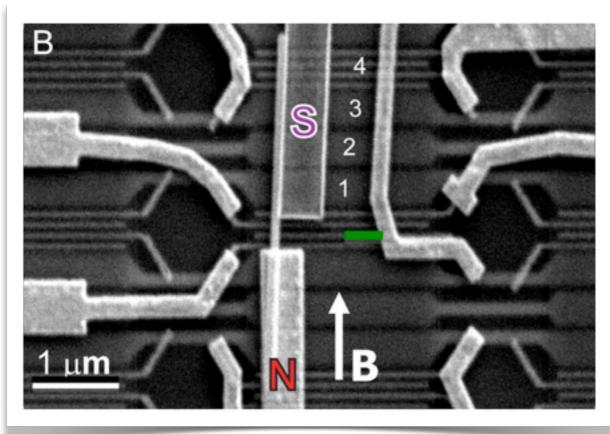
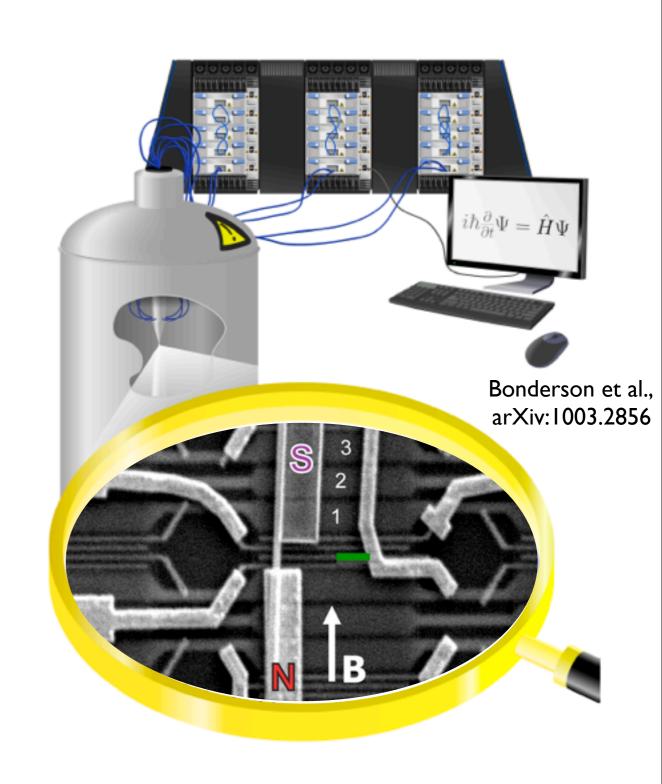
Majorana materializes



Mourik et al., Science 2012



Jason Alicea (Caltech)

Acknowledgments

Anton Akhmerov (Harvard)

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Kirill Shtengel (UCR)

Oleg Starykh (Utah)

Ady Stern (Weizmann)

Miles Stoudenmire (UCI)

Felix von Oppen (Berlin)

Conan Weeks (UBC)

Ruqian Wu (UCI)

Amir Yacoby (Harvard)







Outline

Majorana fermions: what they are & why they're interesting

The quest for Majorana in the solid state

Getting the most out of Majorana fermions

Experimental status & closing remarks

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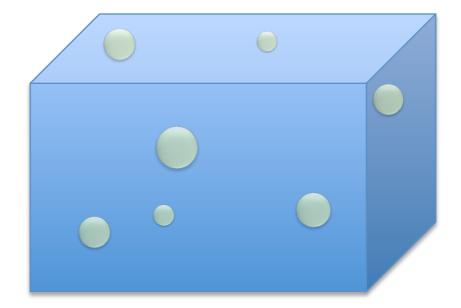
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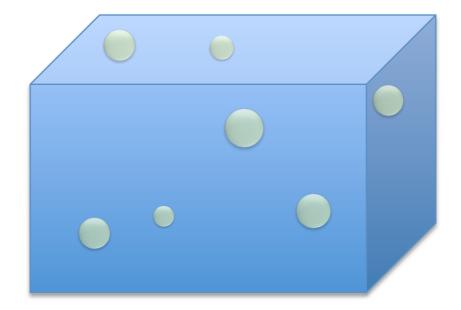
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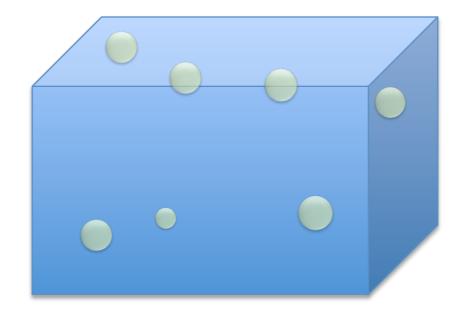
$$\psi(\mathbf{r_1},\ldots,\mathbf{r_N})$$



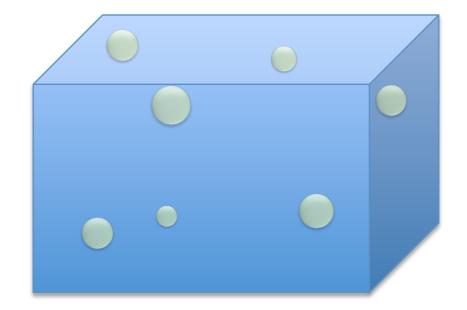
$$\psi(\mathbf{r_1},\ldots,\mathbf{r_N})$$



$$\psi(\mathbf{r_1},\ldots,\mathbf{r_N})$$

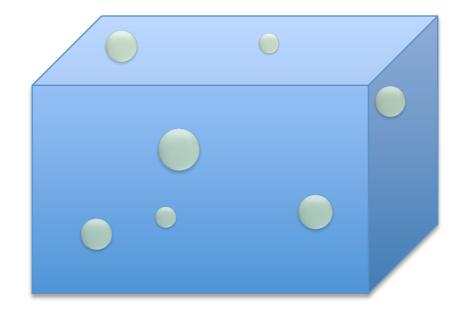


$$\psi(\mathbf{r_1},\ldots,\mathbf{r_N})$$



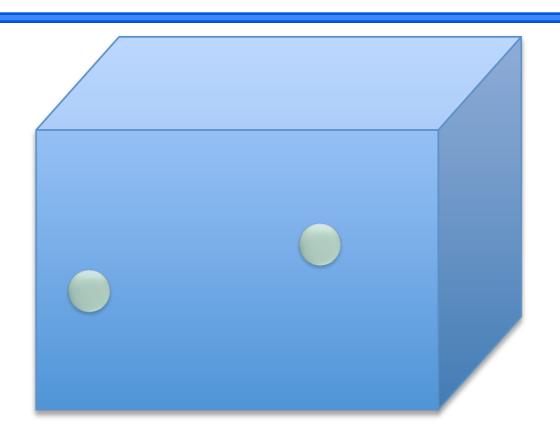
Describes how wavefunctions transform when indistinguishable particles exchange positions

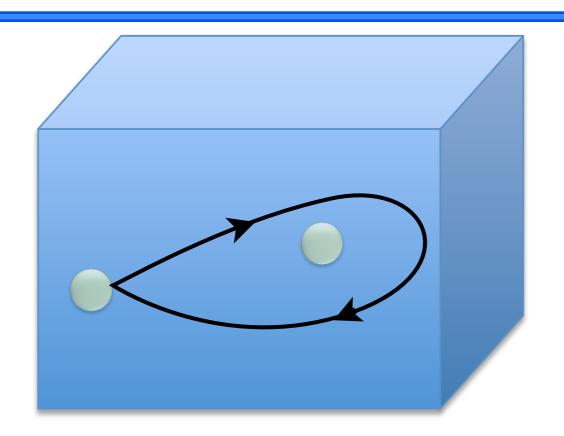
$$\psi(\mathbf{r_1},\ldots,\mathbf{r_N}) \longrightarrow \psi'(\mathbf{r_1},\ldots,\mathbf{r_N})$$

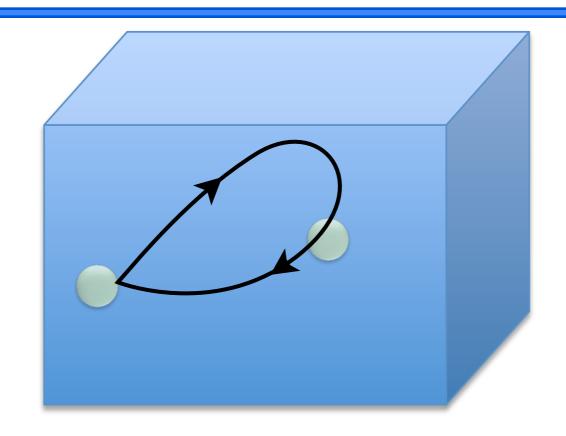


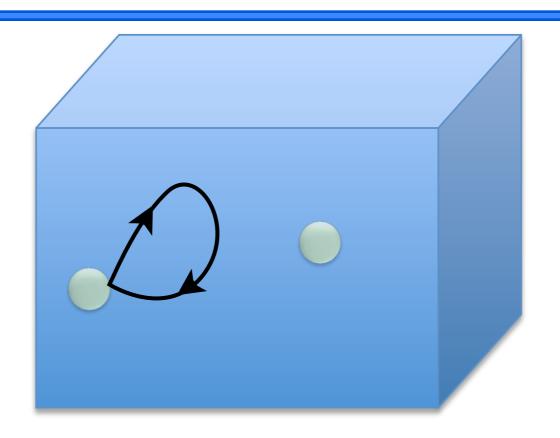
Extraordinarily fundamental!

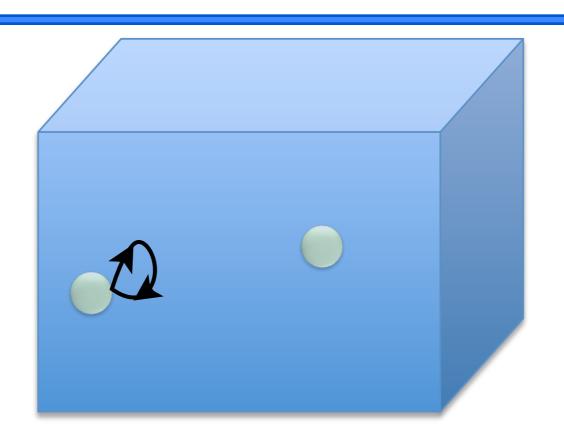
Underlies most condensed matter phenomena.

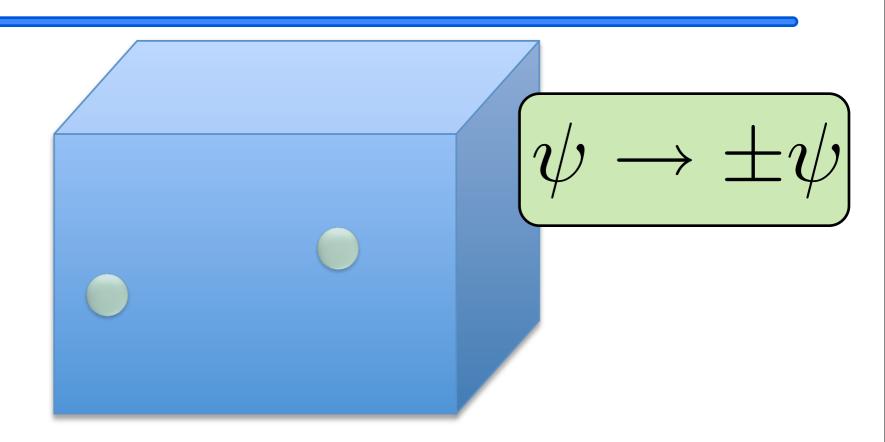


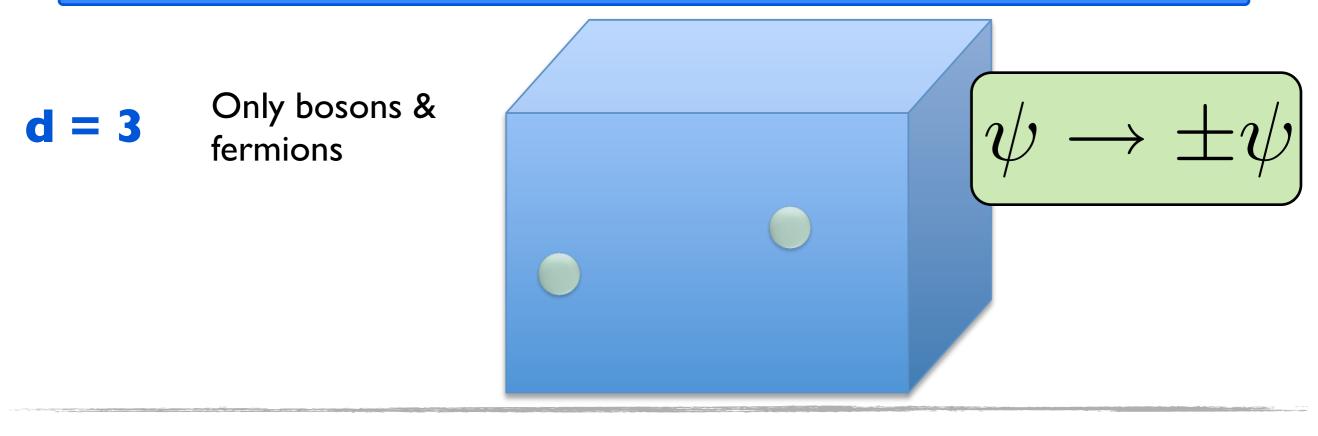


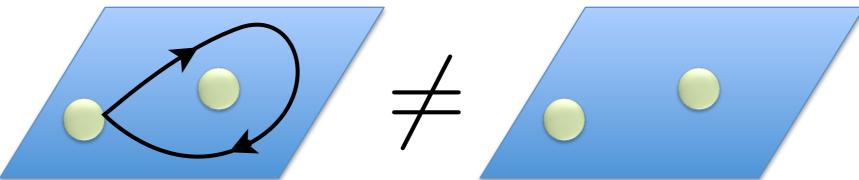


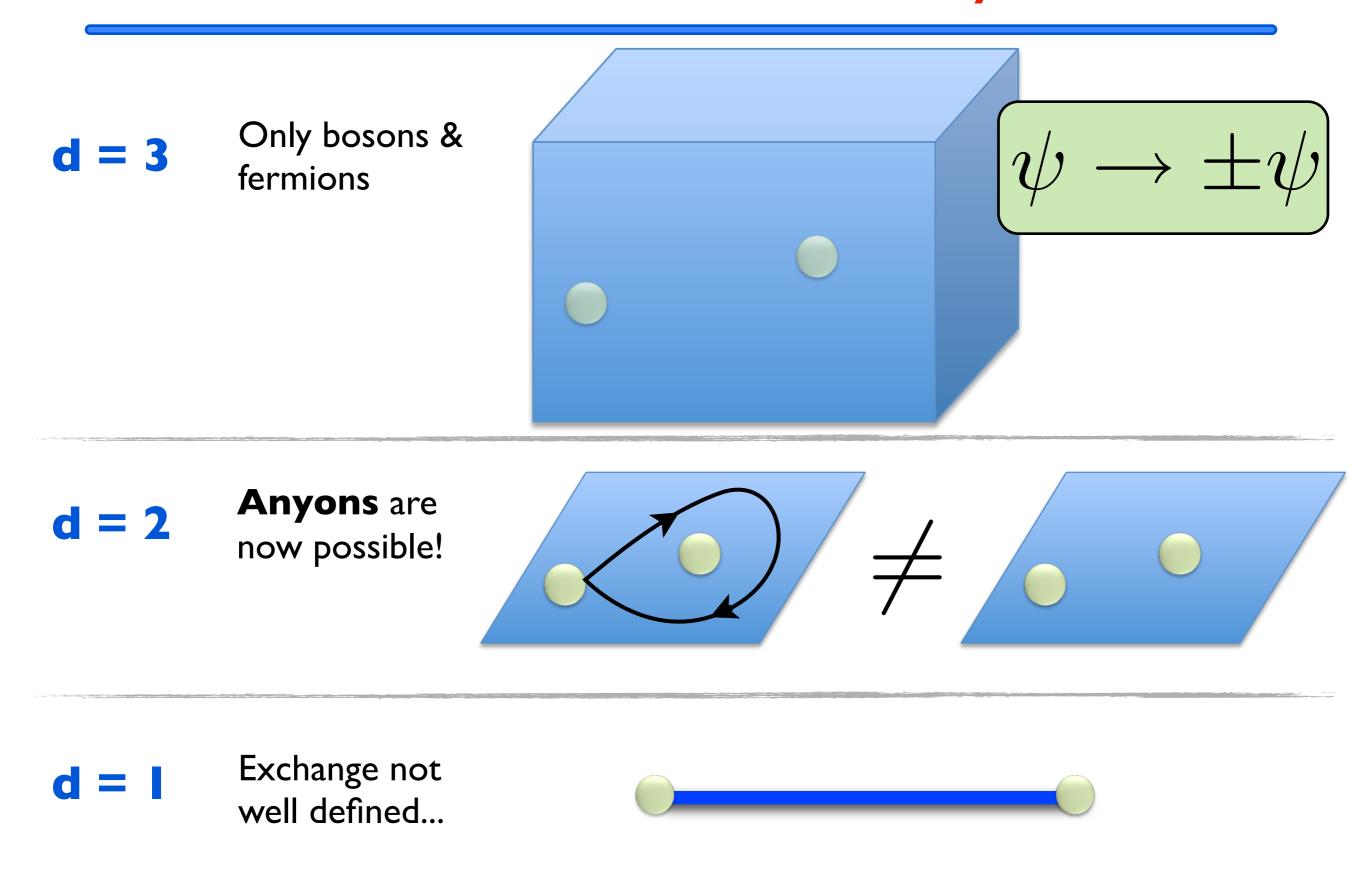


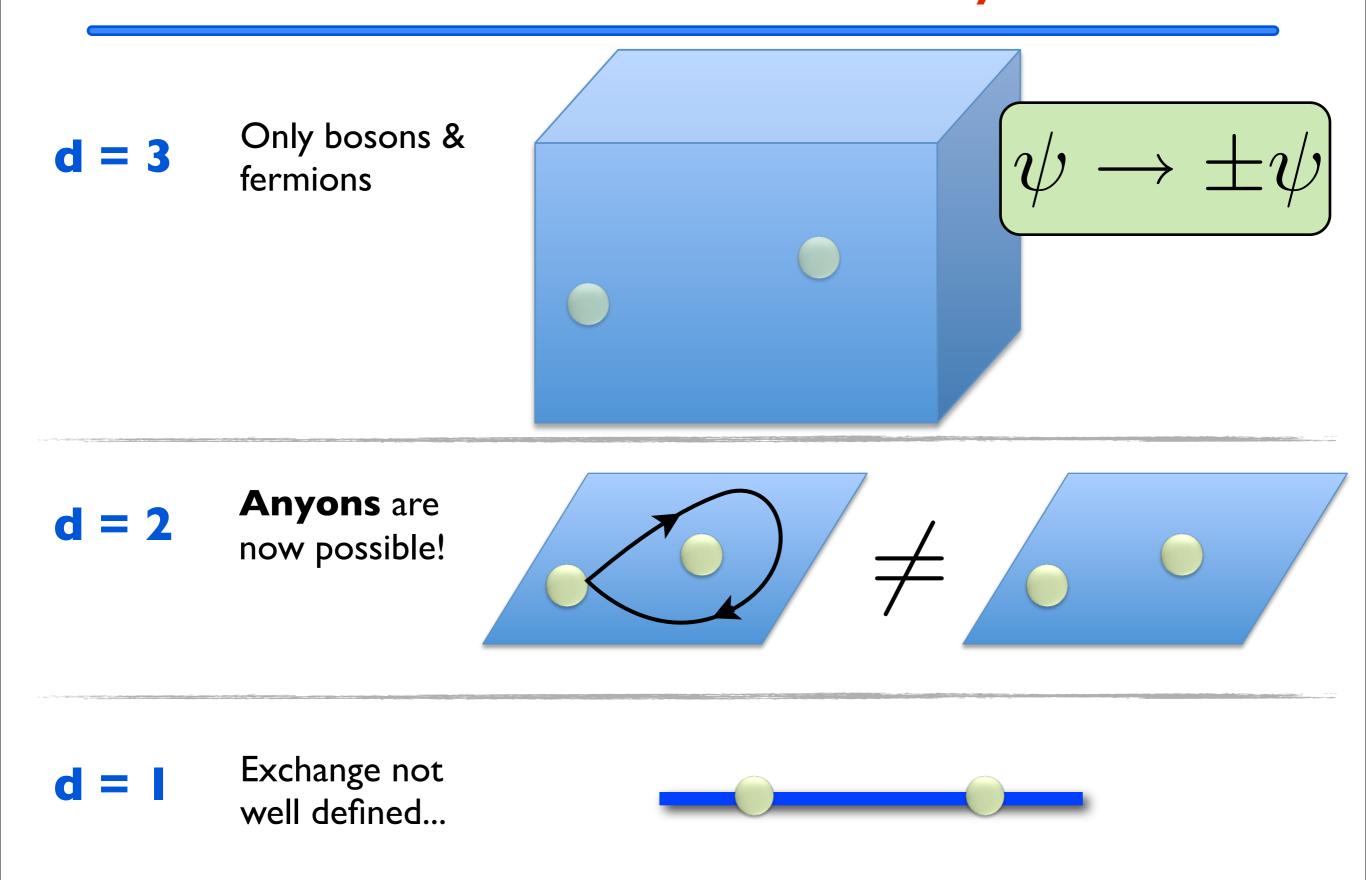


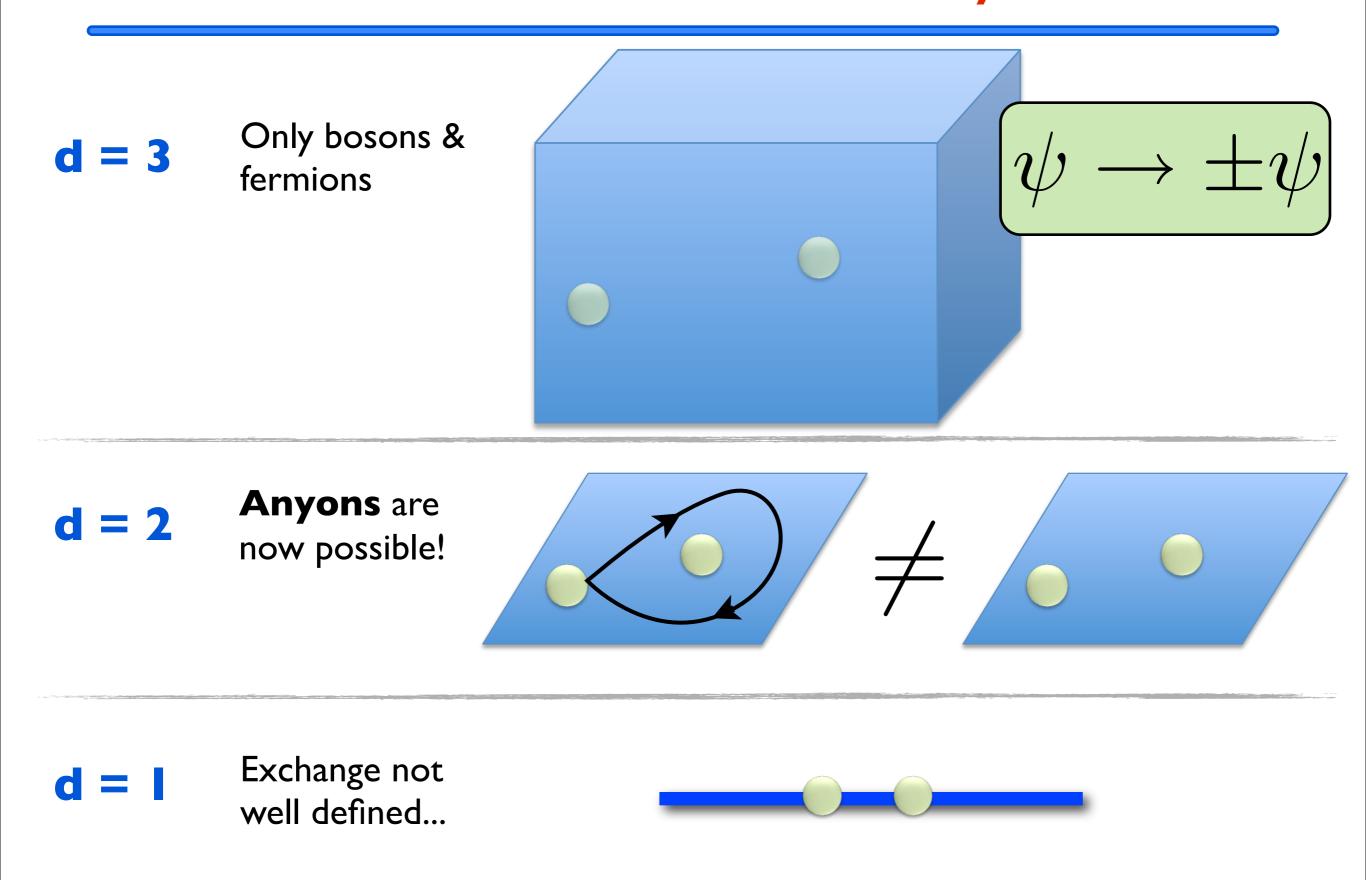


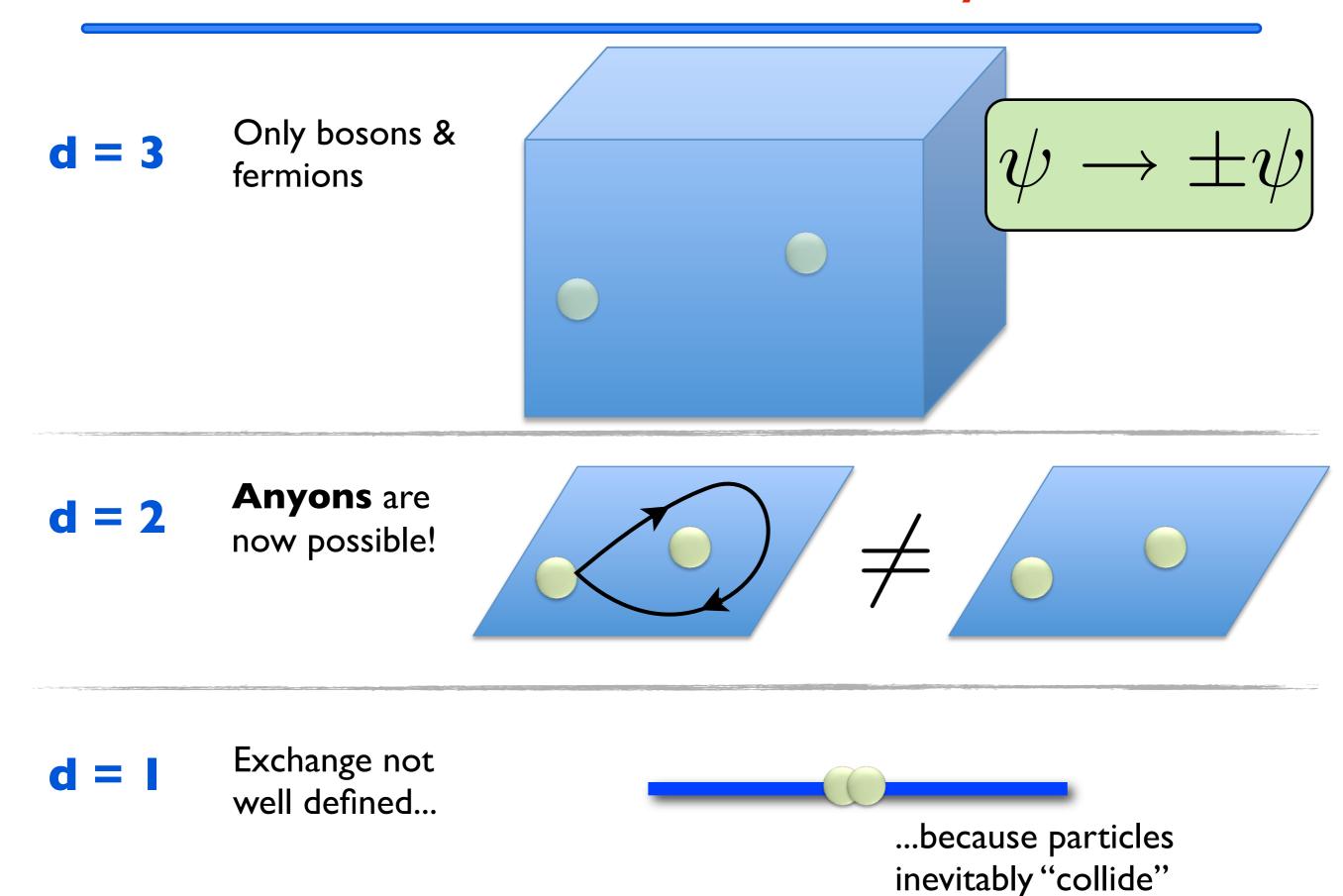




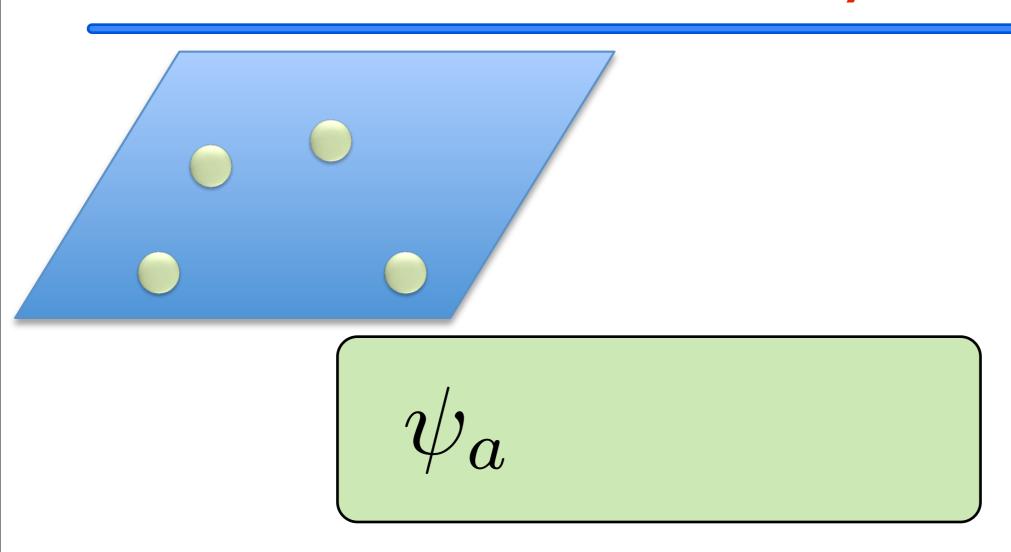




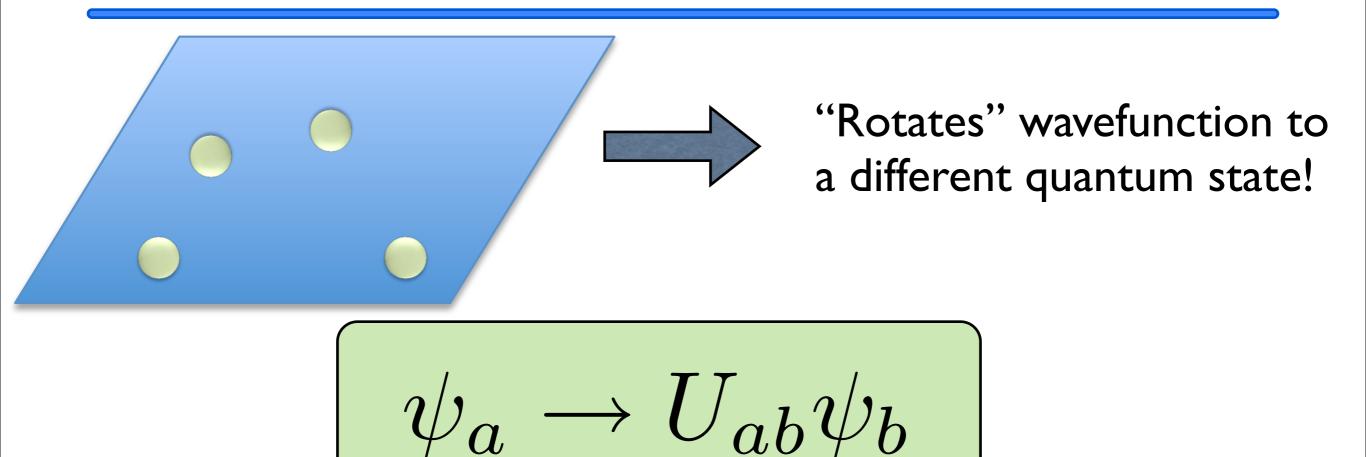




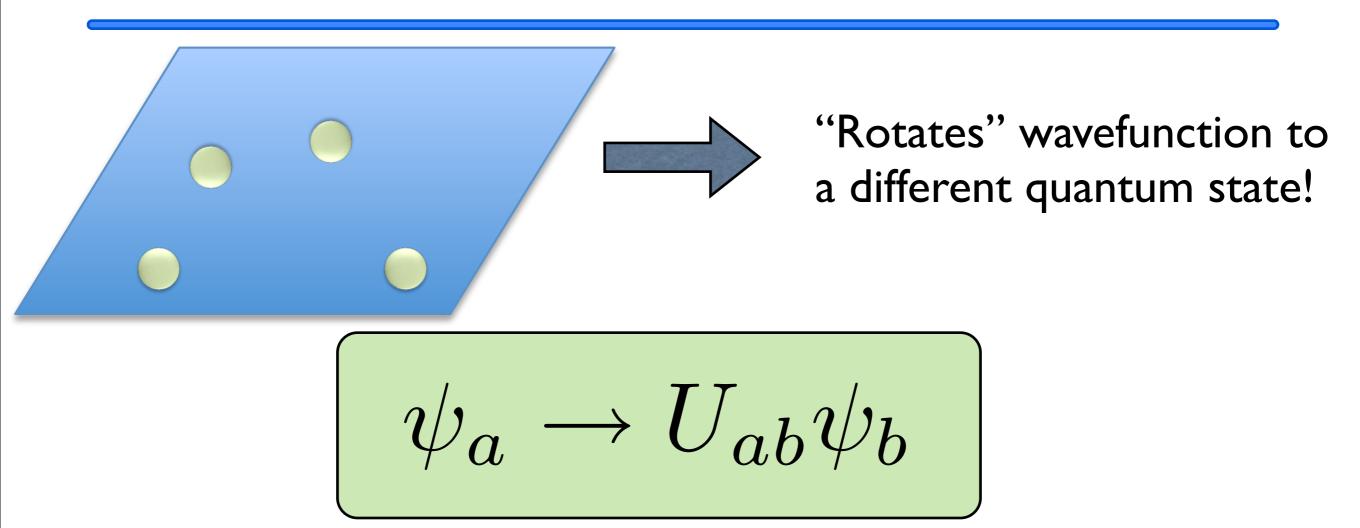
Non-Abelian anyons



Non-Abelian anyons



Non-Abelian anyons

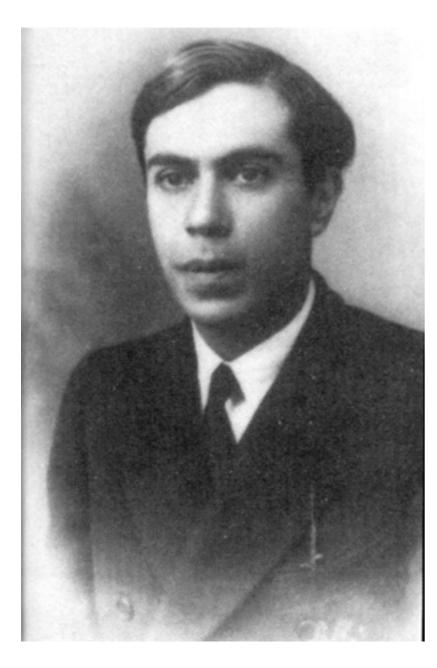


Urgently wanted for topological quantum computation

Kitaev; Freedman; Preskill; Frohlich, etc. Nayak, Simon, Stern, Freedman, & Das Sarma, RMP 80, 1083 (2008)

Simplest source of non-Abelian statistics: Majorana fermions

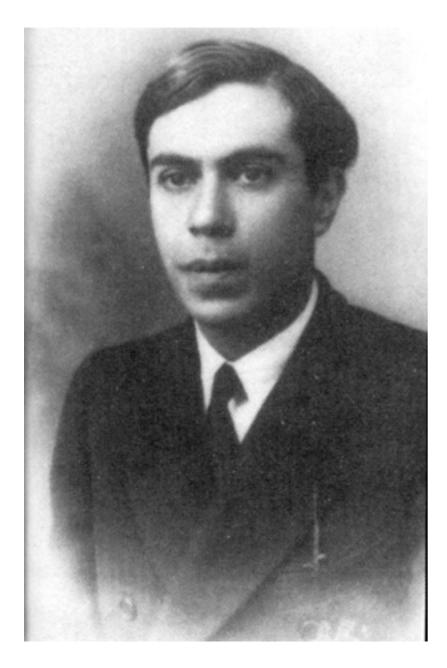
The "inventor" of Majorana fermions



Ettore Majorana (1906-1938?)

"There are many categories of scientists: people of second and third rank, who do their best, but do not go very far; there are also people of first-class rank, who make great discoveries, fundamental to the development of science. But then there are the geniuses, like Galileo and Newton. Well Ettore Majorana was one of them." -Enrico Fermi

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"Majorana had greater gifts than anyone else in the world. Unfortunately he lacked one quality which other men generally have: plain common sense." -Enrico Fermi

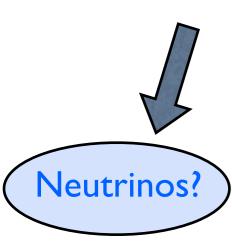
Majorana fermions are their own antiparticle $\gamma = \gamma^{\dagger}$

$$\gamma=\gamma^{\dagger}$$

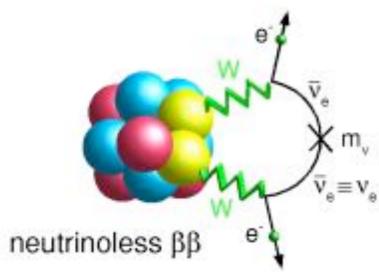


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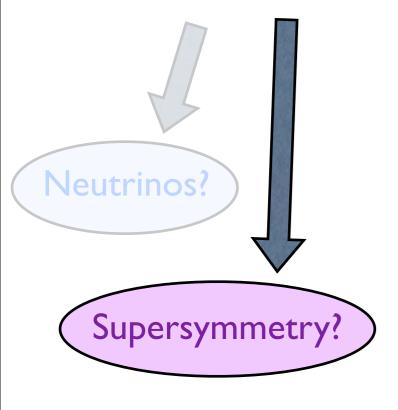


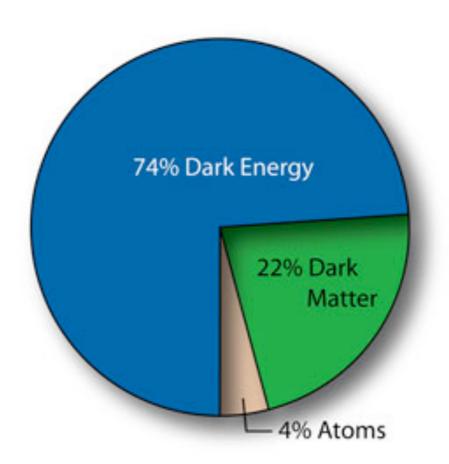




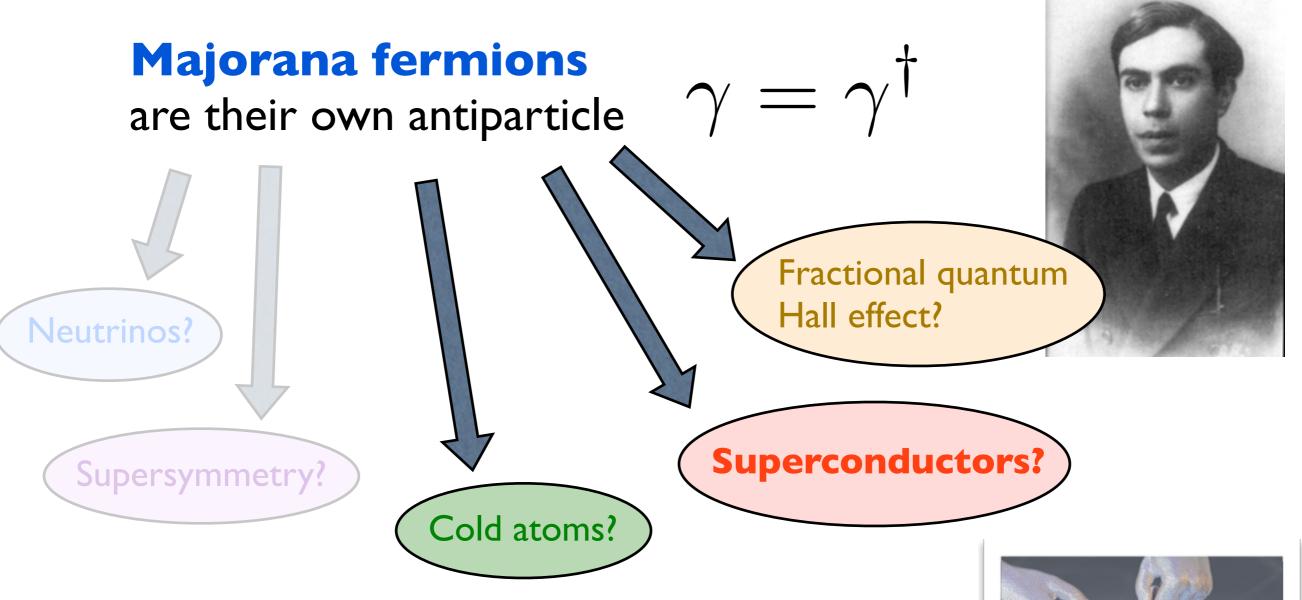
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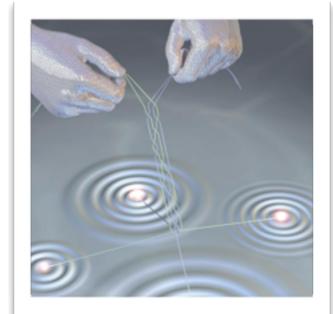








Observation would reveal something quite profound about nature.



Outline

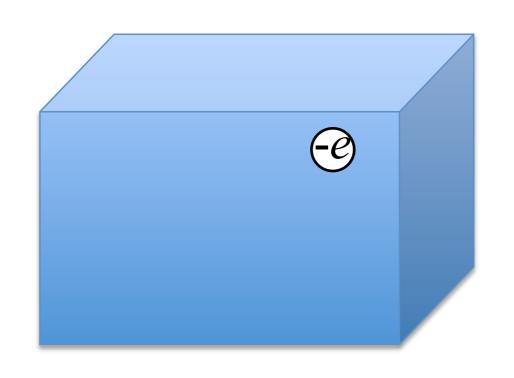
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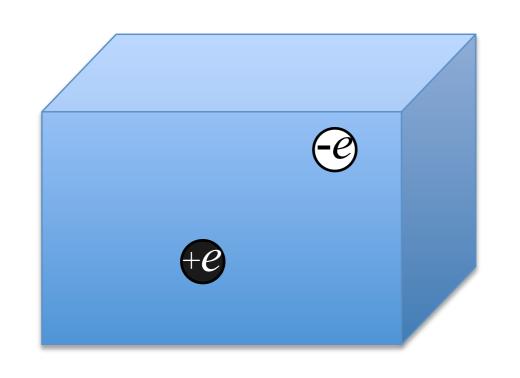
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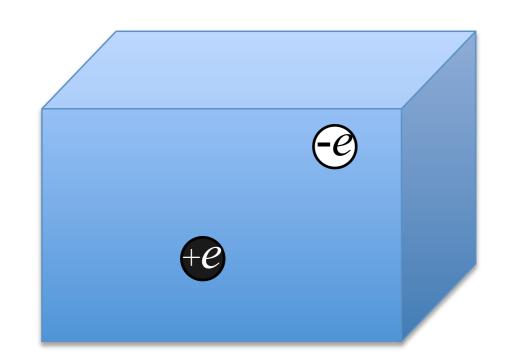
Typical metal or insulator



$$c^\dagger |\psi
angle$$
 (Adds an electron)

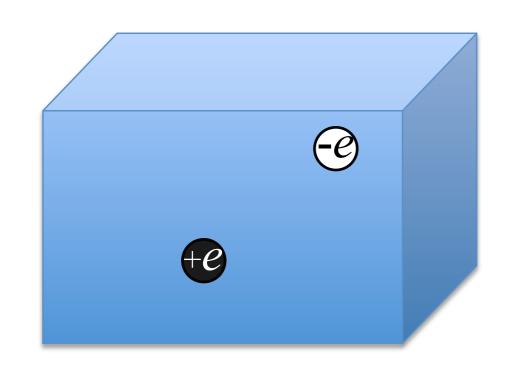


$$c^\dagger |\psi
angle$$
 (Adds an electron) $c|\psi
angle$ (Adds a hole)



$$c^\dagger |\psi
angle$$
 (Adds an electron) $c|\psi
angle$ (Adds a hole) $c^\dagger \neq c$

Majorana appears only through emergent excitations

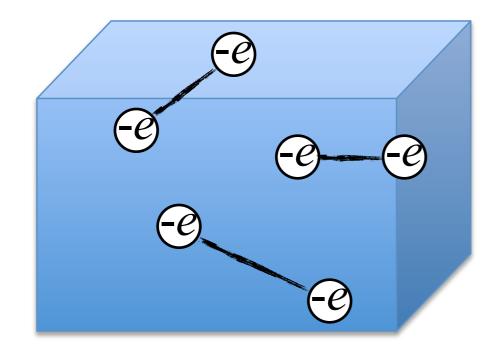


$$c^\dagger |\psi
angle$$
 (Adds an electron)

$$c|\psi
angle$$
 (Adds a hole)

$$c^{\dagger} \neq c$$

Majorana appears only through emergent excitations



Superconductors

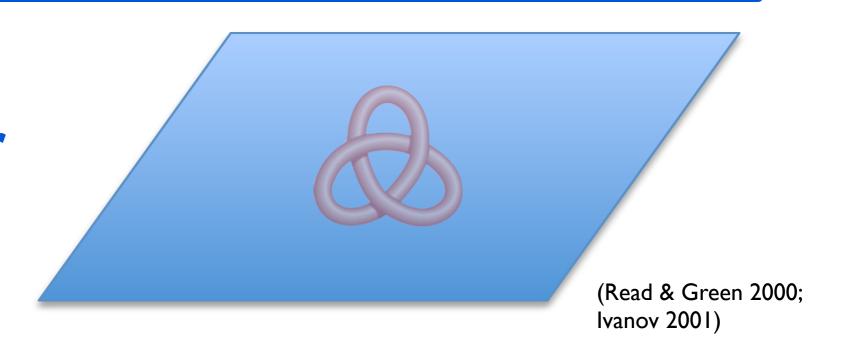
are natural platforms

$$f^{\dagger} \sim uc^{\dagger} + vc$$

Majorana via topological superconductivity



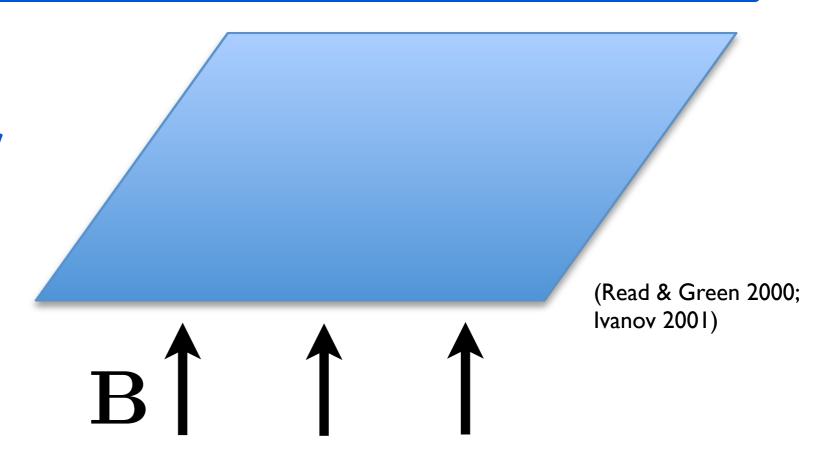
"Spinless" 2D superconductor



Majorana via topological superconductivity



"Spinless" 2D superconductor



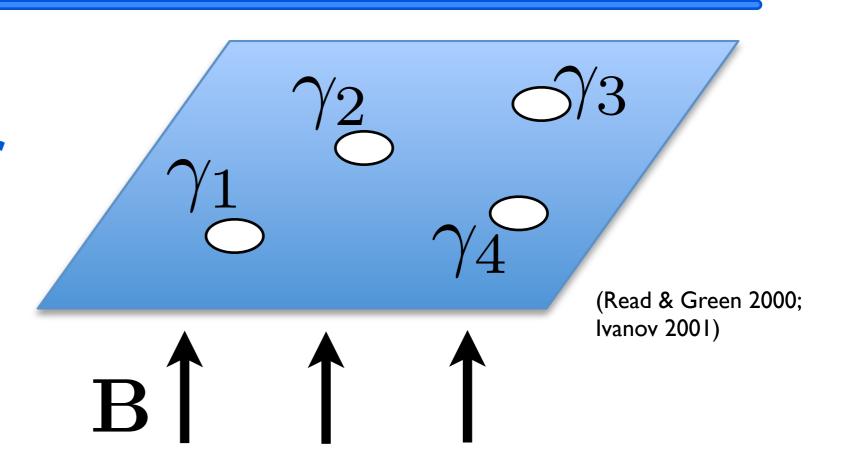
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"Spinless" 2D superconductor

Vortices bind

Majorana zero
modes

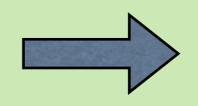


One Majorana = "half" a usual fermion

$$f_A = \gamma_1 + i\gamma_2$$

$$f_B = \gamma_3 + i\gamma_4$$

Ground-state degeneracy + non-locality



Vortices exhibit non-Abelian statistics

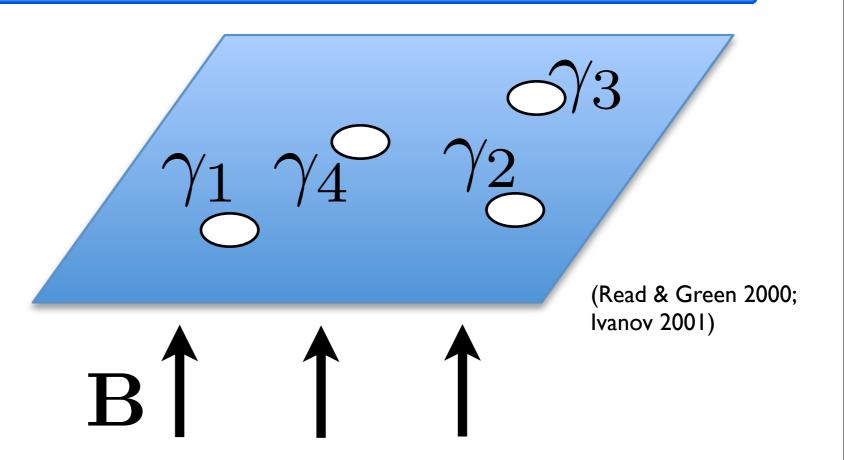
Majorana via topological superconductivity



"Spinless" 2D superconductor

Vortices bind

Majorana zero
modes





"Spinless" ID superconductor



Majorana zero-modes

localize at the ends of the system...

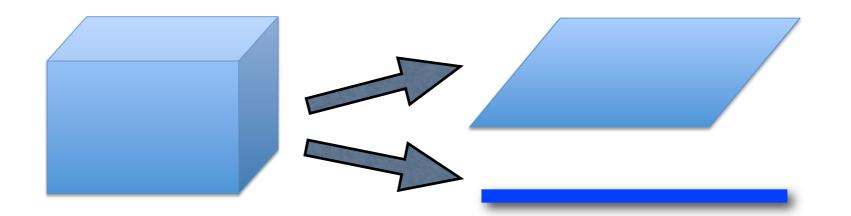
...but are they interesting & useful? **YES!**

(Kitaev 2001)

The basic challenge

"Spinless" ID, 2D superconductivity is hard to find

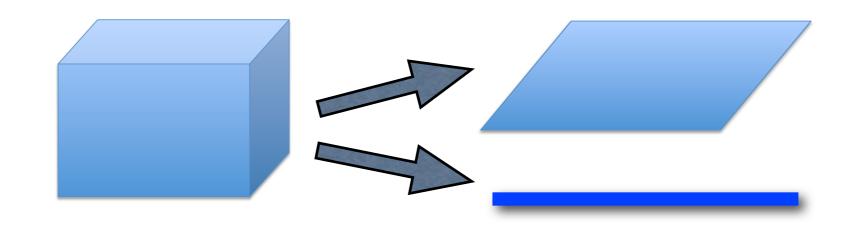
I.We live in 3D



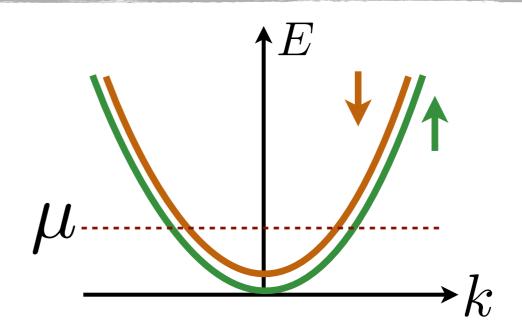
The basic challenge

"Spinless" ID, 2D superconductivity is hard to find

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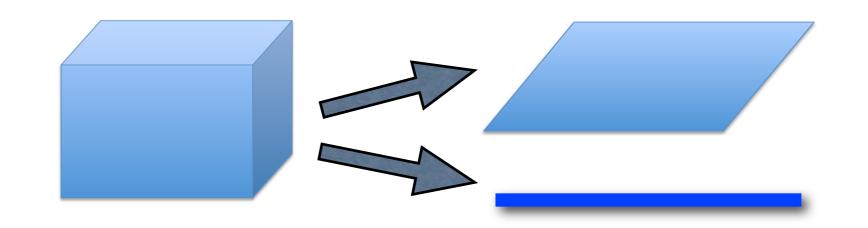
2. Electrons carry spin



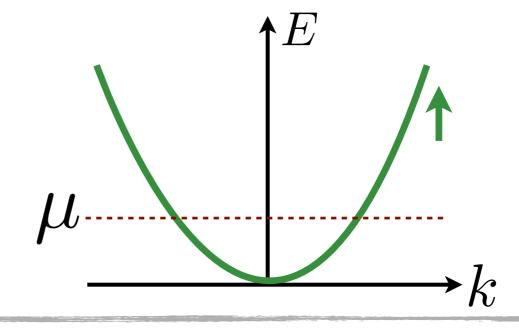
The basic challenge

"Spinless" ID, 2D superconductivity is hard to find

I.We live in 3D



2. Electrons carry spin



3. Vast majority of superconductors form **spin-singlet** Cooper pairs



Two ways forward

1. Search for new compounds w/exotic superconductivity

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Matthias's 6th rule: Stay away from theorists!

Two ways forward

1. Search for new compounds w/exotic superconductivity

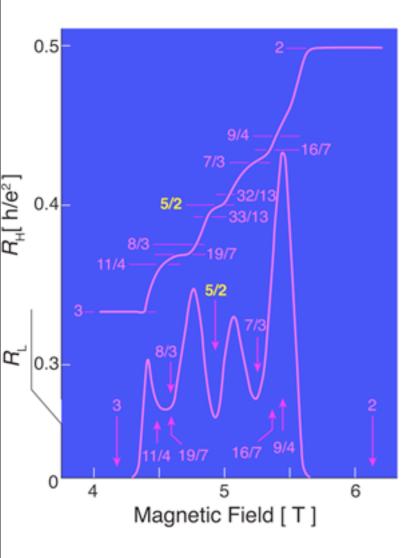
Matthias's 6th rule: Stay away from theorists!

2. "Engineer" topological superconductivity from available materials

Theorists can be useful, particularly if methods involve weakly interacting electrons

Many roads to Majorana fermions in 2D

"Intrinsic"



Willet, Eisenstein, et al. (1987) Moore & Read (1991) Bonderson, Kitaev, Shtengel (2006) Stern & Haperin (2006)

"Engineered"

Conventional Superconductor

3D
Topological Insulator

Fu & Kane (2008)

Conventional Superconductor

2D
Semiconductor

Ferromagnet

Sau, Tewari, Lutchyn, Das Sarma (2010)

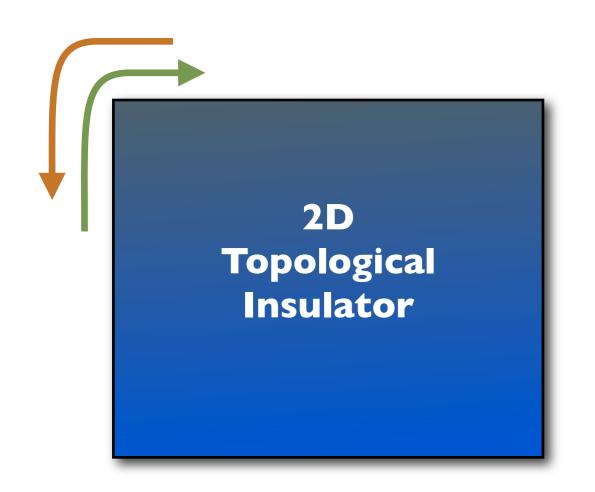
B Conventional Superconductor

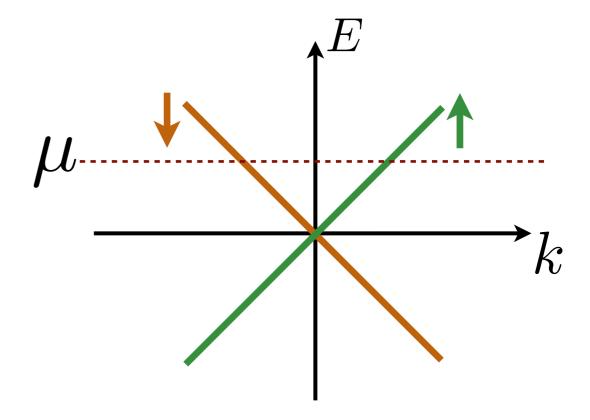
2D Semiconductor

...lots of others

Alicea (2010)

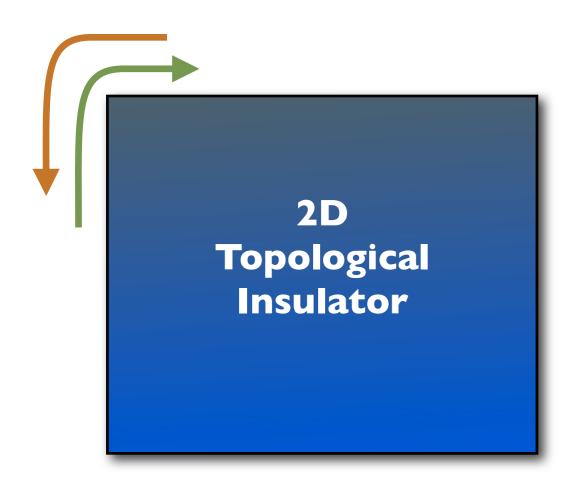
ID "spinless" superconductivity via edge states

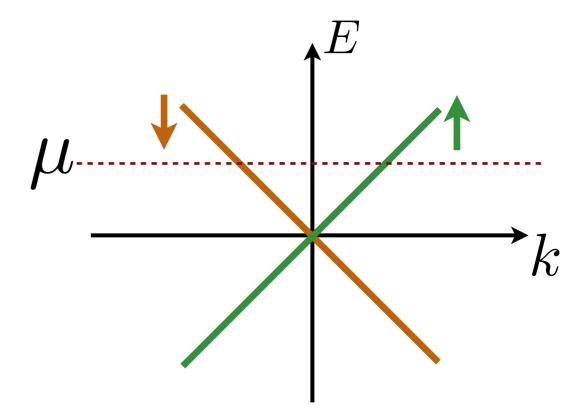


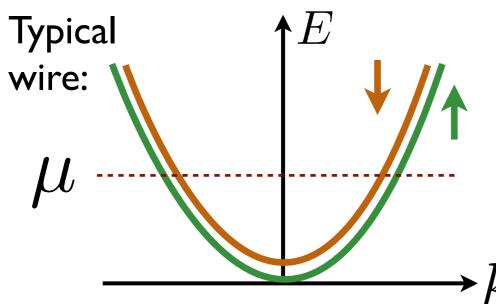


- I. By construction ID & "spinless"
- II. Easy to make superconducting

ID "spinless" superconductivity via edge states

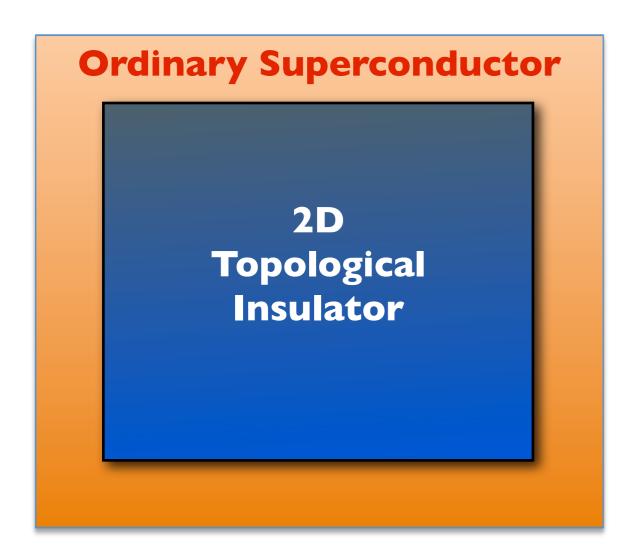


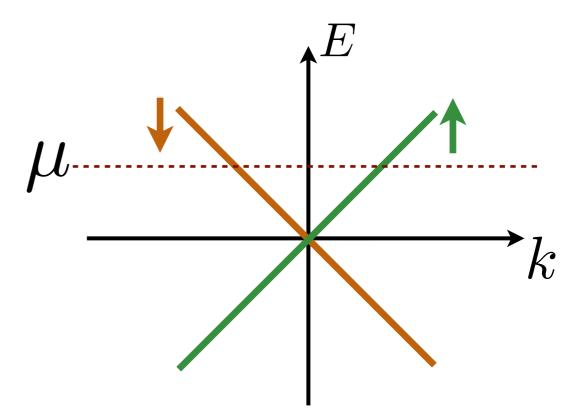




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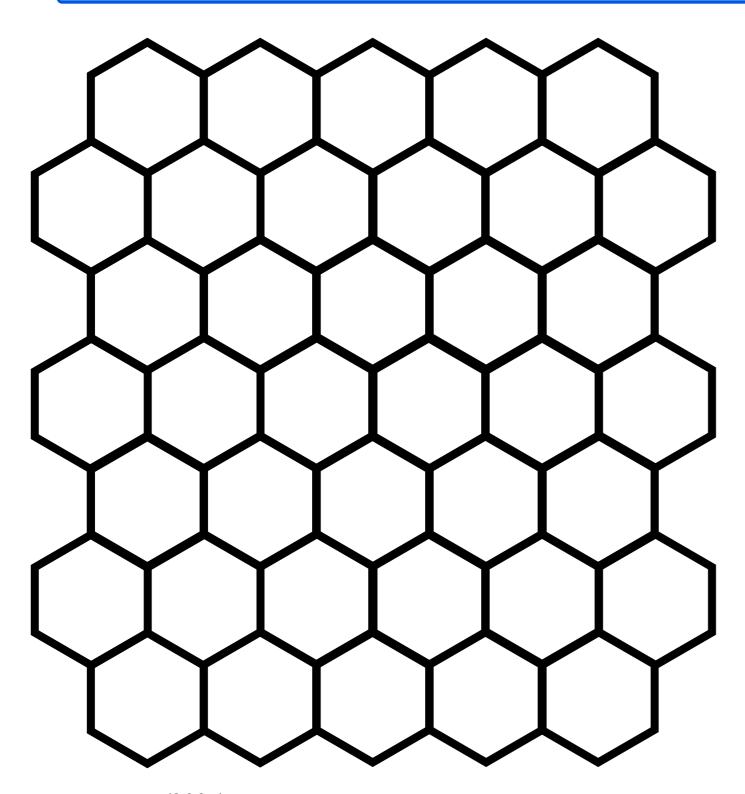




Small number of 2D topological insulators

- I. By construction ID & "spinless"
- II. Easy to make superconducting

Aside: Topological insulator in graphene?

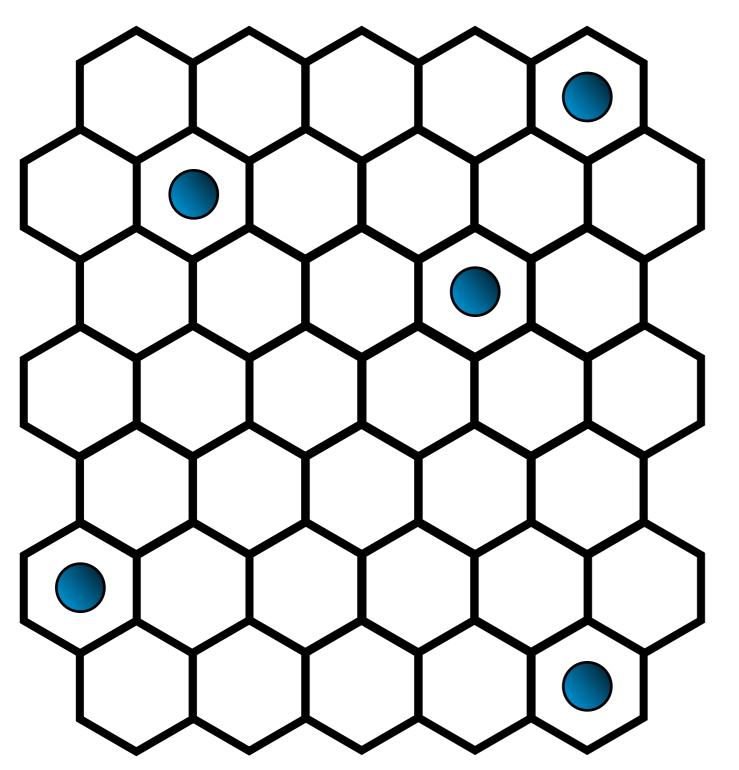


Ist proposed topological insulator, but gap is tiny: <0.01meV

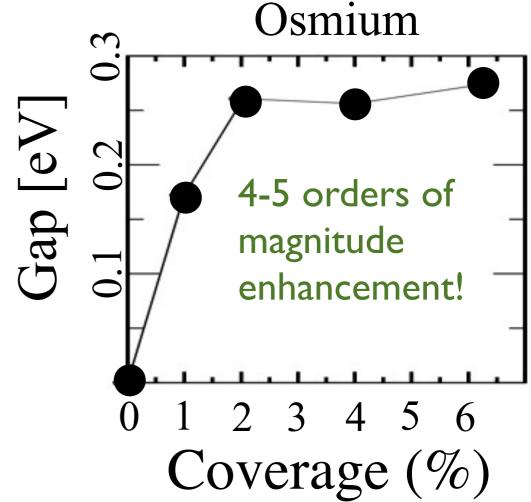
Kane & Mele, PRL (2005)

Weeks, Hu, Alicea, Franz, Wu, PRX (2011); Hu et al., arXiv:1206.4320

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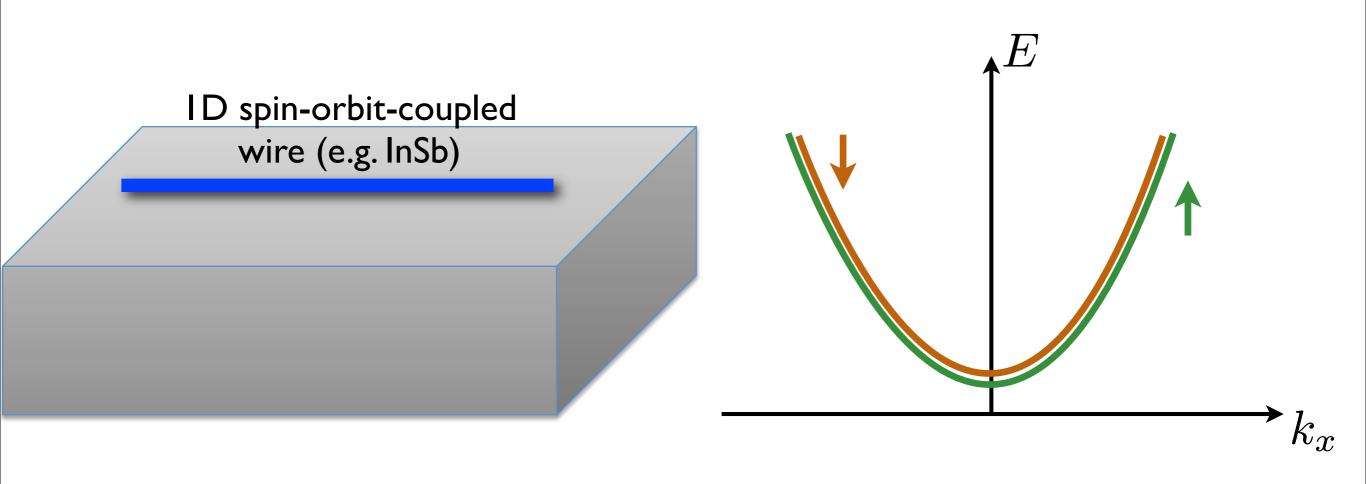


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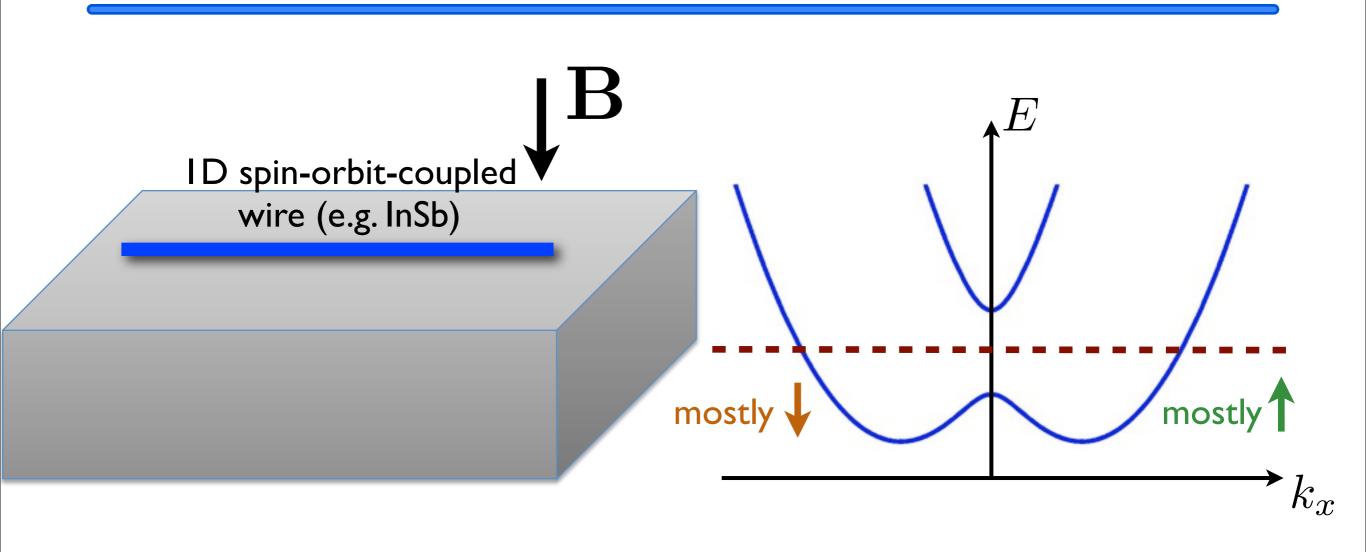
Experiments underway...

Weeks, Hu, Alicea, Franz, Wu, PRX (2011); Hu et al., arXiv:1206.4320

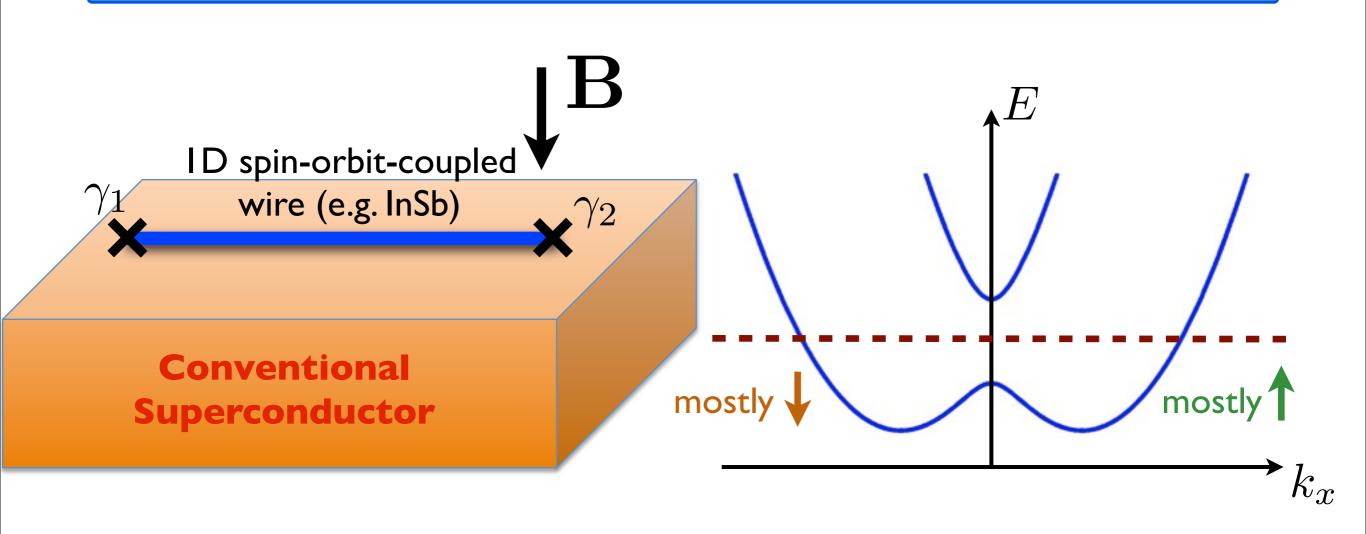
Majorana fermions in 1D wires



Majorana fermions in 1D wires



Majorana fermions in ID wires



Generates a I D 'spinless' superconductor with Majorana fermions!

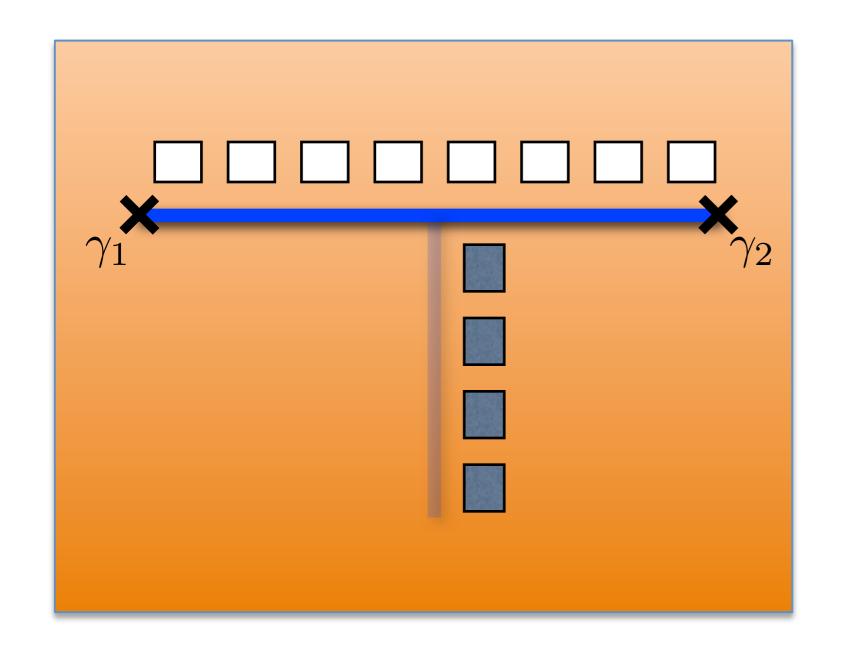
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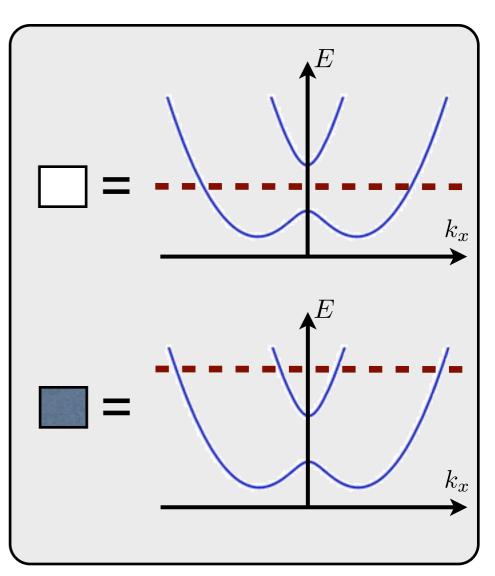
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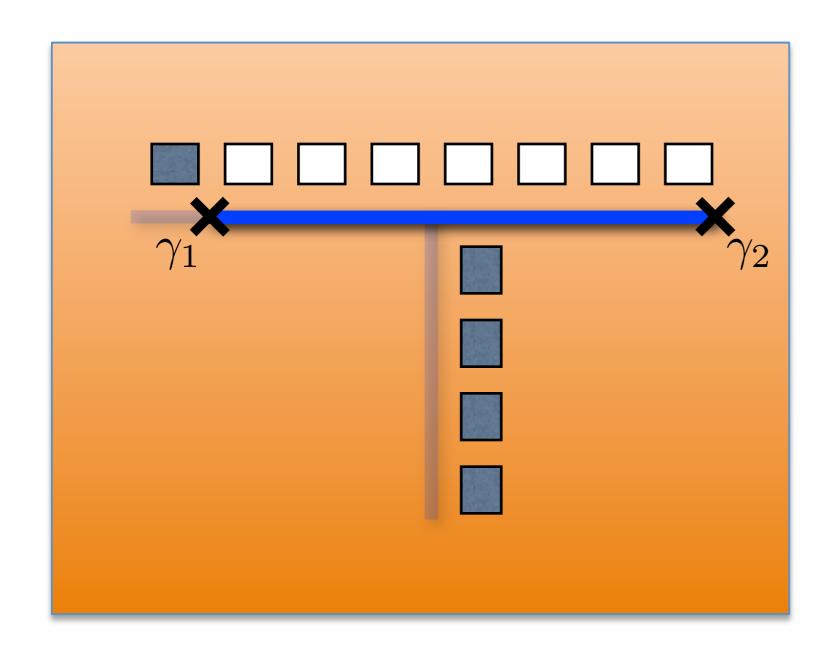
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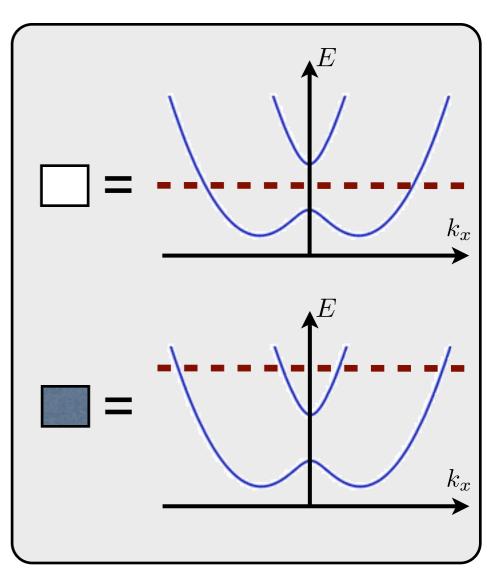
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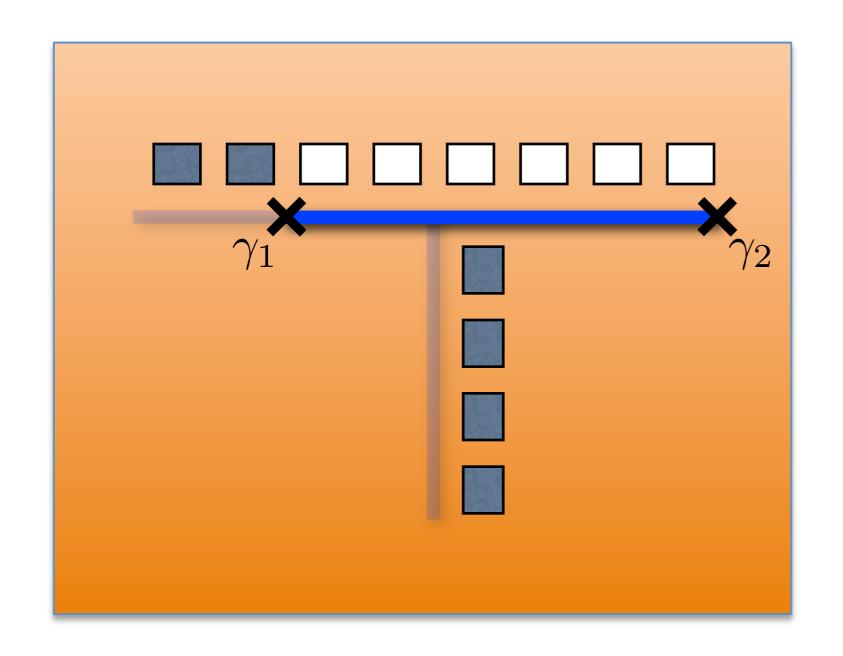
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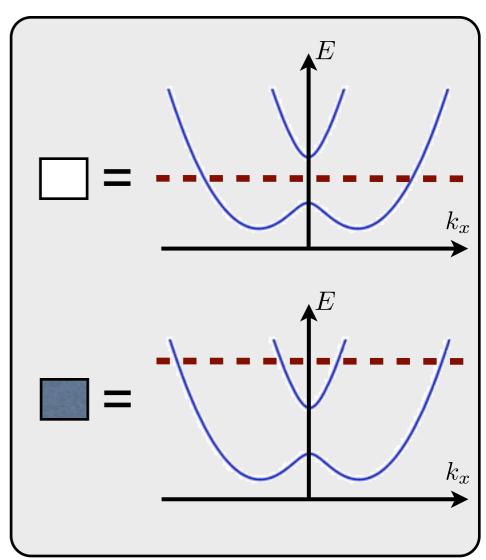


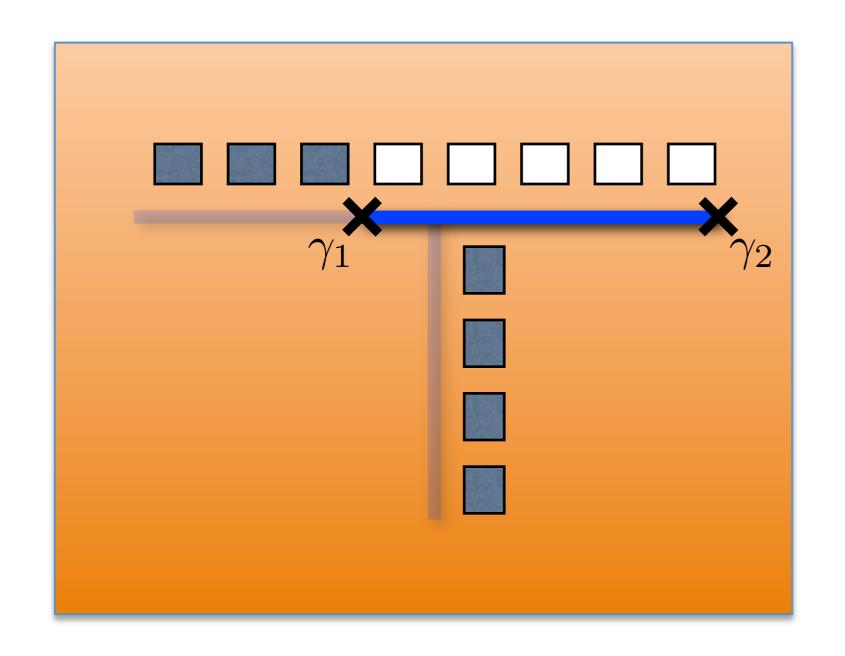


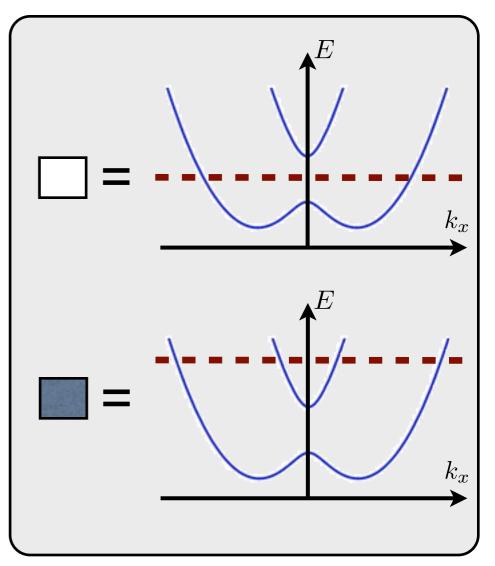


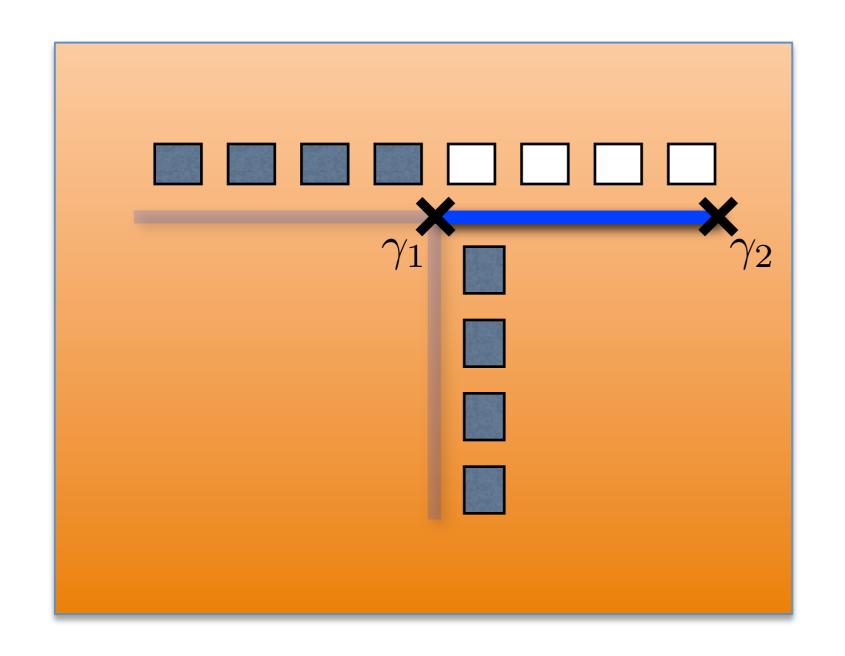


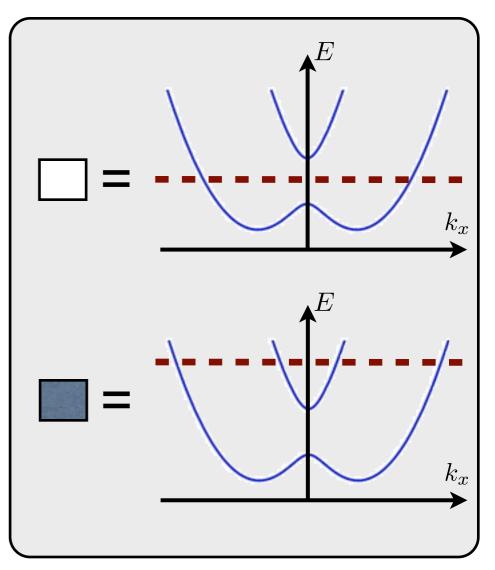


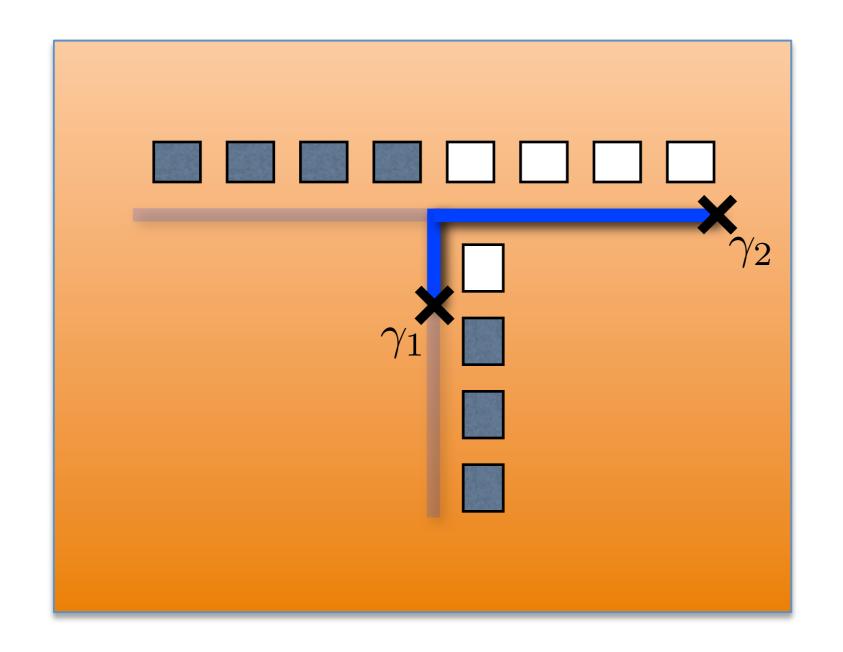


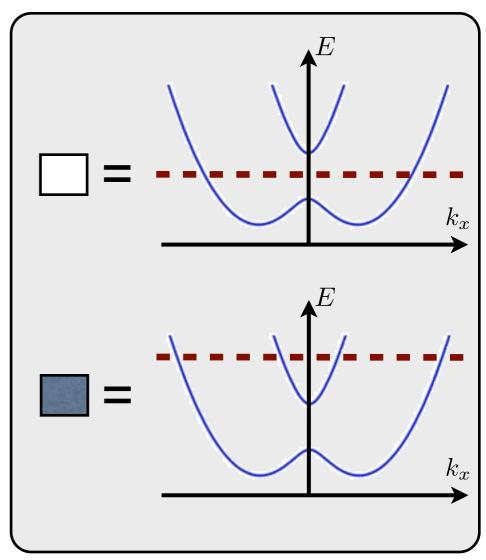


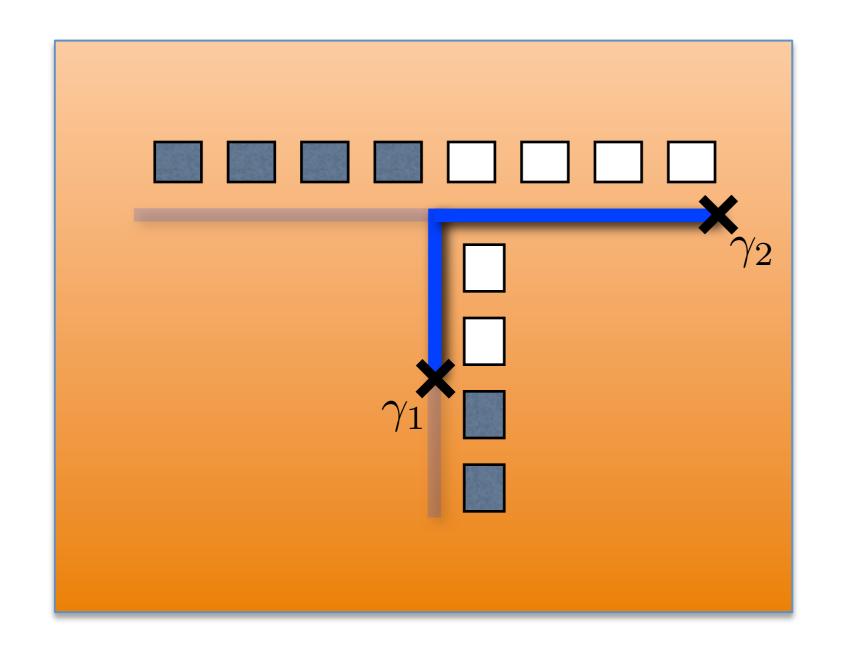


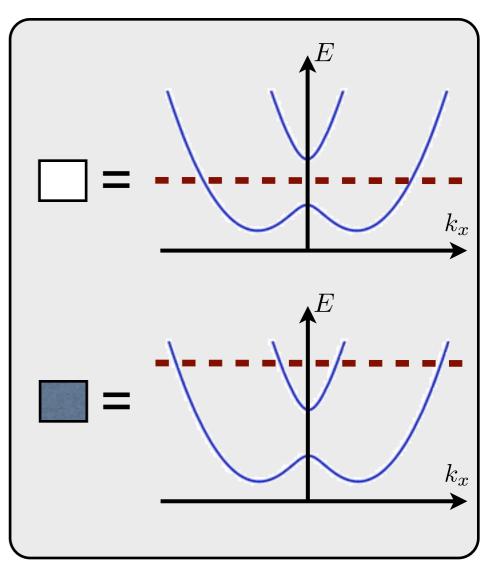


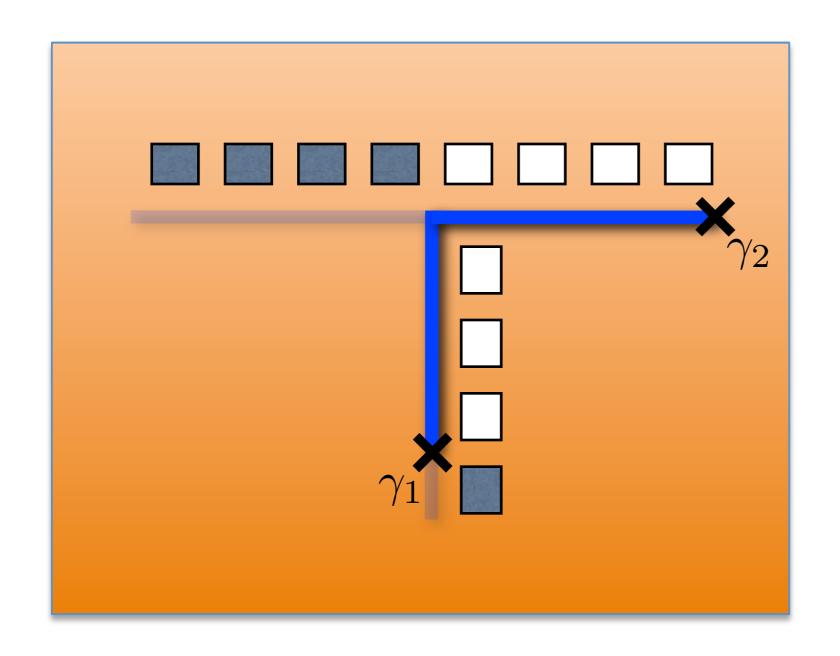


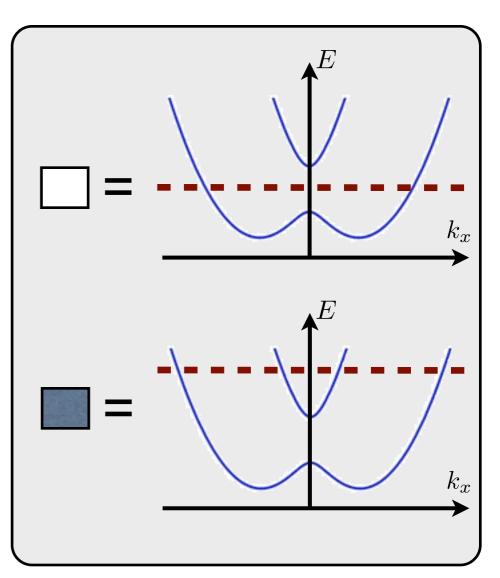


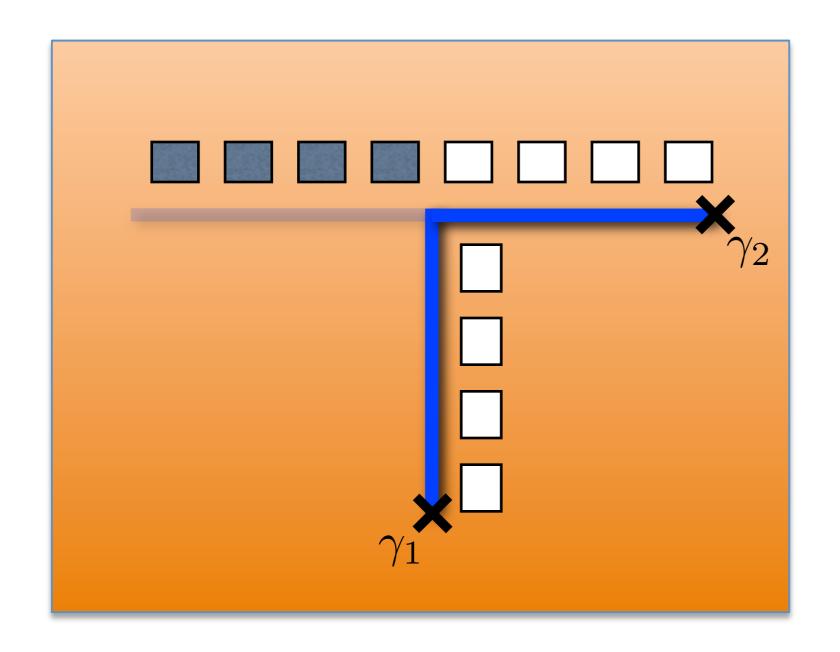


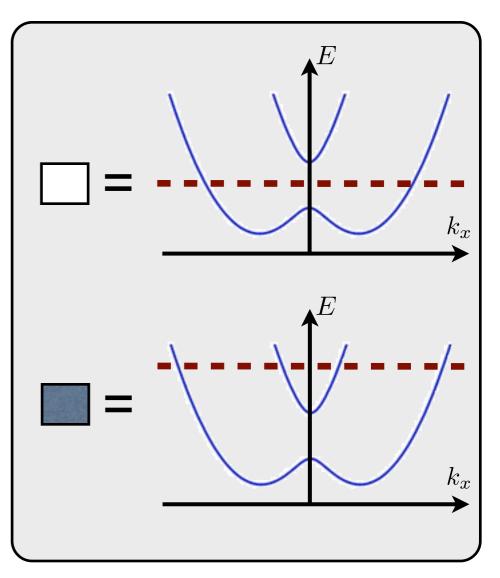


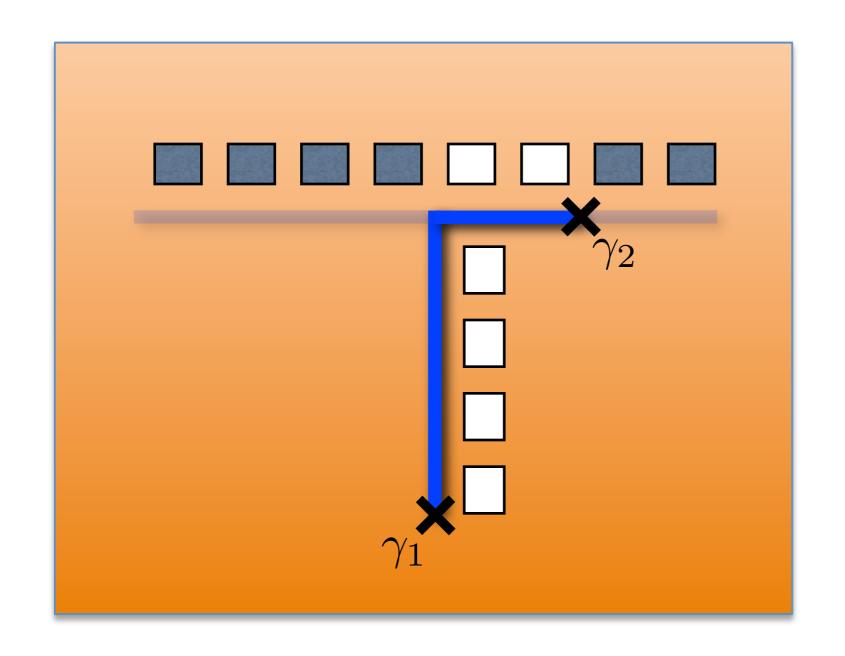


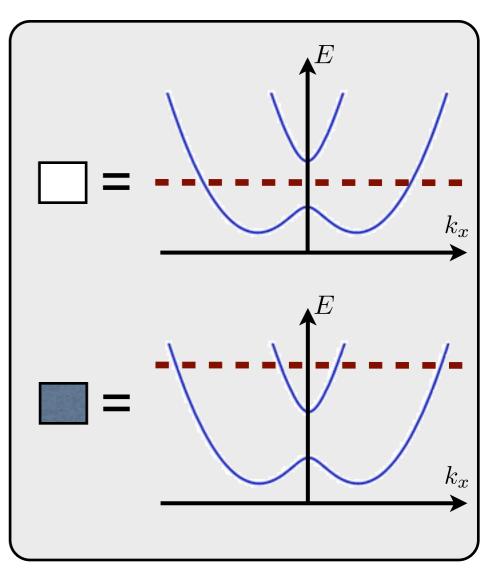


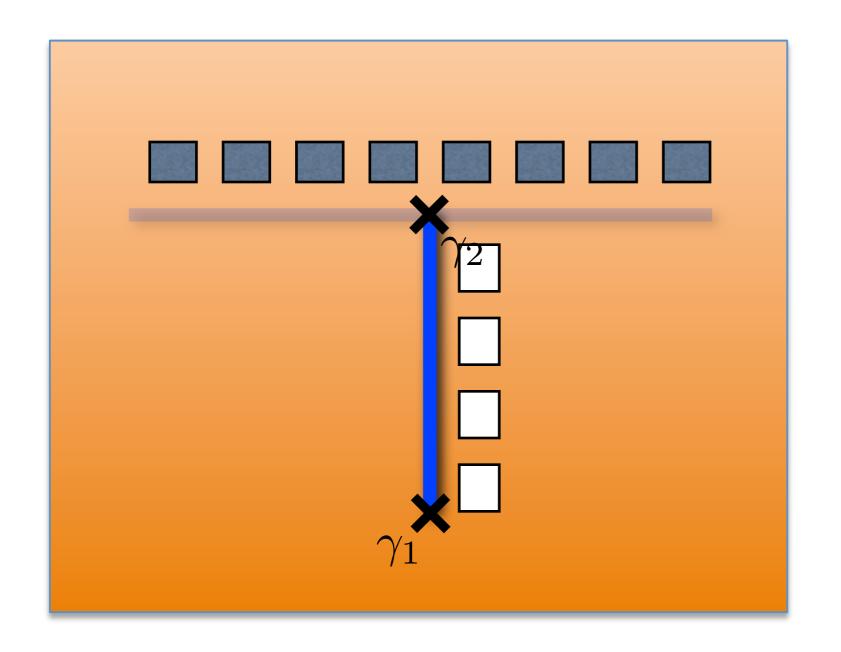


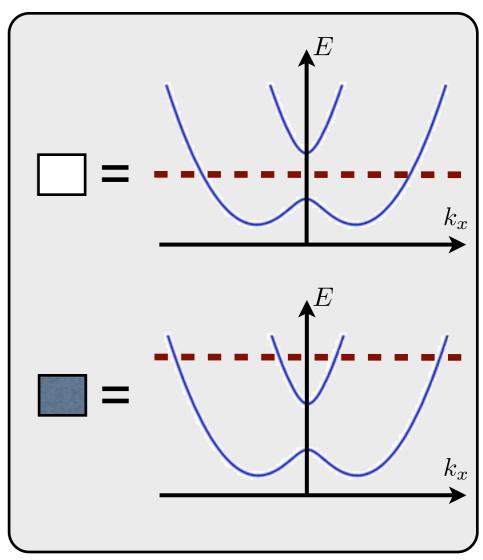


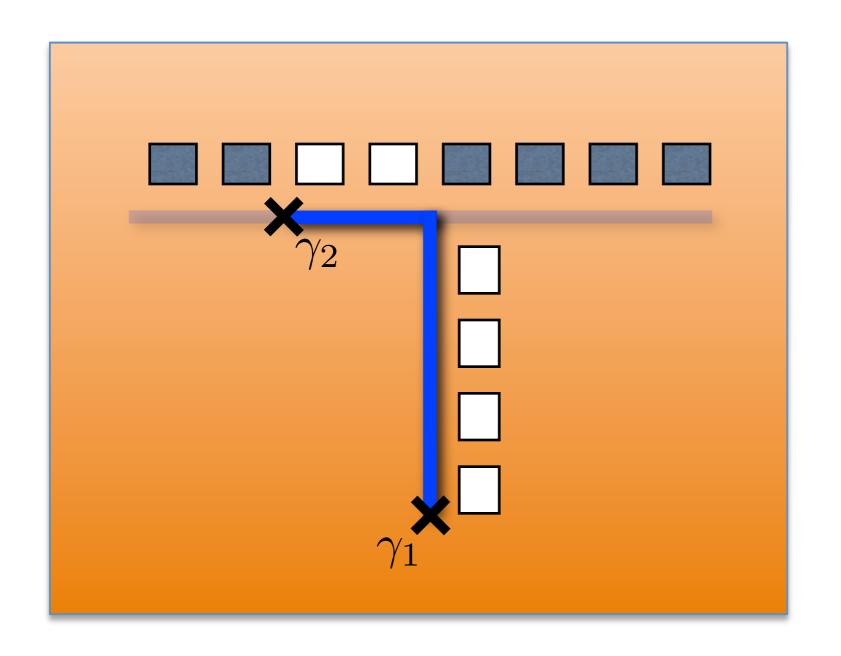


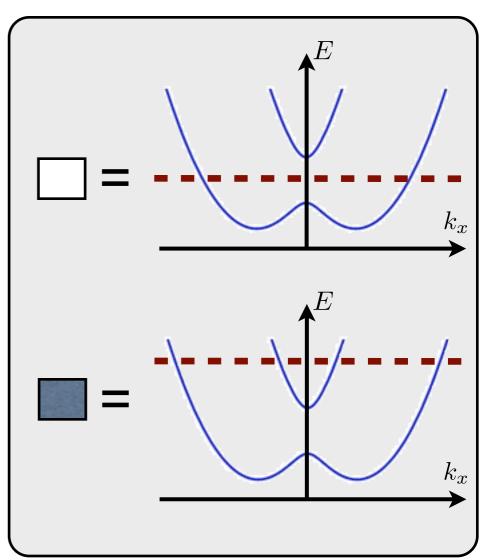


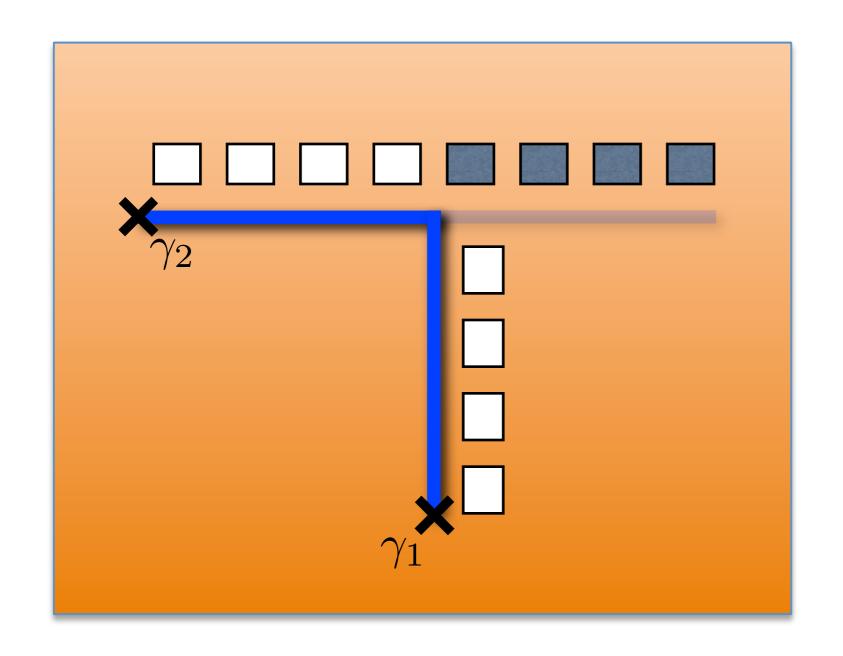


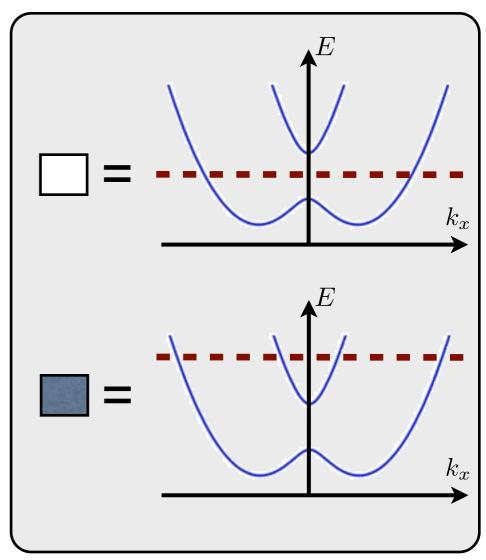


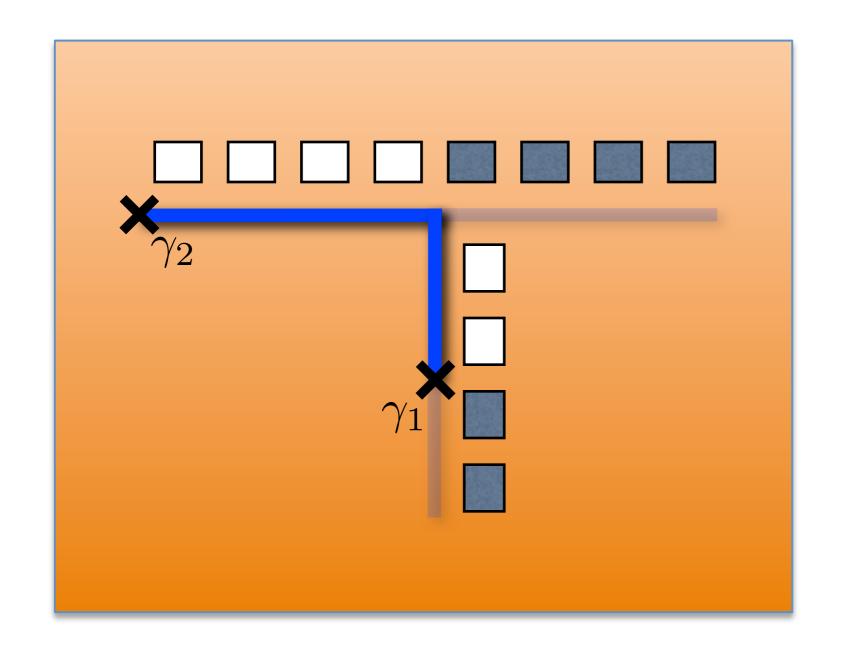


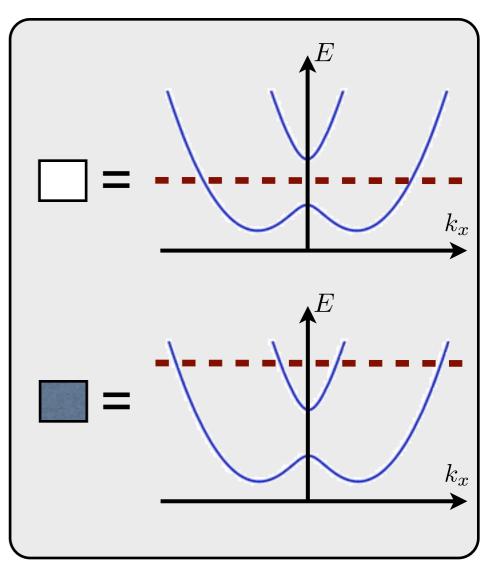


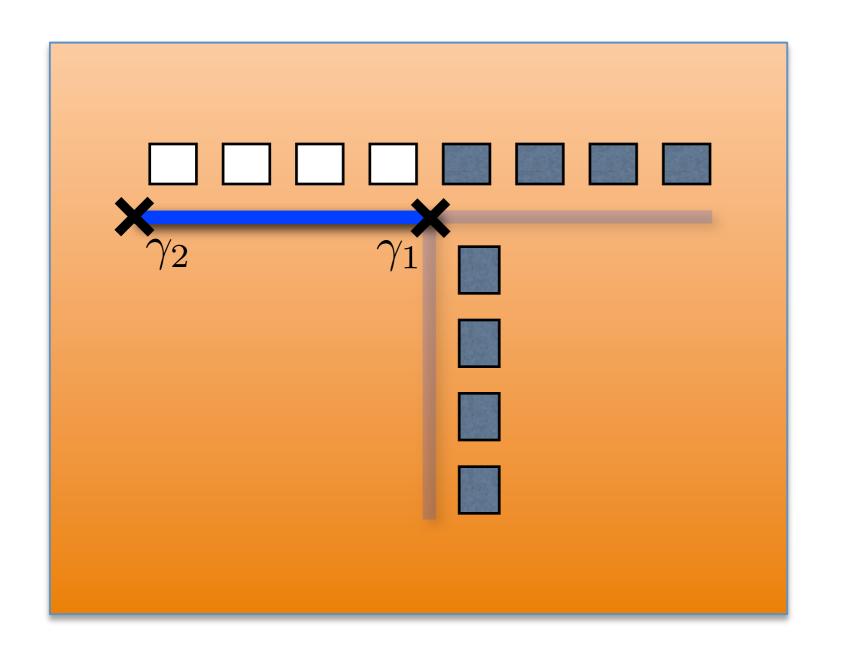


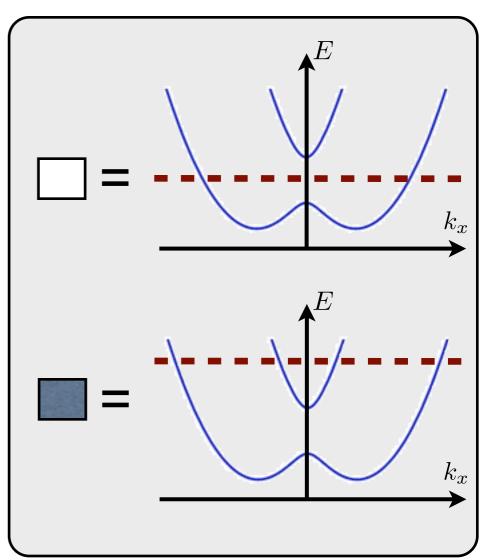


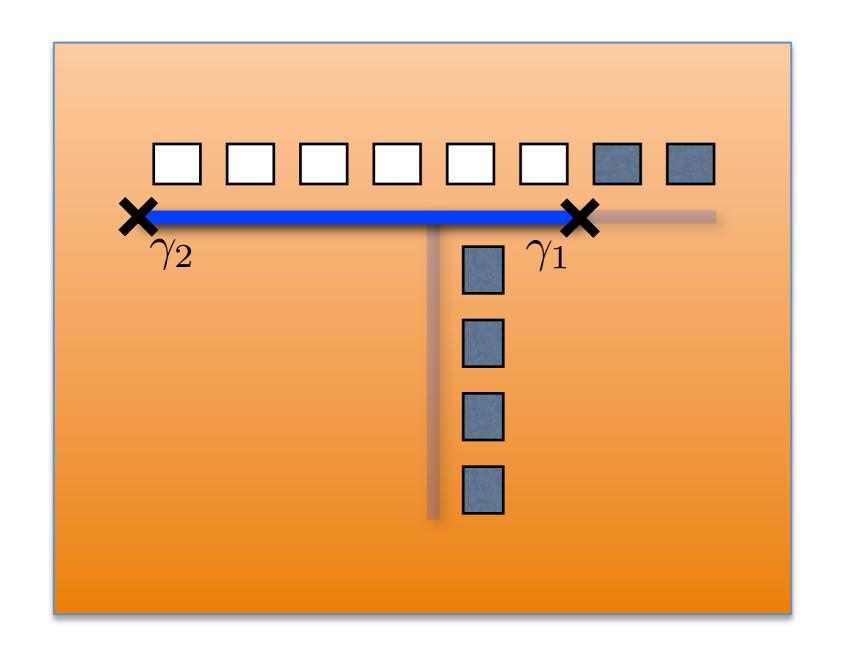


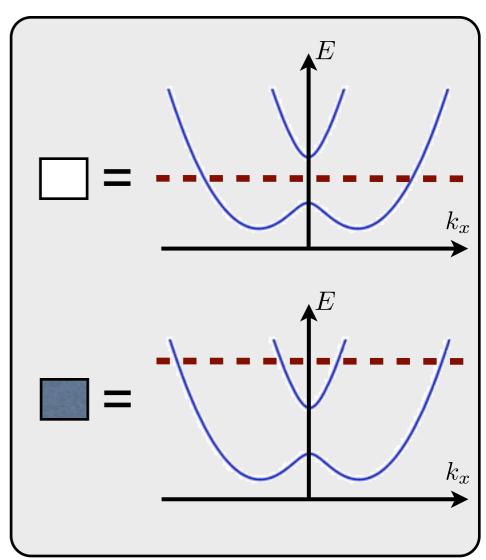


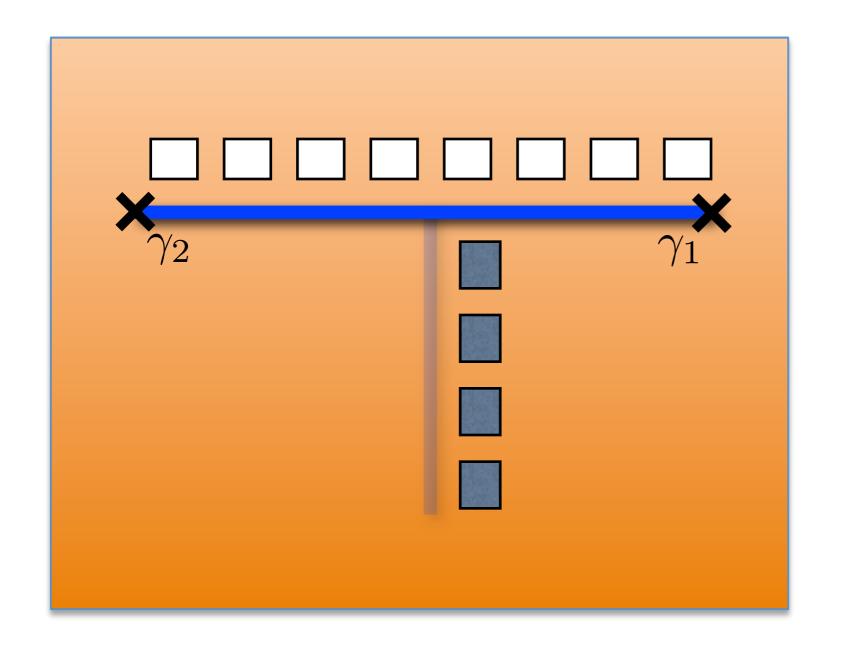


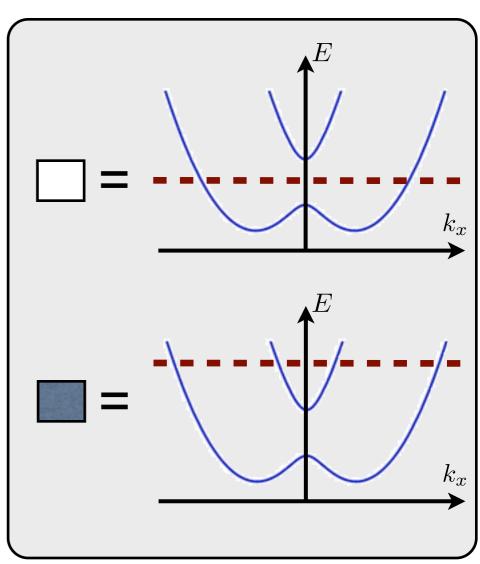






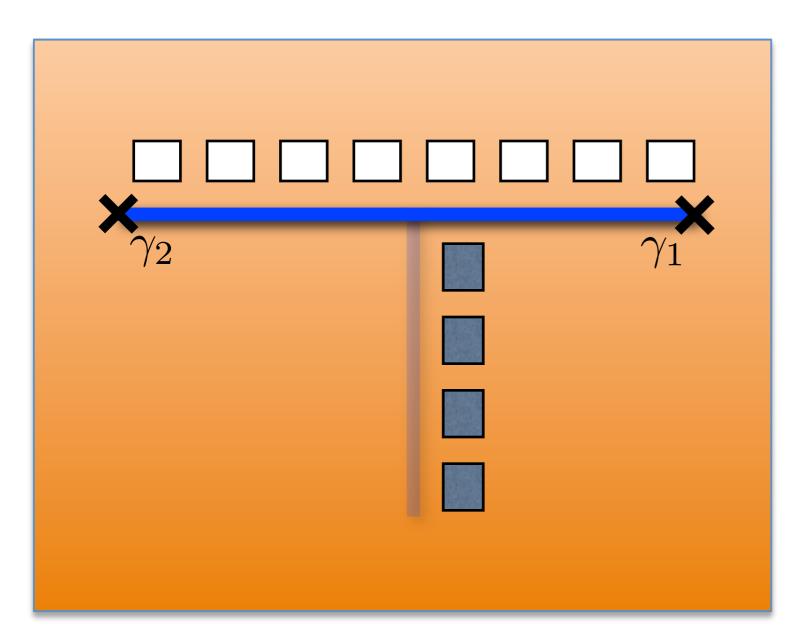


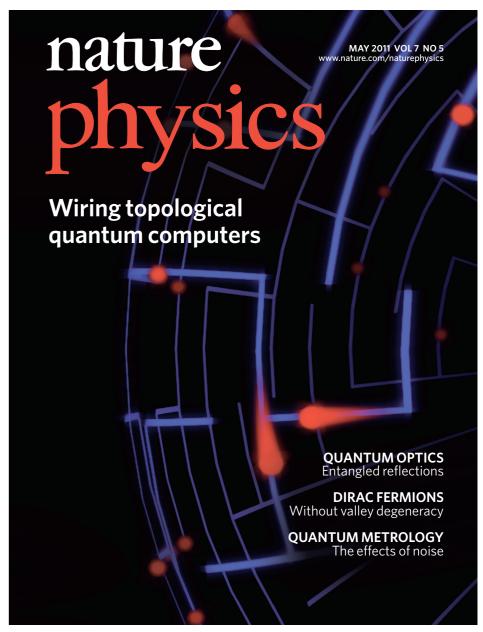




Alicea, Oreg, Refael, von Oppen, Fisher, Nature Phys. 2010 Clarke, Sau, Tewari, PRB 2010 Halperin, Oreg, Stern, Refael, Alicea, von Oppen, PRB 2011 Non-Abelian statistics possible using ID wires!

Harnessing non-Abelian statistics

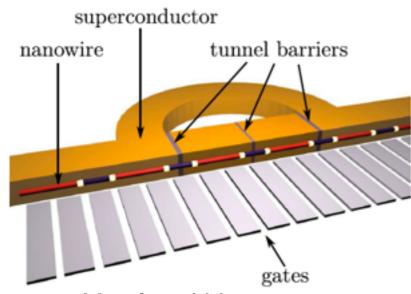




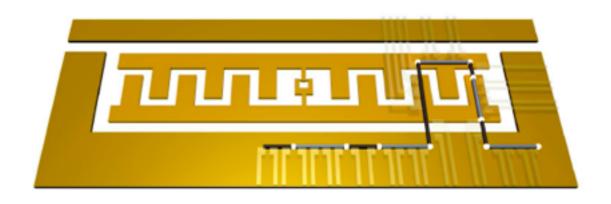
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Blueprints for quantum computers

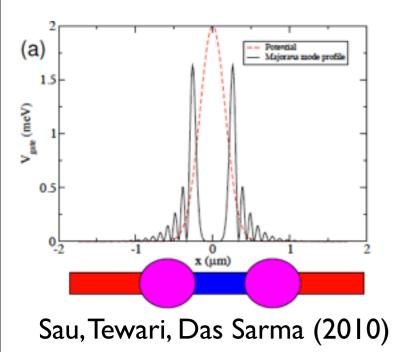
Need to supplement braiding with additional operations...

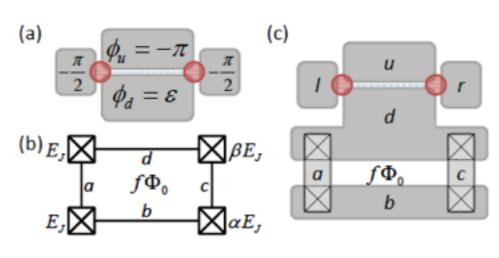


Hassler, Akhmerov, Hou, Beenakker (2010)

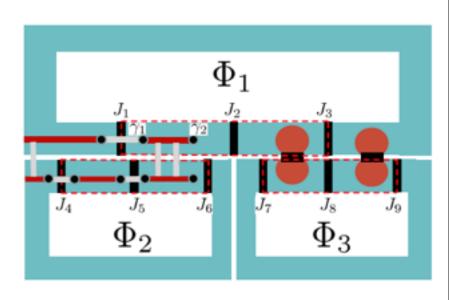


Hassler, Akhmerov, Beenakker (2011)





Jiang, Kane, Preskill (2010)



Bonderson and Lutchyn (2010)

Outline

Majorana fermions: what they are & why they're interesting

The quest for Majorana in the solid state

Getting the most out of Majorana fermions

Experimental status & closing remarks

Signatures of Majorana Fermions in Hybrid Superconductor-Topological Insulator Devices

J. R. Williams,¹ A. J. Bestwick,¹ P. Gallagher,¹ Seung Sae Hong,² Y. Cui,^{3,4} Andrew S. Bleich,⁵ J. G. Analytis,^{2,4} I. R. Fisher,^{2,4} and D. Goldhaber-Gordon¹



Signatures of Majorana Fermions in Hybrid Superconductor-Semiconductor Nanowire Devices



V. Mourik,¹* K. Zuo,¹* S. M. Frolov,¹ S. R. Plissard,² E. P. A. M. Bakkers,^{1,2} L. P. Kouwenhoven¹†

Evidence of Majorana fermions in an Al – InAs nanowire topological superconductor

Anindya Das*, Yuval Ronen*, Yonatan Most, Yuval Oreg, Moty Heiblum#, and Hadas Shtrikman

Observation of Majorana Fermions in a Nb-InSb Nanowire-Nb Hybrid Quantum Device

M. T. Deng, C. L. Yu, G. Y. Huang, M. Larsson, P. Caroff, and H. Q. Xu1,3,*

Observation of the fractional ac Josephson effect: the signature of Majorana particles

Leonid P. Rokhinson,^{1,2,*} Xinyu Liu,³ and Jacek K. Furdyna³

Anomalous Modulation of a Zero-Bias Peak in a Hybrid Nanowire-Superconductor Device

A. D. K. Finck, D. J. Van Harlingen, P. K. Mohseni, K. Jung, and X. Li Phys. Rev. Lett. 110, 126406 (2013)



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Superconductor-Nanowire Devices from Tunneling to the Multichannel Regime: Zero-Bias Oscillations and Magnetoconductance Crossover

H. O. H. Churchill, 1, 2 V. Fatemi, 2 K. Grove-Rasmussen, 3 M. T. Deng, 4 P. Caroff, 4 H. Q. Xu, 4, 5 and C. M. Marcus



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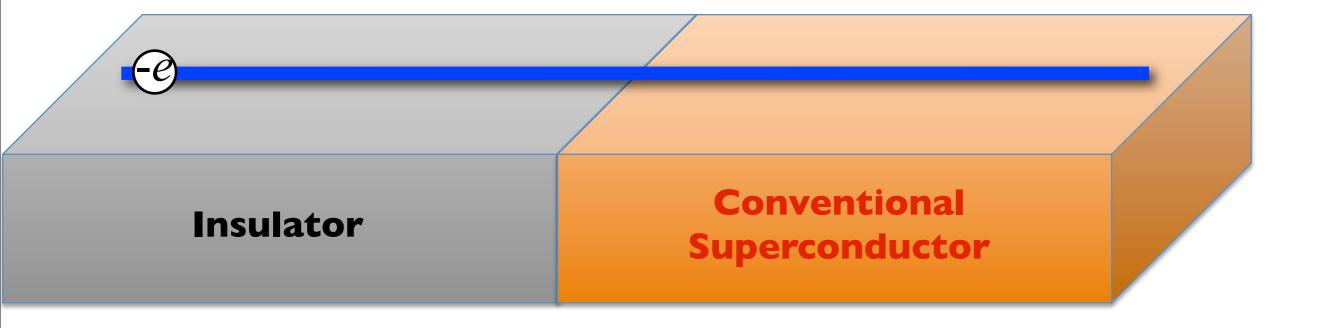
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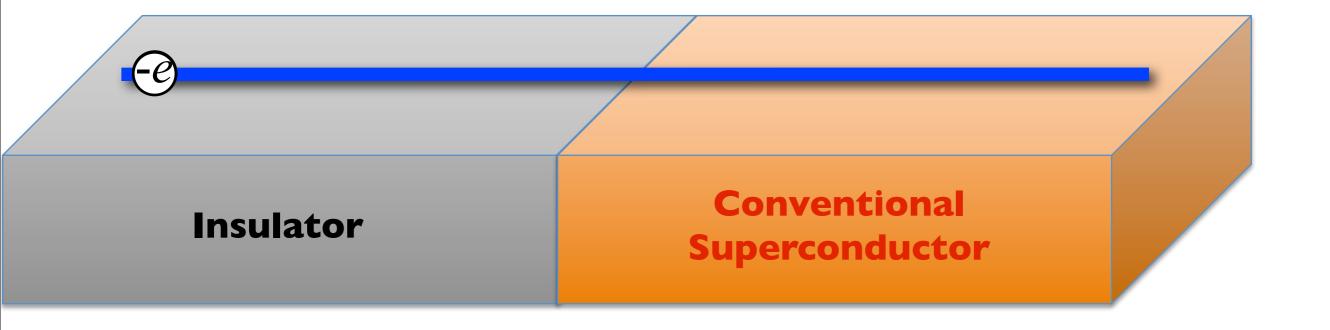
Detection via transport

Normal reflection

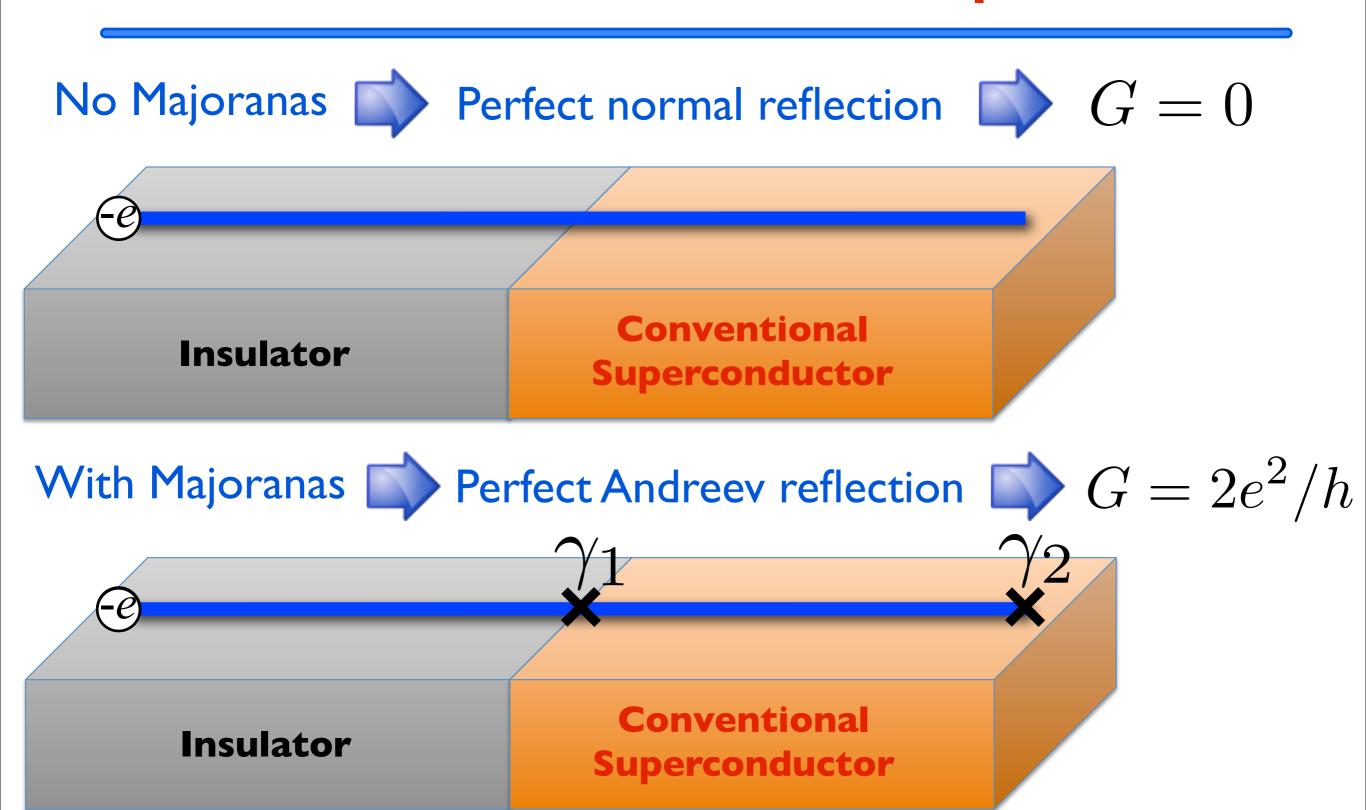


Detection via transport

Andreev reflection

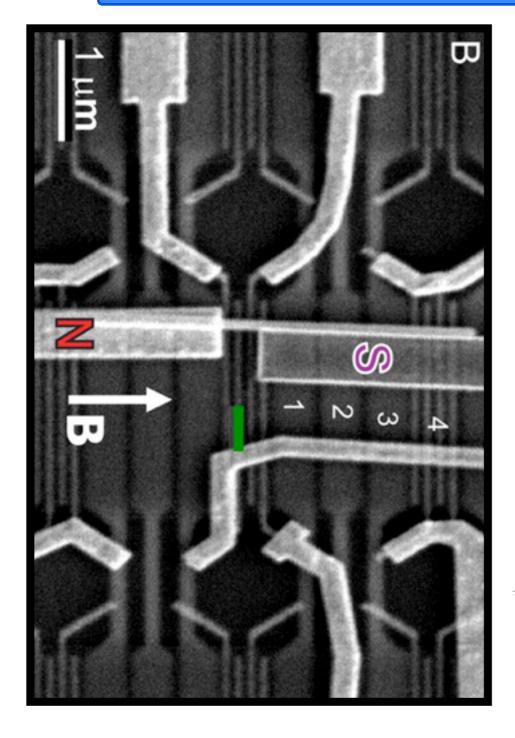


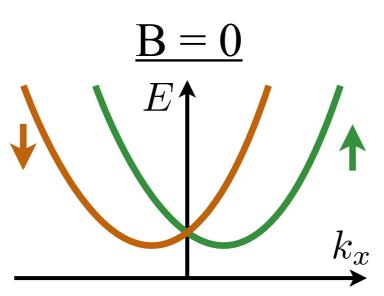
Detection via transport

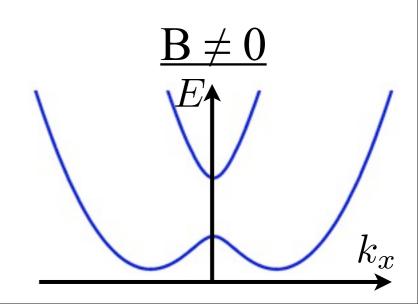


Sengupta et al. (2001); Bolech, Demler (2007); Law, Lee, Ng (2009); Fidkowski, Alicea, Lindner, Lutchyn, Fisher (2012)

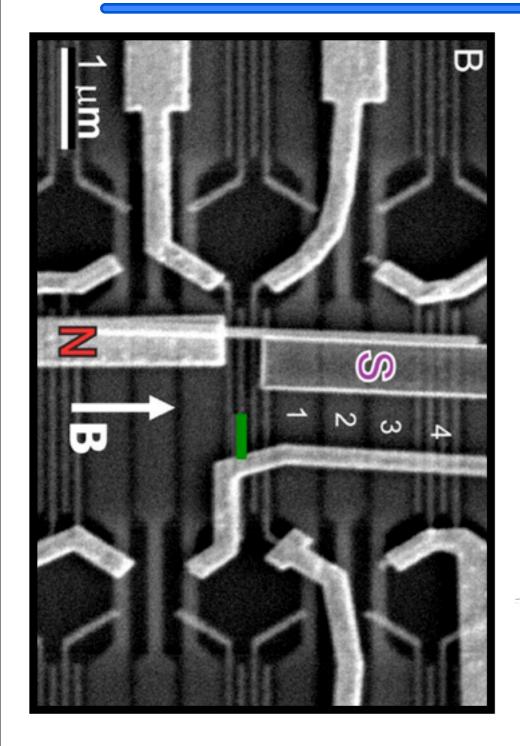
Experimental results

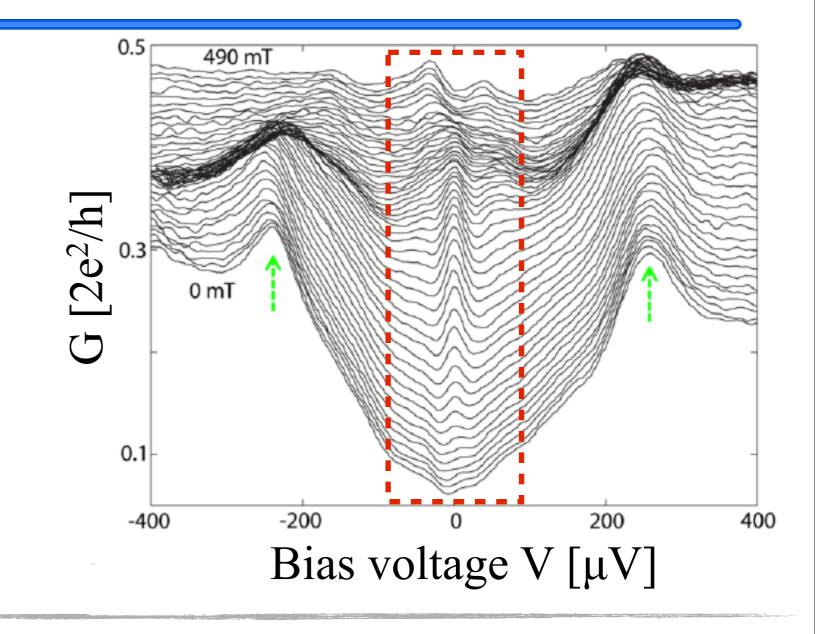


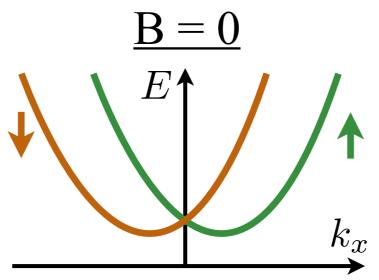


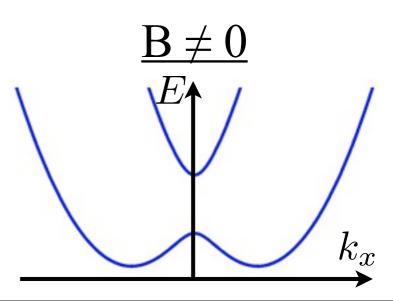


Experimental results

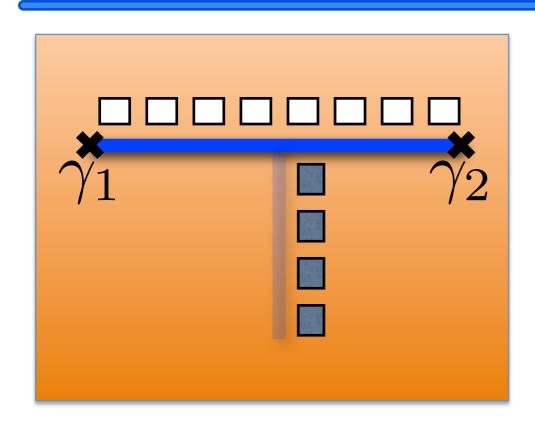


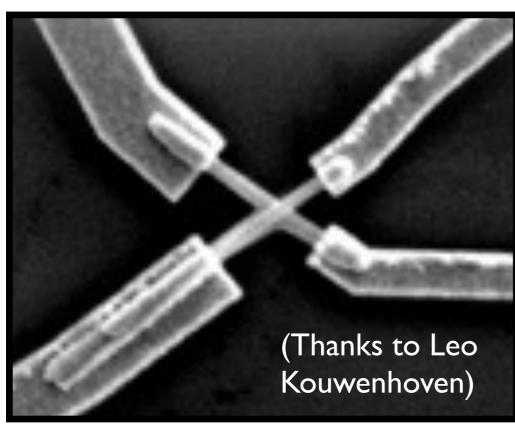


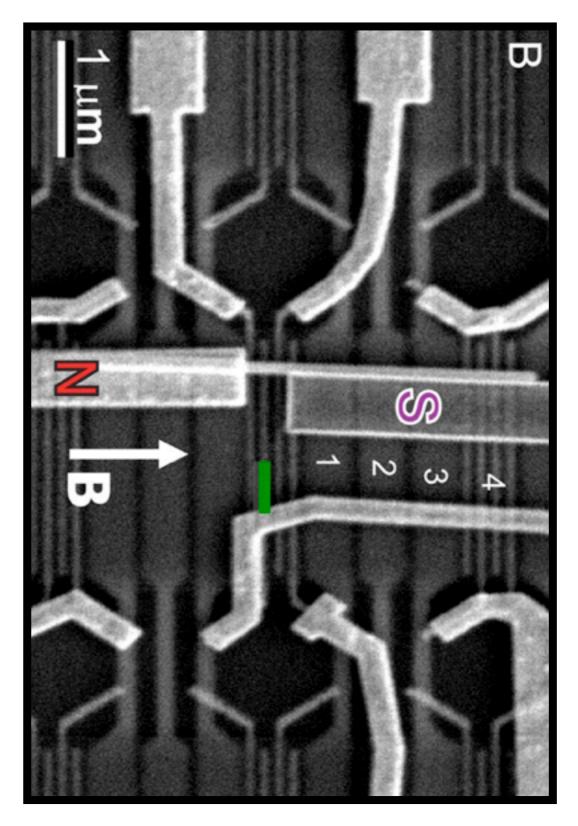




Braiding on the horizon?







Mourik et al., Science 2012

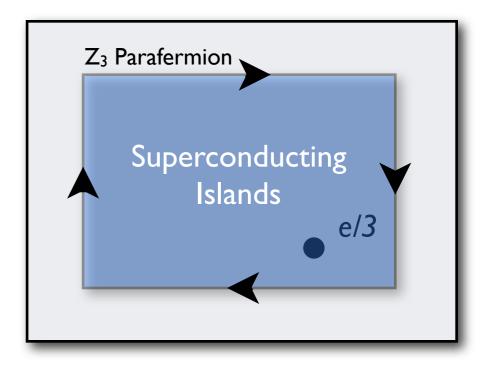


"More is different"...

...even at the macroscale

Topological insulators
Non-Abelian anyons
Majorana fermions
Parafermions
Fibonacci

can be "engineered" by combining simple ingredients



Mong, Clarke, JA, Lindner, Fendley, Nayak, Oreg, Stern, Berg, Shtengel, Fisher, arXiv:1307.4403

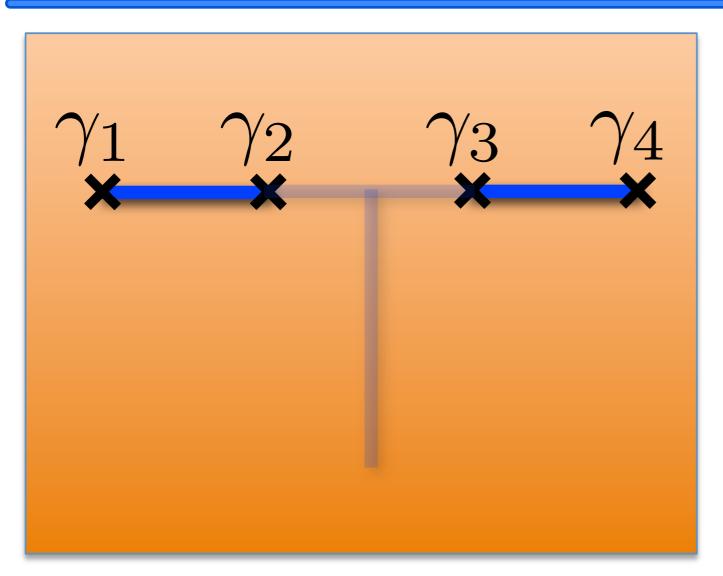
Thanks for your attention!

Recent reviews:

I. Beenakker, Annual Review of Condensed Matter Physics 4, 113 (2013)

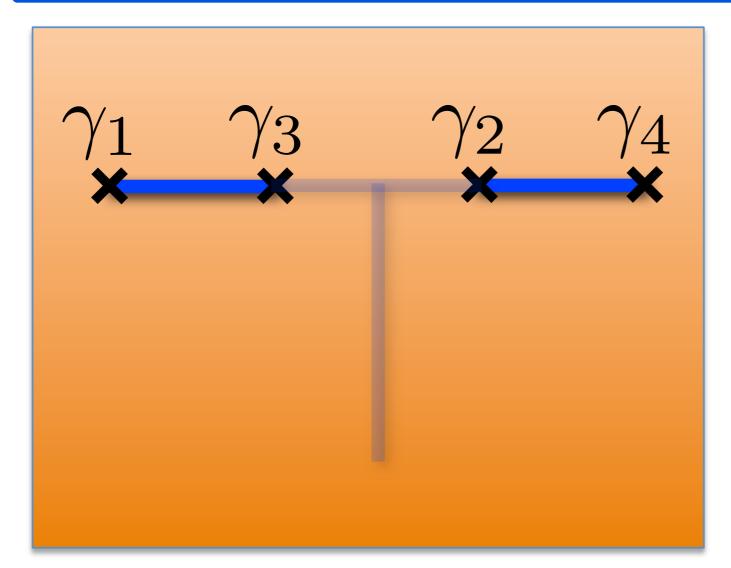
2. Alicea, Reports on Progress in Physics **75**, 076501 (2012)

Confirming non-Abelian statistics



- I. Nucleate Majoranas from the vacuum
- 2. Check that fusing pairs you created returns the ground state
- 3. Exchange Majoranas

Confirming non-Abelian statistics



5. Can detect excitation using Josephson measurements

- I. Nucleate Majoranas from the vacuum
- 2. Check that fusing pairs you created returns the ground state
- 3. Exchange Majoranas
- 4. Fusing pairs in same way as in 2 should now yield excited state with 50% probability