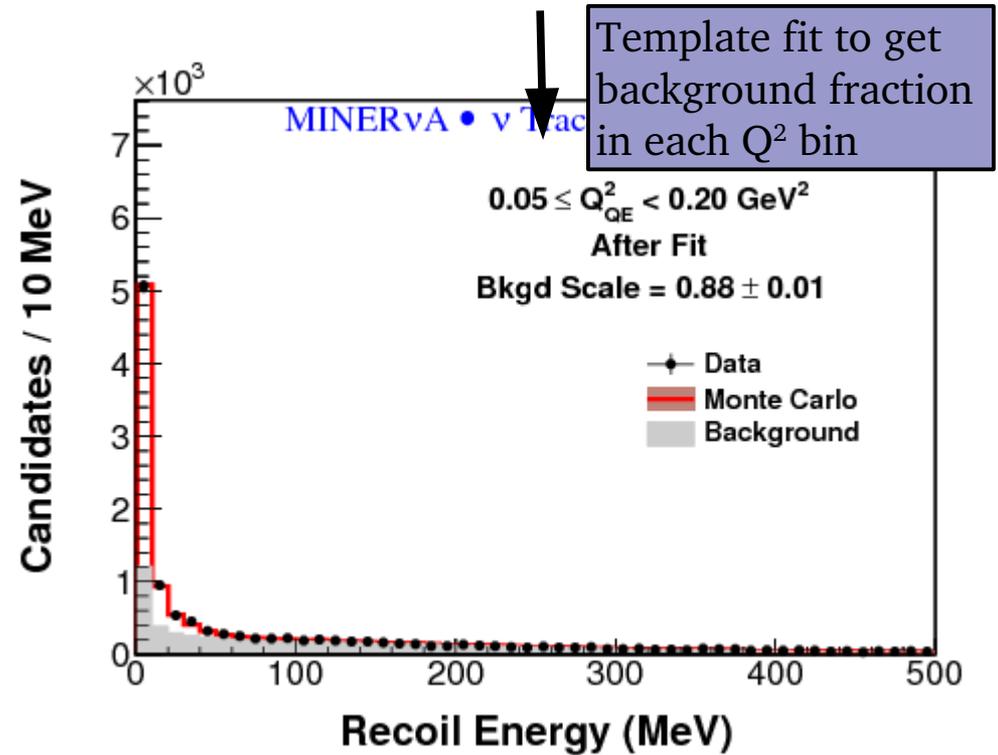
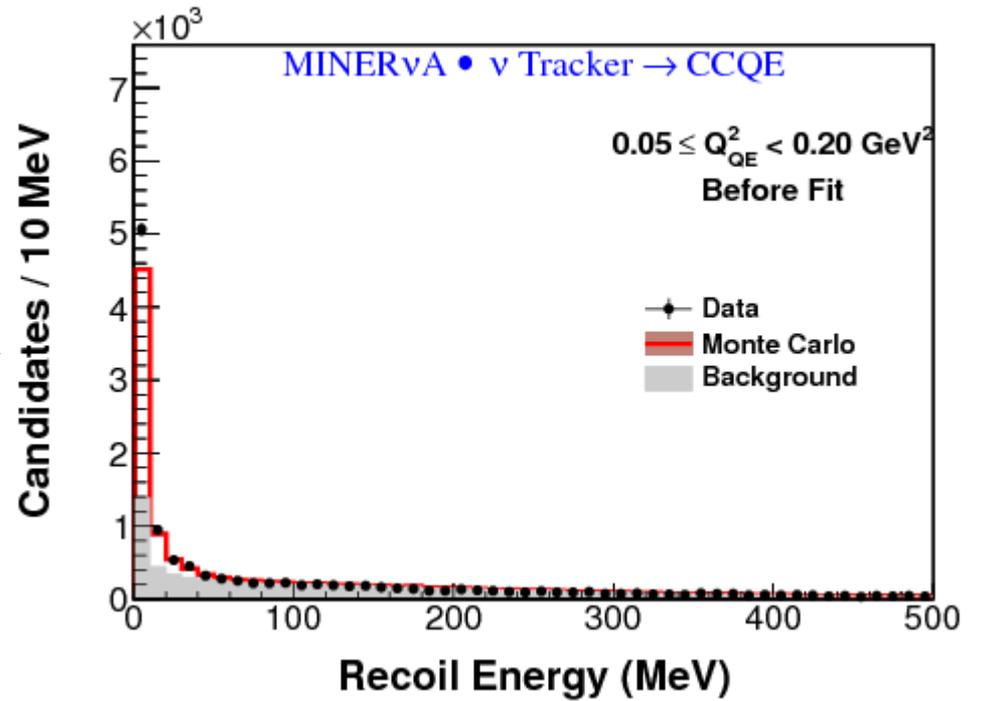
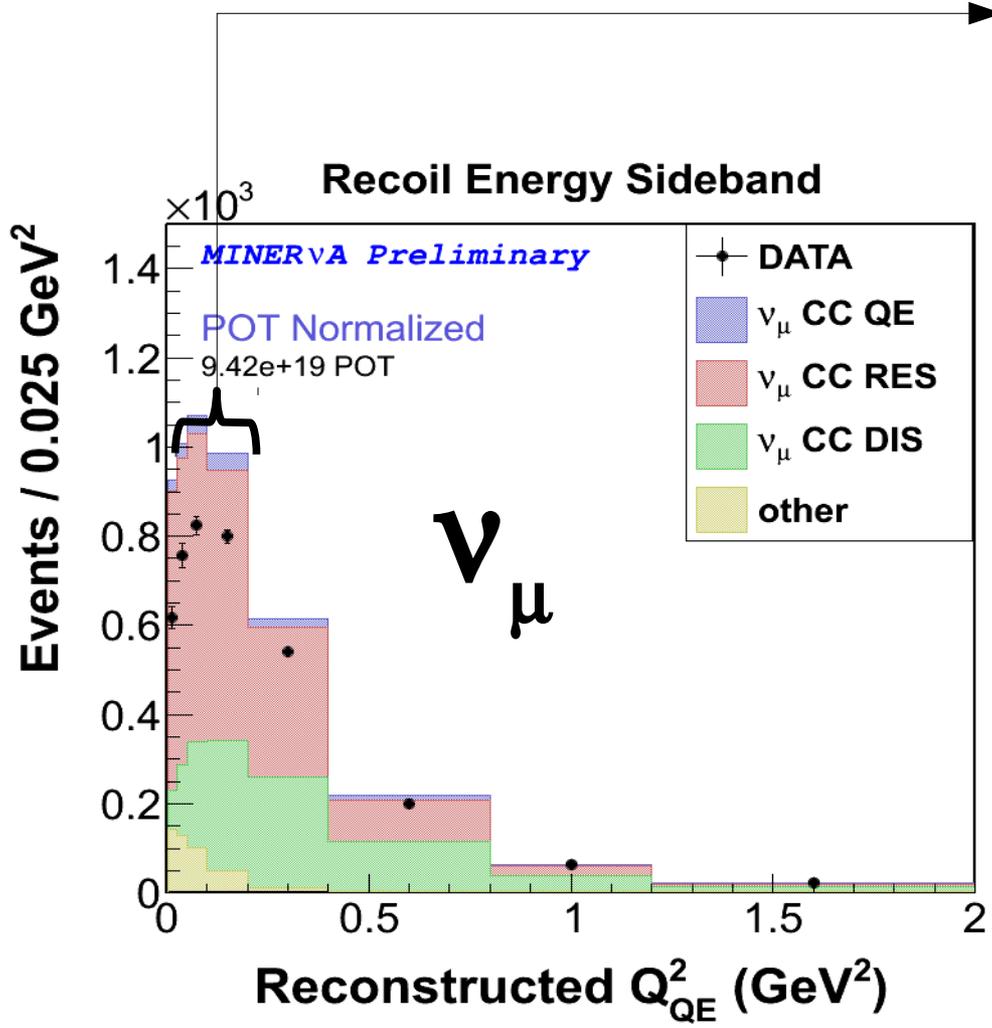


$$Q^2 = 2E_\nu(E_\mu - p_\mu \cos \theta_\mu) - m_\mu^2$$

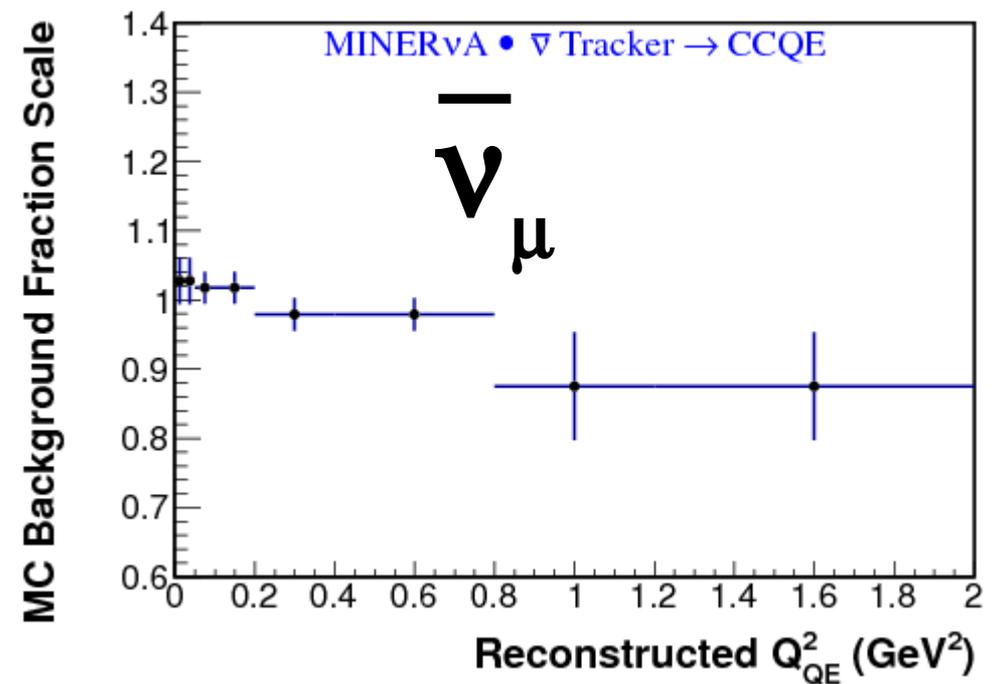
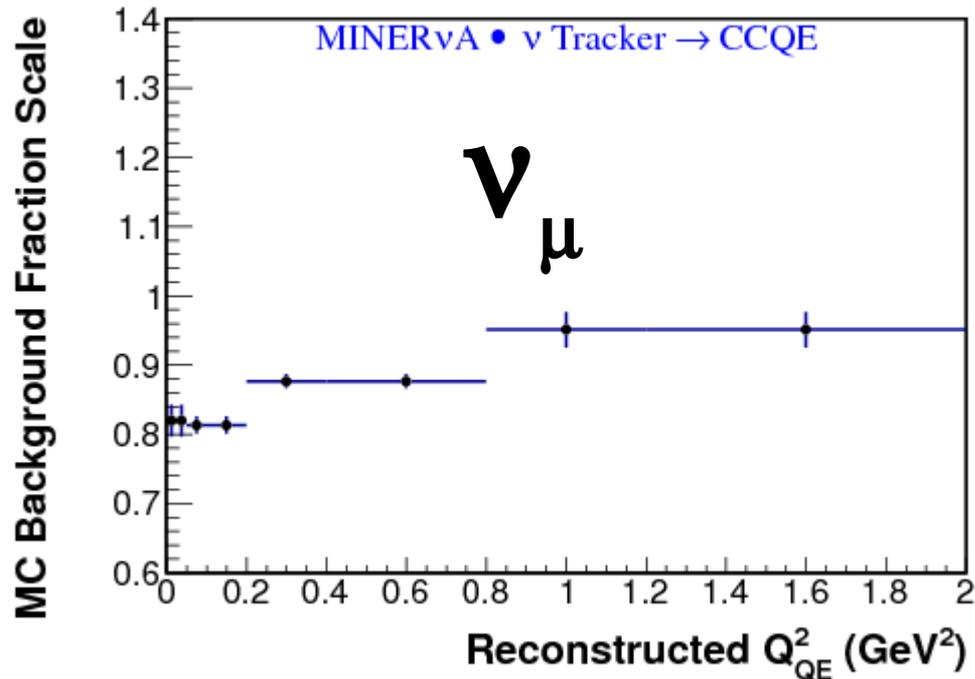
29,620 events  
Efficiency: 47%  
Purity: 49%

16,467 events  
Efficiency: 54%  
Purity: 77%

# Constraining Background



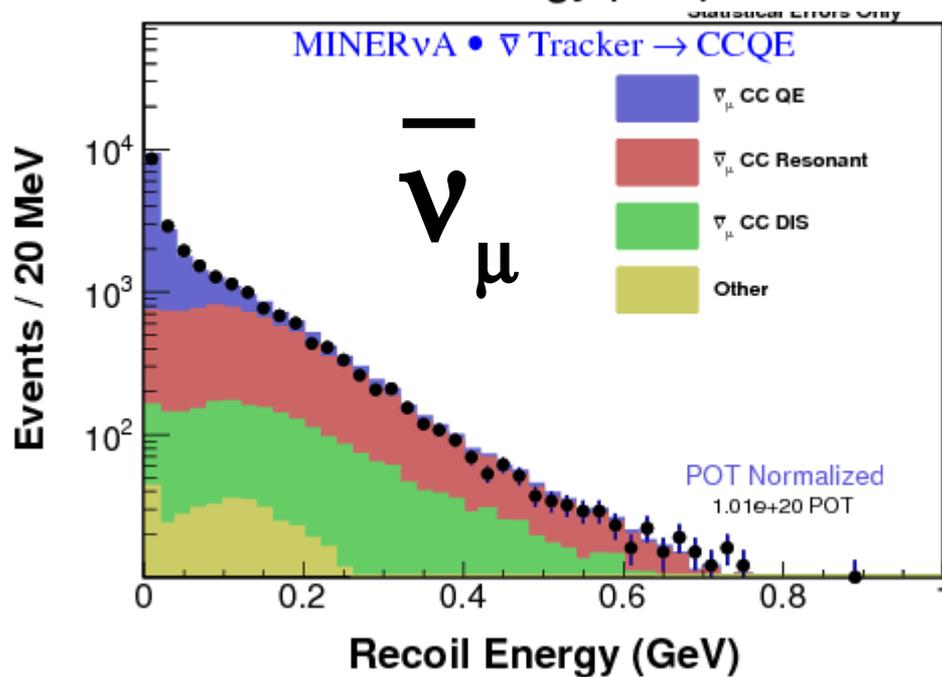
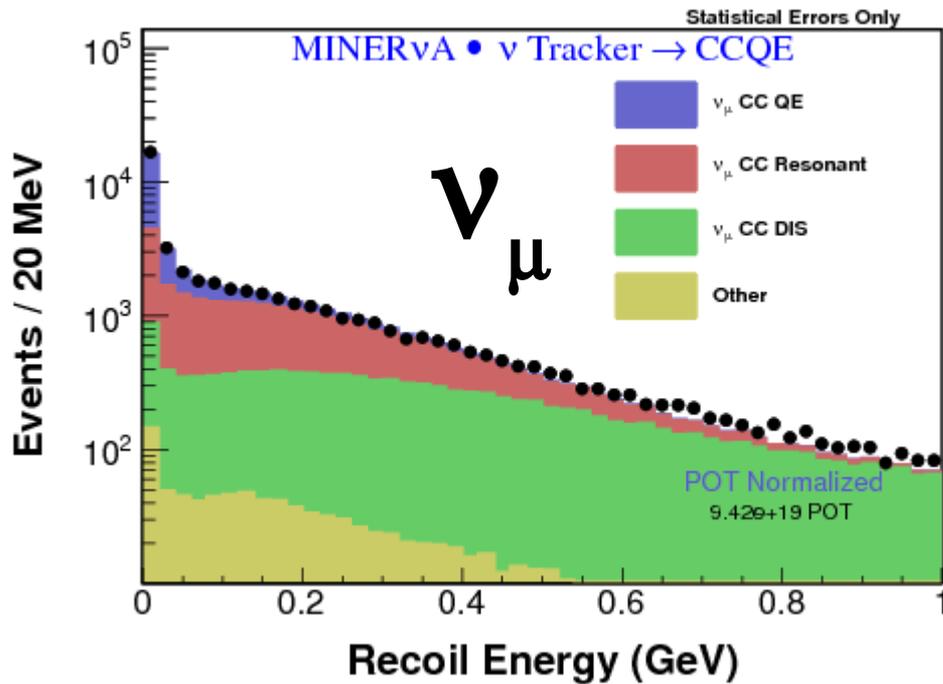
# Background Scale Factors



Data indicates MC background for  $\nu_{\mu}$  needs to be scaled down by 10-20% at low  $Q^2$

More pure anti-neutrino channel needs smaller corrections

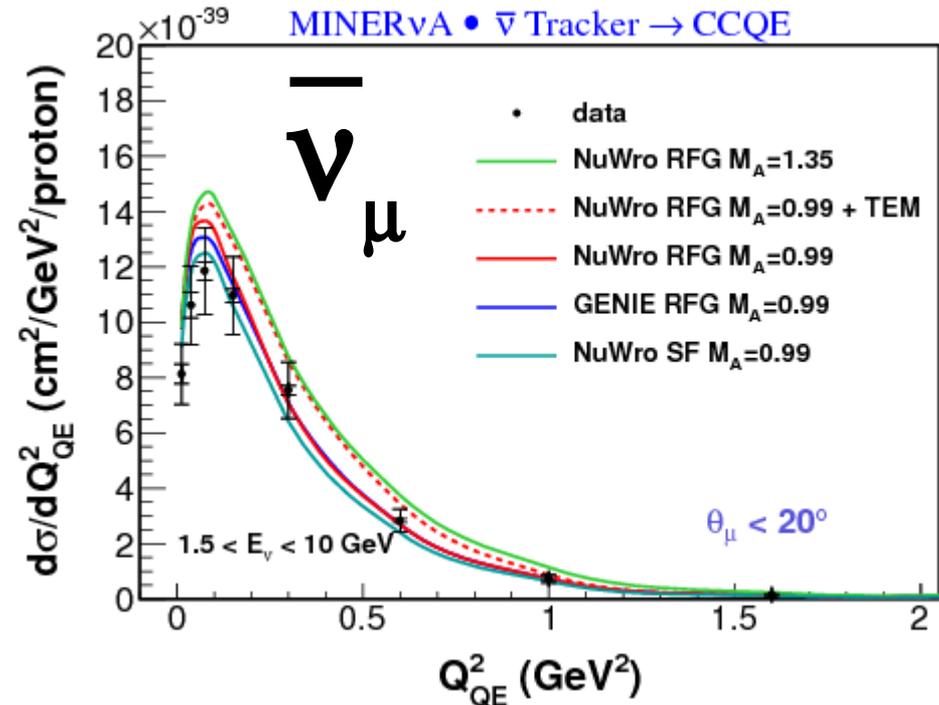
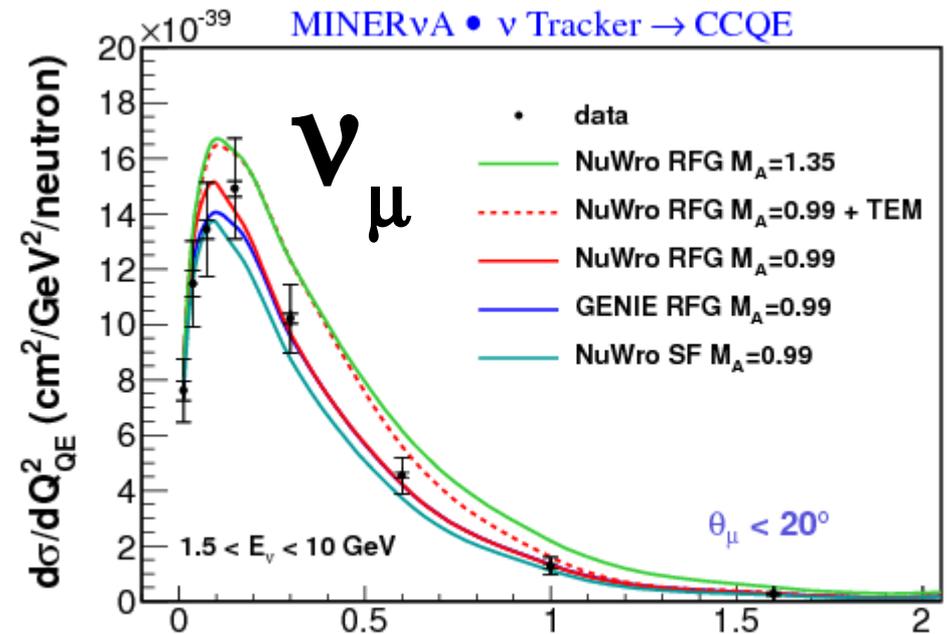
# Recoil energy after the fit



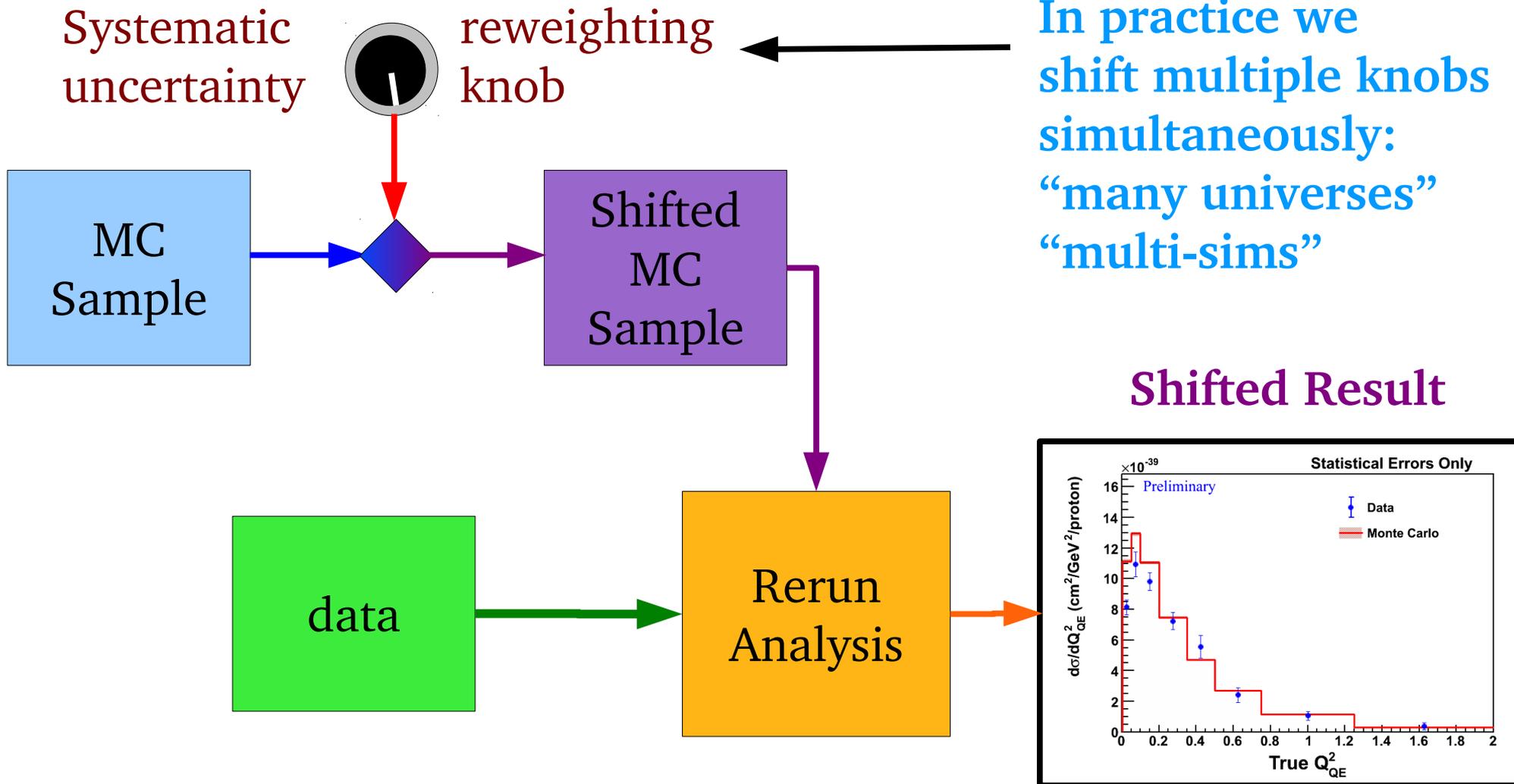
Fits successfully describe the recoil energy distribution over the whole kinematic range

# Differential Cross-sections

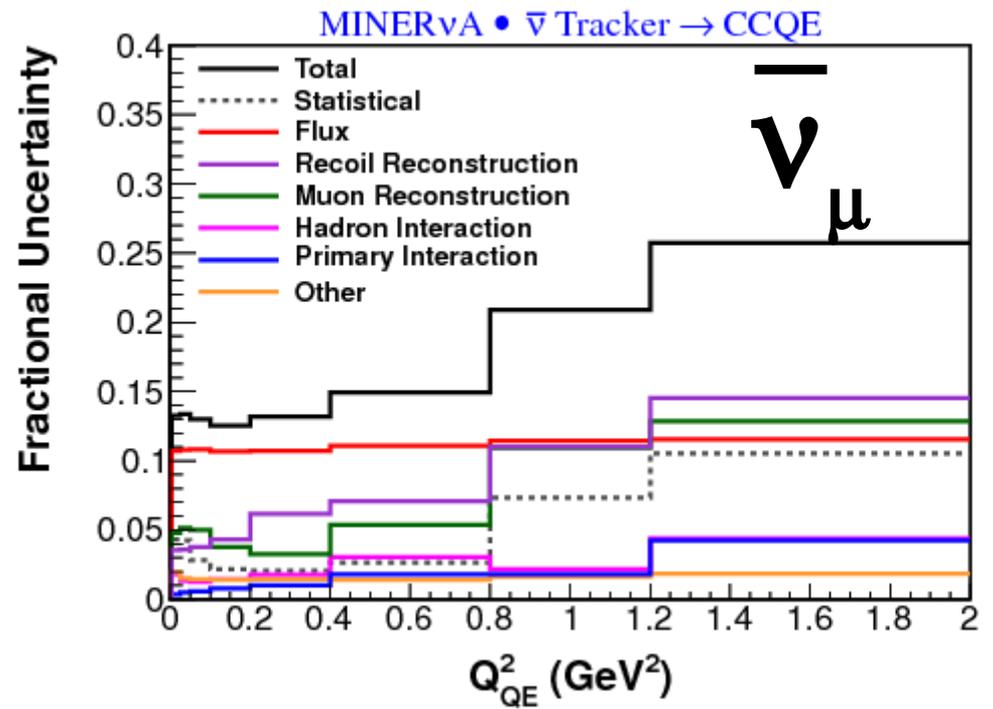
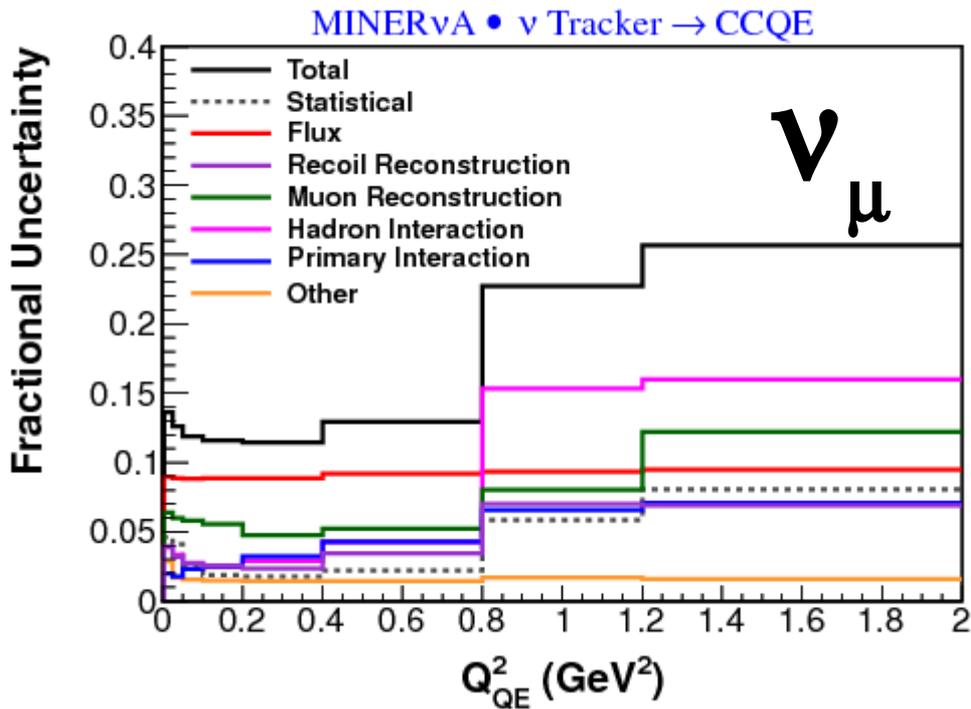
- Background subtraction
- Iterative unfolding to true  $Q^2$  distribution
- Efficiency correction
- Fiducial mass accounting
- Incorporation of the flux



# Systematic Uncertainties

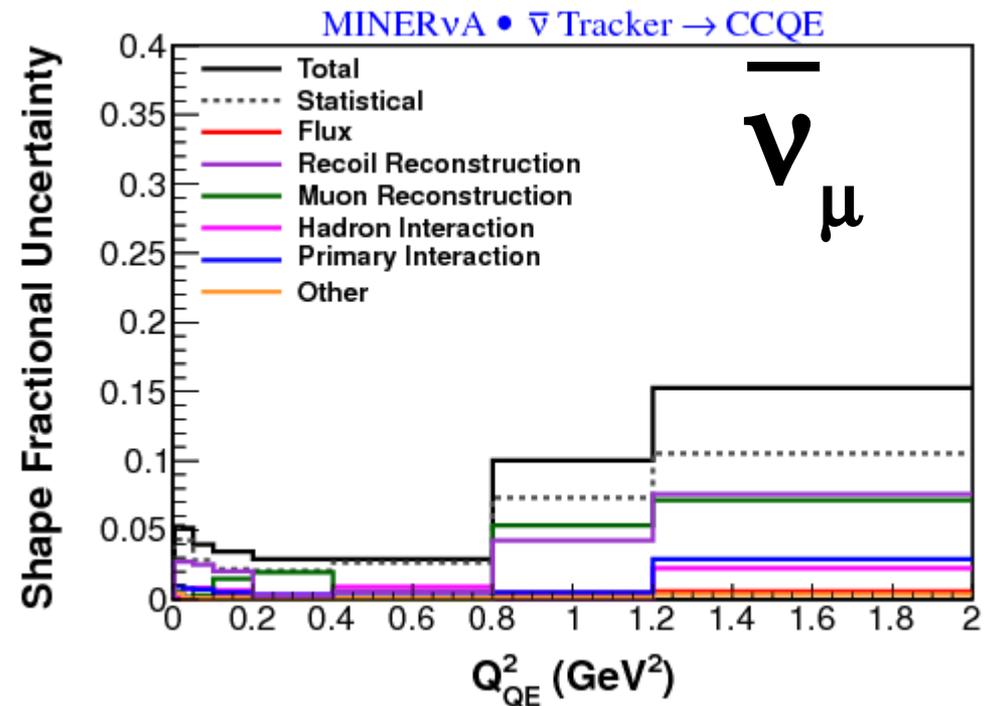
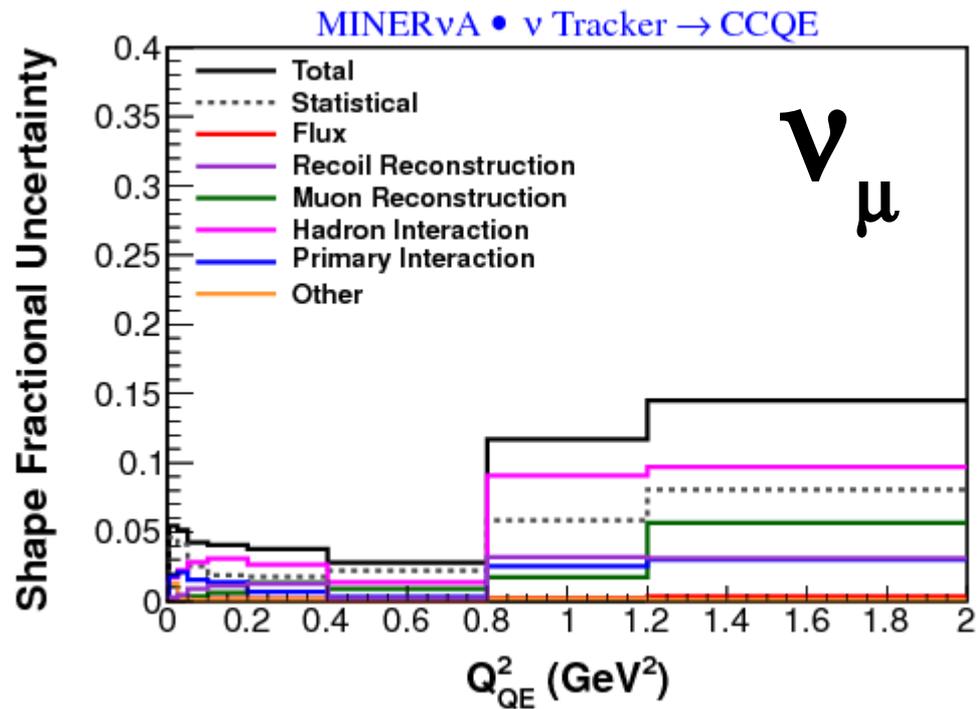


# Systematic Error Bands



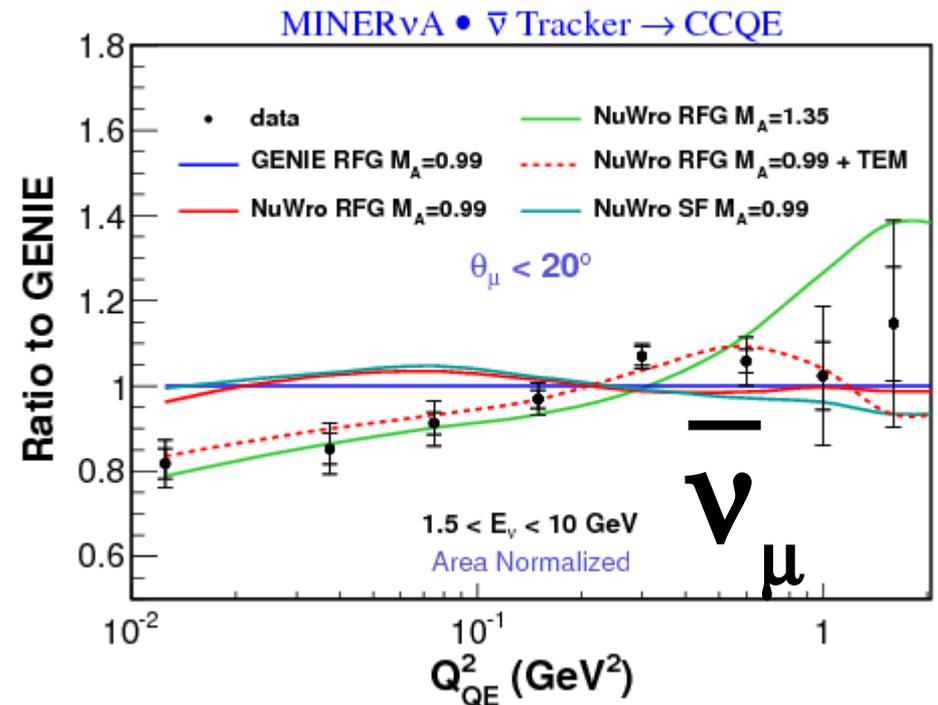
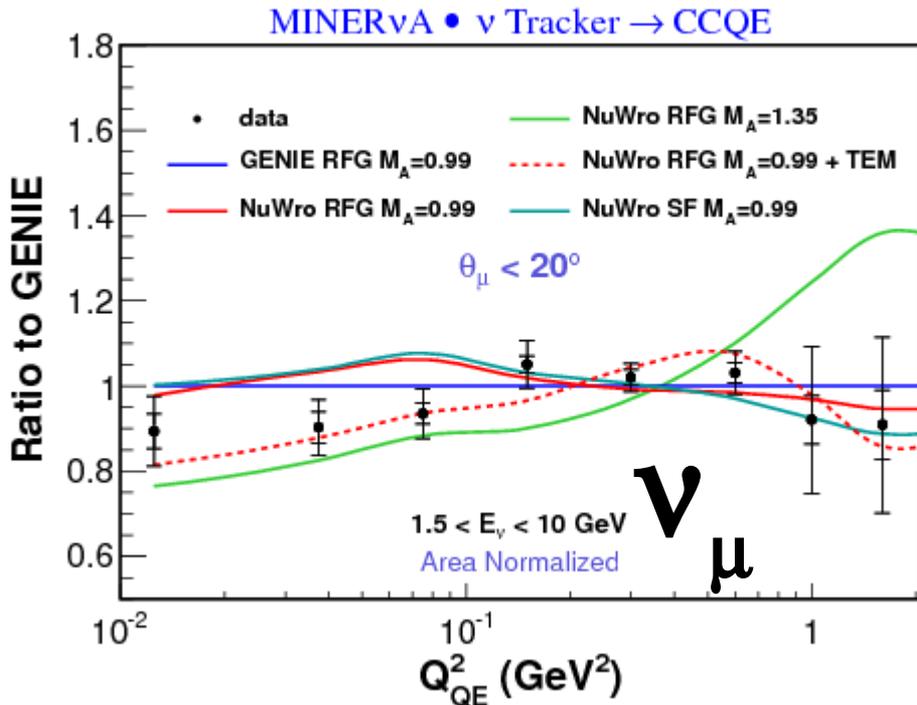
Most significant error: neutrino flux

# Shape uncertainties

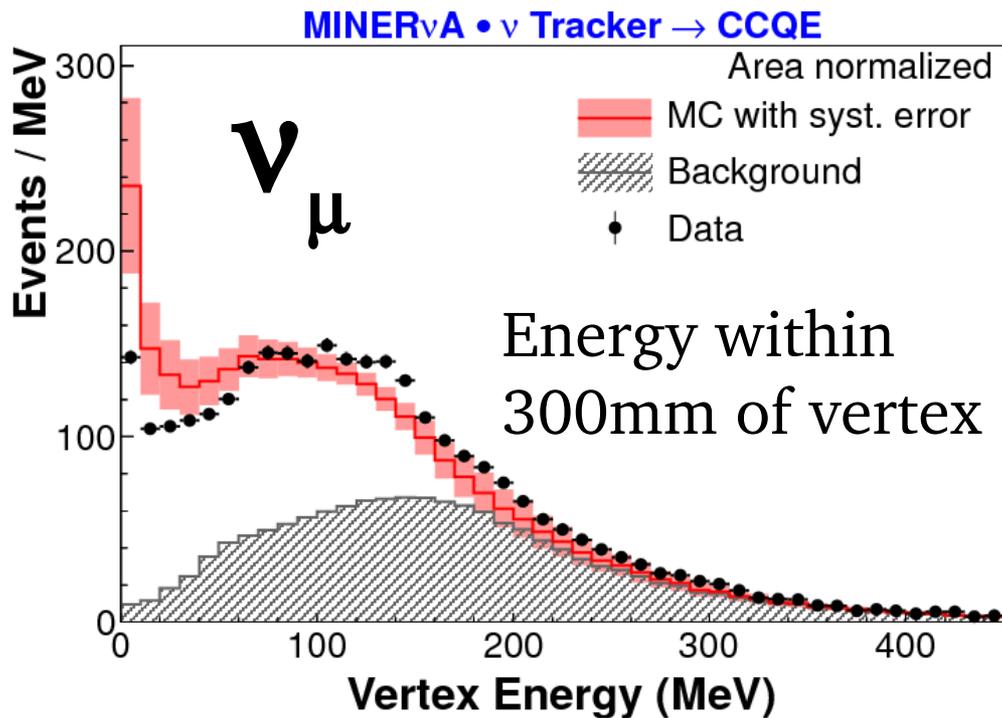


The shape of  $d\sigma/dQ^2$  has smaller errors and is physics sensitive.

# $d\sigma/dQ^2$ shape



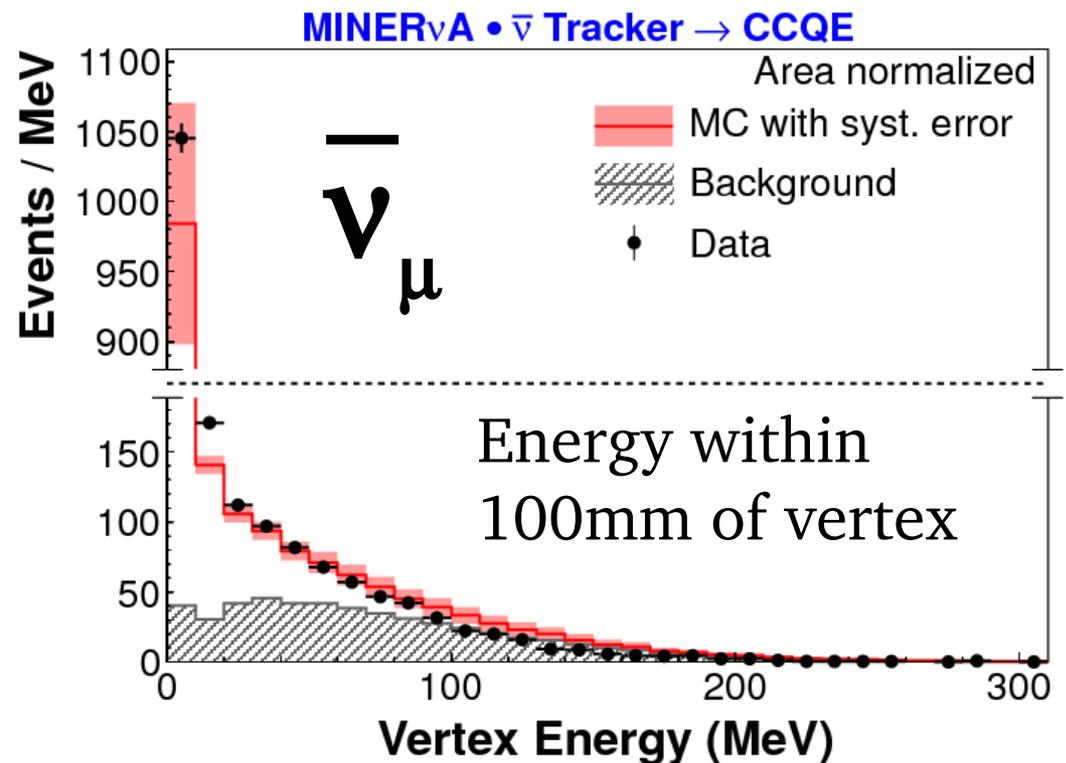
Best match is to an RFG model with  $M_A=0.99 \text{ GeV}$  but with  $G_M^V$  modified in accordance with electron scattering data – “transverse enhancement” (TEM)



# Vertex Energy

Excess of energy at the vertex seen in neutrino mode. Not explained by any systematic uncertainty.

Relatively good agreement in anti-neutrino mode

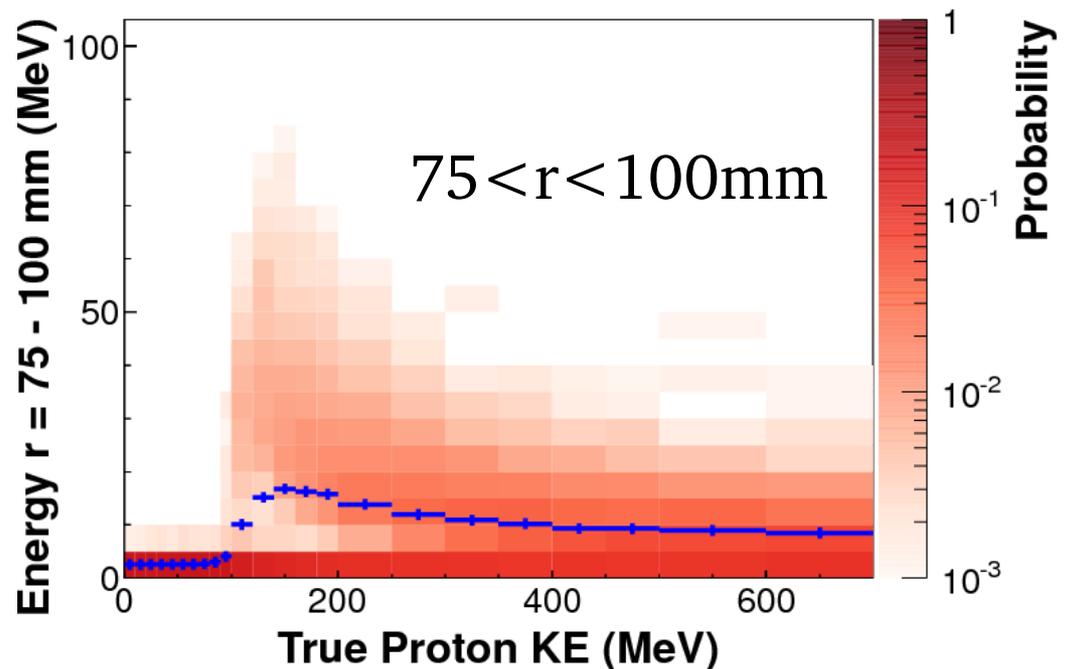
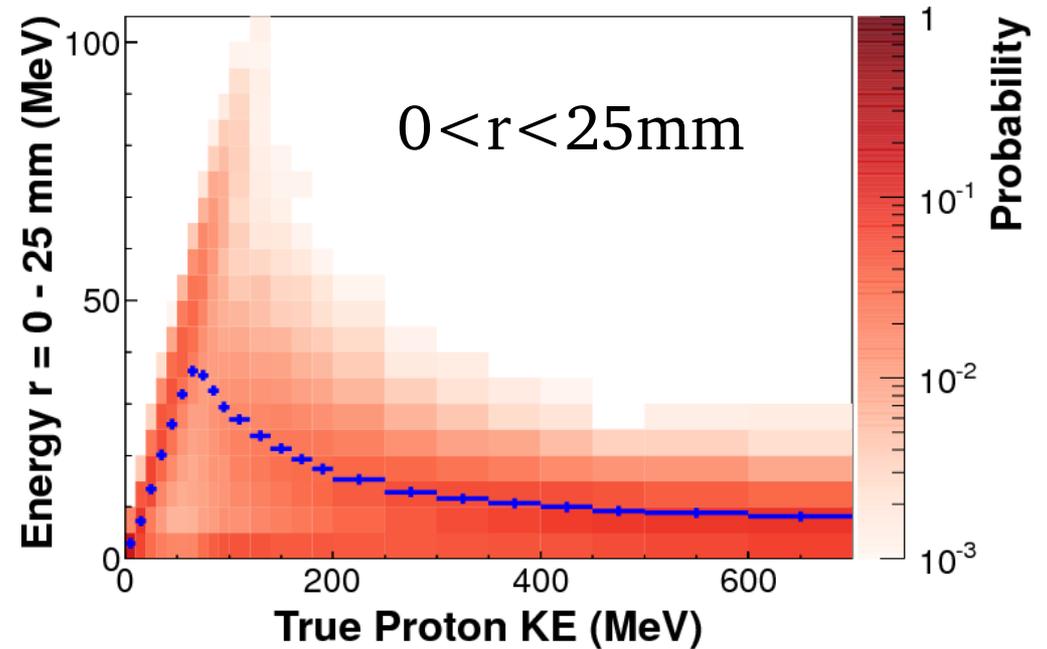


# Vertex Energy Fit

Hypothesis: Some QEL-like events due to scattering on correlated np pairs.

Would result in an nn final state for anti-neutrinos but a pp pair for neutrinos.

Test this by adding in an additional proton to some events. Fit vertex energy in radial slices.



# Vertex Energy Fit

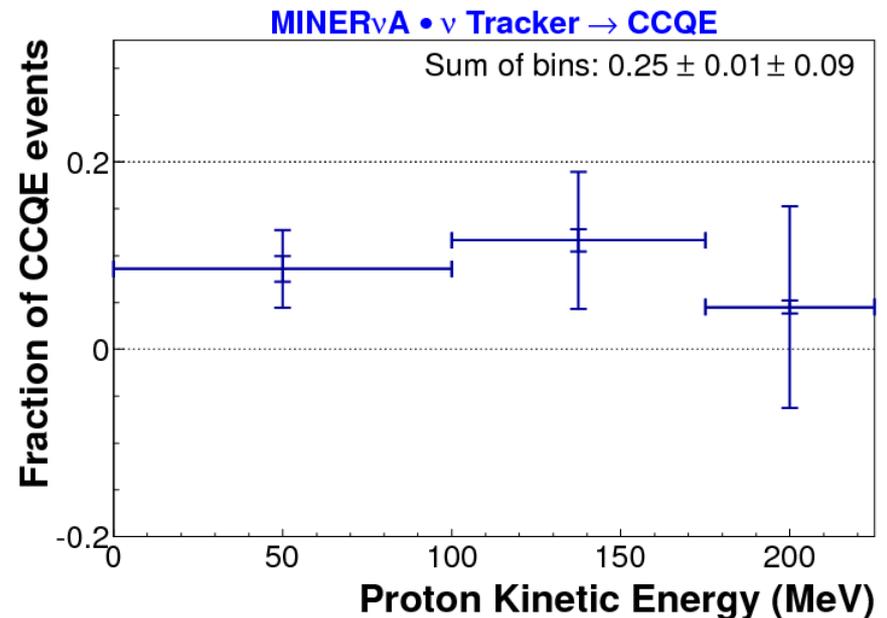
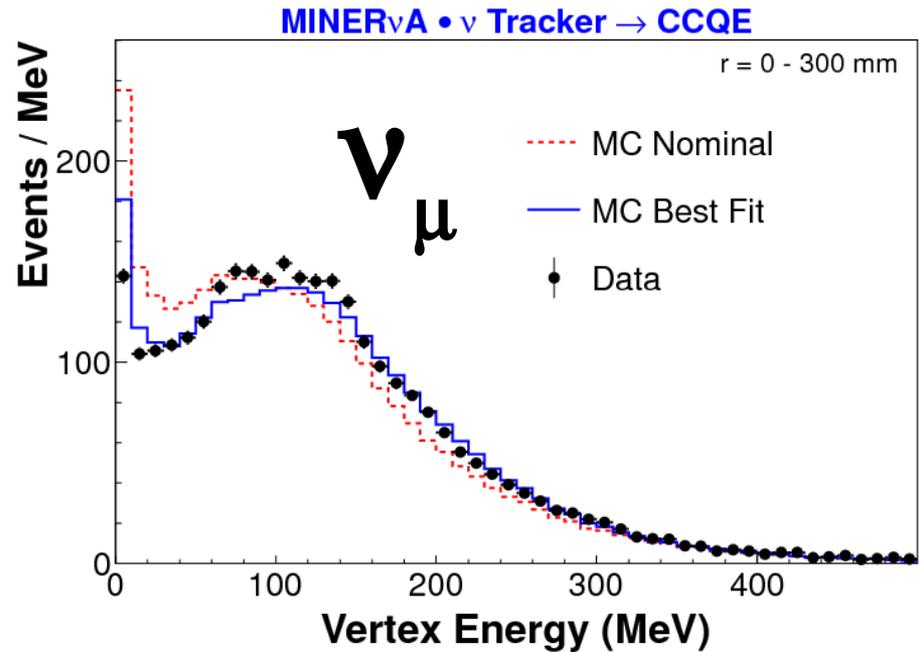
## Result:

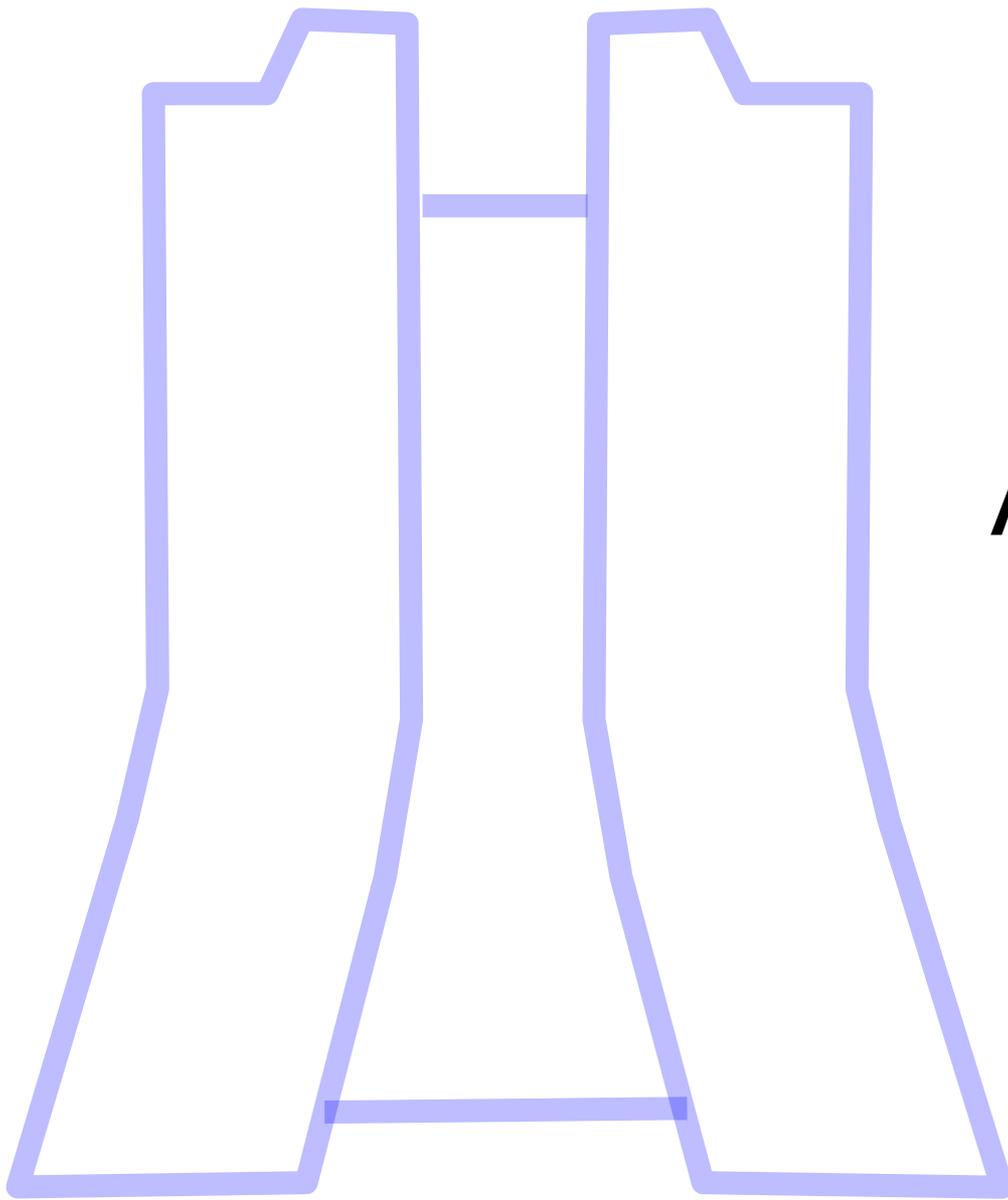
Neutrinos: Best agreement if  $25 \pm 9\%$  of events have an additional proton with a flat energy distribution from  $0 < E_{\text{vtx}} < 200 \text{ MeV}$

No additional protons needed in anti-neutrino mode.

## Conclusion

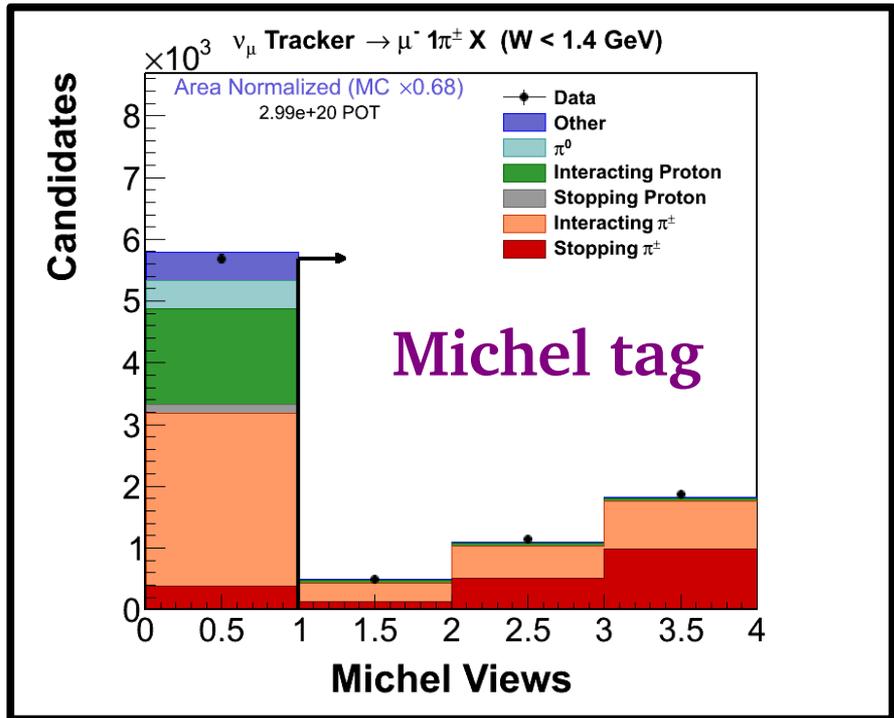
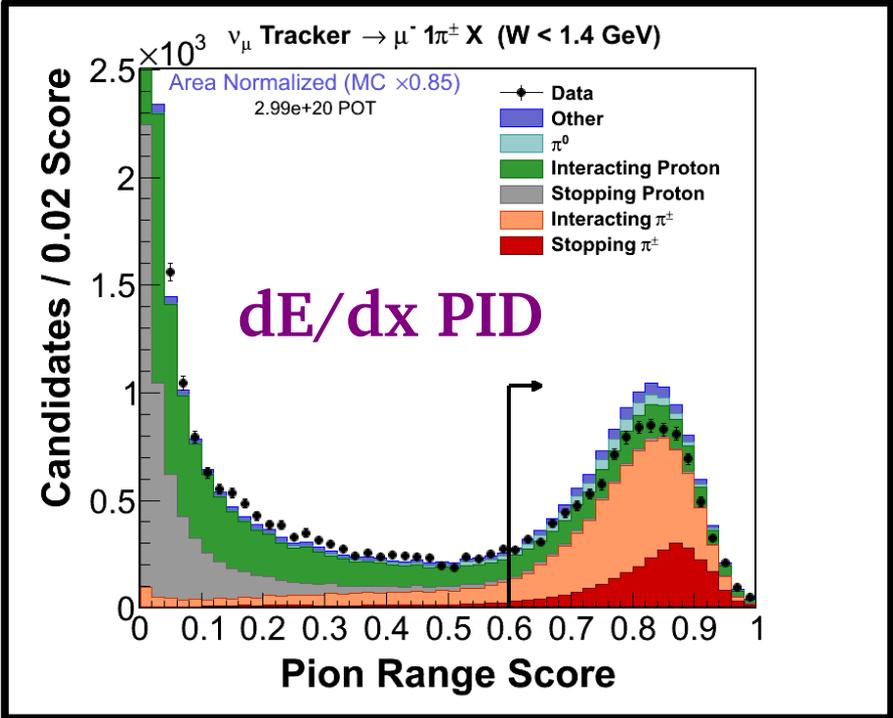
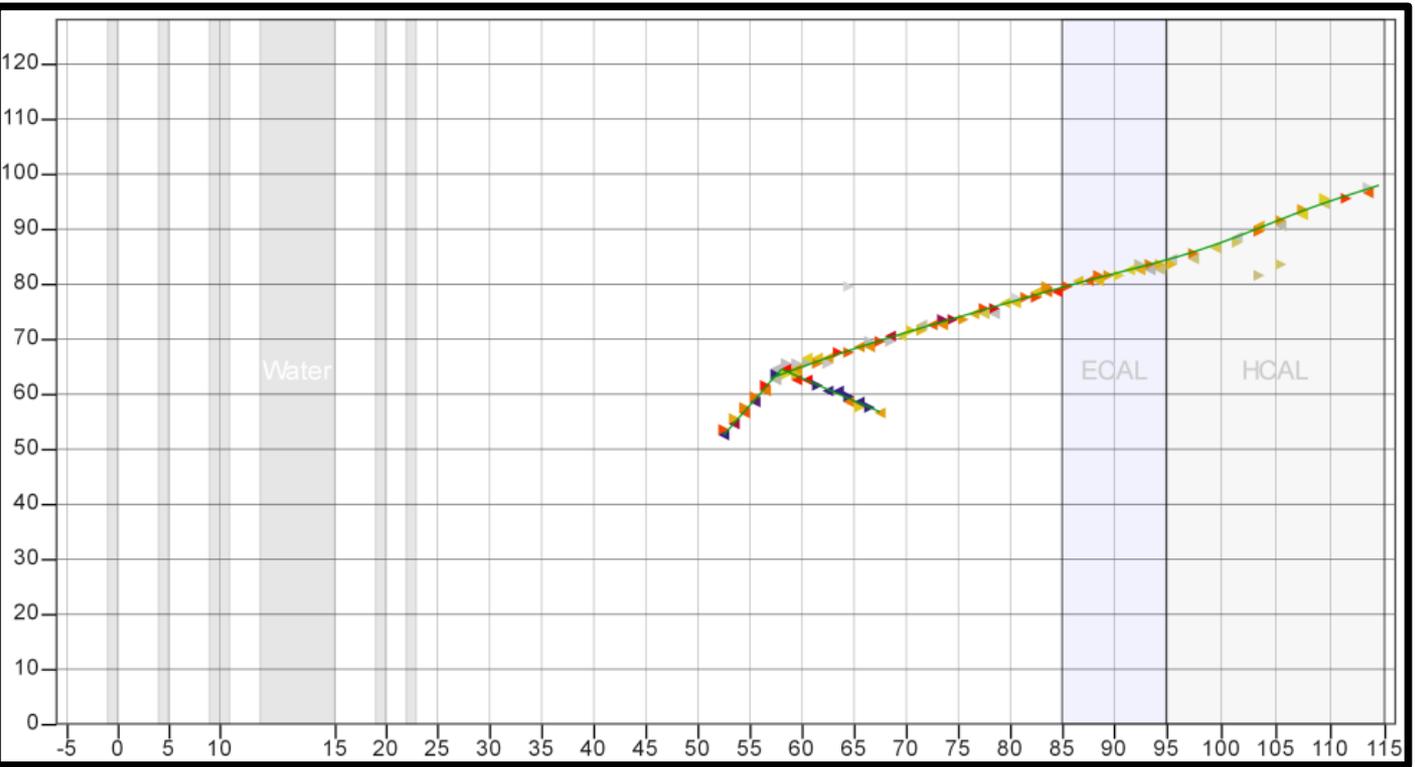
Neutrino cross-sections and energy reconstruction sensitive to multi-body effects. Generator tuning badly needed.





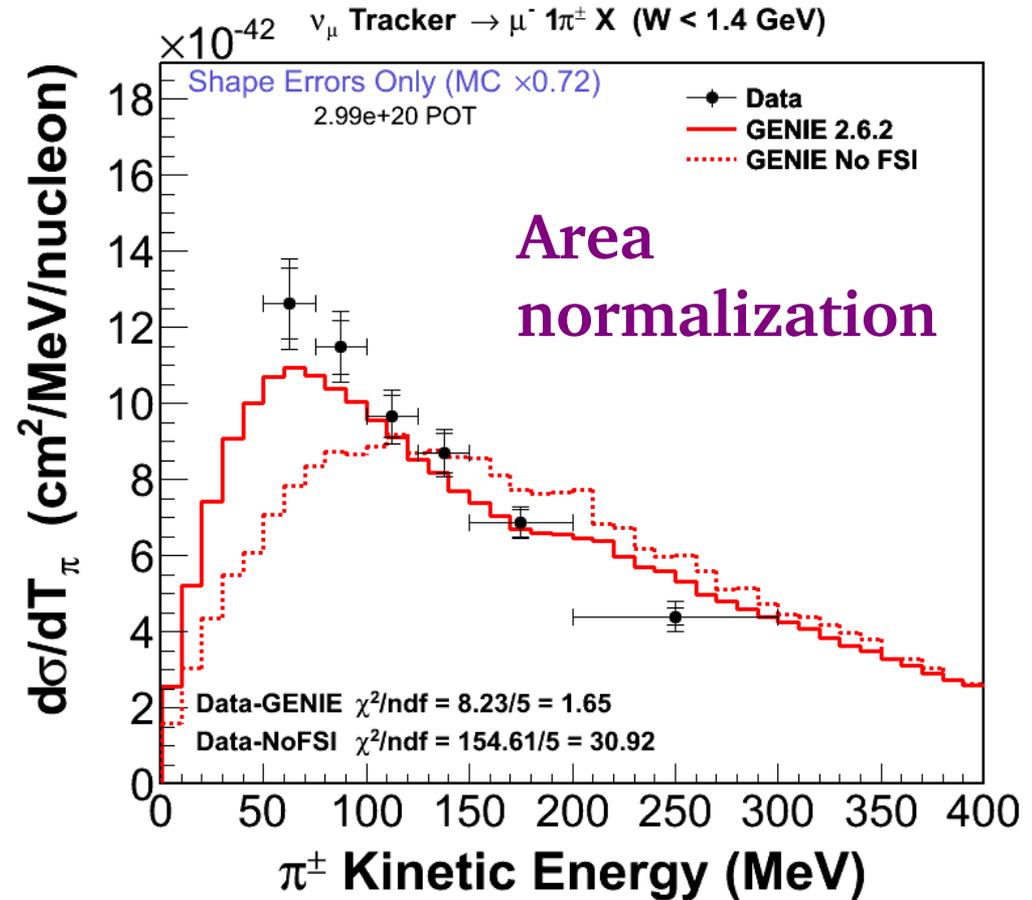
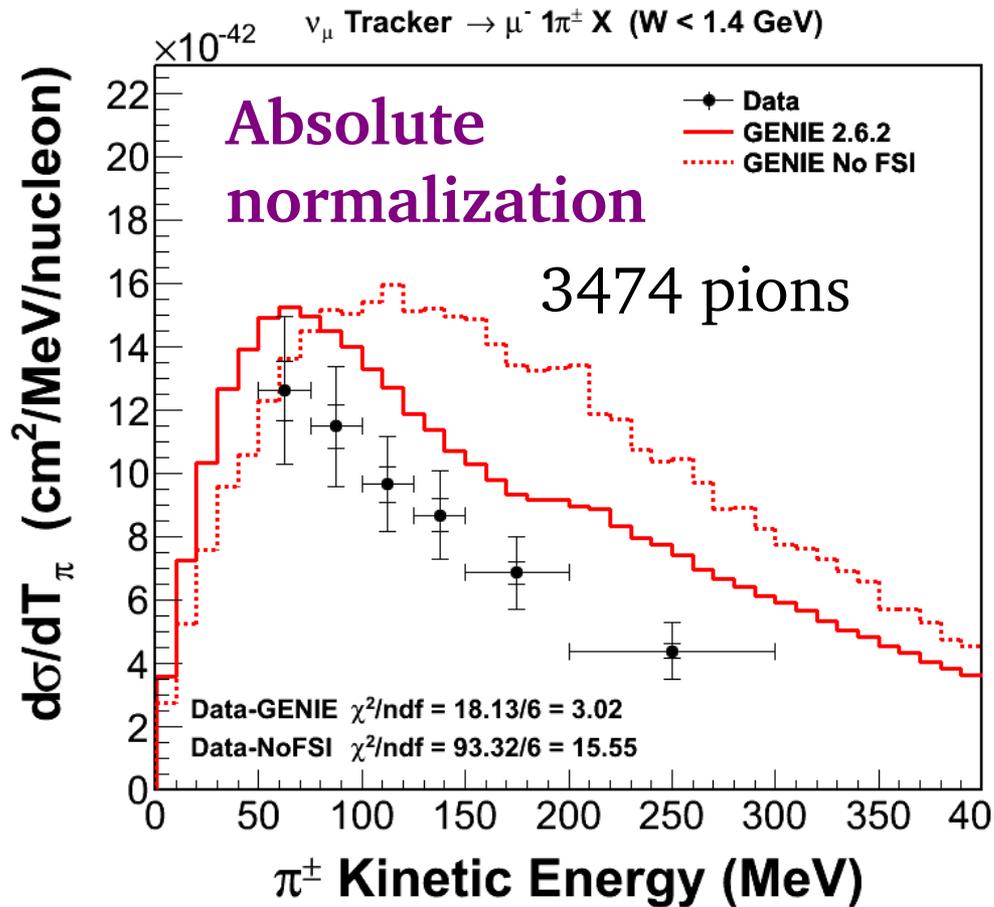
# Additional Results

Single  $\pi^\pm$   
 production  
 $\nu_\mu (C,H) \rightarrow \pi X$   
 $W < 1.4 \text{ GeV}$   
 $d\sigma/dT_\pi, d\sigma/d\theta_\pi$



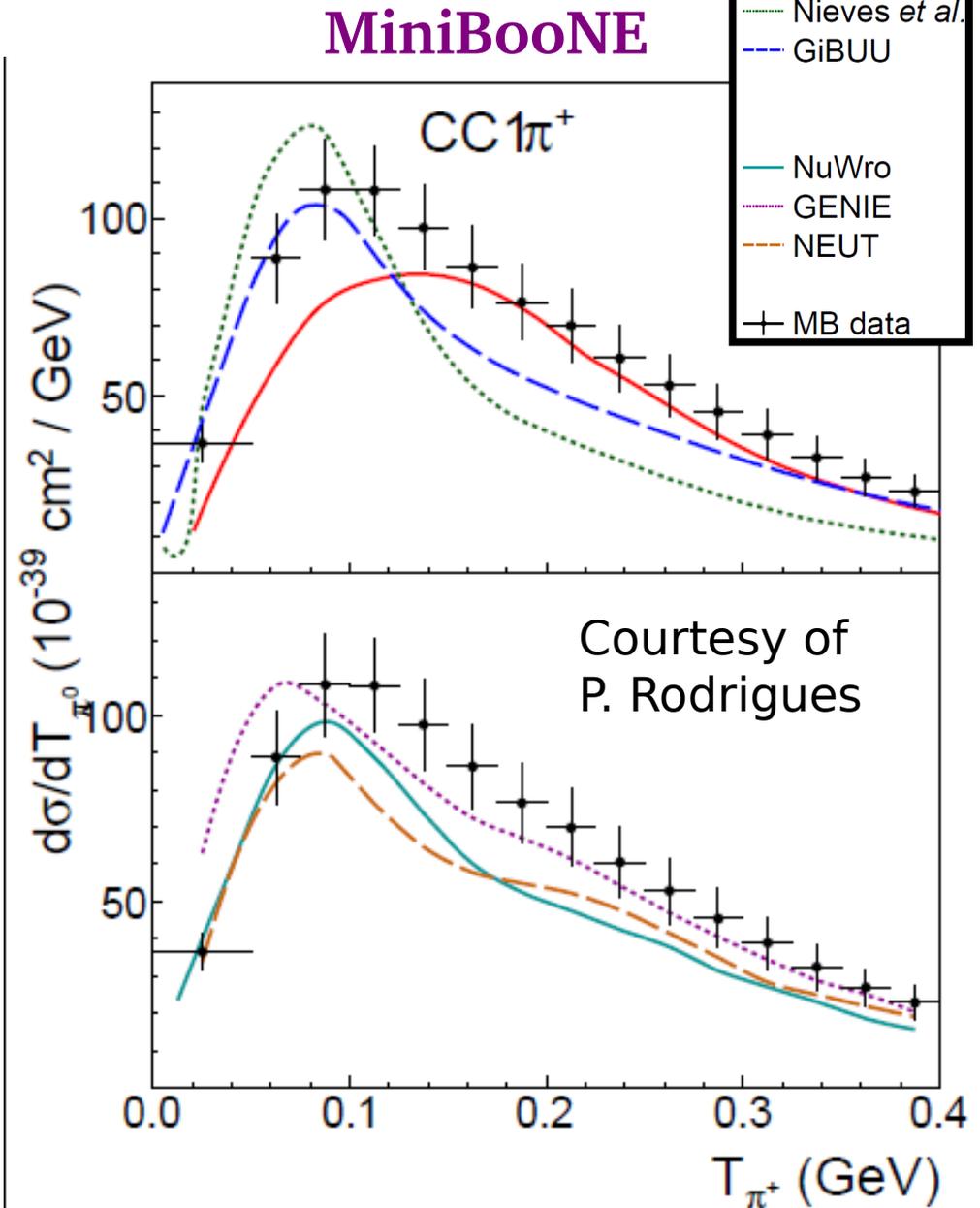
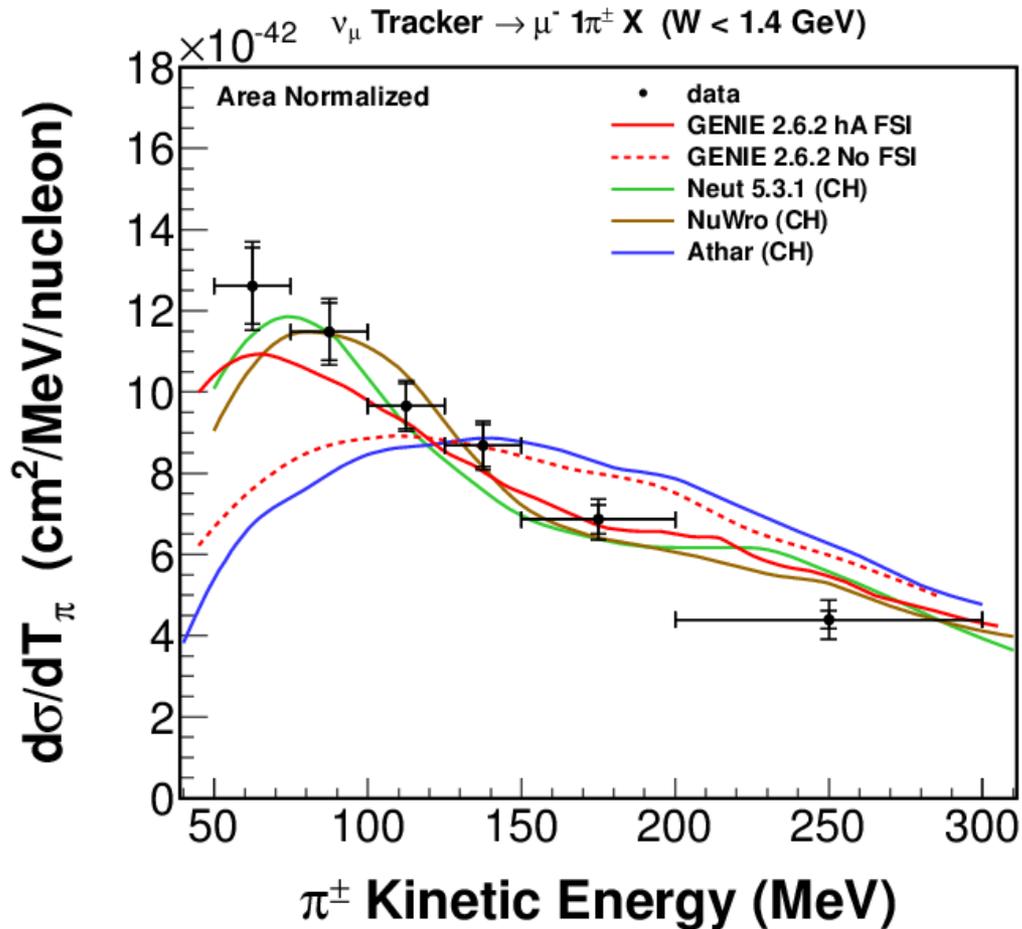
# Single $\pi^\pm$ production

Mostly  $\pi^+$



**Conclusion:** data are sensitive to FSI and provide model tests

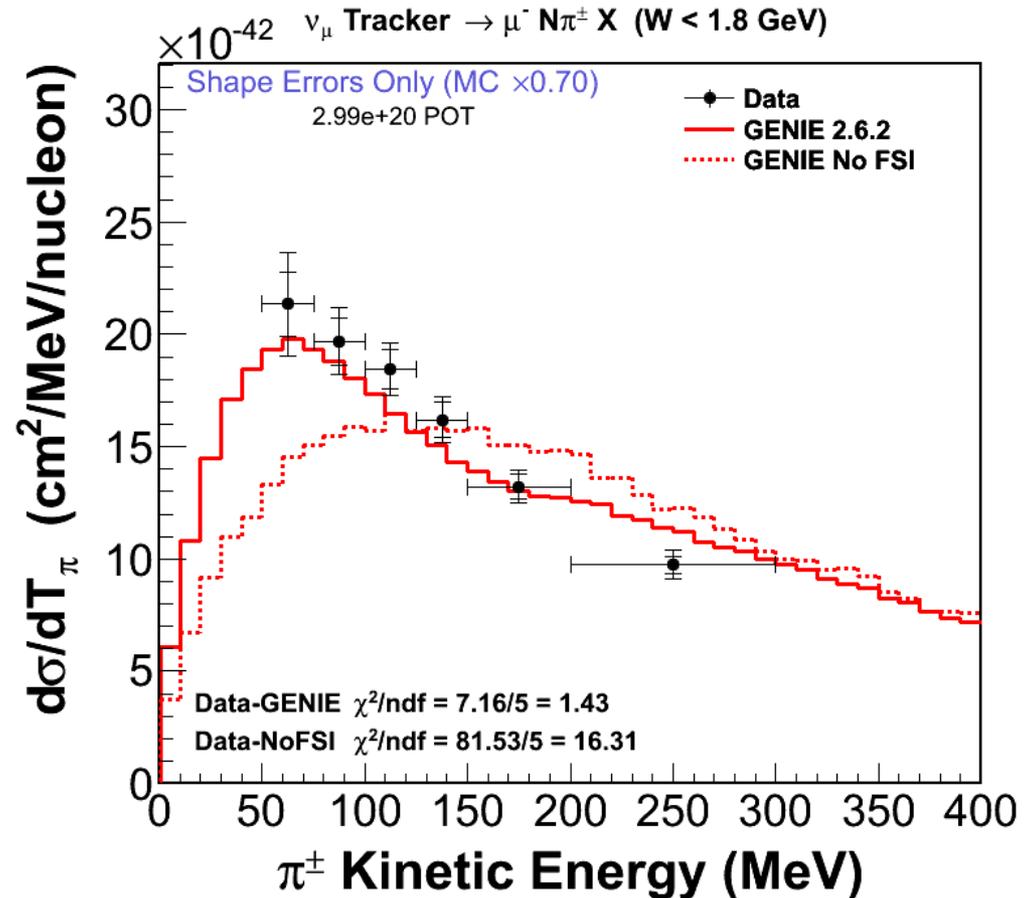
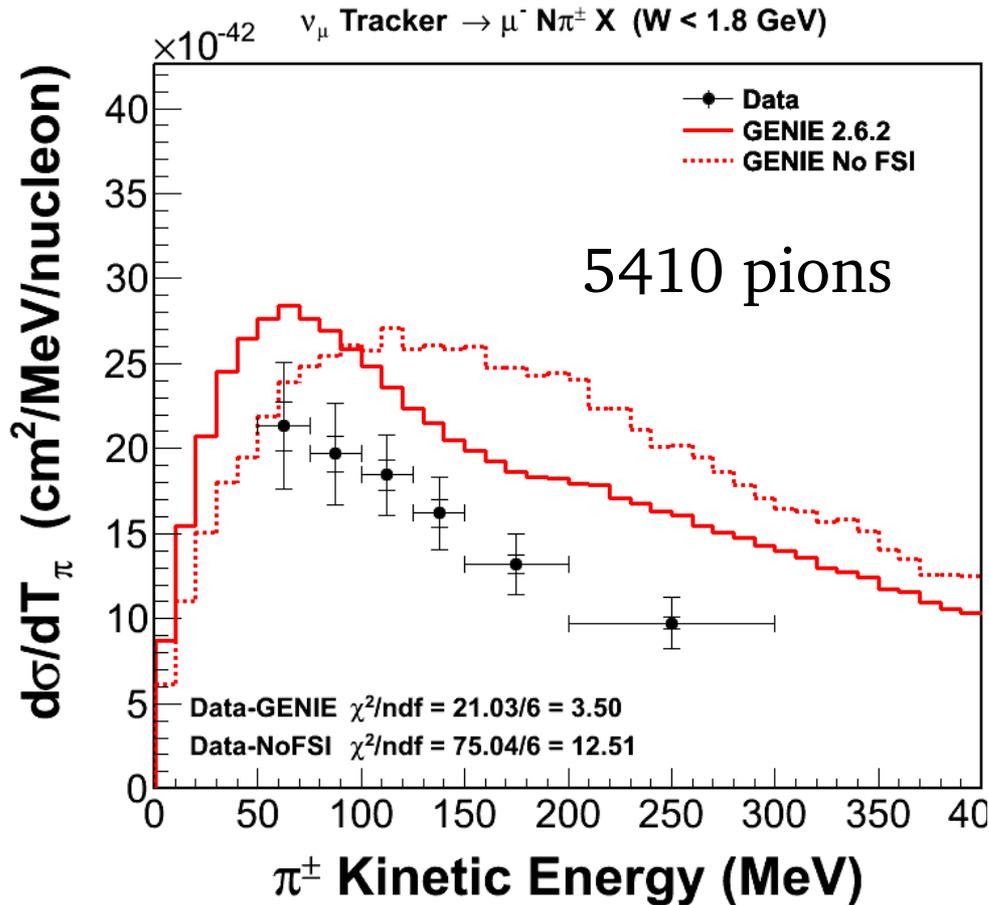
# Single $\pi^+$ production



**Conclusion:** MC codes tend to agree better than micro-physical calculations (*for now...*)

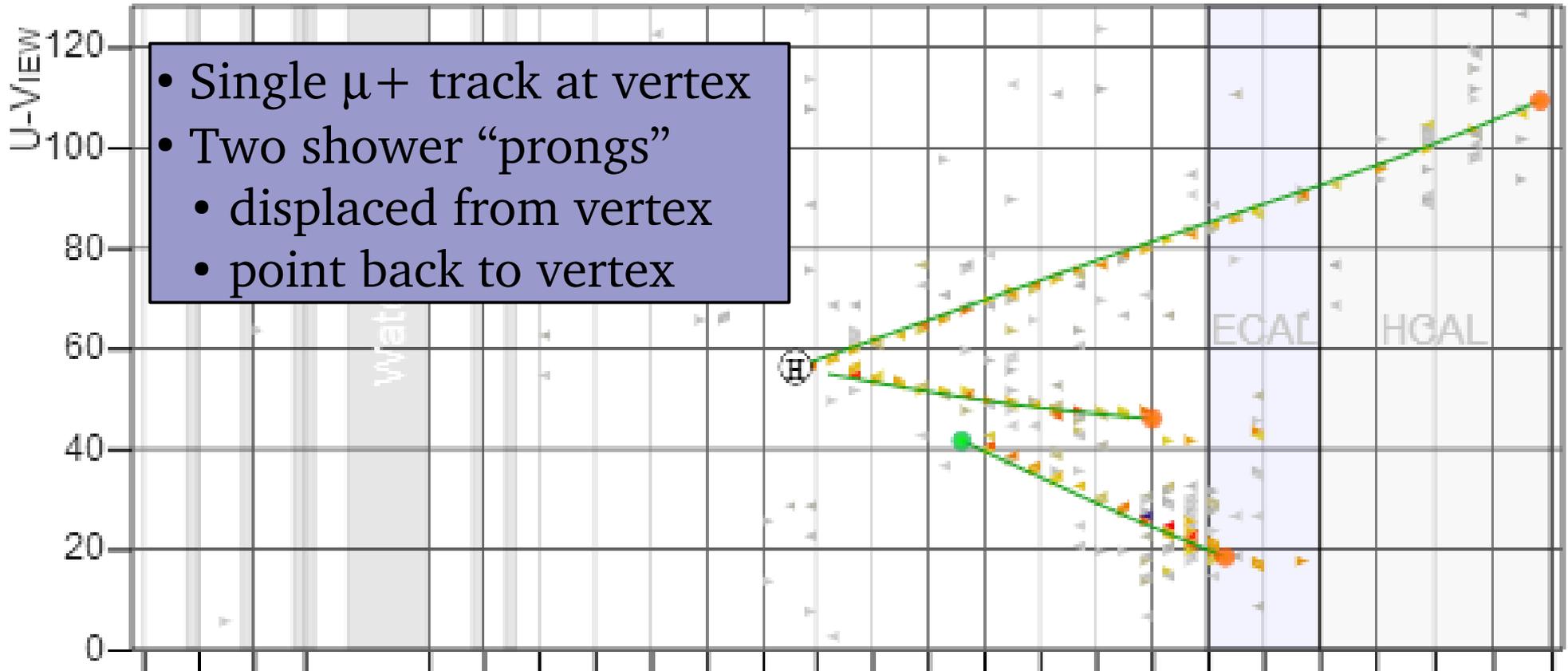
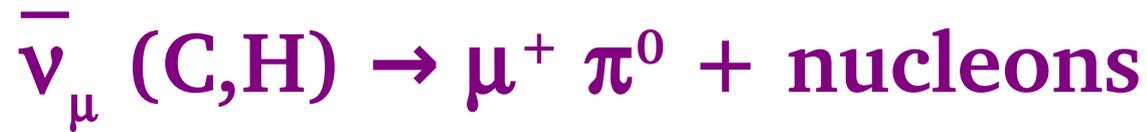
# Multi- $\pi^\pm$ production

Mostly  $\pi^+$



Work in  
progress

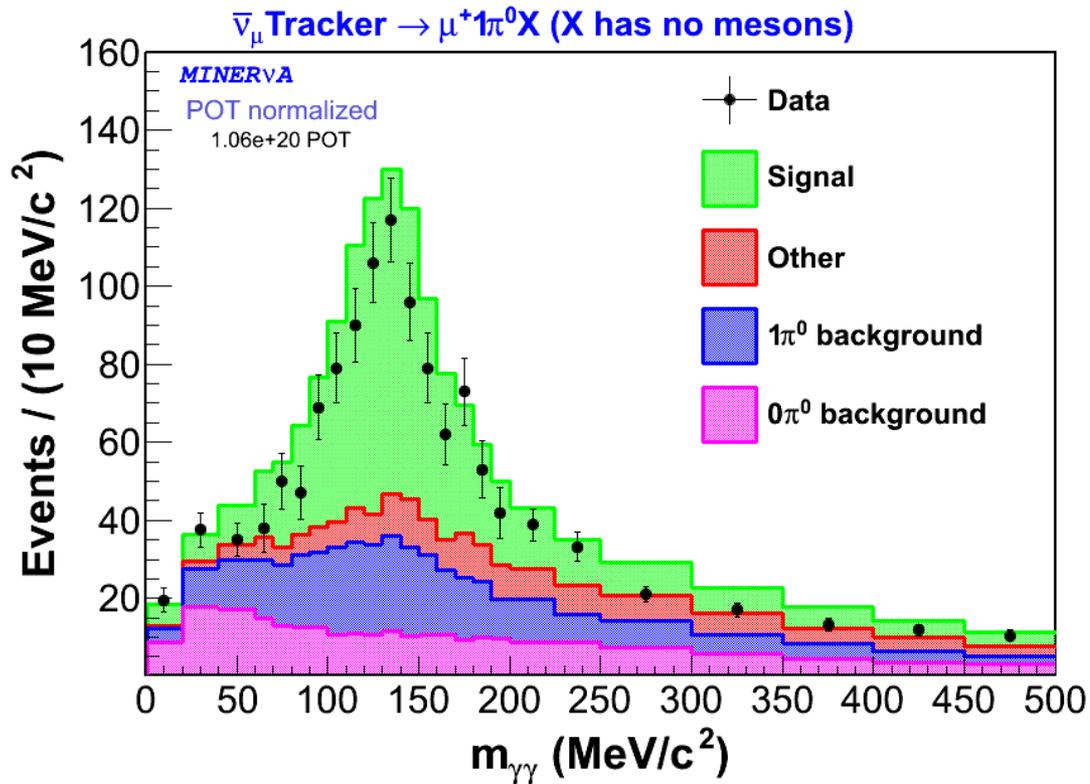
# Single $\pi^0$ production



**NC mode:  $\nu_\mu (\text{C,H}) \rightarrow \nu_\mu \pi^0 + \text{nucleons}$**

**is the main background in  $\nu_\mu \rightarrow \nu_e$  searches**

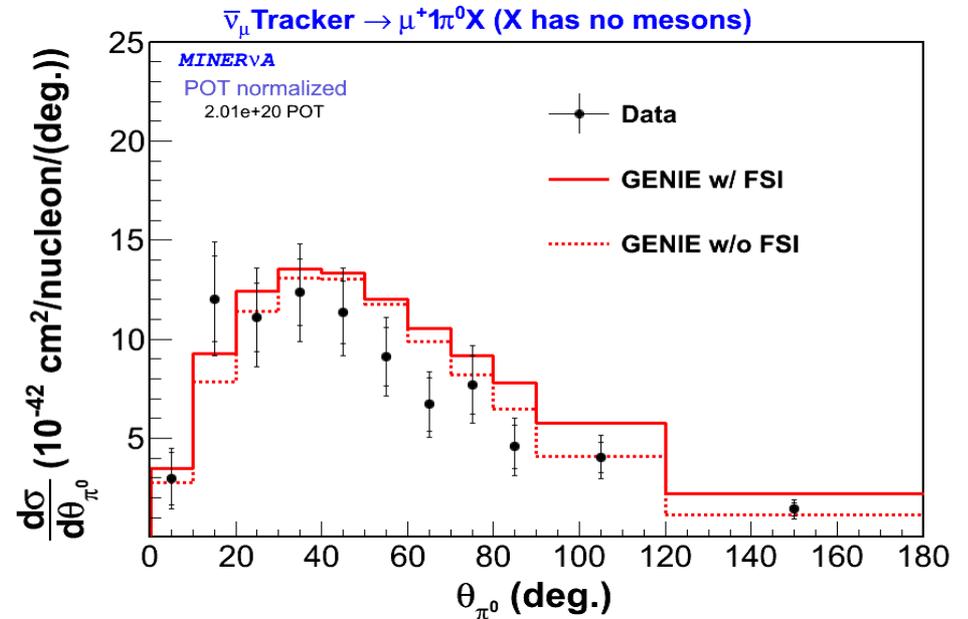
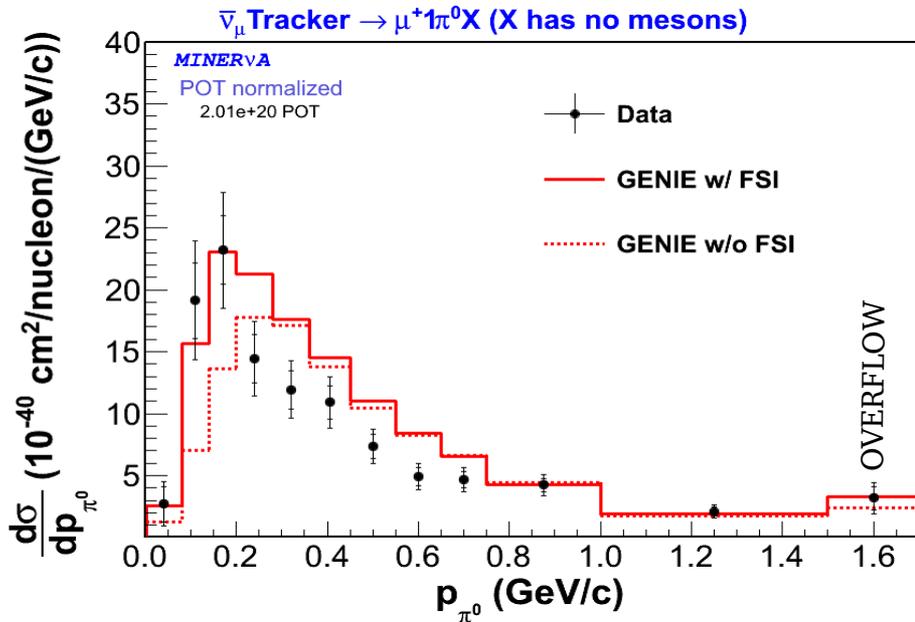
# Single $\pi^0$ production



## MC background breakdown:

- 1) **Background 1**: events with  $\pi^0$  in the final state plus charged pion (so it's not our signal)
- 2) **Background 2**: events with no final state  $\pi^0$ , but there is secondary  $\pi^0$ s, e.g., from  $\pi$ -charge exchange
- 3) **Background 3**: events with no final state nor secondary  $\pi^0$ s

# Single $\pi^0$ Cross-sections



- Data are in better agreement with the cross section with FSI
- Cross section with FSI is above that without FSI across momentum range
- Above 0.3 GeV/c, cross sections with and without FSI are similar
- Below 0.3 GeV/c, cross sections with and without FSI are very different

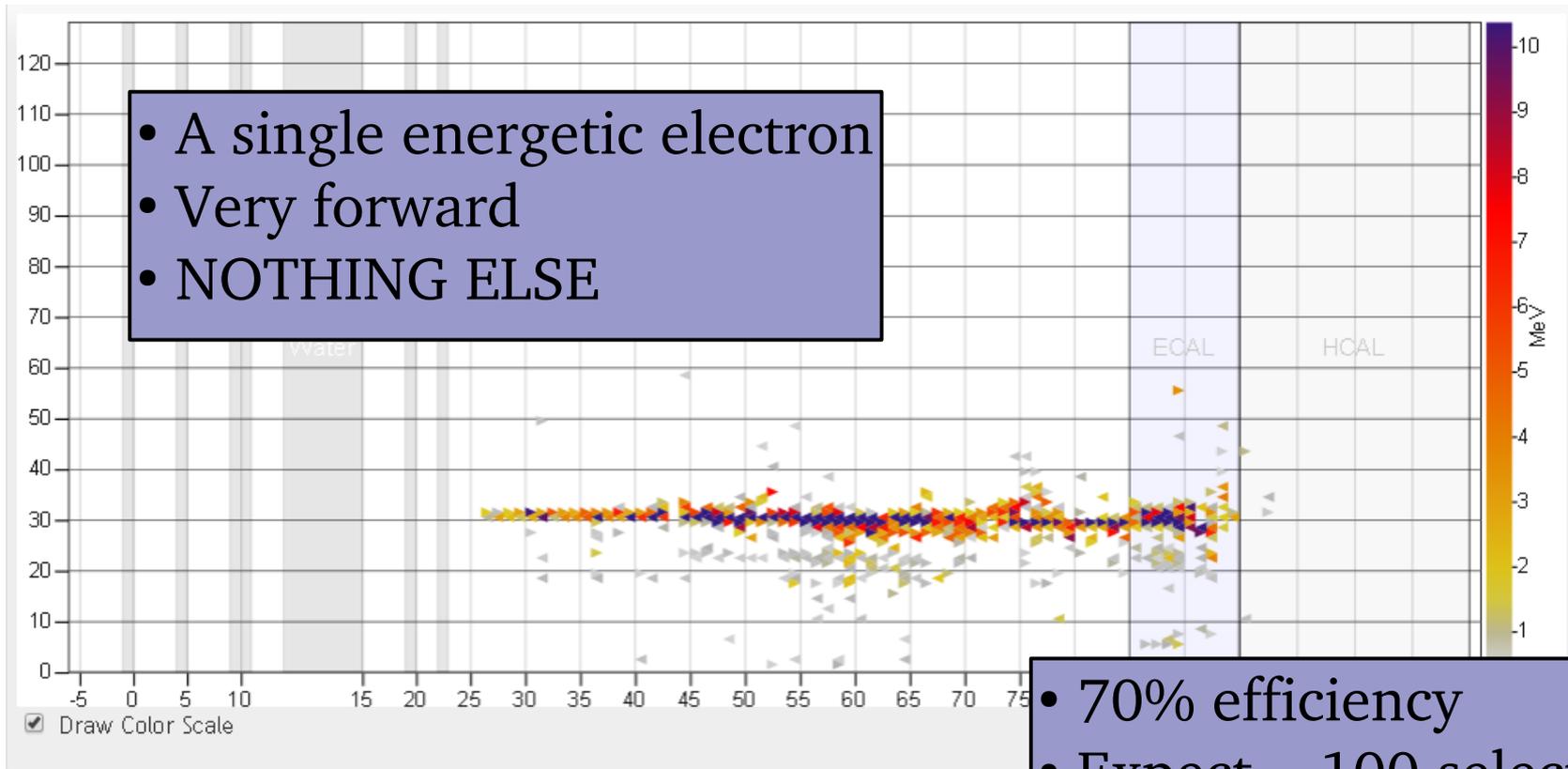
- FSI produce slightly more both forward and backward going signal

# $\nu$ - electron scattering

Standard candle  
cross-section, precisely  
predicted by the SM

$$\frac{d\sigma(\nu_\mu e^- \rightarrow \nu_\mu e^-)}{dy} = \frac{G_F^2 m_e E_\nu}{2\pi} \left[ \left( \frac{1}{2} - \sin^2 \theta_W \right)^2 + \sin^4 \theta_W (1-y)^2 \right]$$

$\sim 10^{-41} \text{ cm}^2 = 0.01 \text{ fb}$



- A single energetic electron
- Very forward
- NOTHING ELSE

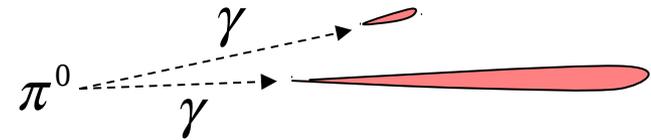
- 70% efficiency
- Expect  $\sim 100$  selected events for  $3.43 \times 10^{20}$  POT in the NuMI LE beam

# $\nu$ - electron scattering

Major background from events with a  $\pi^0$  where 1  $\gamma$  is lost

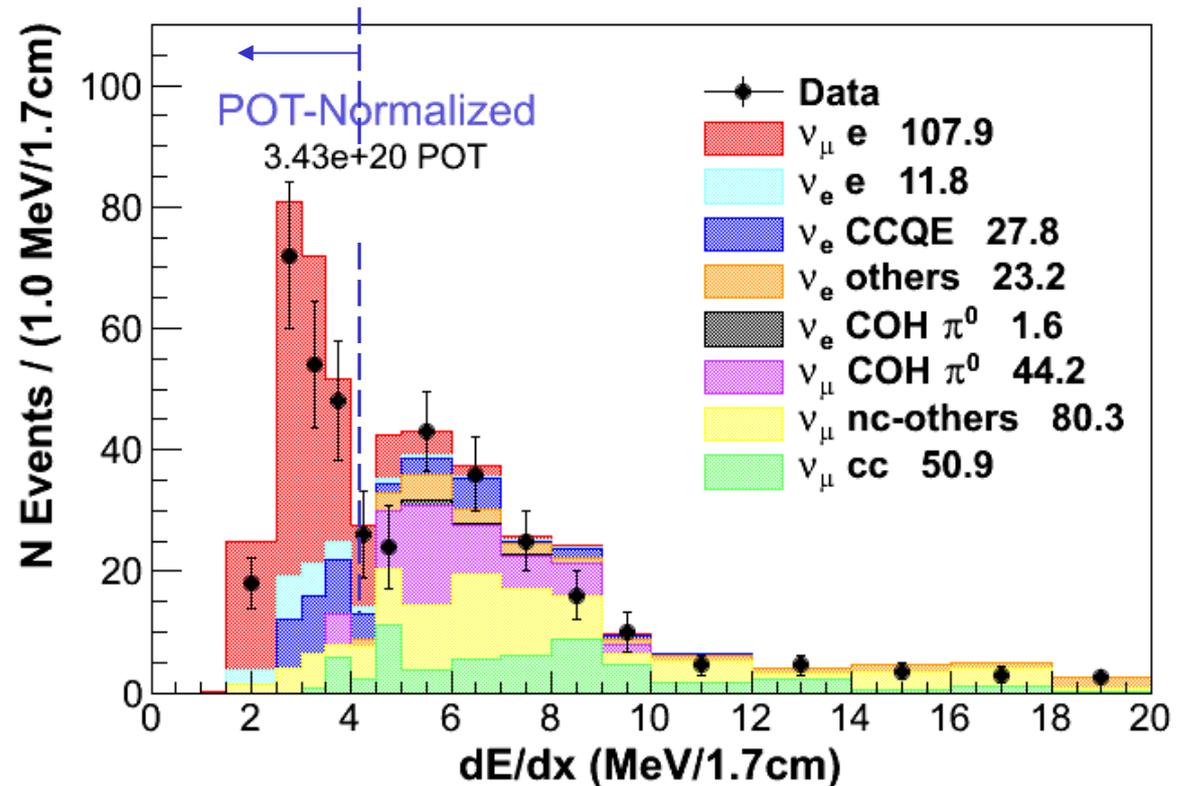
$$\nu_{\mu} A \rightarrow \nu_{\mu} A \pi^0 \quad \text{NC-coherent } \pi^0$$

$$\nu_{\mu} N \rightarrow \nu_{\mu} N \pi^0 \quad \text{NC-resonant } \pi^0$$



Background rejection  
Look at  $dE/dx$  near  
the start of the shower

electron = 1 MIP  
gamma = 2 MIPs

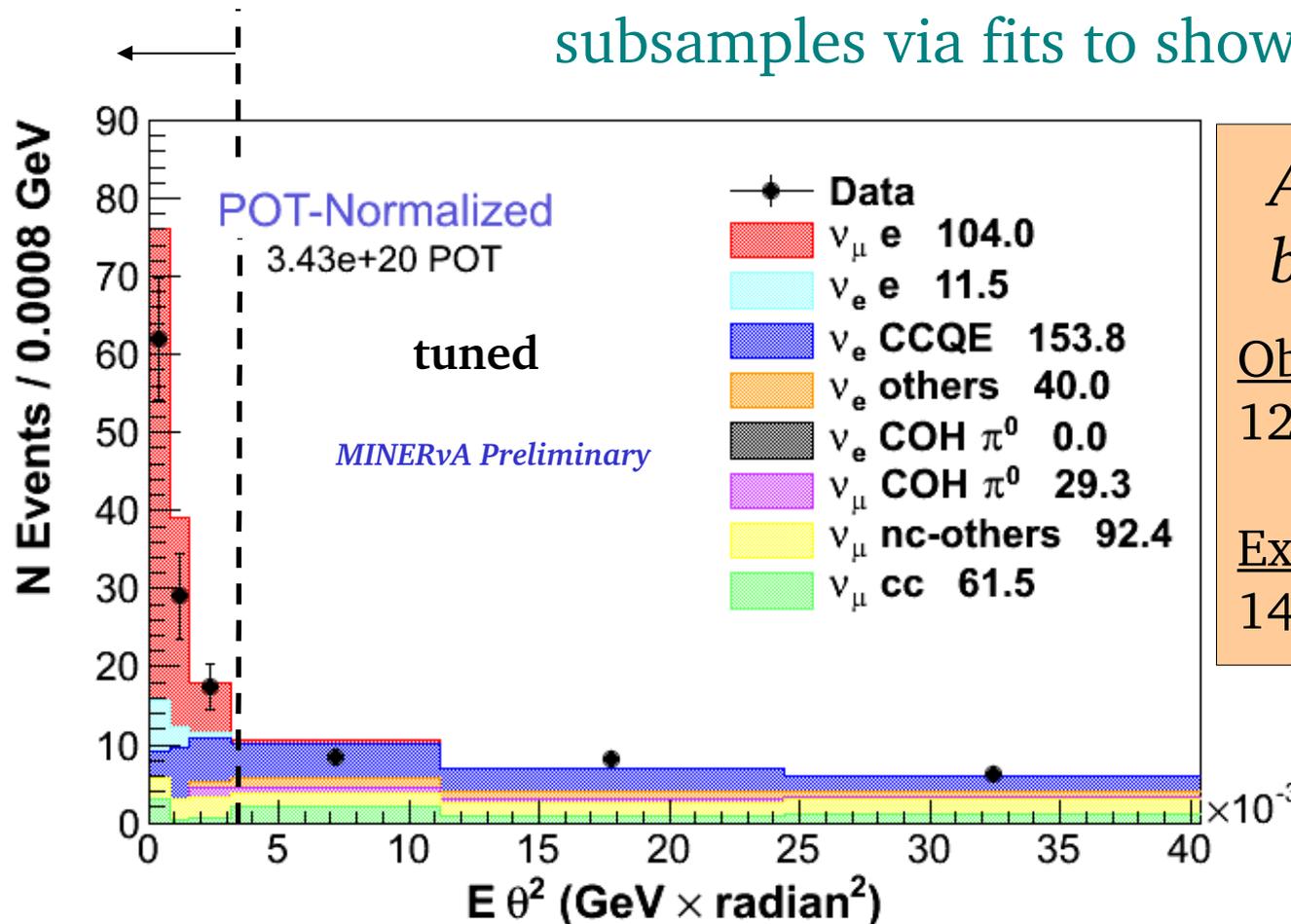


# $\nu$ - electron scattering

Background from  $\nu_e$  CC interactions removed via  $E\theta^2$  cut

Data driven background constraint

$E\theta^2 < 0.0032 \text{ GeV} \cdot \text{rad}^2$  via sidebands in  $dE/dx$ ,  $E\theta^2$ . Sensitivity to subsamples via fits to shower topological variables.



*After efficiency and background corrections*

Observed

$123.8 \pm 17.0$  (stat)  $\pm 9.1$  (syst)

Expected

$147.5 \pm 22.9$  (flux)

*Gives a constraint on the flux comparable to current uncertainty.*

# Other analyses in progress

- QEL:
  - two tracks.  $Q^2$  reco with muon and proton arms compared
  - $d^2\sigma/d\theta_\mu dp_\mu$  for numu and numubar
  - Michel tag to remove inelastic background
  - nuclear targets
- Coherent pion production
- Inclusive scattering off of nuclear targets to explore the EMC effect
- $\nu_e$  QEL, K production, & the flux
- Many additional channels (e.g., all  $\nu A$  NC) and the ME beam adds kinematic reach to existing measurements.
- Also, for NO $\nu$ A, T2K, LBNE I hope the community will engage in a generator tuning effort similar to that of the collider program.

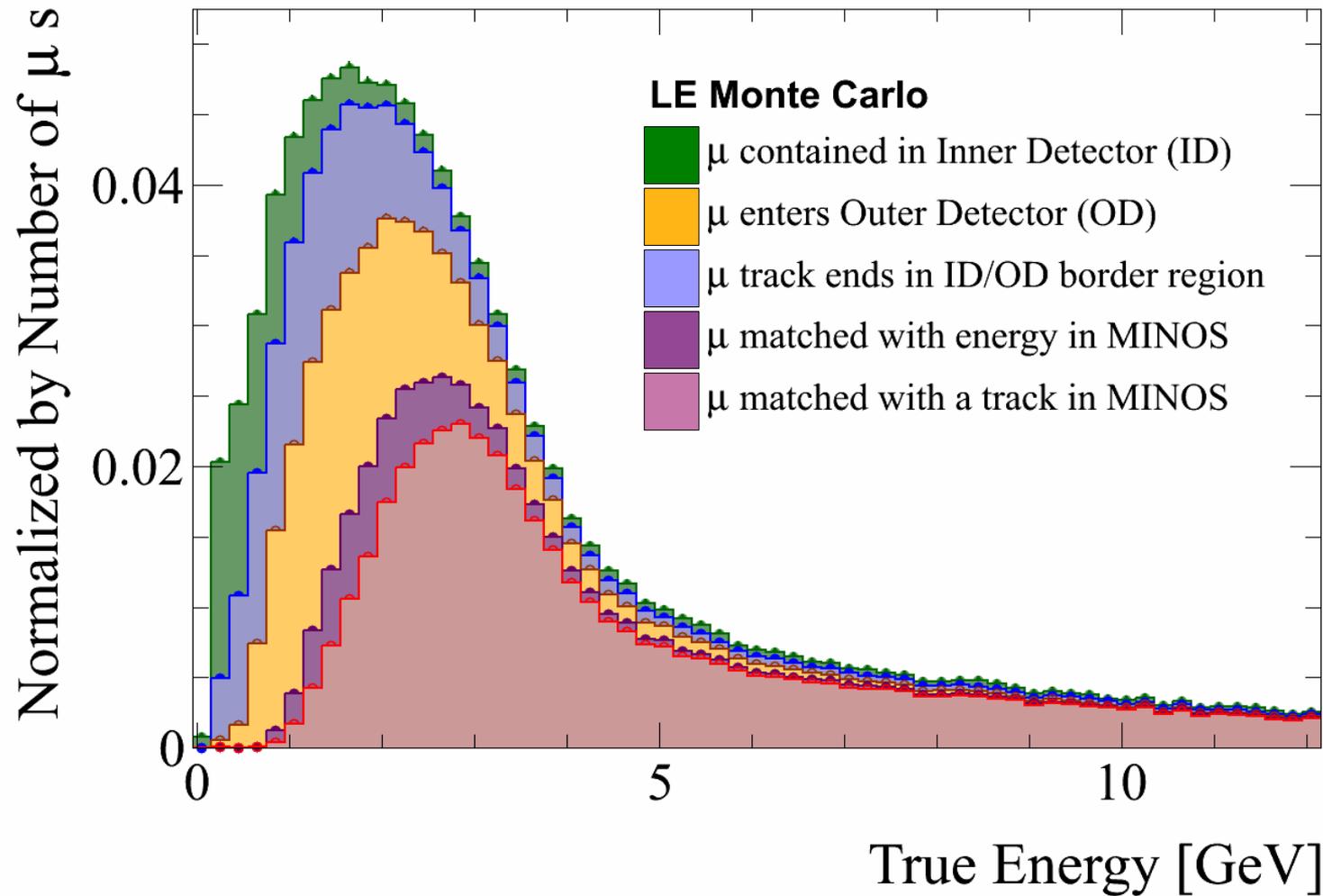


Thank you!  
¡Muchas  
Gracias!

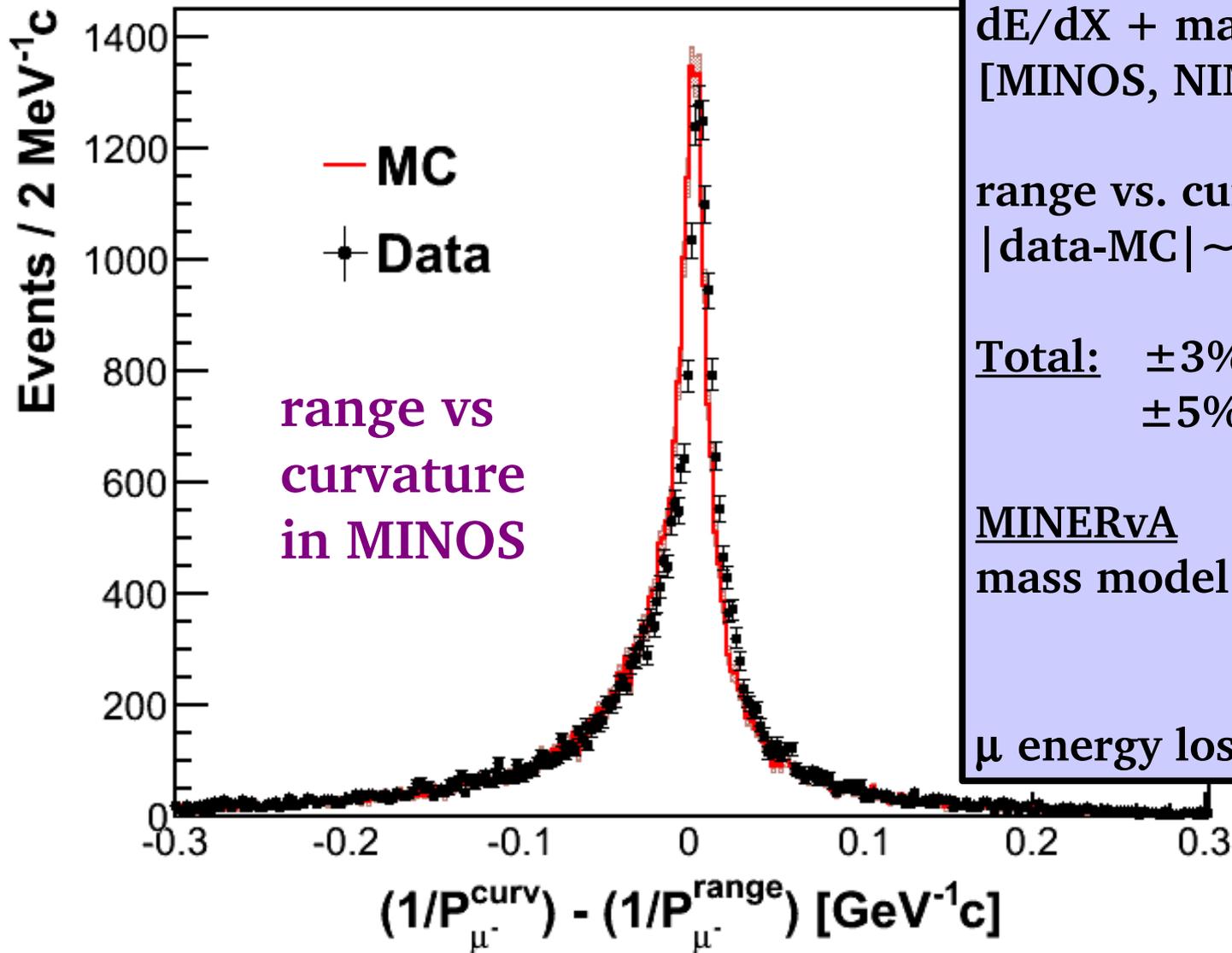
Centro Brasileiro de Pesquisas Físicas  
Fermilab  
University of Florida  
Universidad de Guanajuato  
Hampton University  
Inst. Nucl. Reas. Moscow  
Mass. Col. Lib. Arts  
Northwestern University  
Otterbein University  
Pontificia Universidad Catolica del Peru  
University of Pittsburgh  
University of Rochester  
Rutgers University  
Tufts University  
University of Minnesota at Duluth  
Universidad Nacional de Ingeniería  
Universidad Técnica Federico Santa María  
William and Mary

# Where do the muons go?

Good acceptance into MINOS for  $\theta_{\mu} < 20^{\circ}$



# Muon energy uncertainty



## MINOS

dE/dX + mass model = 2%  
[MINOS, NIM A 596, 190 (2008)]

range vs. curvature  
|data-MC| ~25 MeV

Total: ±3% p > 1.5 GeV  
±5% P < 1.5 GeV

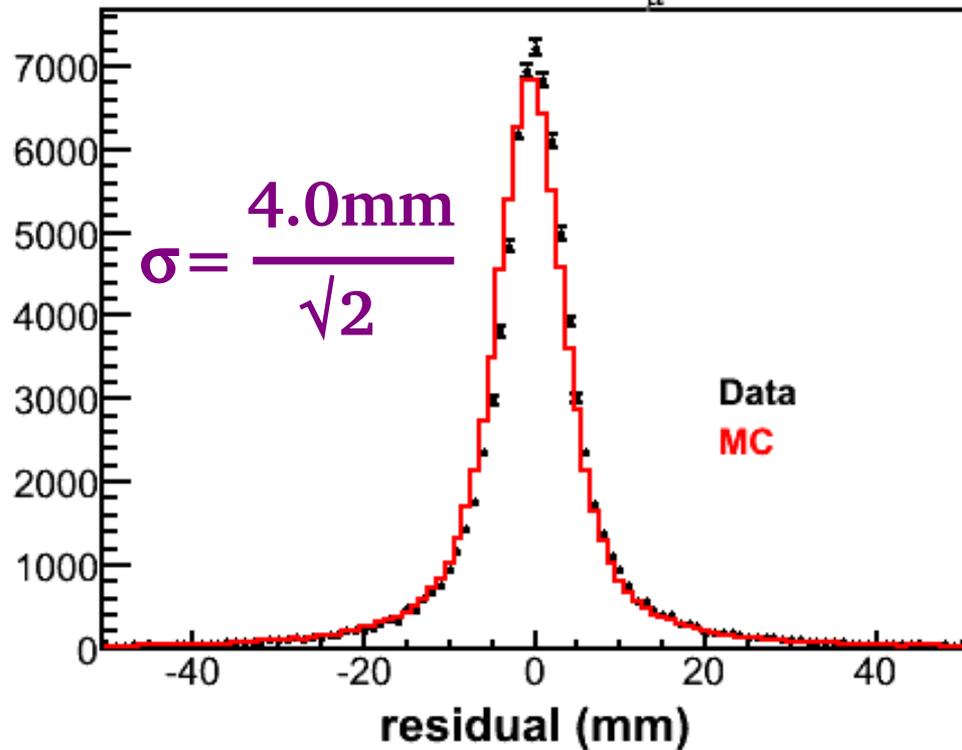
## MINERvA

mass model = 11 MeV tracker  
= 17 MeV Nucl. Tgts.

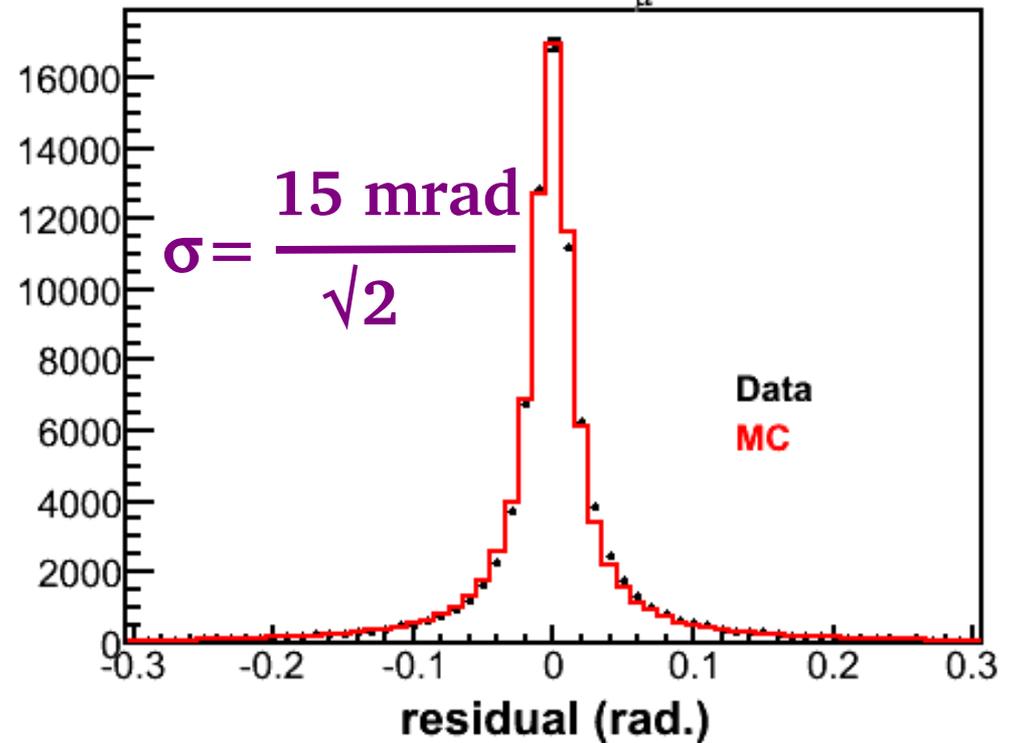
μ energy loss = 30 MeV

# Tracking resolutions

Vertex Y Residual,  $p_{\mu} \leq 20 \text{ GeV/c}$



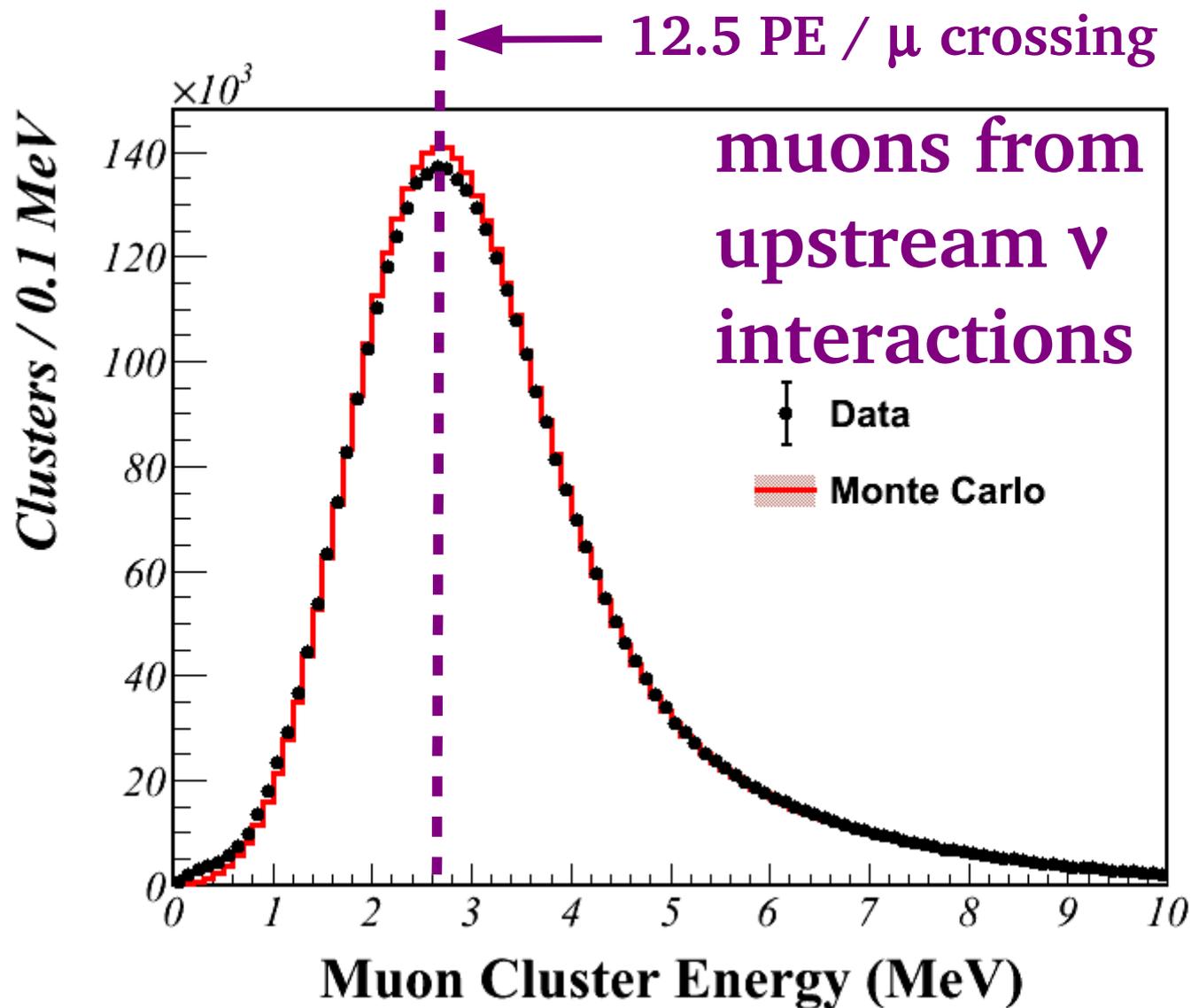
dY/dZ Residual,  $p_{\mu} \leq 20 \text{ GeV/c}$



Split-track study of rock  $\mu$   
in tracker region



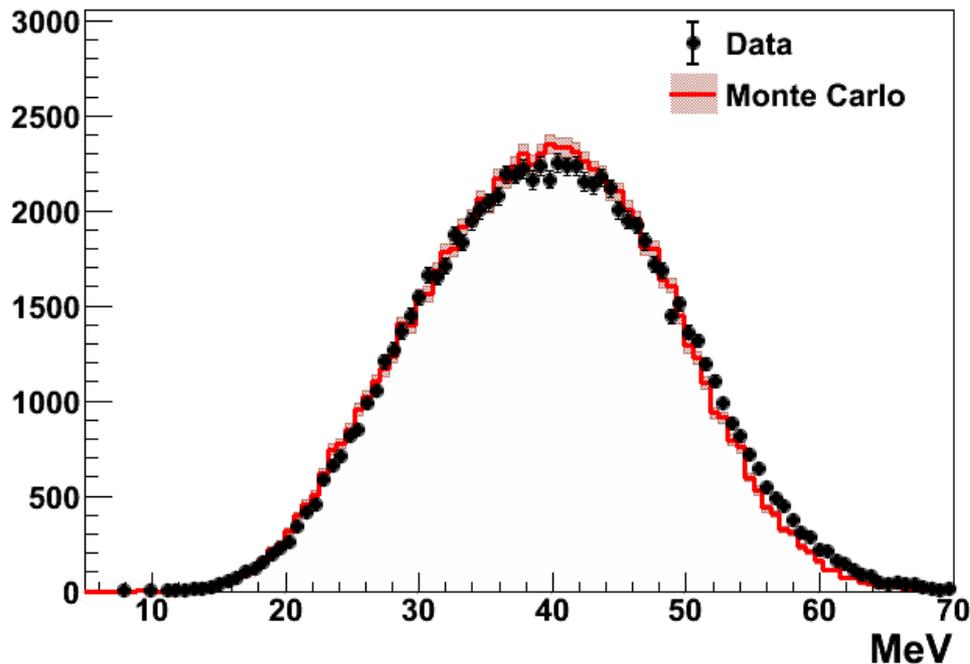
# visible energy scale



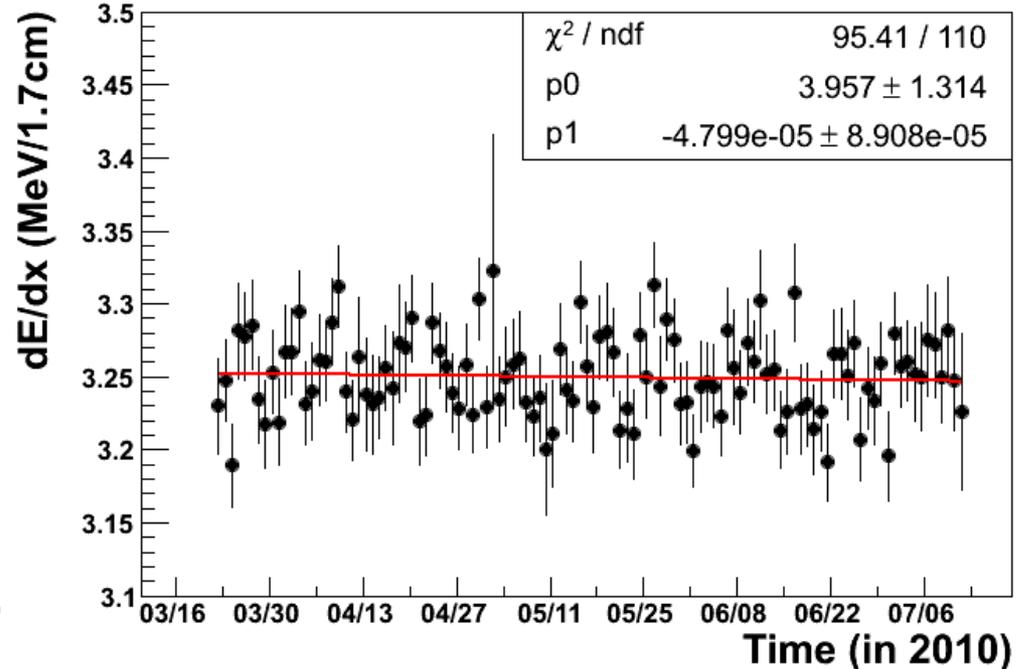
# Michel electrons

$$\text{Michel} = \mu \rightarrow e \bar{\nu}$$

Michel electron energy

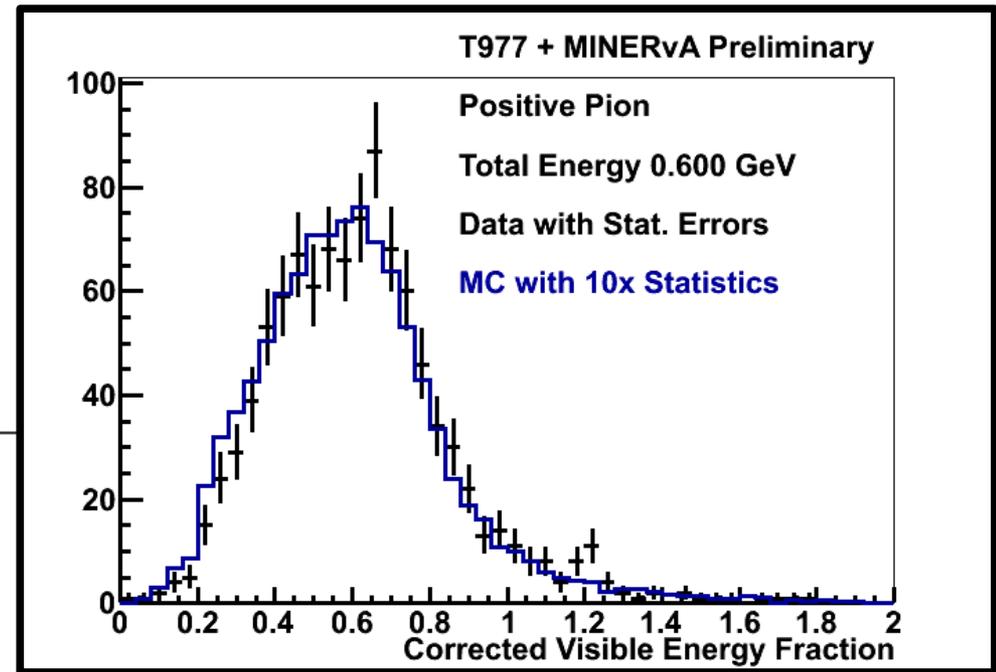
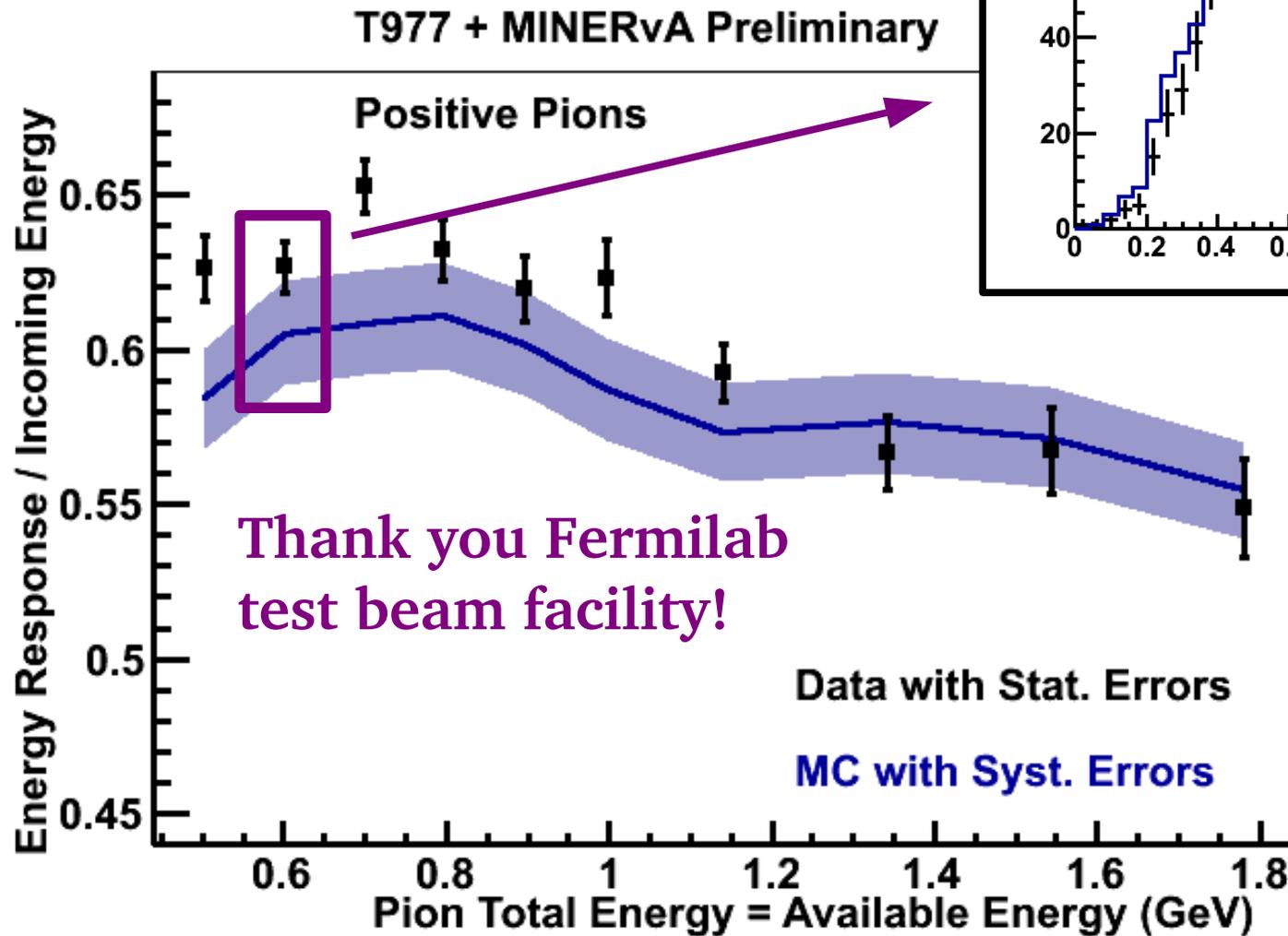


Michel electron dE/dx vs time



Cross-check on  $\mu$  derived energy scale  
EM response uncertainty = 3%  
A nice stable detector!

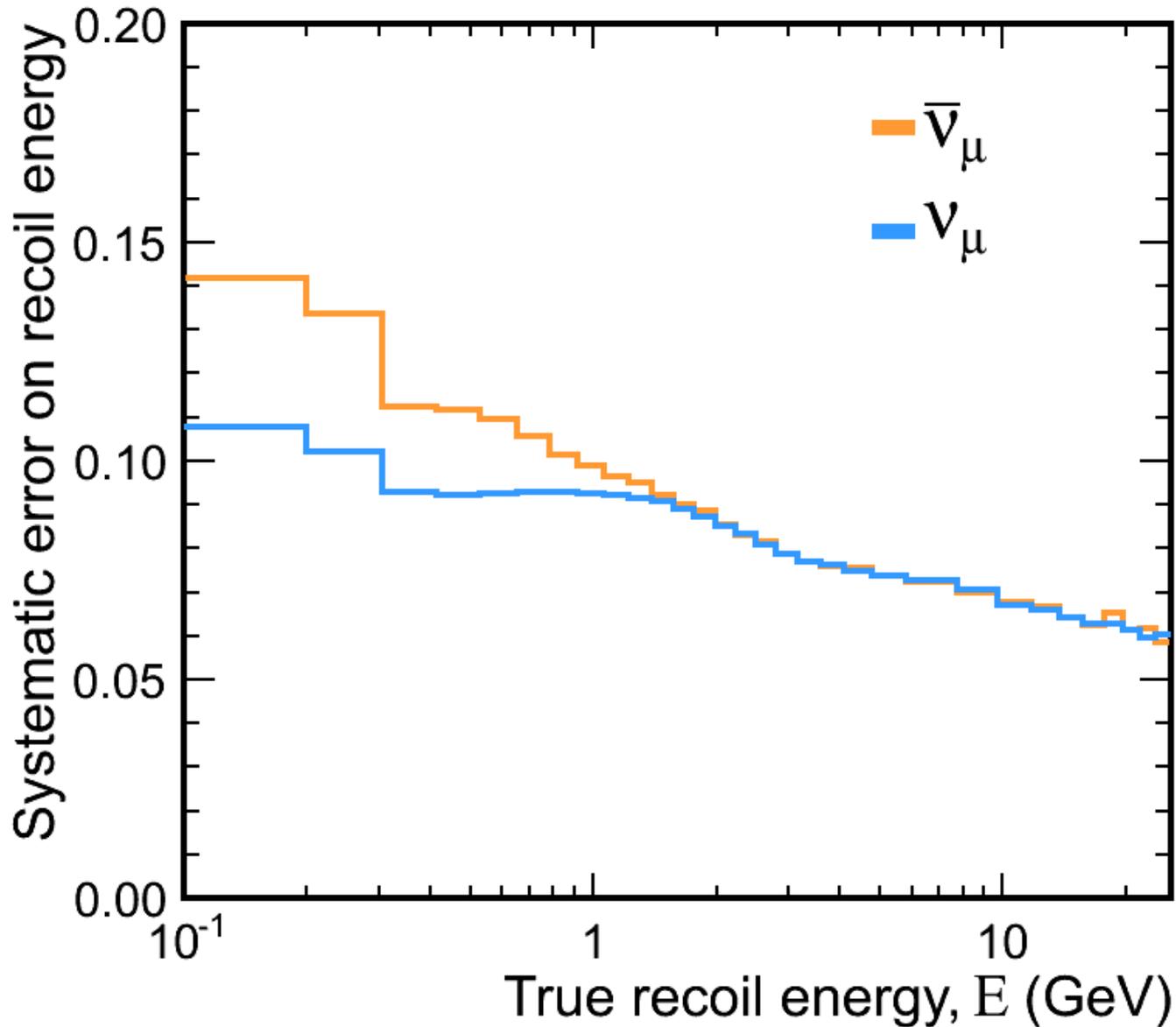
# FNAL-T977 Test Beam



$\pi^+$  agreement  $\sim 5\%$   
 $\pi^-$  a bit better  
p a bit worse (10%)

Resolution well modeled

# shower energy uncertainty



**Convolution of  
single particle  
uncertainties**

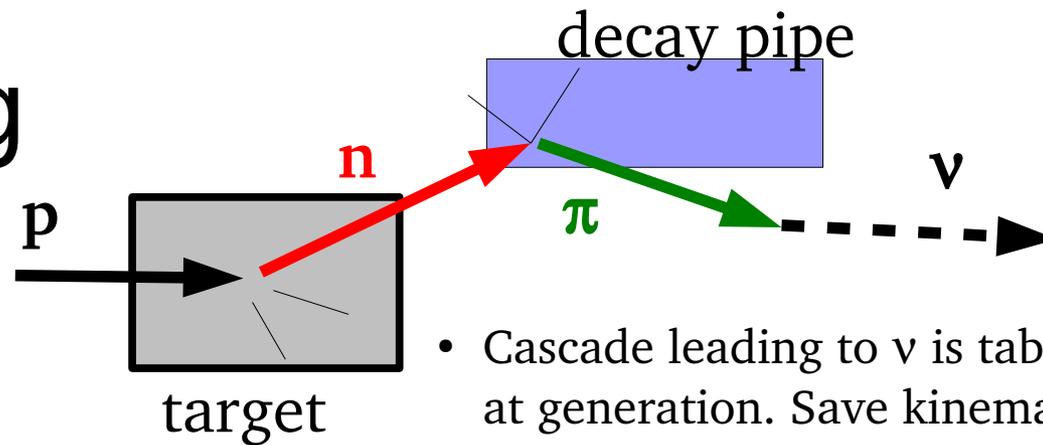
$\pi, K = 5\%$

$e, \gamma = 3\%$

$p = 10\%$

$n = 20\%$

# Constraining the flux



- Cascade leading to  $\nu$  is tabulated at generation. Save kinematics & material
- In analysis, interactions reweighted as  $\sigma(\text{data})/\sigma(\text{MC})$
- Includes correction for beam attenuation in the target.

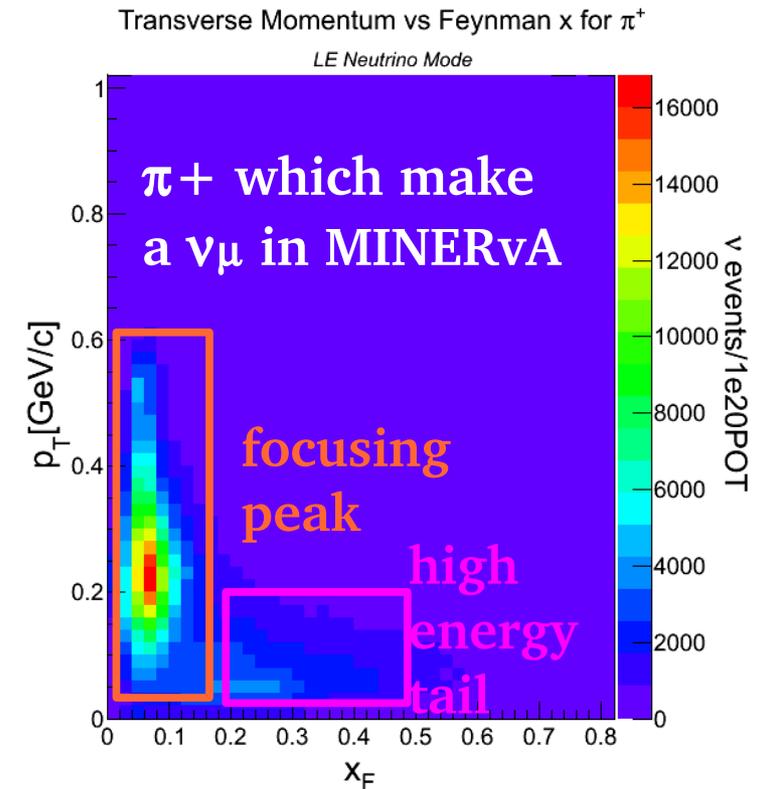
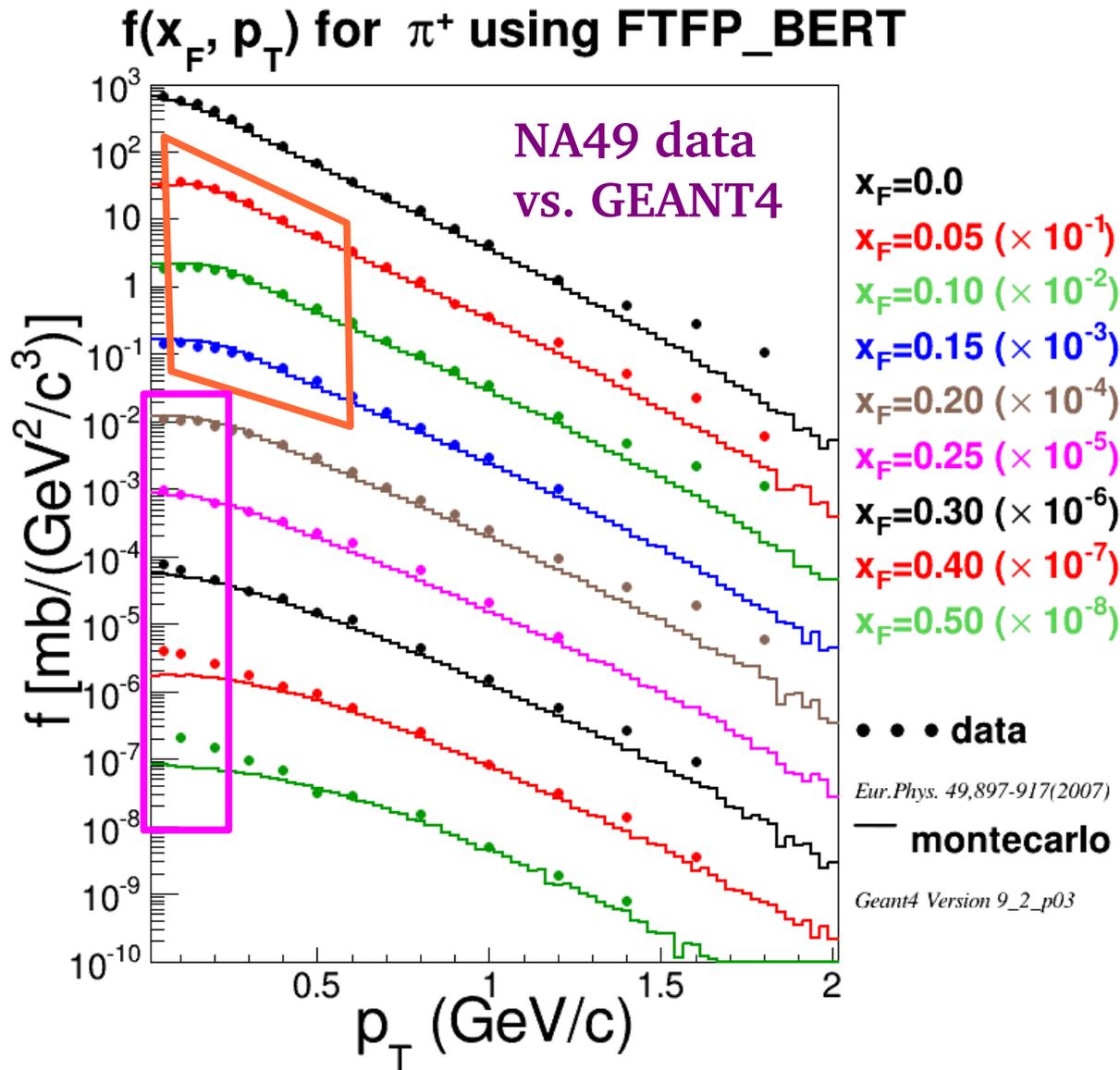
## Datasets Used

- NA49 pC @ 158 GeV
  - $\pi^\pm$  production for  $x_F < 0.5$  [*Eur.Phys.J. C49 (2007) 897*]
  - $K^\pm$  production for  $x_F < 0.2$  [*G. Tinti Ph.D. thesis*]
  - p production for  $x_F < 0.9$  [*Eur.Phys.J. C73 (2013) 2364*]
- MIPP pC @ 120 GeV [*A. Lebedev Ph.D. thesis*]
  - $K/\pi$  ratio + NA49 extends kaon coverage to  $x_F < 0.5$
- Weights applied for  $12 < p_{\text{incident}} < 120$  GeV.
  - Data cross-section scaled using FLUKA [[www.fluka.org](http://www.fluka.org)]
  - Checked by comparing to NA61 pC  $\rightarrow \pi^\pm$  X at 31 GeV/c [*Phys.Rev. C84 (2011)034604*]
- Interactions on Al, Fe, He and Air treated as if on C

} some  $p_T$  dependence

# NA49: pC $\rightarrow$ $\pi, K, p, n$ @ 158 GeV

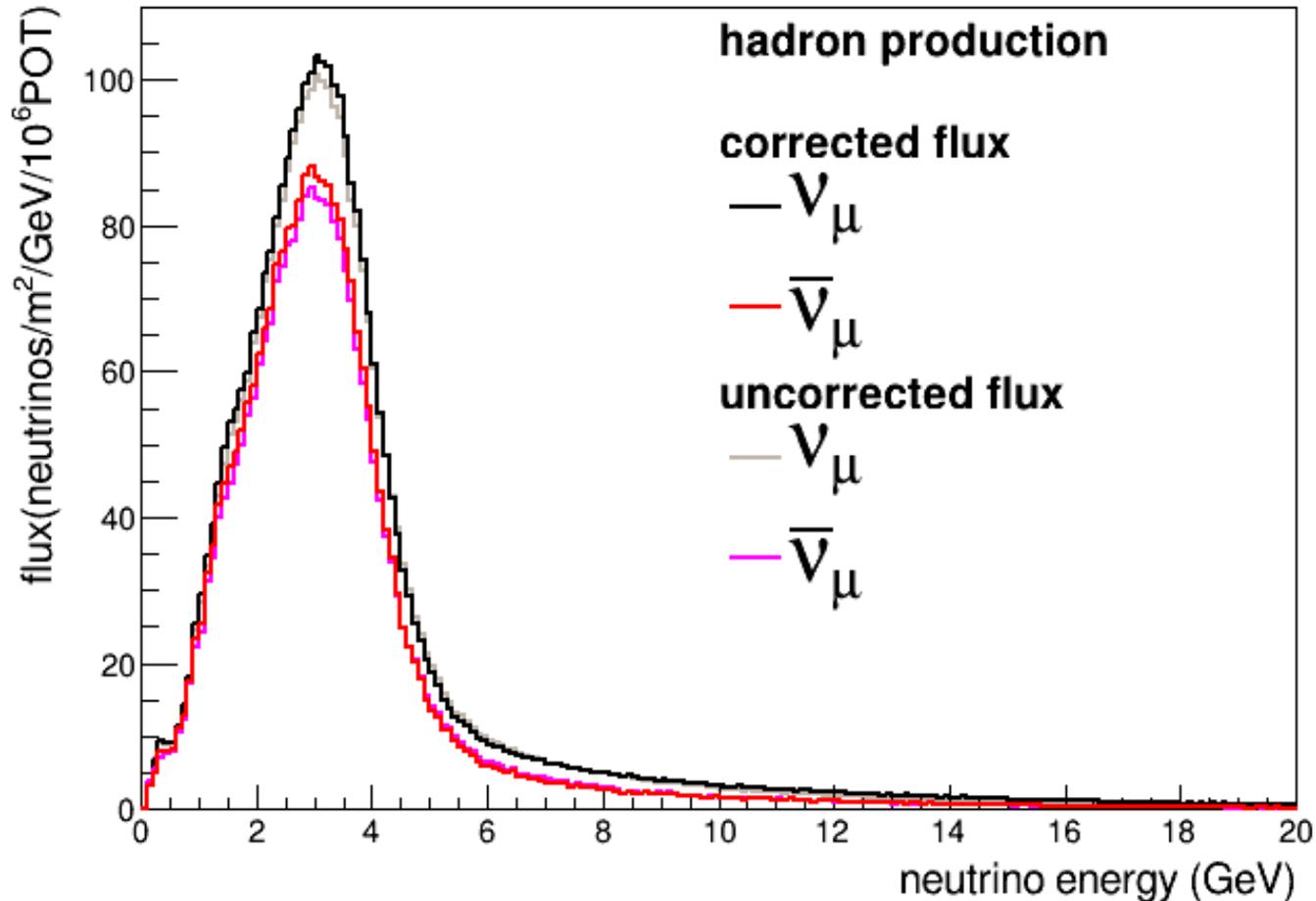
$f(x_F, p_T) = E d^3\sigma/dp^3 =$  invariant production cross-section



**Uncertainties**  
7.5% systematic  
2-10% statistical

# The Flux

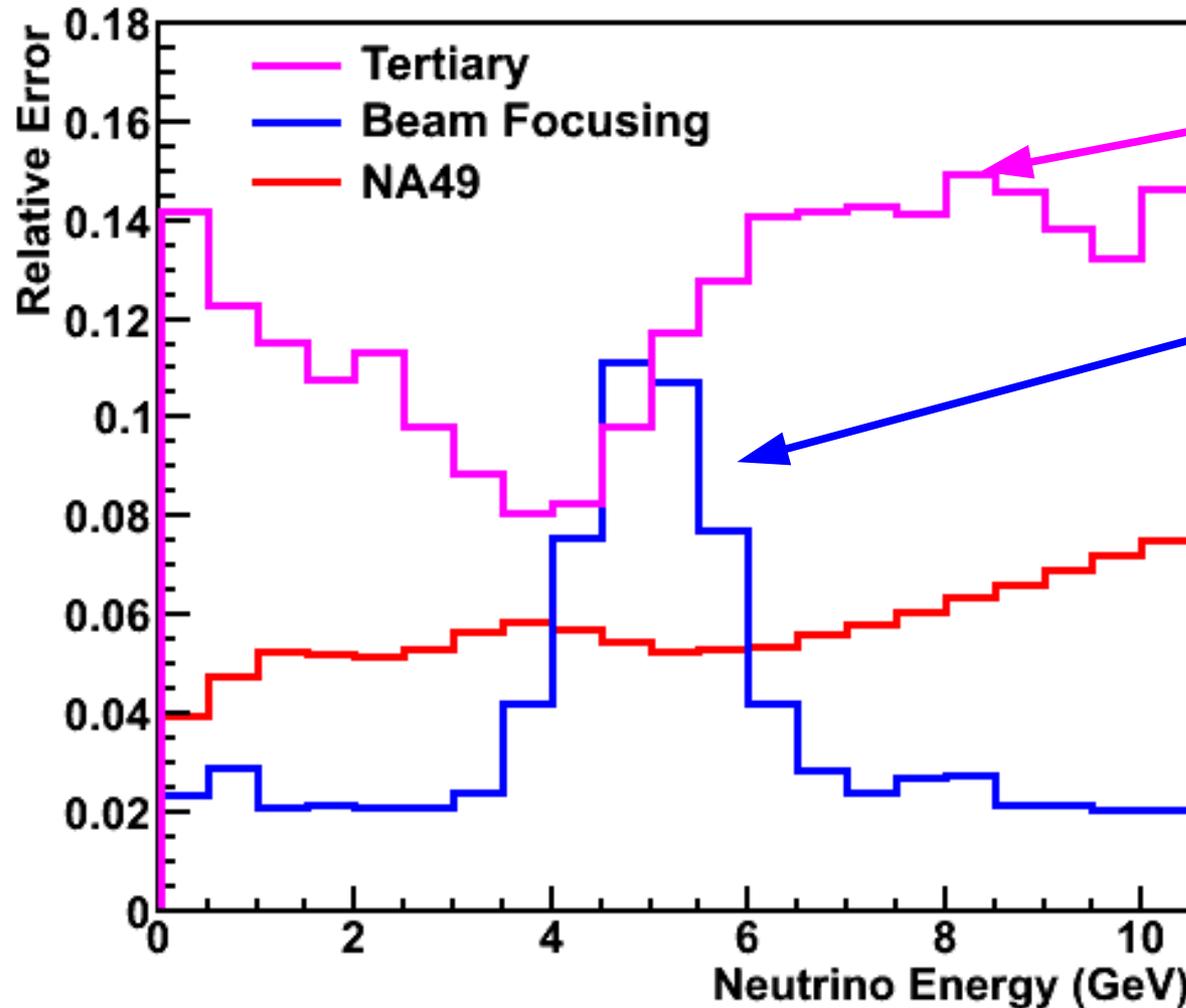
NuMI Low Energy Beam, FTFP, Dec 2013



GEANT4 based  
simulation of the  
NuMI beamline.

G4 9.4.p02  
FTFP physics list

# Flux Uncertainties

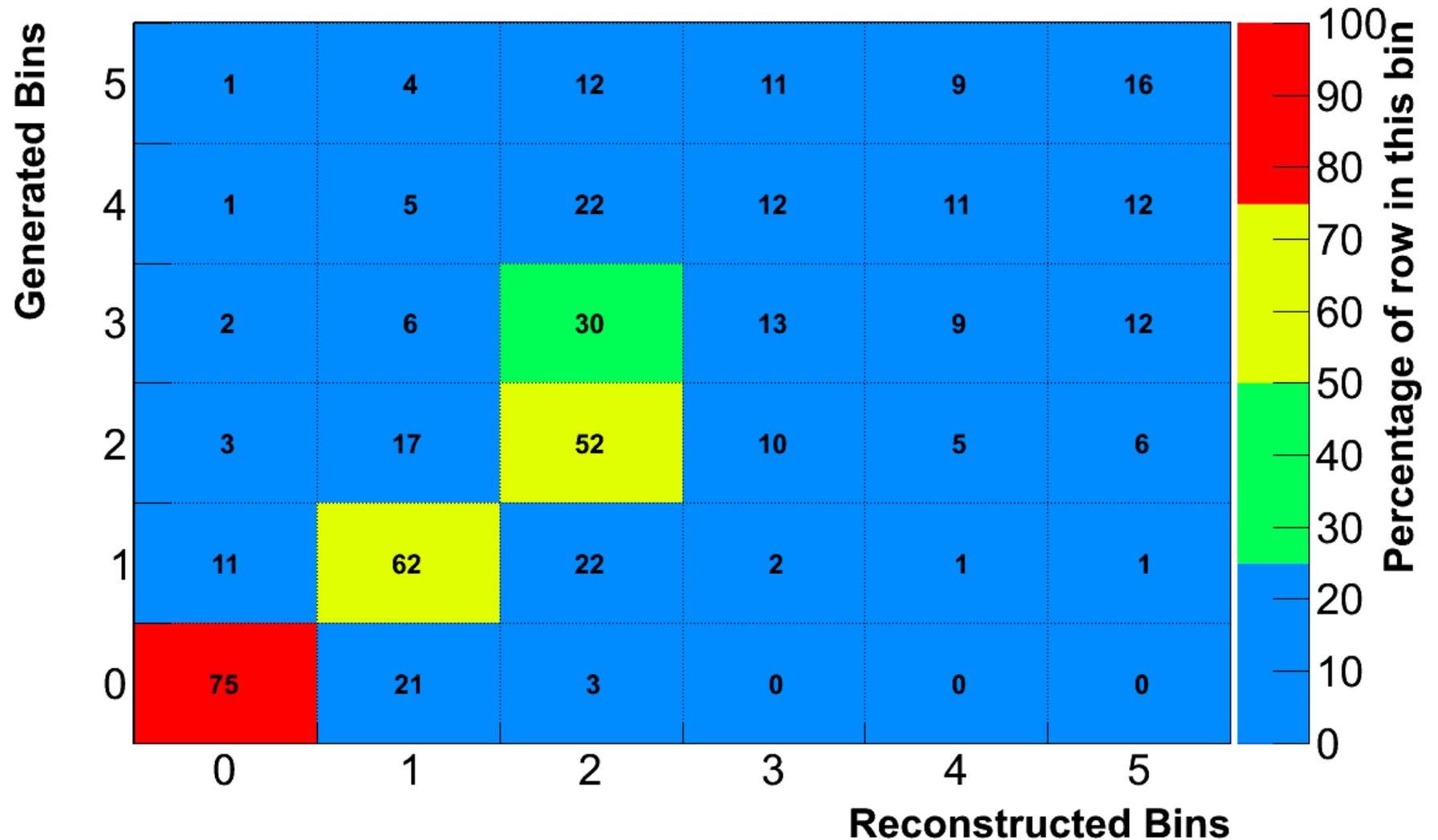


“Tertiary”  
= non-NA49  
model spread

Z. Pavlovic,  
PhD Thesis,  
Texas (2008)

# $X_{Bj}$ smearing

Bin Migration in Bjorken x - Iron of Target 5



## Cross Section Model Uncertainties

Uncertainty	1 $\sigma$
$M_A$ (Elastic Scattering)	$\pm 25\%$
Eta (Elastic scattering)	$\pm 30\%$
$M_A$ (CCQE Scattering)	+25% -15%
CCQE Normalization	+20% -15%
CCQE Vector Form factor model	on/off
CC Resonance Normalization	$\pm 20\%$
$M_A$ (Resonance Production)	$\pm 20\%$
$M_V$ (Resonance Production)	$\pm 10\%$
1pi production from $\nu p / \bar{\nu} n$ non-resonant interactions	$\pm 50\%$
1pi production from $\nu n / \bar{\nu} p$ non-resonant interactions	$\pm 50\%$
2pi production from $\nu p / \bar{\nu} n$ non-resonant interactions	$\pm 50\%$
2pi production from $\nu n / \bar{\nu} p$ non-resonant interactions	$\pm 50\%$
Modify Pauli blocking (CCQE) at low $Q^2$ (change PB momentum threshold)	$\pm 30\%$

## Intranuclear Rescattering Uncertainties

Uncertainty	1 $\sigma$
Pion mean free path	$\pm 20\%$
Nucleon mean free path	$\pm 20\%$
Pion fates – absorption	$\pm 30\%$
Pion fates – charge exchange	$\pm 50\%$
Pion fates – Elastic	$\pm 10\%$
Pion fates – Inelastic	$\pm 40\%$
Pion fates – pion production	$\pm 20\%$
Nucleon fates – charge exchange	$\pm 50\%$
Nucleon fates – Elastic	$\pm 30\%$
Nucleon fates – Inelastic	$\pm 40\%$
Nucleon fates – absorption	$\pm 20\%$
Nucleon fates – pion production	$\pm 20\%$
AGKY hadronization model – $x_F$ distribution	$\pm 20\%$
Delta decay angular distribution	On/off
Resonance decay branching ratio to photon	$\pm 50\%$

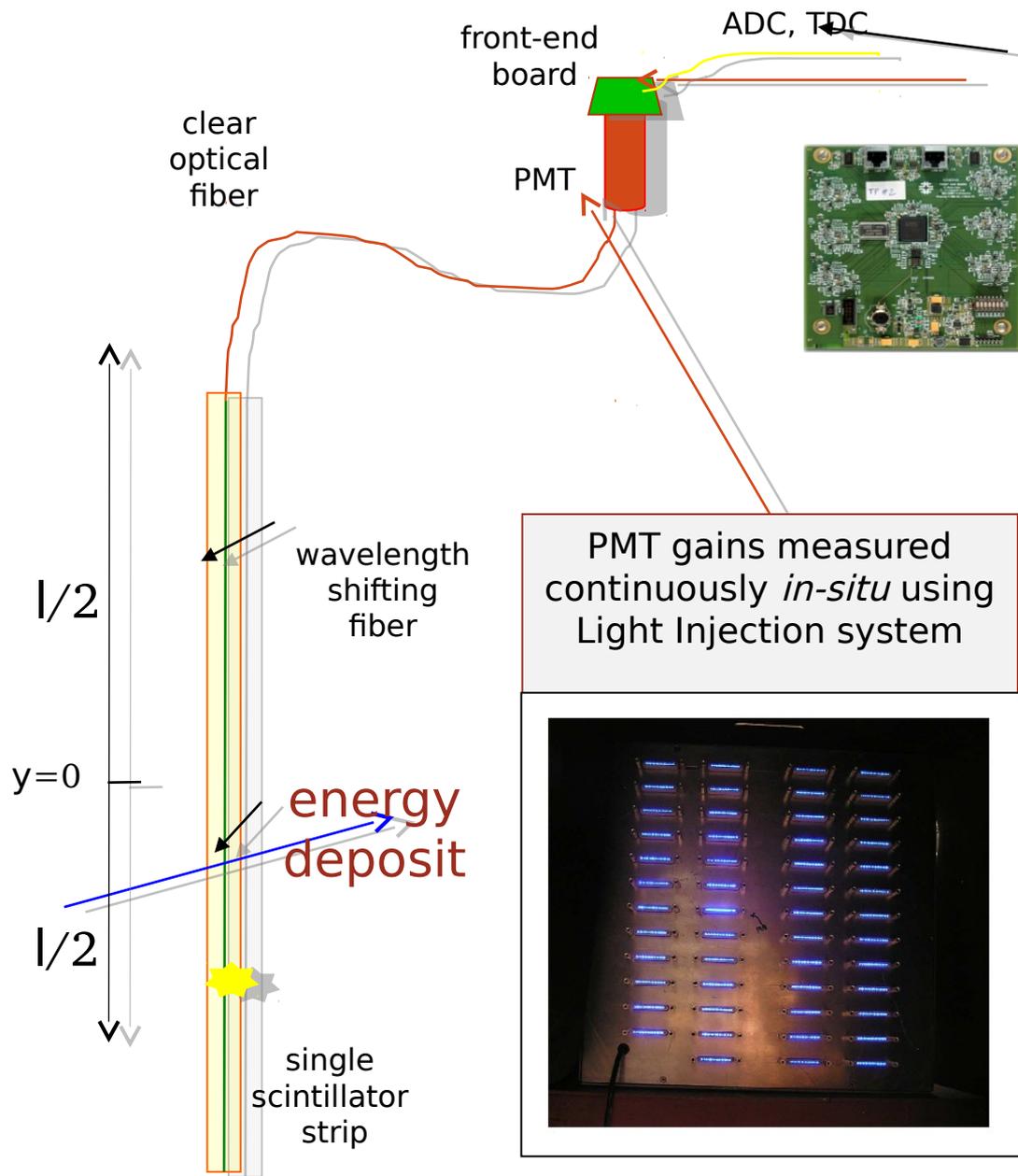
References: (1) [www.genie-mc.org](http://www.genie-mc.org), (2) arXiv:0806.2119, (3) D. Bhattacharya, Ph. D Thesis (U. Pittsburgh) 2009.

# Nuclear Target Event Rates

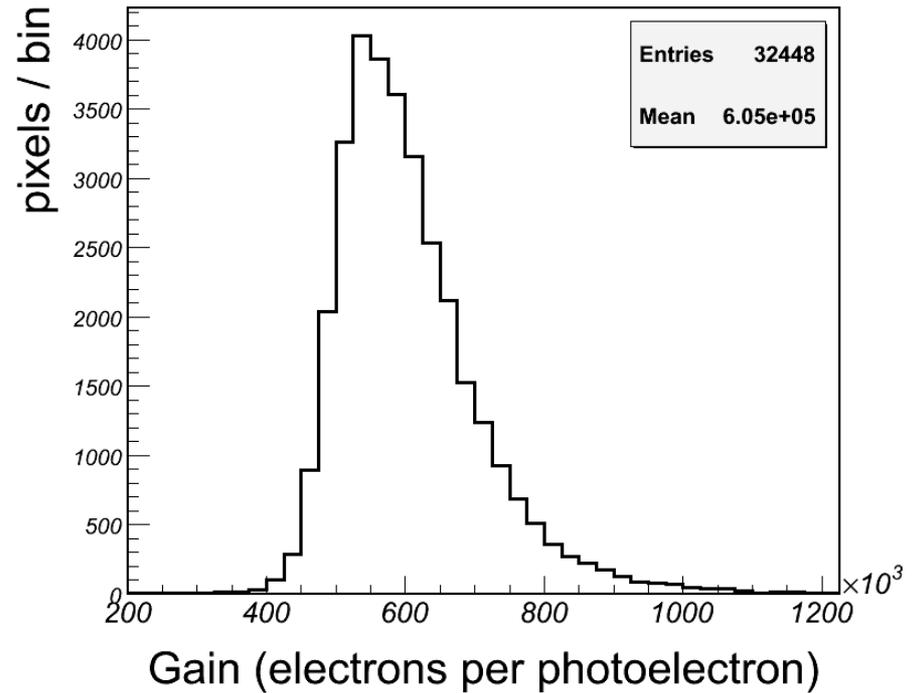
Target	Fiducial Mass	$\nu_{\mu}$ CC Events in $1.0e20$ P.O.T.
Plastic	6.43 tons	340k
Helium	0.25 tons	14k
Carbon	0.17 tons	9.0k
Water	0.39 tons	20k
Iron	0.97 tons	54k
Lead	0.98 tons	57k

GENIE 2.6, FLUKA08, 90cm radius, 116 tracker modules

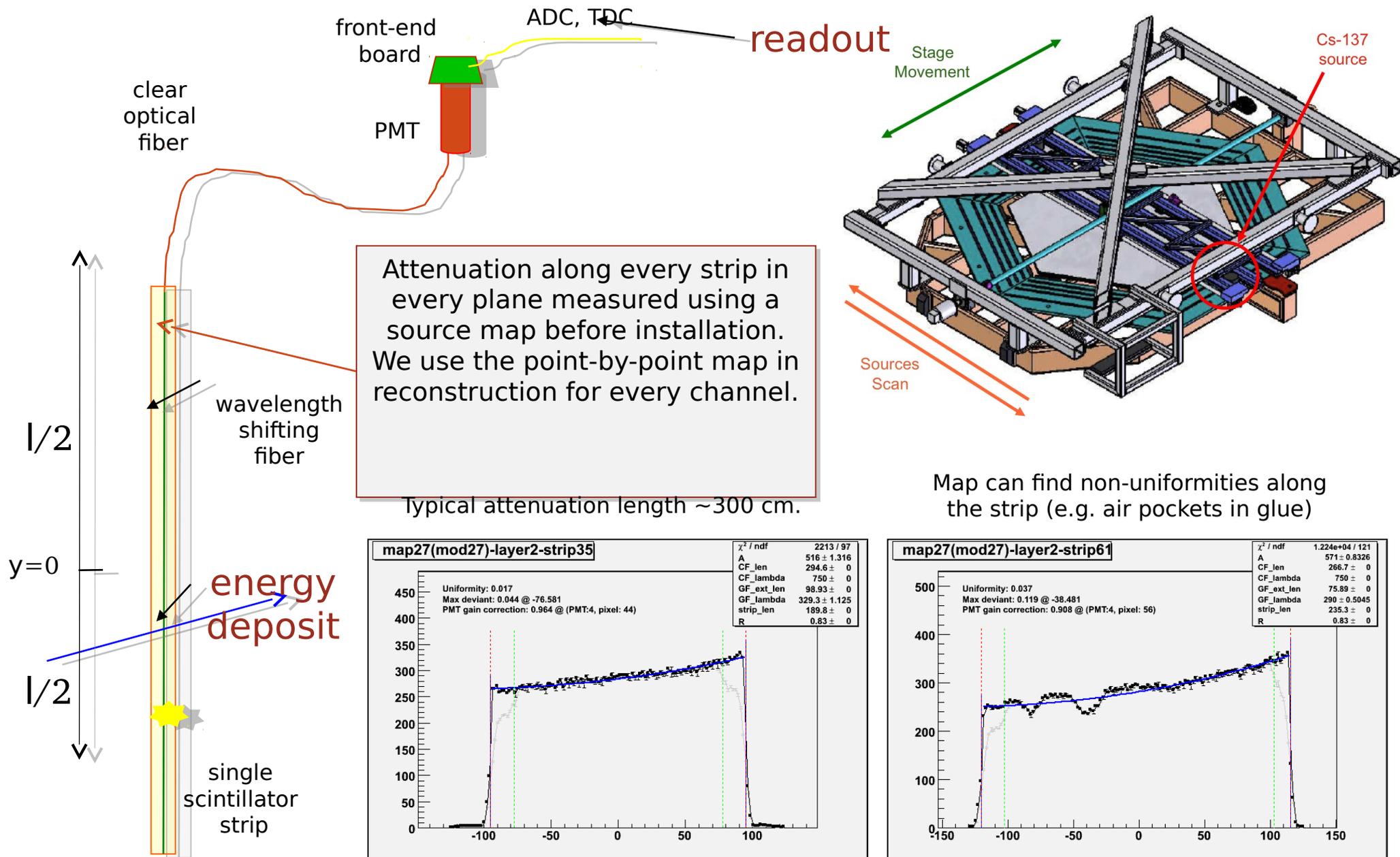
# Detector Calibration



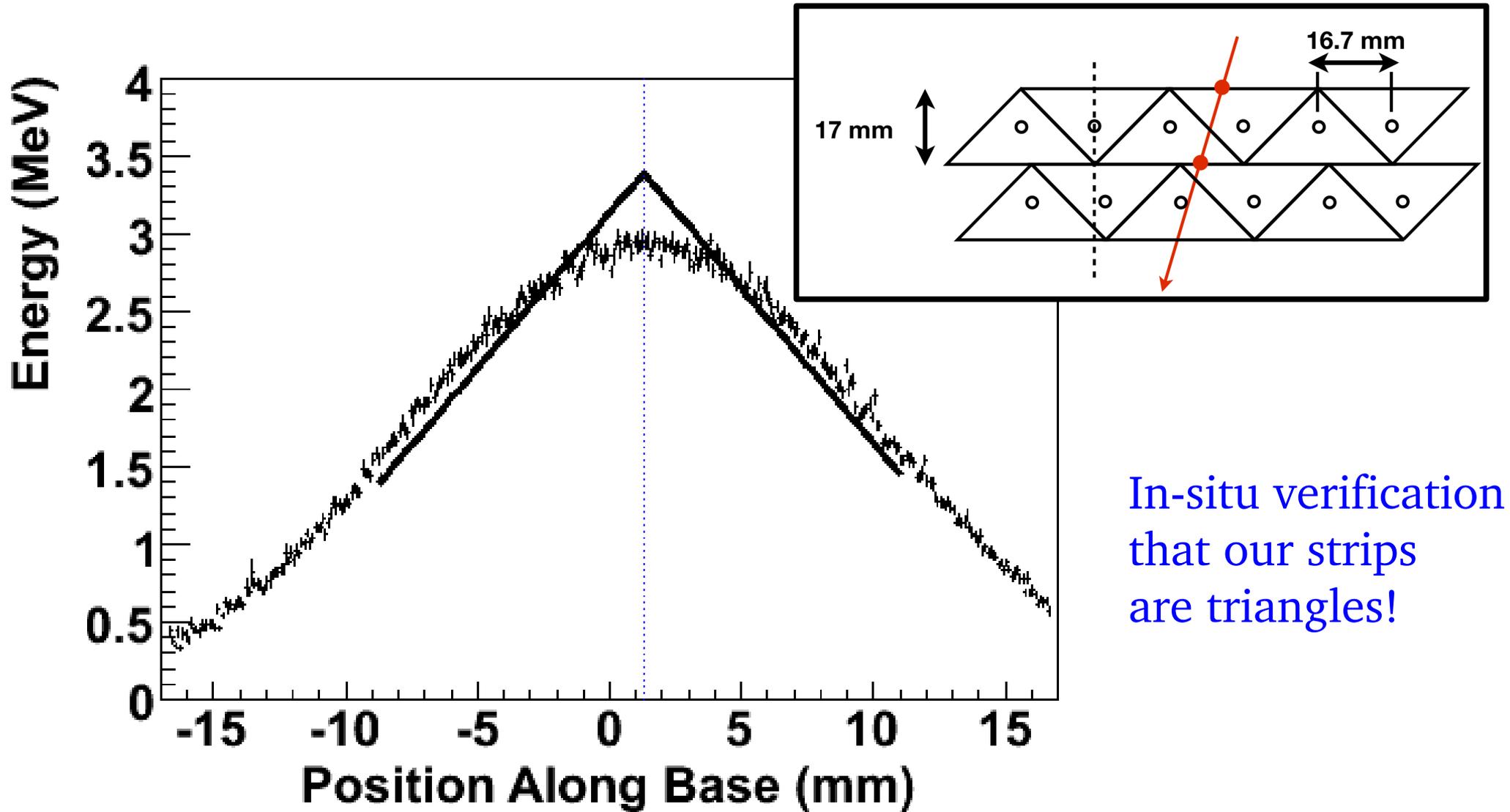
Charge to ADC conversion function measured on a test stand for every channel on every board before installation on the detector



# Detector Calibration

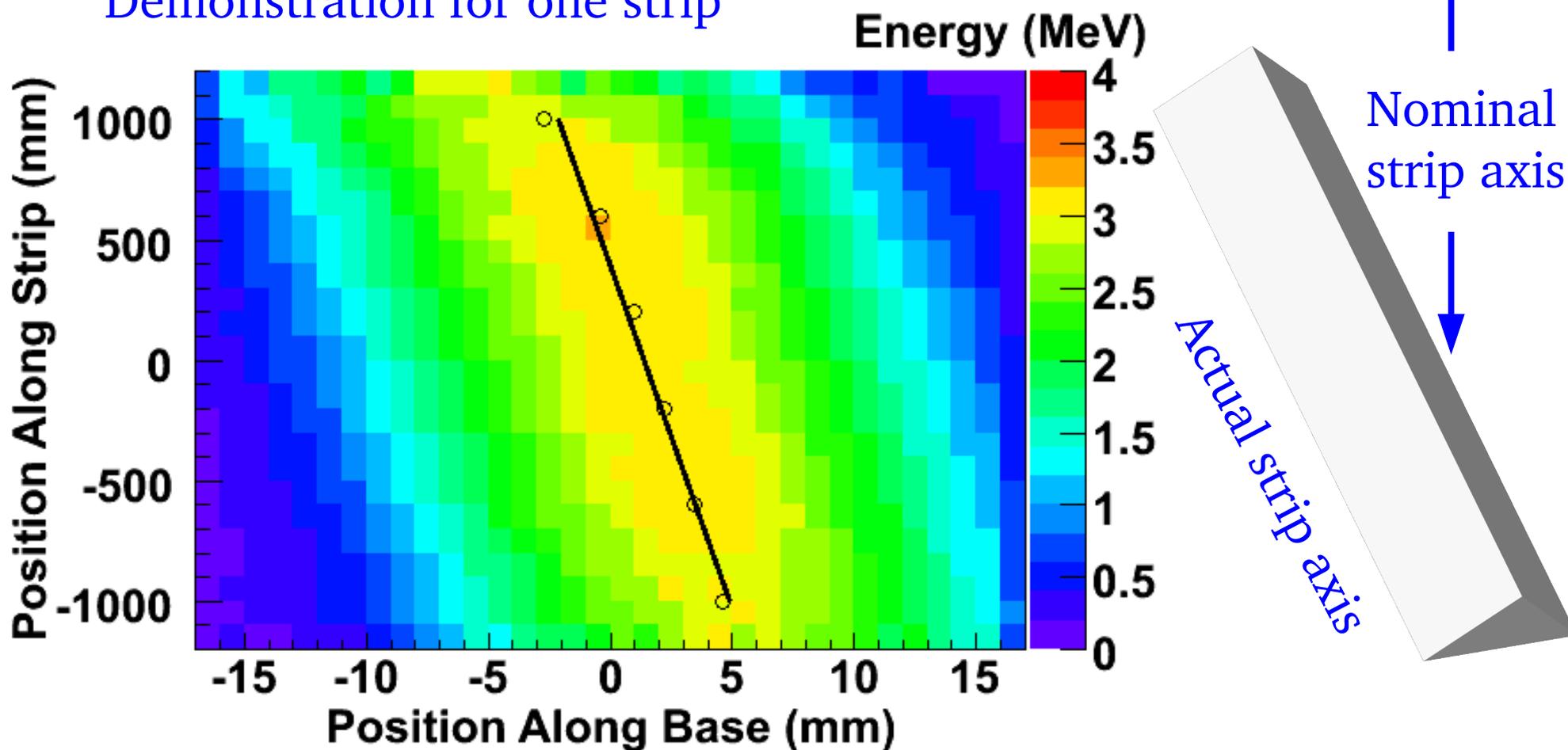


# Alignment and strip response

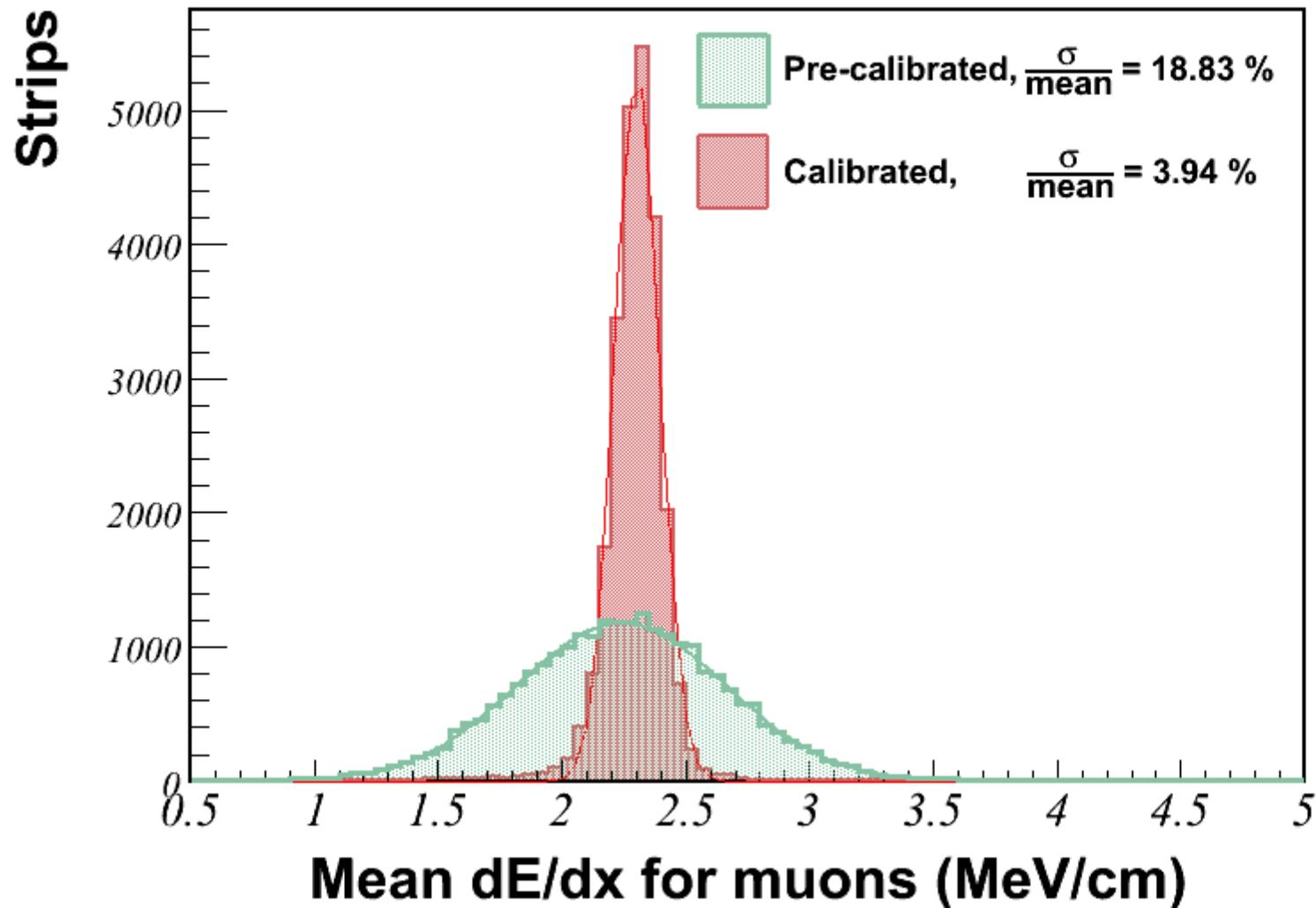


# Alignment and strip response

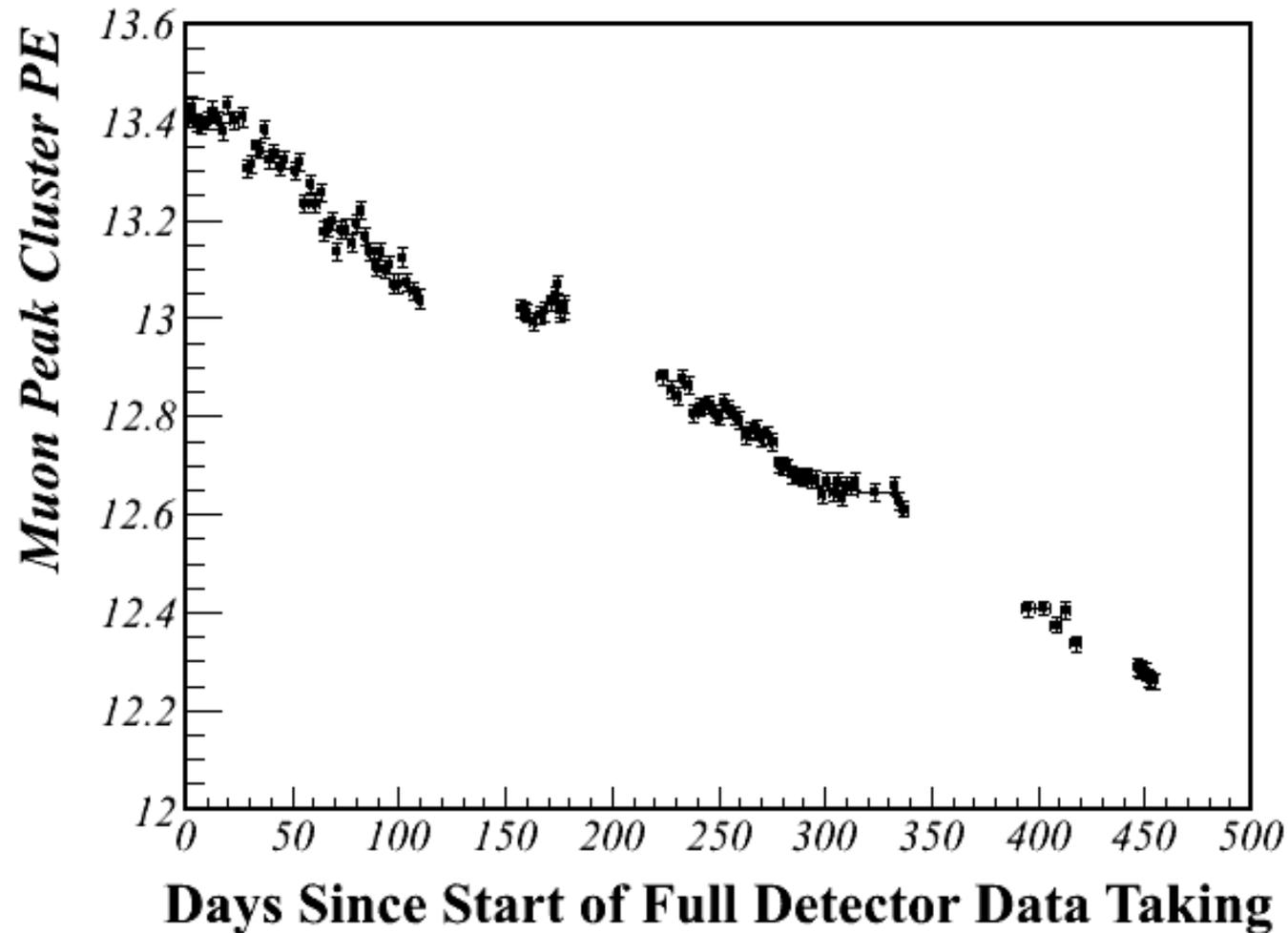
Demonstration for one strip



# Alignment and strip response



# Response vs. Time

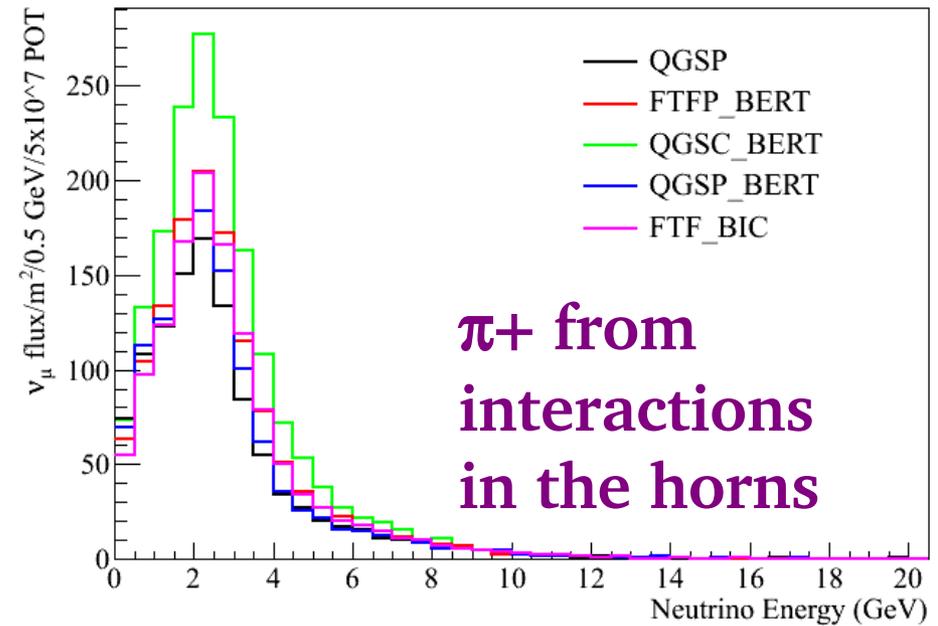
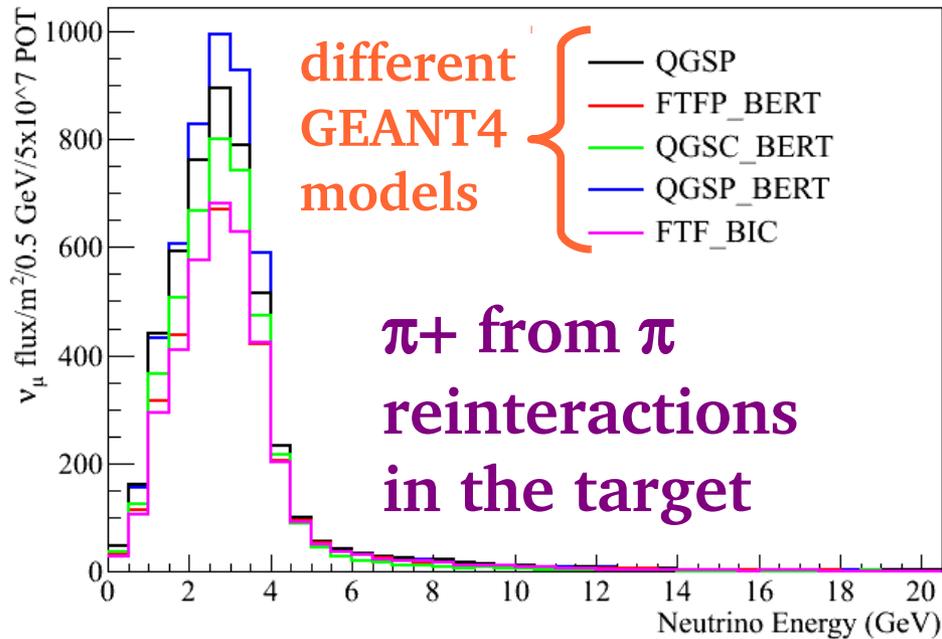


Minerva 1 (days 0-107): light loss = 10.1% per year

Minerva 5 (days 222-335): light loss = 7.1% per year

# Model Spread Uncertainties

## Non-NA49 uncertainties from maximum model spread



### Categories

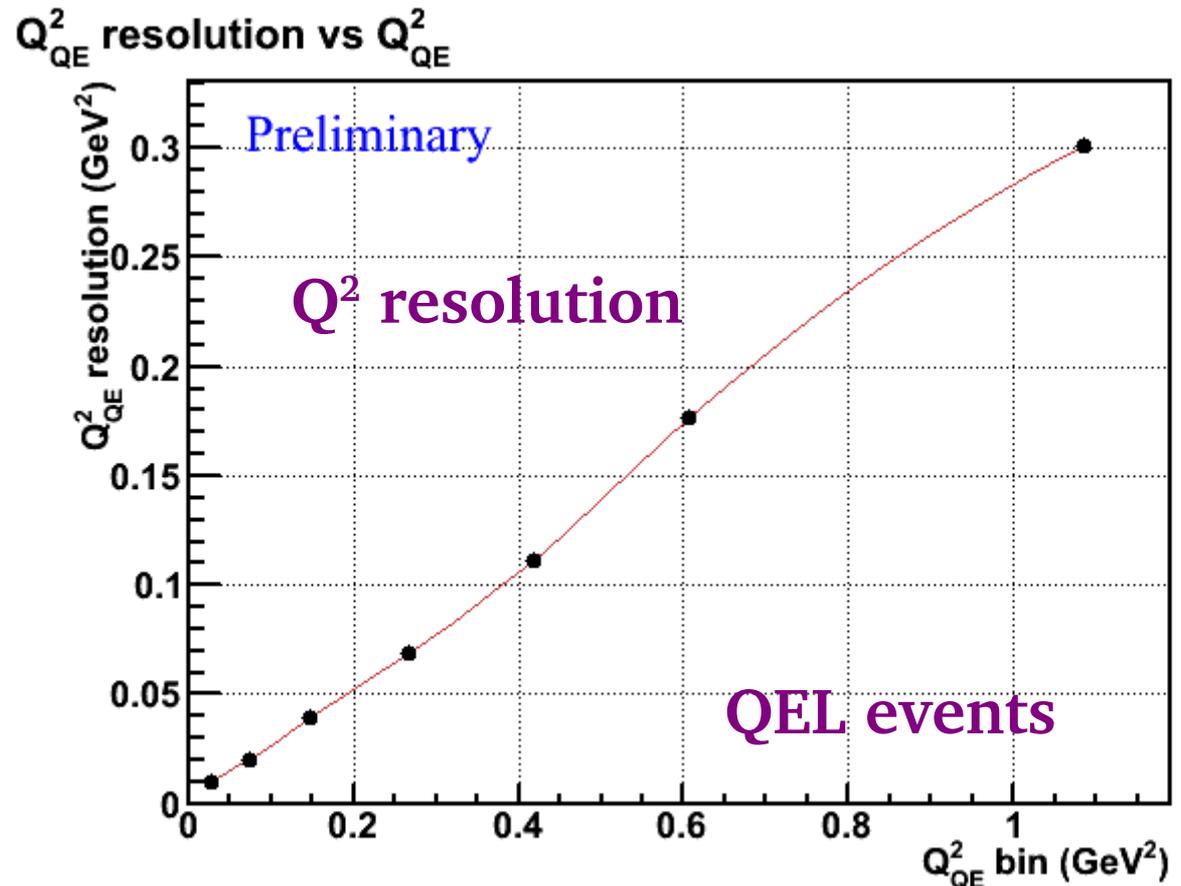
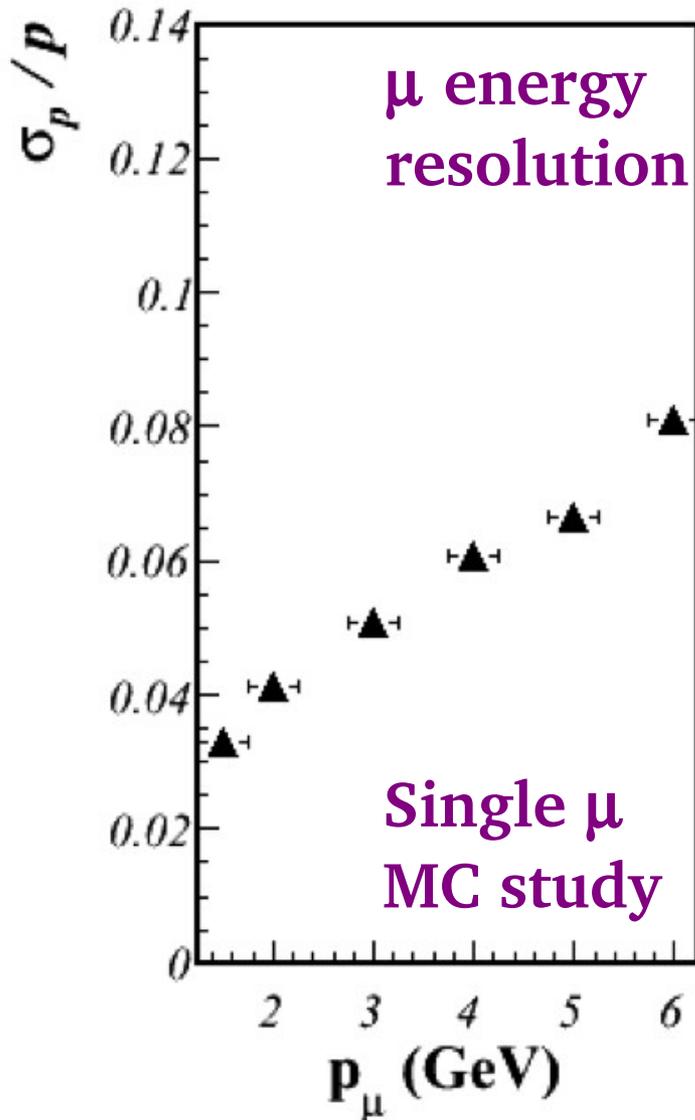
$\pi, K, p, n$ , other secondary interactions in target

production in horns, decay pipe walls & He, target hall chase

Large project to

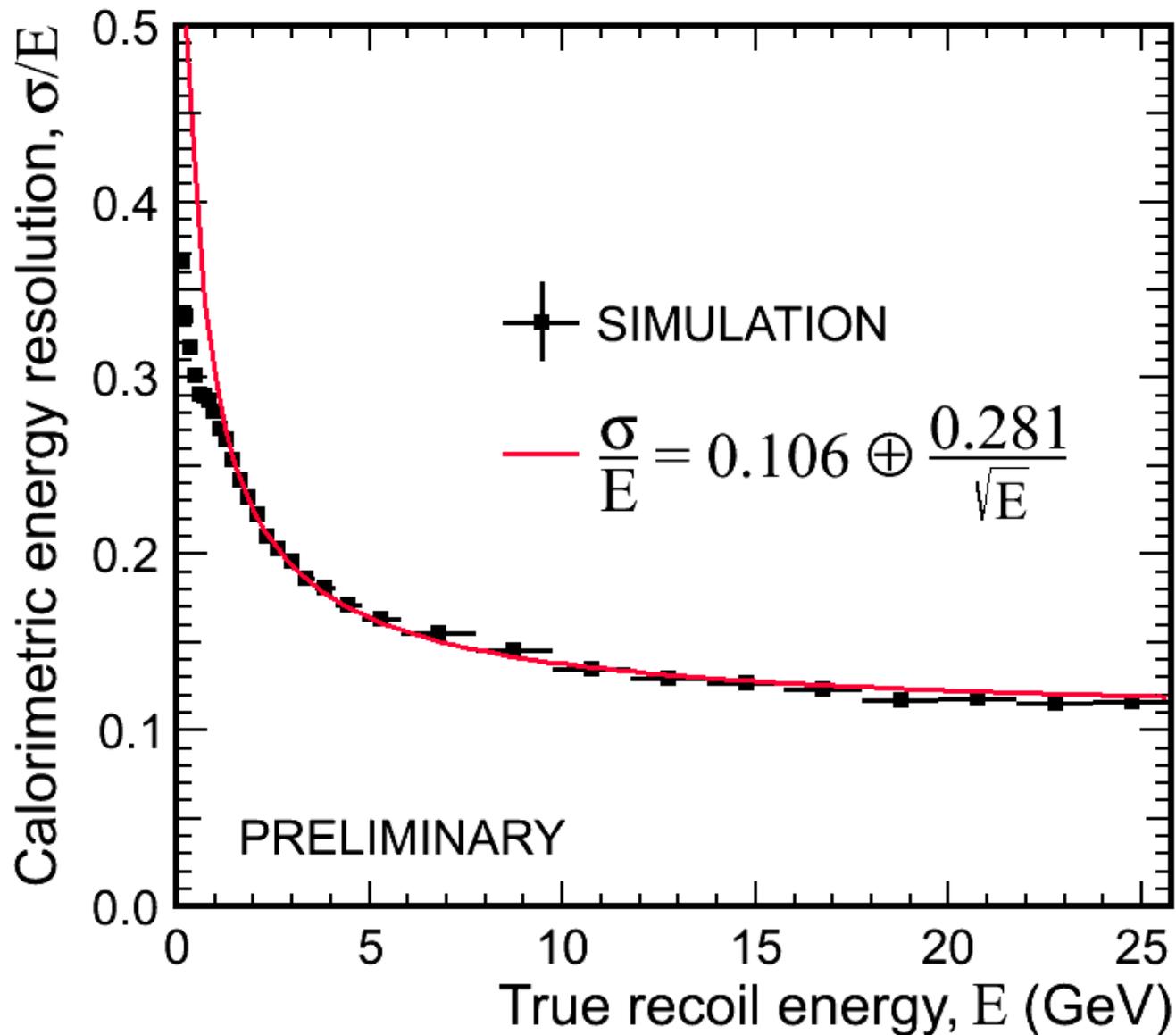
- (a) add more models
- (b) gradually replace model spread with existing and new data

# $\mu$ energy & $Q^2$ resolution



$$Q^2 = (4\text{-momentum transfer})^2$$

# shower energy resolution



# GENIE

QEL: BBBA05 FF,  $M_A$  is 0.99 GeV/c<sup>2</sup>

Resonance: Rein & Sehgal (K, ρ, η production, Δ-Nγ)

Coherent-π: Rein-Sehgal

DIS: GRV94/GRV98 with Bodek-Yang

DIS and QEL charm (S.G.Kovalenko, Sov.J.Nucl.Phys.52:934 (1990))

1π and 2π channels tuned in transition region to electron scattering and neutrino data.

Nuclear Model: RFGM with NN correlations

Hadronization Model: AGKY – transitions between KNO-based and JETSET

T. Yang, AIP Conf. Proc.967:269-275 (2007)

Formation zone: SKAT  $\mu^2=0.08$  GeV<sup>2</sup>

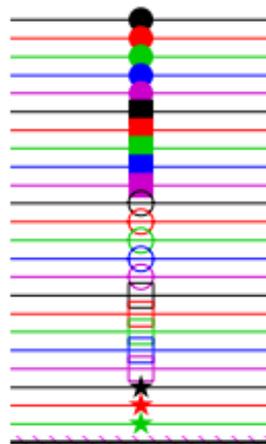
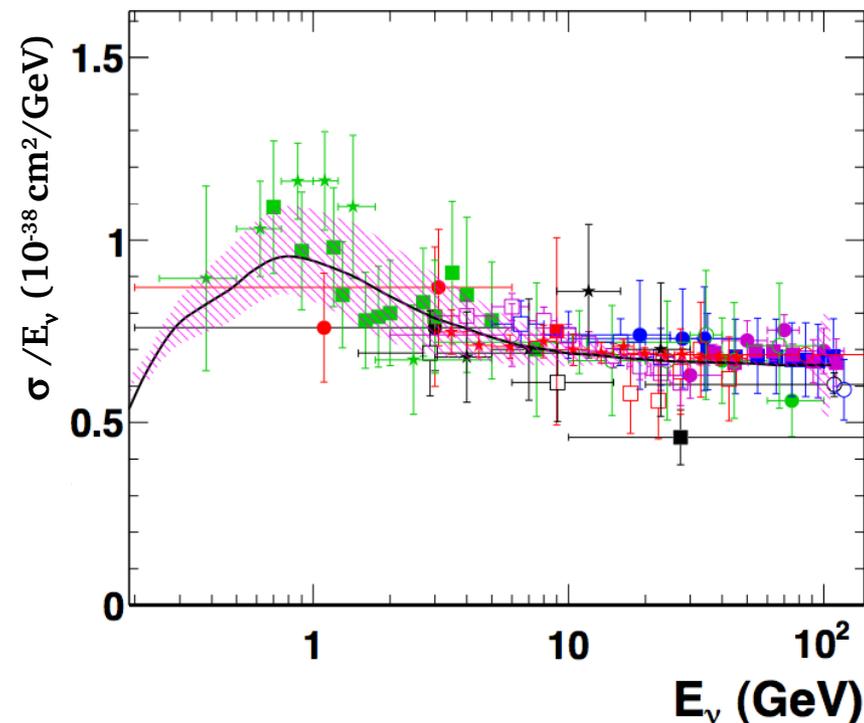
Intranuclear Rescattering: cascade model

INTRANUKE-hA (S. Dytman, AIP Conf Proc, 896, pp. 178-184 (200))

anchored to π,p/n-Fe data, scaled to all nucl

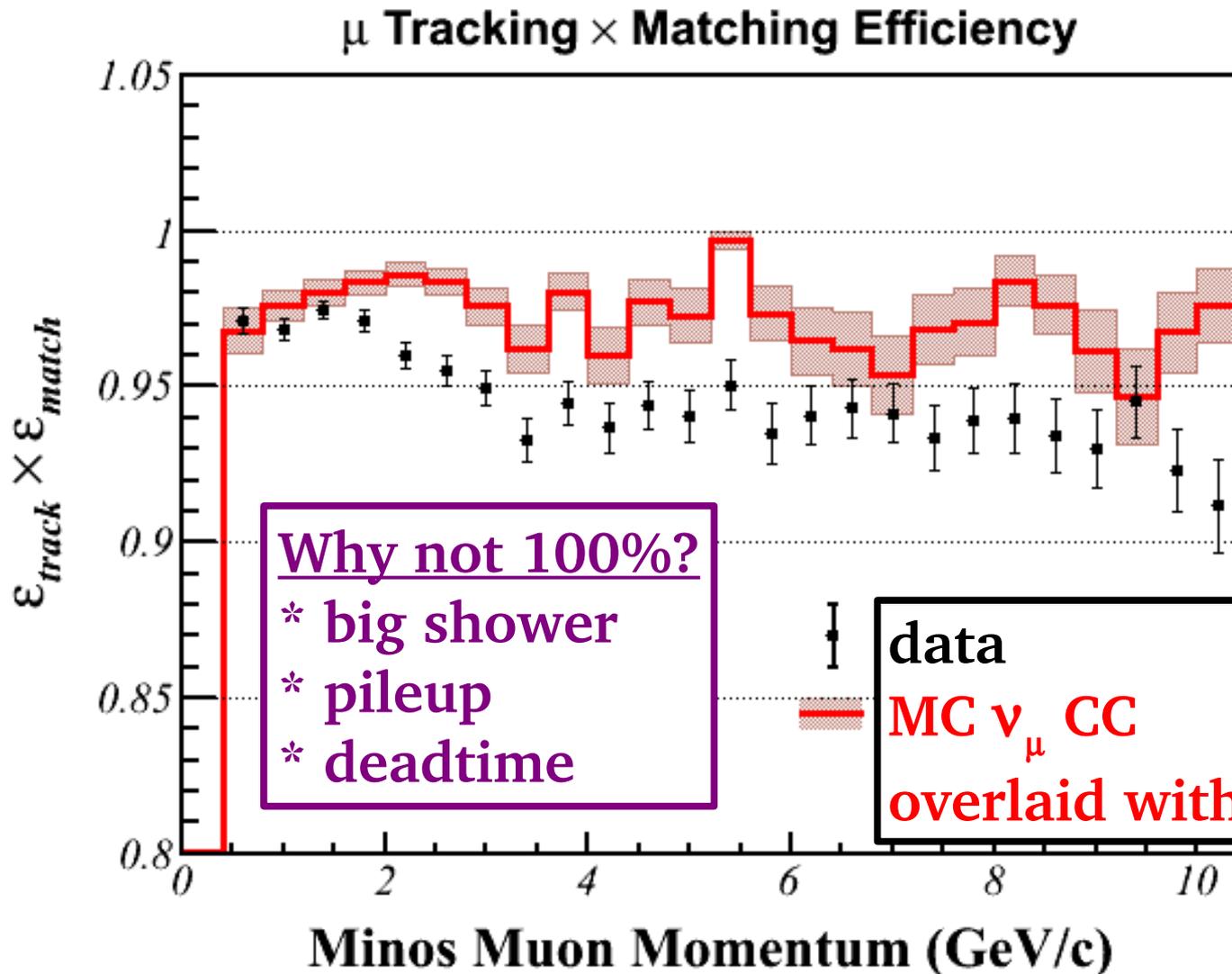
[www.genie-mc.org](http://www.genie-mc.org); NIM A614 (2010) 87-104

$\nu_\mu$  CC inclusive



ANL\_12ET.2 [Barish et al., Phys. Lett. B66:291 (1977)]  
 ANL\_12ET.4 [Barish et al., Phys. Rev. D18:2521 (1979)]  
 BBBA05 [Bossetti et al., Phys. Lett. B70:273 (1977)]  
 BBBA05.0 [Colley et al., Zeit. Phys. C2:187 (1979)]  
 BBBA05.2 [Bossetti et al., Phys. Lett. B110:167 (1982)]  
 BBBA05.3 [Parker et al., Nucl. Phys. B232:1 (1984)]  
 BBBA05.4 [Baltay et al., Phys. Rev. Lett. 44:916 (1980)]  
 BBBA05.5 [Baker et al., Phys. Rev. D25:617 (1982)]  
 BBBA05.6 [Seigman et al., Nevis Report 292 (1996)]  
 BBBA05.7 [MacFarlane et al., Zeit. Phys. C26:1 (1984)]  
 BBBA05.8 [Jonker et al., Phys. Lett. B99:265 (1981)]  
 BBBA05.9 [Allaby et al., Zeit. Phys. C38:403 (1988)]  
 BBBA05.10 [Kitagaki et al., Phys. Rev. Lett. 49:98 (1982)]  
 BBBA05.11 [Baker et al., Phys. Rev. Lett. 51:735 (1983)]  
 BBBA05.12 [Eichten et al., Phys. Lett. B46:274 (1973)]  
 BBBA05.13 [Gardamelle, 0 [Ciampolillo et al., Phys. Lett. B84:281 (1979)]  
 BBBA05.14 [Gardamelle, 10 [Morfin et al., Phys. Lett. B104:235 (1981)]  
 BBBA05.15 [HEP\_I\_TEP.0 [Asratyan et al., Phys. Lett. B76:239 (1978)]  
 BBBA05.16 [HEP\_I\_TEP.2 [Voverko et al., Sov. J. Nucl. Phys. 30:528 (1979)]  
 BBBA05.17 [HEP\_I\_TEP.0 [Anikeev et al., Zeit. Phys. C70:39 (1996)]  
 BBBA05.18 [SKAT.0 [Baranov et al., Phys. Rev. D81:255 (1979)]  
 BBBA05.19 [MINOS.0 [Adamson et al., Phys. Rev. D81:072002 (2010)]  
 BBBA05.20 [SciBooNE.0 [Nakajima et al., Phys. Rev. D83:012005 (2011)]  
 genie

# Tracking x Matching Efficiency



Method  
 ID clean  $\mu$  in  
 MINOS, point back  
 to MINERvA  
 Single event MC  
 correction  
 $-4.6 \pm 2.5\%$

# Normalization corrections

$\nu_{\mu}$  beam

Source	MC scale factor	uncertainty
MINERvA tracking efficiency	0.956	2.5%
MINOS $\mu$ acceptance	0.975	2.5%
MINOS pileup	0.972	0.6%
Catastrophic dead time	0.983	1.0%
Signal removed by deadtime cuts*	0.970	0.1%
Mass Model	1.000	1.4%
POT scale	1.000	2.0%
<b>Total</b>	<b>f=0.865</b>	<b>4.0%</b>

reco. effects on single event MC

\*QEL analyses only

other