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Test of the Equivalence Principle in the Laboratory

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Mass does not add up

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Proton



Electron



^1H



Mass does not add up

Proton



Electron



1H



938 272 013 eV/c²



510 999 eV/c²



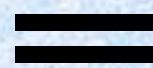
938 782 999 eV/c²

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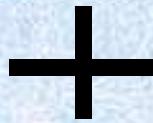
Electron



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938 272 013 eV/c²

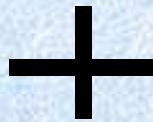


510 999 eV/c²



938 782 999 eV/c²

938 272 013 eV /c²



510 999 eV/c²



938 783 012 eV/c²

Mass defect = binding Energy

13.6 eV/c²

Binding Energy = $\Delta E_{\text{pot}} - \Delta E_{\text{kin}}$

The non-linearity is rather small

but occurs also in
gravitationally
bound systems

Mass defect for 1 kg of
Earth: $\Delta m = 0.46 \mu g$

Mass defect for 1 kg of
Moon: $\Delta m = 0.02 \mu g$



EARTHRISE
OVER THE MOON

YEAR: 1969
MISSION: APOLLO 11
TARGET: LUNA

View from the Apollo 11 spacecraft showing the Earth rising above the Moon's horizon.

The mass of an object



$$m = \sum m_c + \sum E_{kin} - \sum E_{pot}$$

Newton's Principia (1689)

Newton's 2nd Law

$$F_i = m_i a$$

Gravitational Law

$$F_G = G m_{g1} m_{g2} / r^2$$

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Equivalence Principle (EP): $m_i = m_g$

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Is the Equivalence Principle valid for all contributions to the mass?

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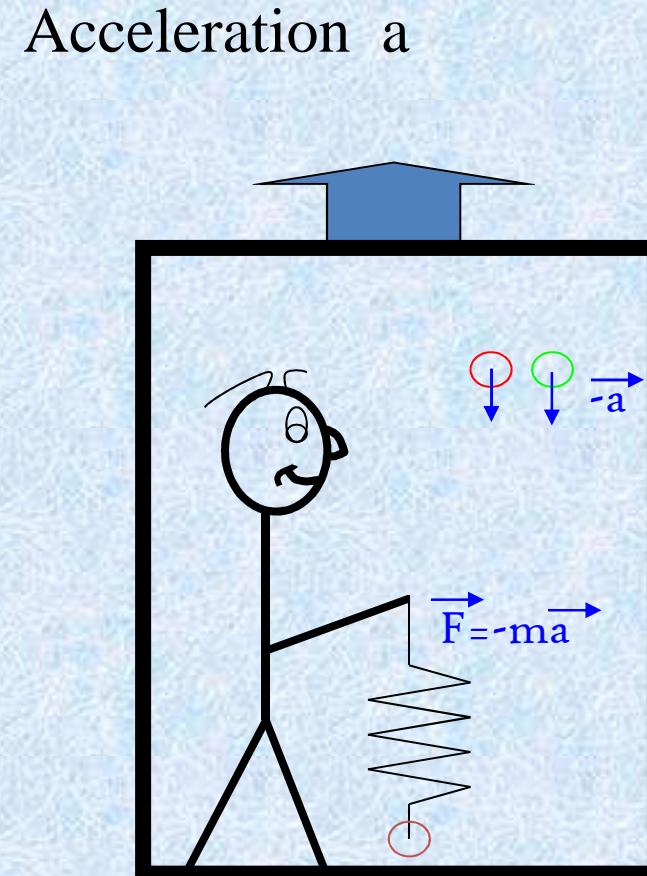
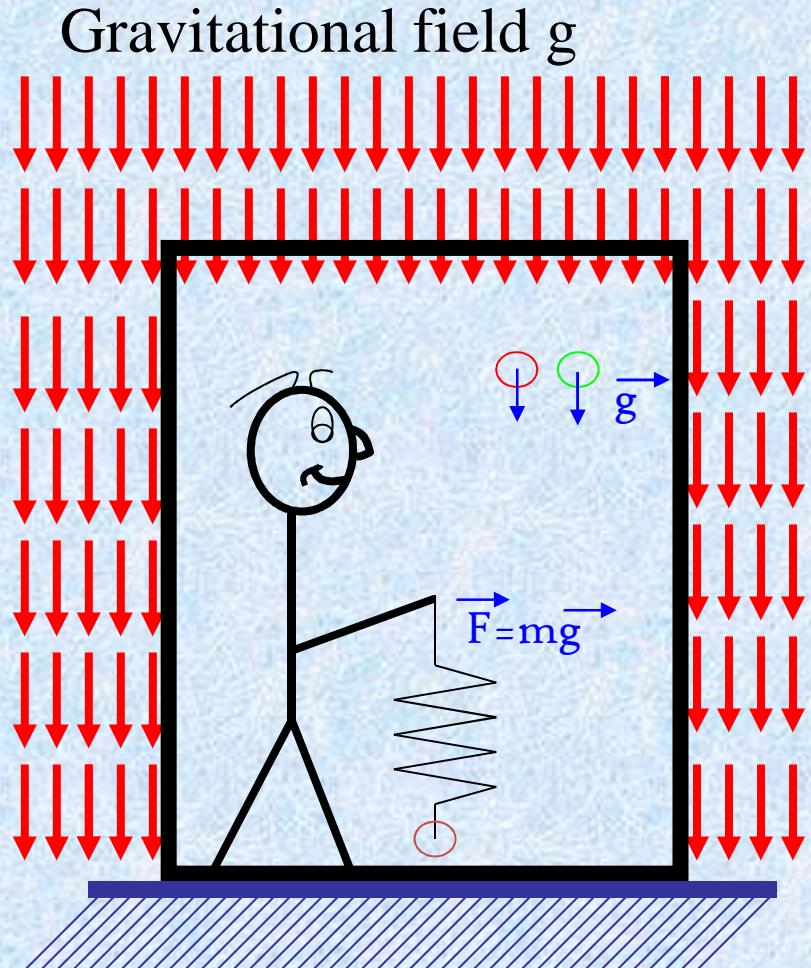
Equivalence Principle (EP): $m_i = m_g$

Is the Equivalence Principle valid for all contributions to the mass?

Weak Equivalence Principle: Gravitational binding energy is excluded.

Strong Equivalence Principle: Includes all 4 fundamental interactions.

In General Relativity



Inertial mass = gravitational mass, $m_I = m_G$ for all bodies

The known unknowns

• What do we know about what we don't know?

• What do we know about what we know?

• What do we know about what we don't know about what we know?

• What do we know about what we know about what we don't know?

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The known unknowns

- GR is not a quantum theory.

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- Cosmological constant problem.

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- Is there another force (5th force)?
- ...

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EP-Tests provide a big bang for the buck!

Searching for new interactions

$$V(r) = \alpha G \left(\frac{q_1}{\mu_1} \right) \left(\frac{q_2}{\mu_2} \right) \frac{m_1 m_2}{r_{12}} e^{-r_{12}/\lambda}$$

Strength relative to gravity

Source Test mass

Interaction range

Searching for new interactions

$$V(r) = \alpha G \left(\frac{q_1}{\mu_1} \right) \left(\frac{q_2}{\mu_2} \right) \frac{m_1 m_2}{r_{12}} e^{-r_{12}/\lambda}$$

Source Test mass

Strength relative to gravity Interaction range

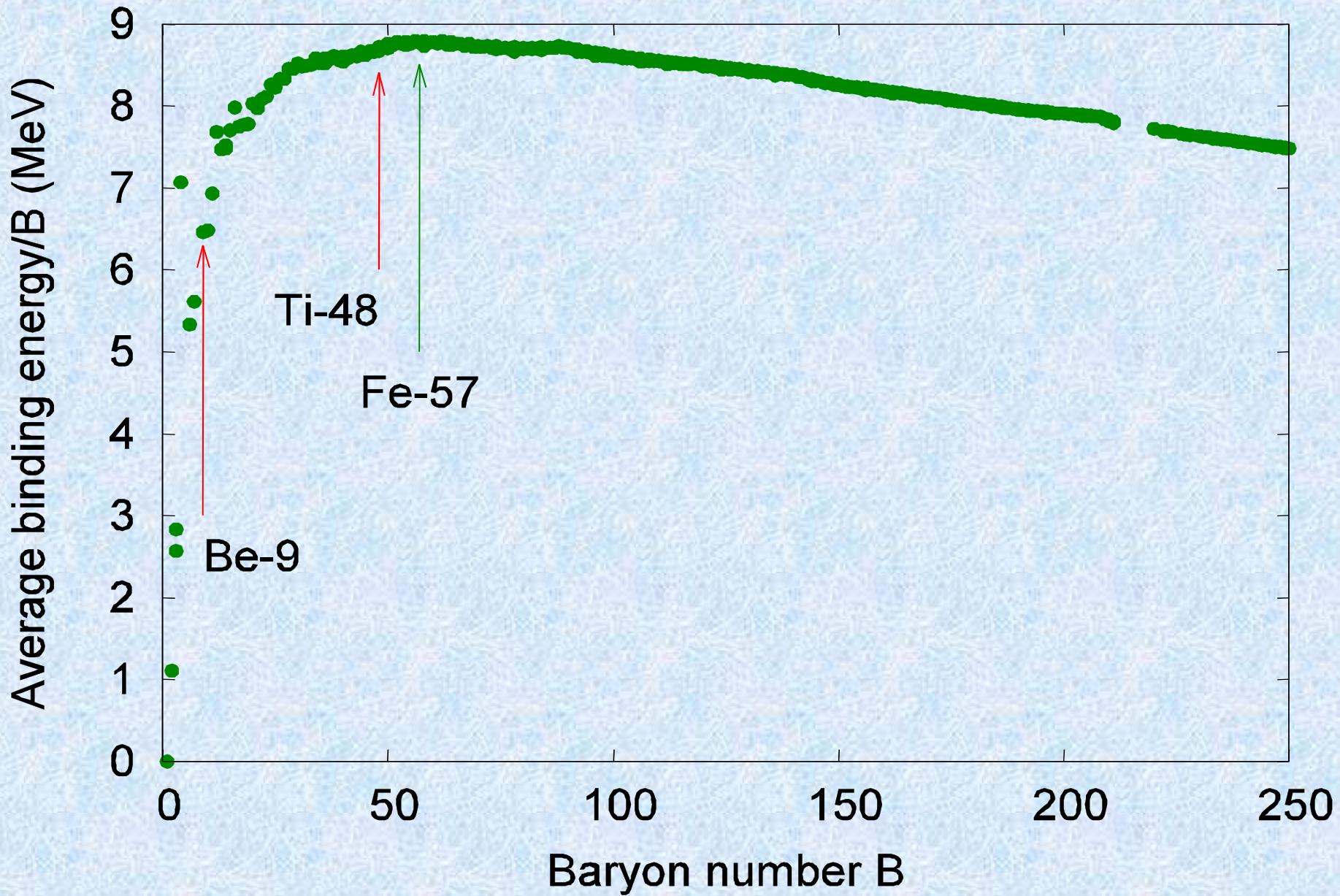
Assumed charge	Be q/ μ	Ti q/ μ	Al q/ μ	Be-Ti ($\times 10^{-2}$)	Be-Al ($\times 10^{-2}$)
N	0.554 80	0.541 47	0.518 87	1.33	3.59
Z	0.443 84	0.459 61	0.481 81	-1.58	-3.80

and any linear combinations: $q(\Psi) = Z \cos \Psi + N \sin \Psi$

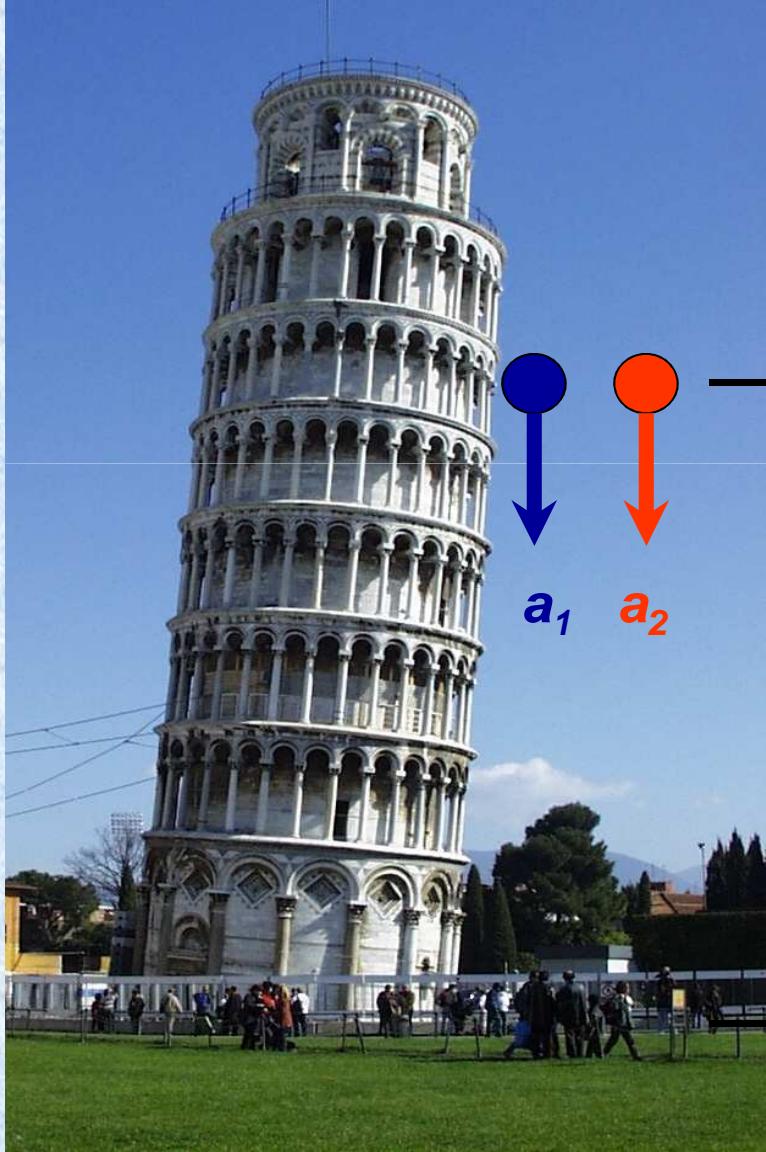
q/μ

	Mass (u)	$q=B$	q/μ
$^1_1 p$	1.007 3	1	0.992 8
$^1_0 n$	1.008 7	1	0.991 4
$^9_4 Be$	9.101 2	9	0.998 7
$^{48}_{22} Ti$	47.947 9	48	1.001 1

B/μ varies, because



1st Tests of the Equivalence Principle



$$F = m_G g$$

$$F = m_I a$$

$$a = \frac{m_G}{m_I} g$$

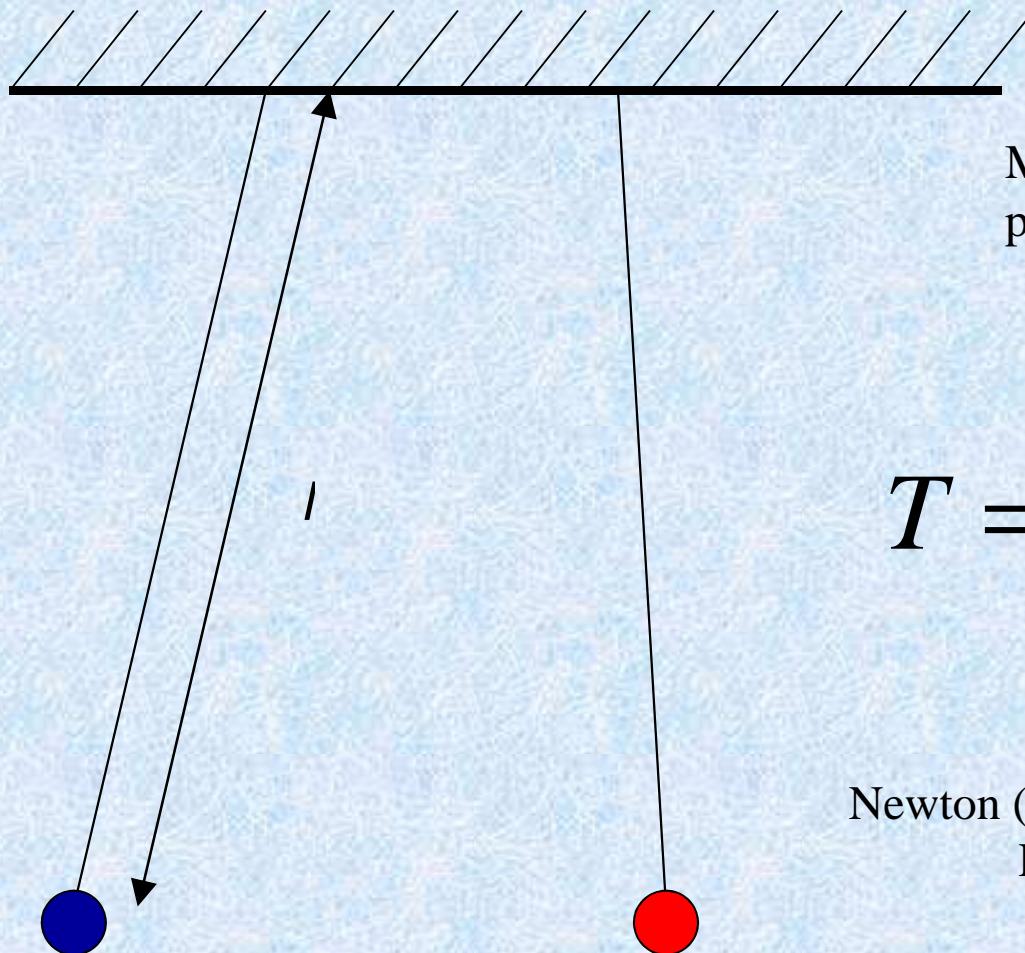
Time t to fall from h :

$$t = \sqrt{\frac{2h}{m_G/m_I g}}$$

1600 Galileo:

$$\eta = \frac{a_1 - a_2}{\frac{1}{2}(a_1 + a_2)} \approx 0.1$$

2nd Generation Tests



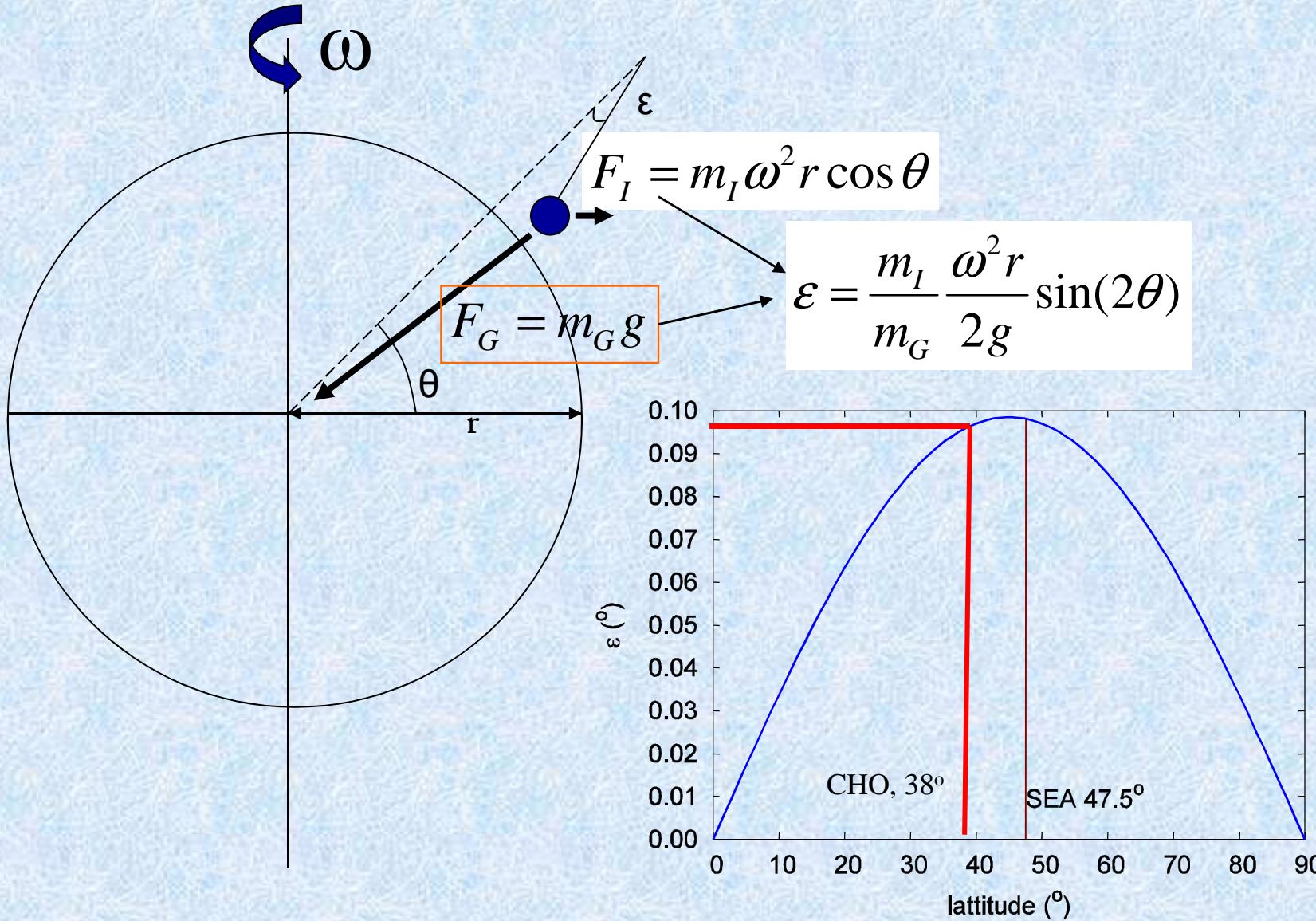
Measurement of the swing
periods of pendula:

$$T = 2\pi \sqrt{\frac{L}{g} \frac{m_I}{m_G}}$$

Newton (1686), Bessel (1830),
Potter (1923)

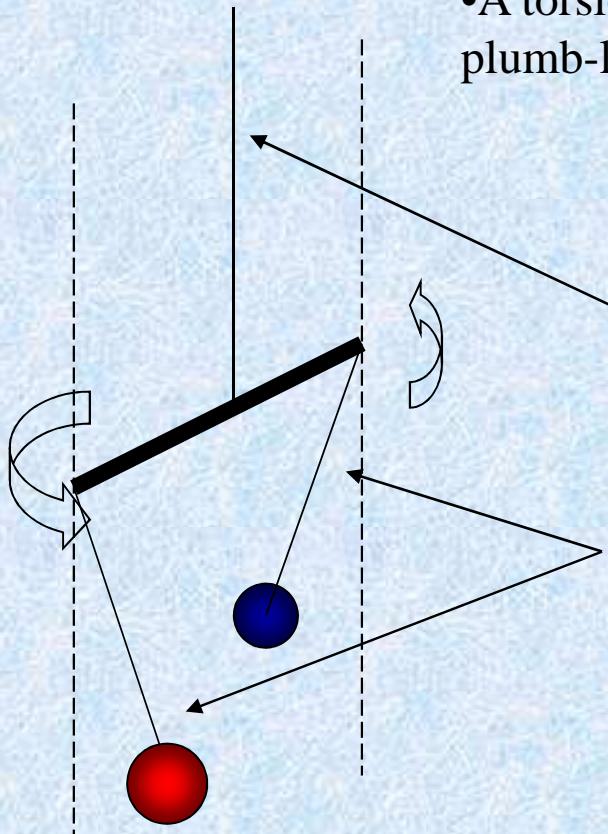
$$\eta \approx 2 \times 10^{-5}$$

Eötvös Experiments



The torsion balance

- A violation of the EP would yield to different plumb-line for different materials.
- A torsion balance can be used to measure the difference in plumb-lines:



Torsion fiber hangs like the average plumb line.

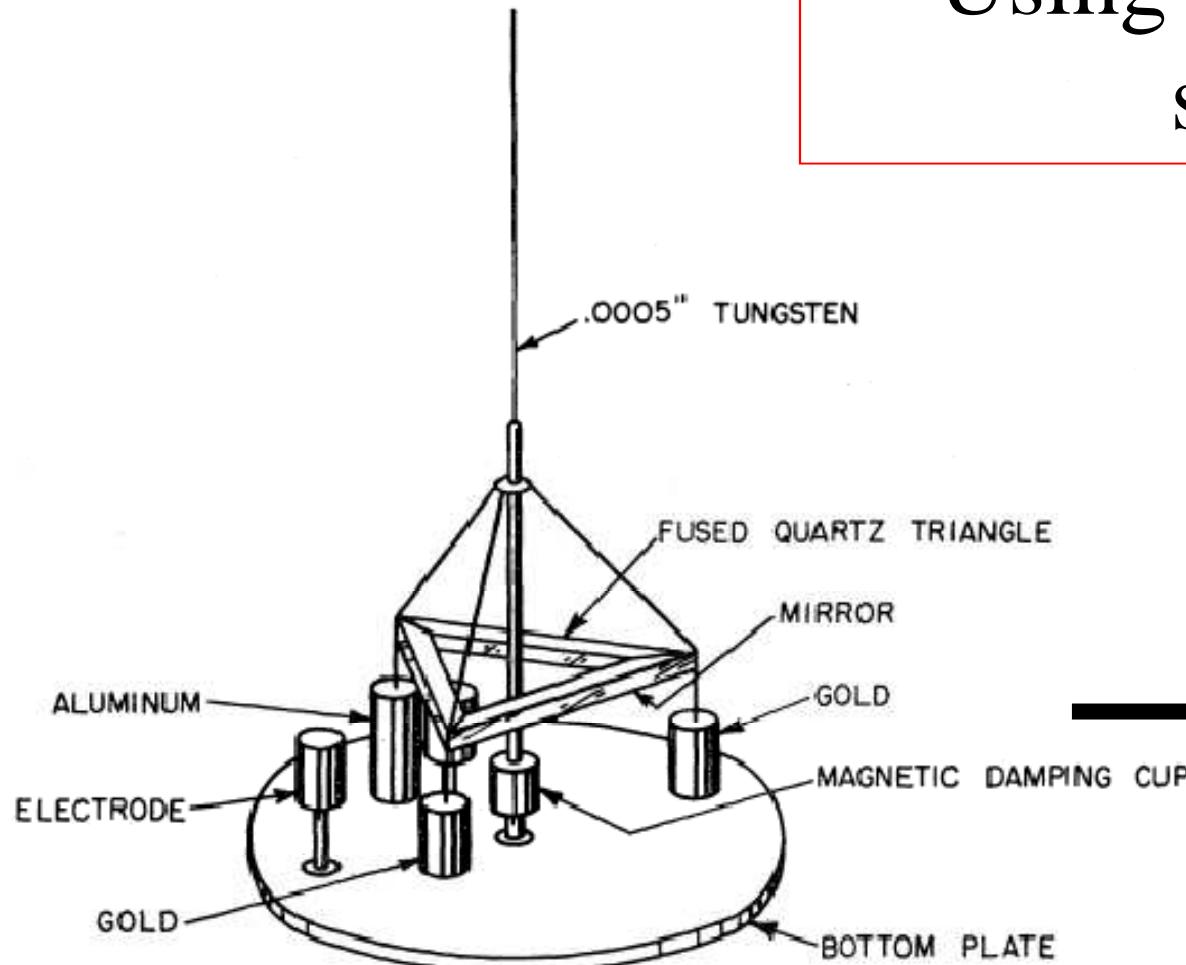
Difference in plumb lines produces a torque on the beam.

-> twist in the fiber

Eötvös (1922) $\eta \approx 5 \times 10^{-9}$

Dicke's idea

Using the Sun as a
source



→ Sun

$$\eta \approx 1 \times 10^{-11}$$

Historical overview

$$\eta = \frac{|a_1 - a_2|}{\frac{1}{2}(a_1 + a_2)}$$

year

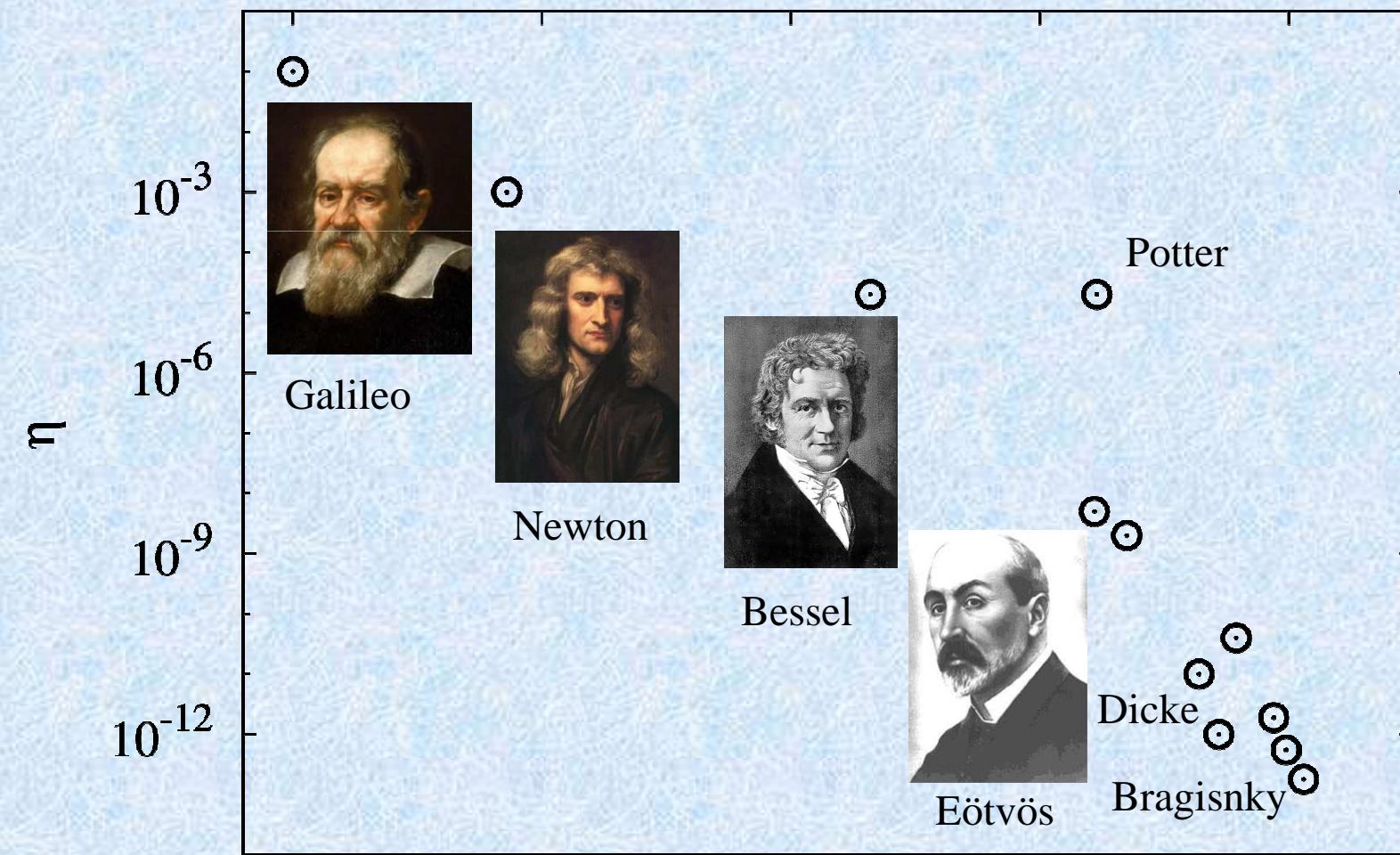
1600

1700

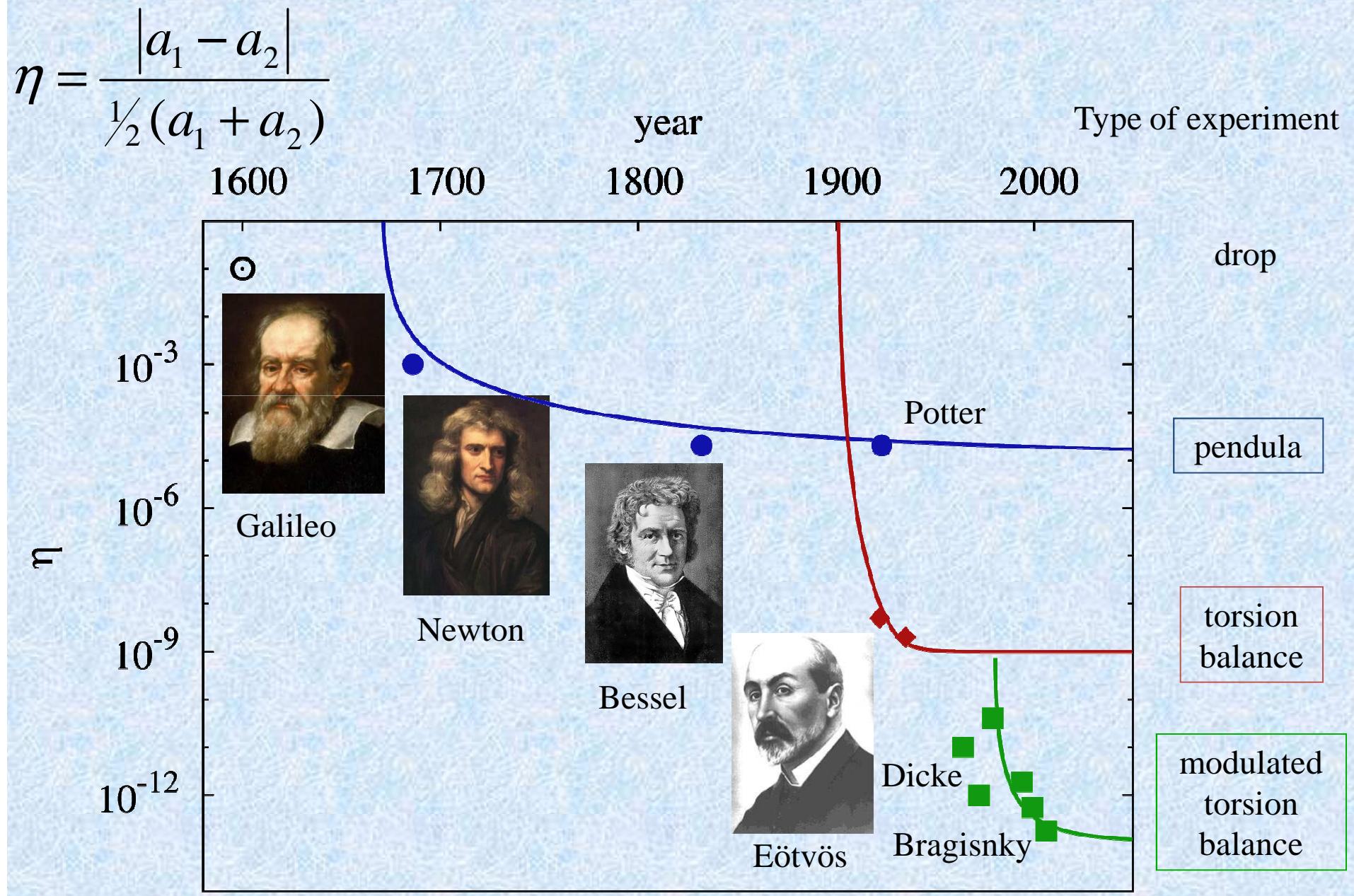
1800

1900

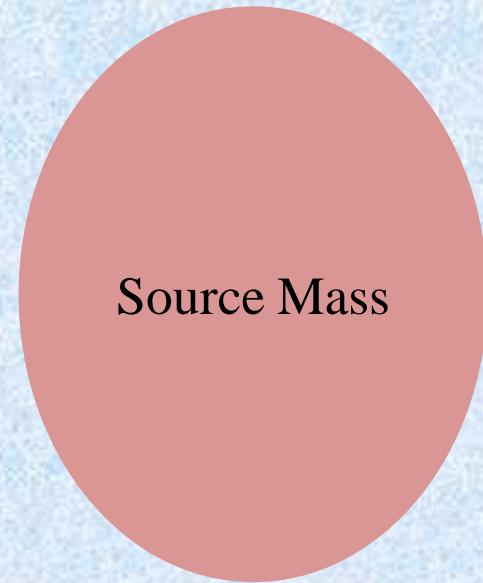
2000



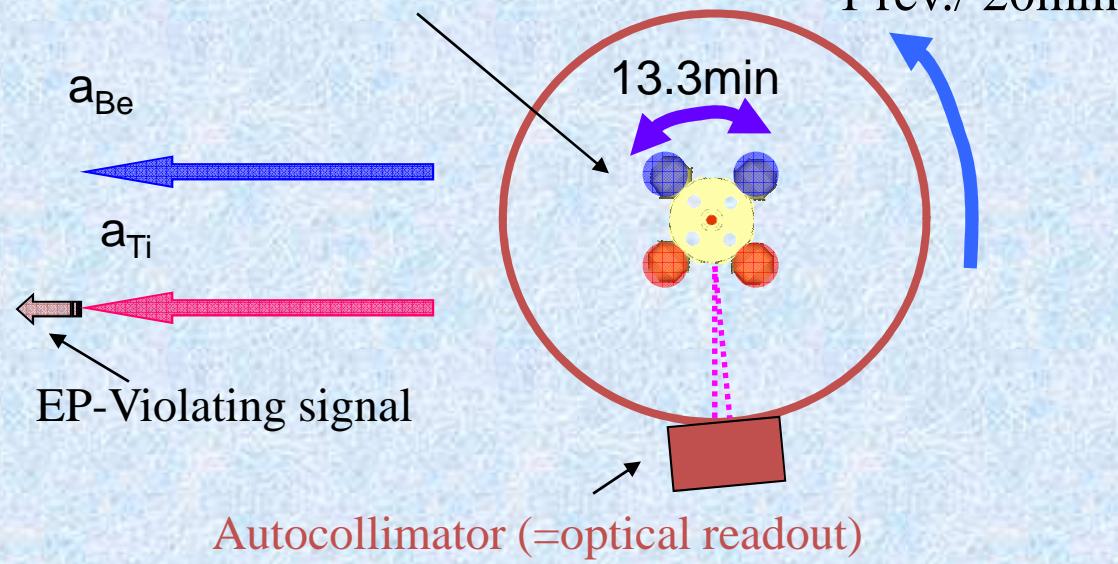
Historical overview



Principle of our experiment

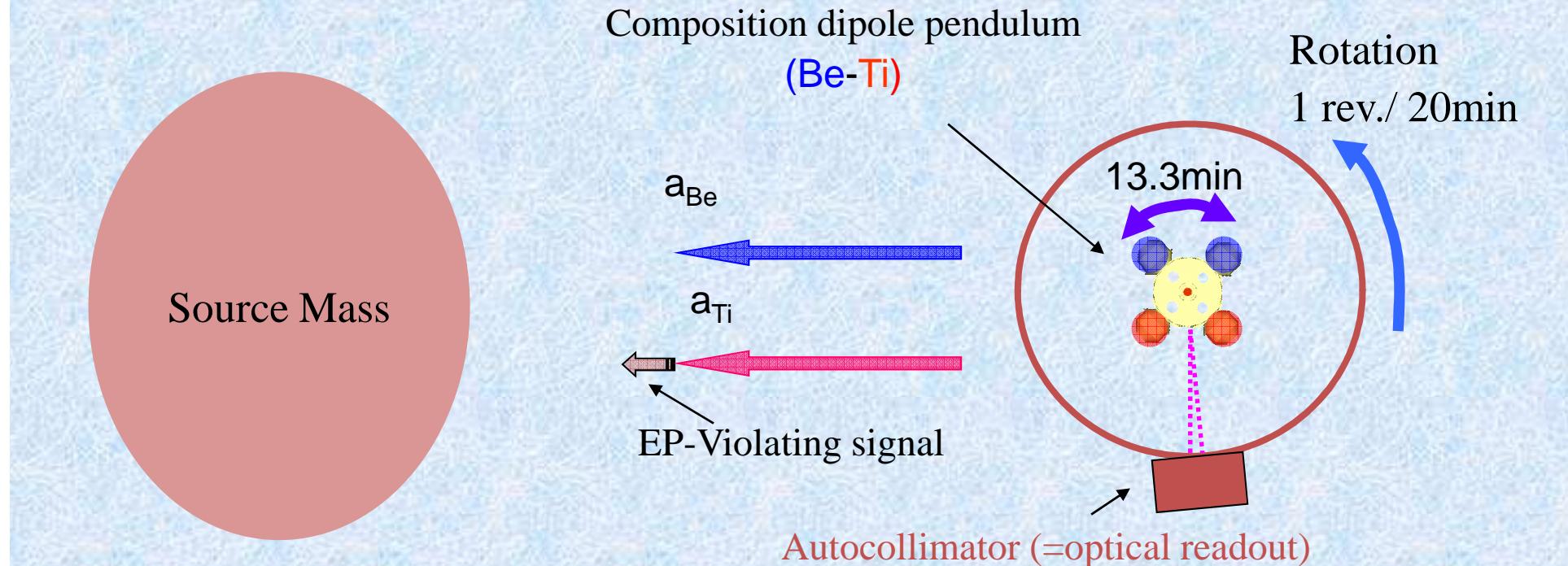


Composition dipole pendulum
(Be-Ti)

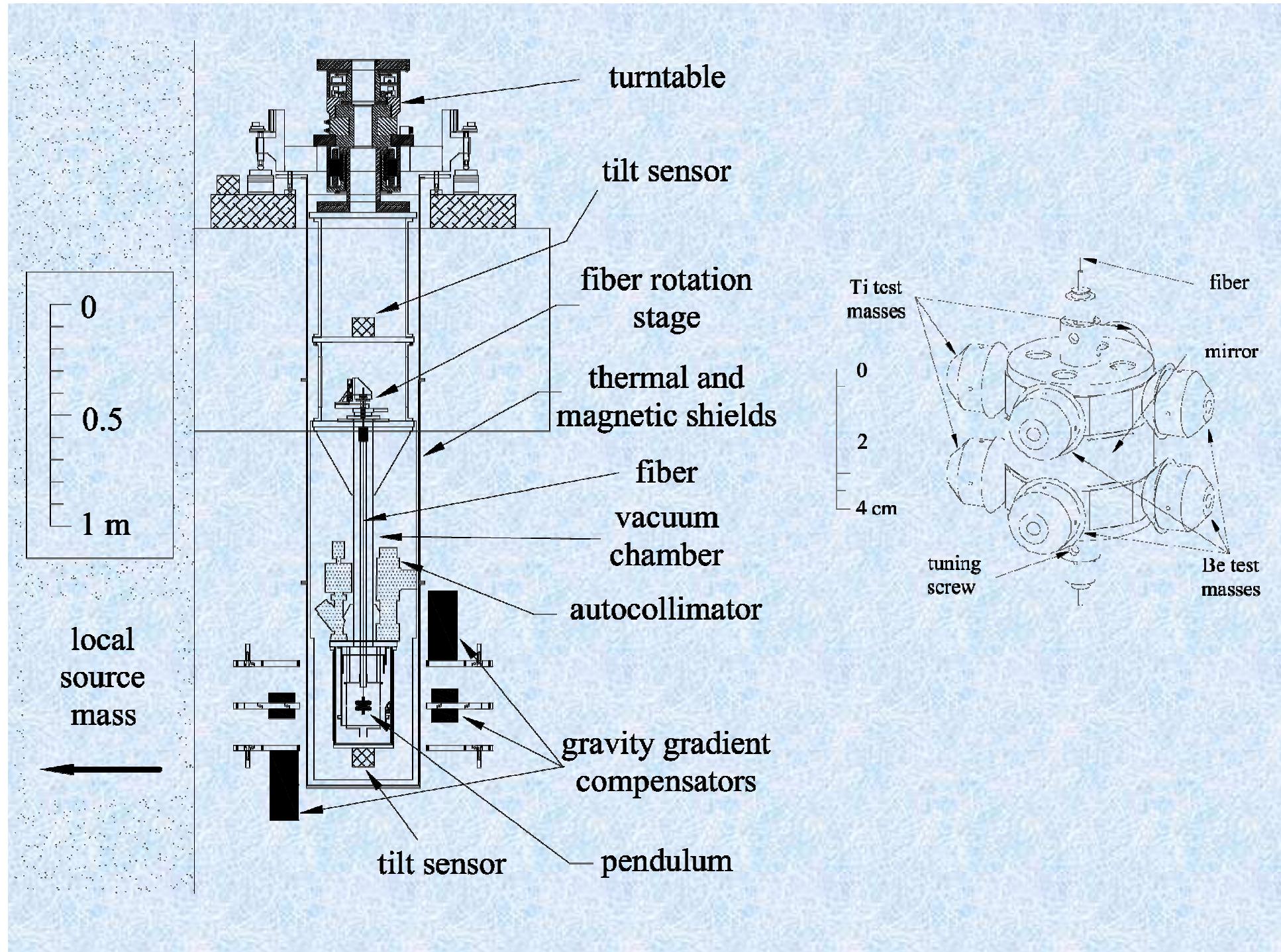


Rotation
1 rev./ 20min

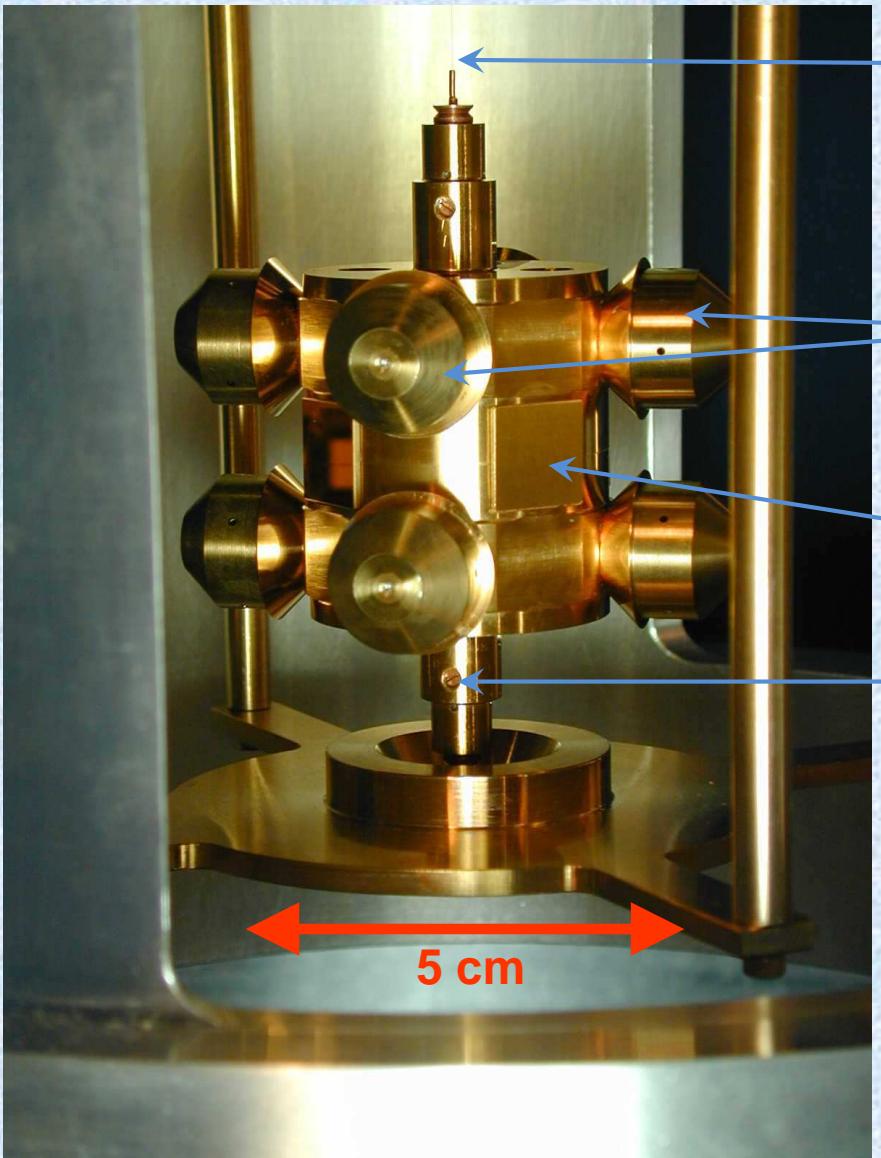
Principle of our experiment



source mass	λ (m)	horizontal acc.	acc. (ms^{-2})
local masses (hill)	1 - 10^4	$< 7 \times 10^{-5}$	Northwest
entire earth	10^6 - 10^7	1.7×10^{-3}	North
Sun	10^{11} - ∞	5.9×10^{-3}	modulated
Milky Way (incl. DM)	10^{20} - ∞	1.9×10^{-10}	modulated



The torsion pendulum



20 μm diameter tungsten fiber
(length: 108 cm)
 $\kappa=2.36 \text{ nNm}$

8 test masses (4 Be & 4 Ti)
4.84 g each (within 0.1 mg)
(can be interchanged)

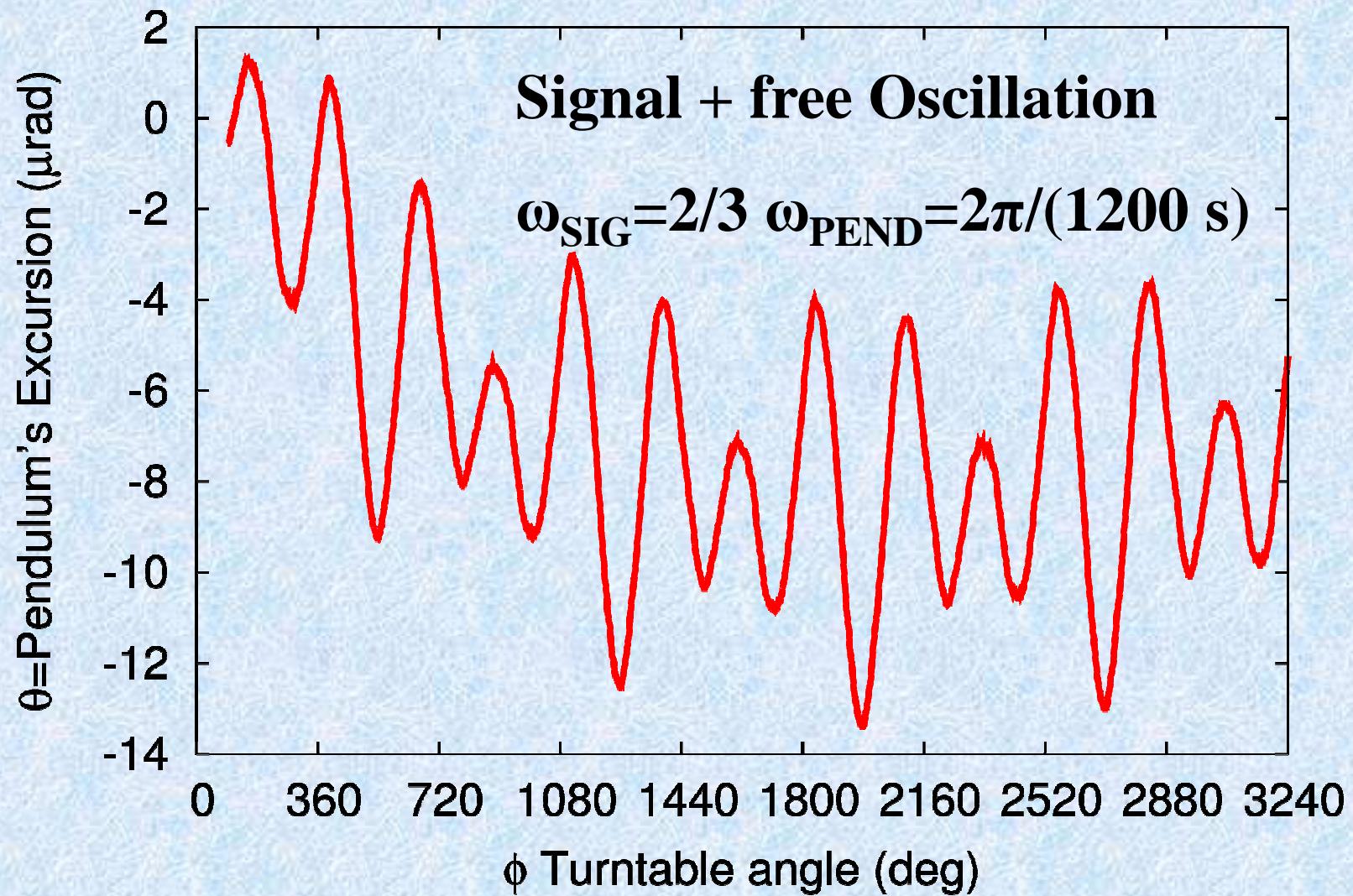
4 mirrors

tuning screws for adjusting
tiny asymmetries

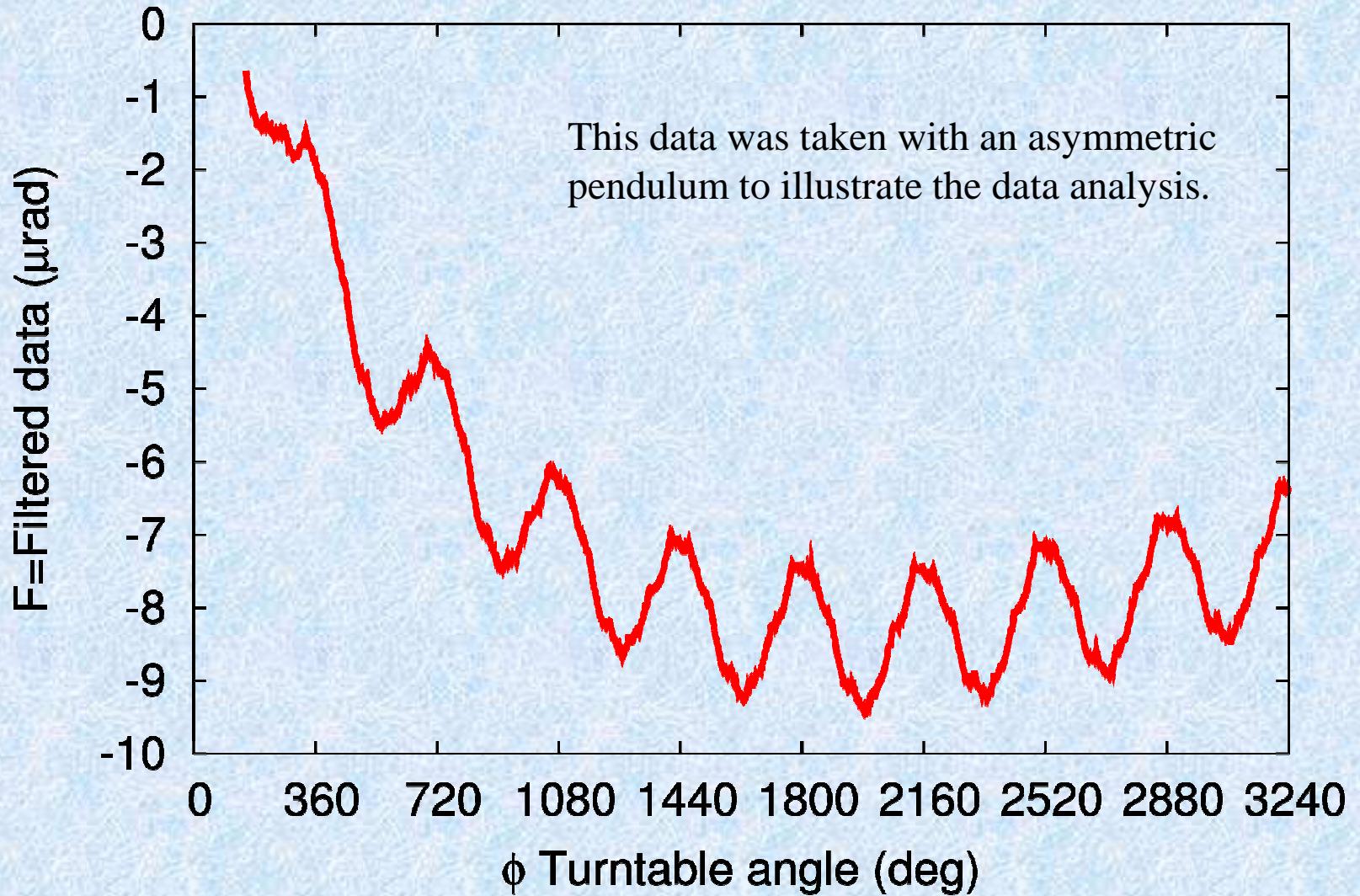
Data:

torsional period:	800 s
quality factor:	4000
decay time:	11d 19 hrs
machining tolerance:	5 μm
total mass :	70 g

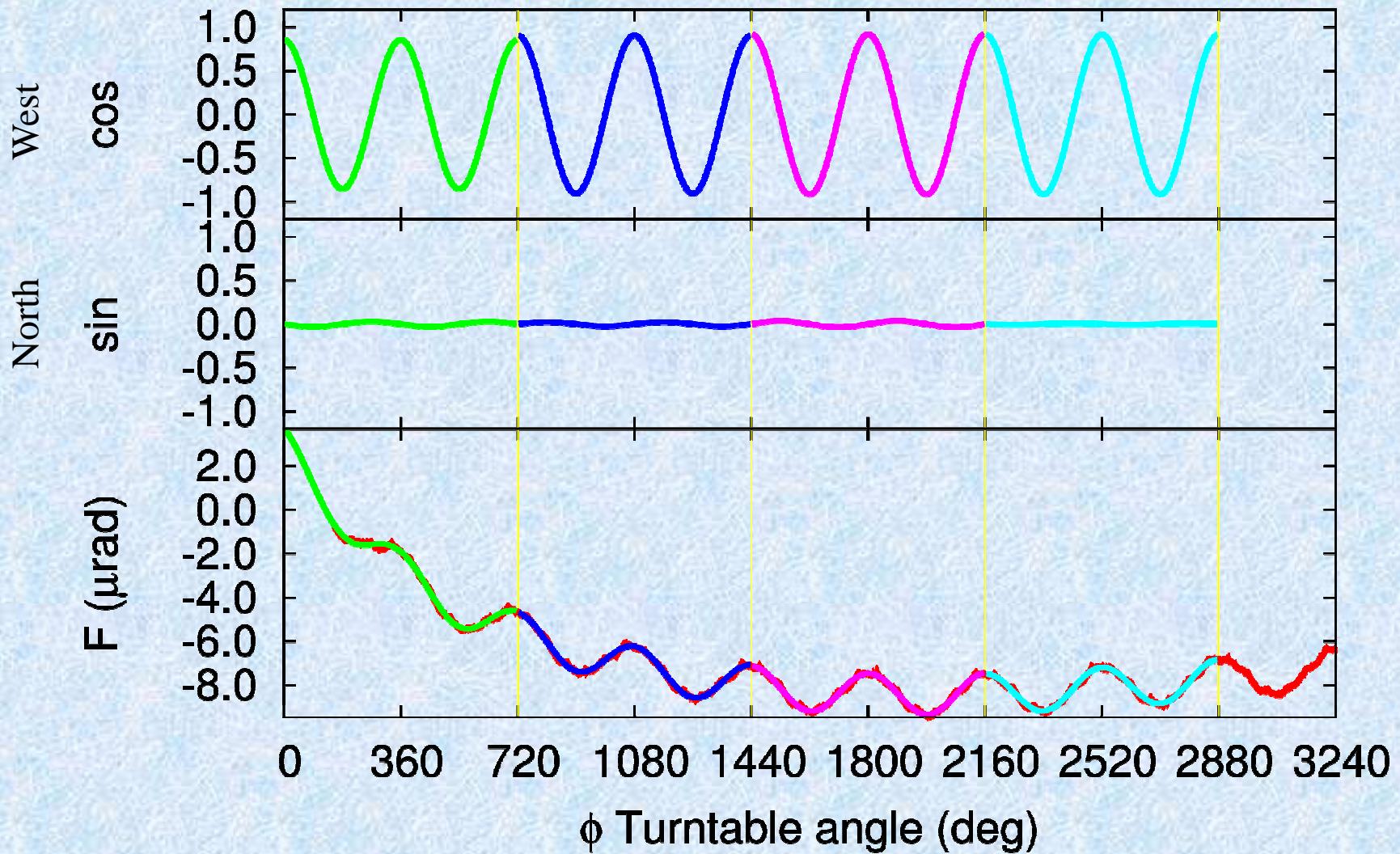
Raw data



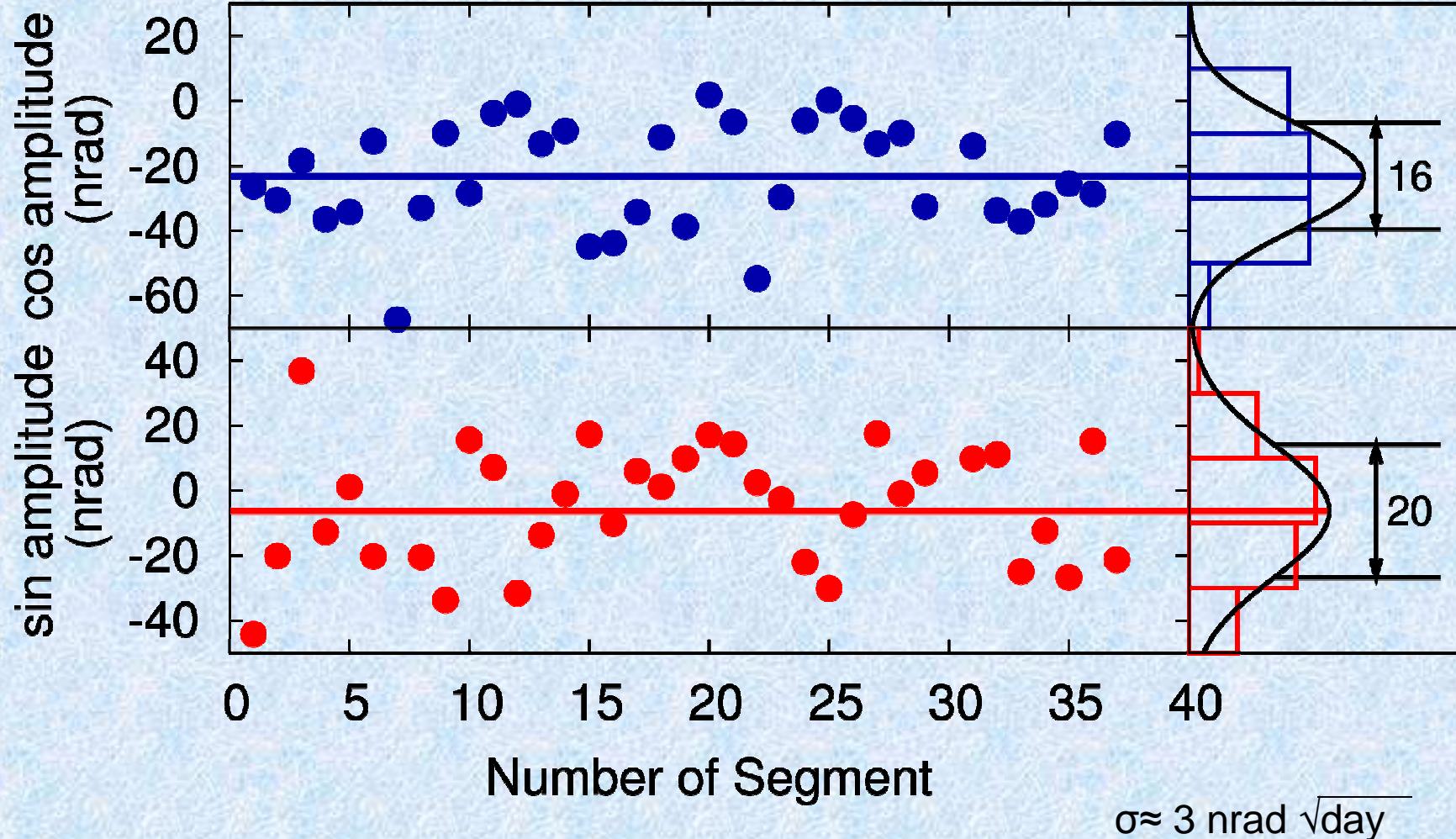
$$\text{Filtered } F(t) = \Theta(t - T/4) + \Theta(t + T/4)$$



Segmented & fitted

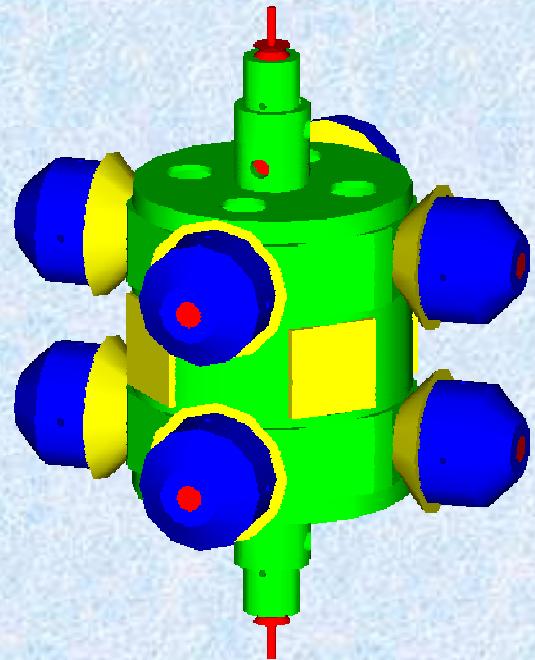


A day of data



$$\sigma \approx 3 \text{ nrad} \sqrt{\text{day}}$$

Conversion of angle to differential acceleration



$$6.41 \times 10^{-15} \text{ m/s}^2 / \text{nrad}$$

$$\Delta a = \frac{\kappa}{4 md} \varphi$$

Can be measured with
an uncertainty of
3 nrad per day

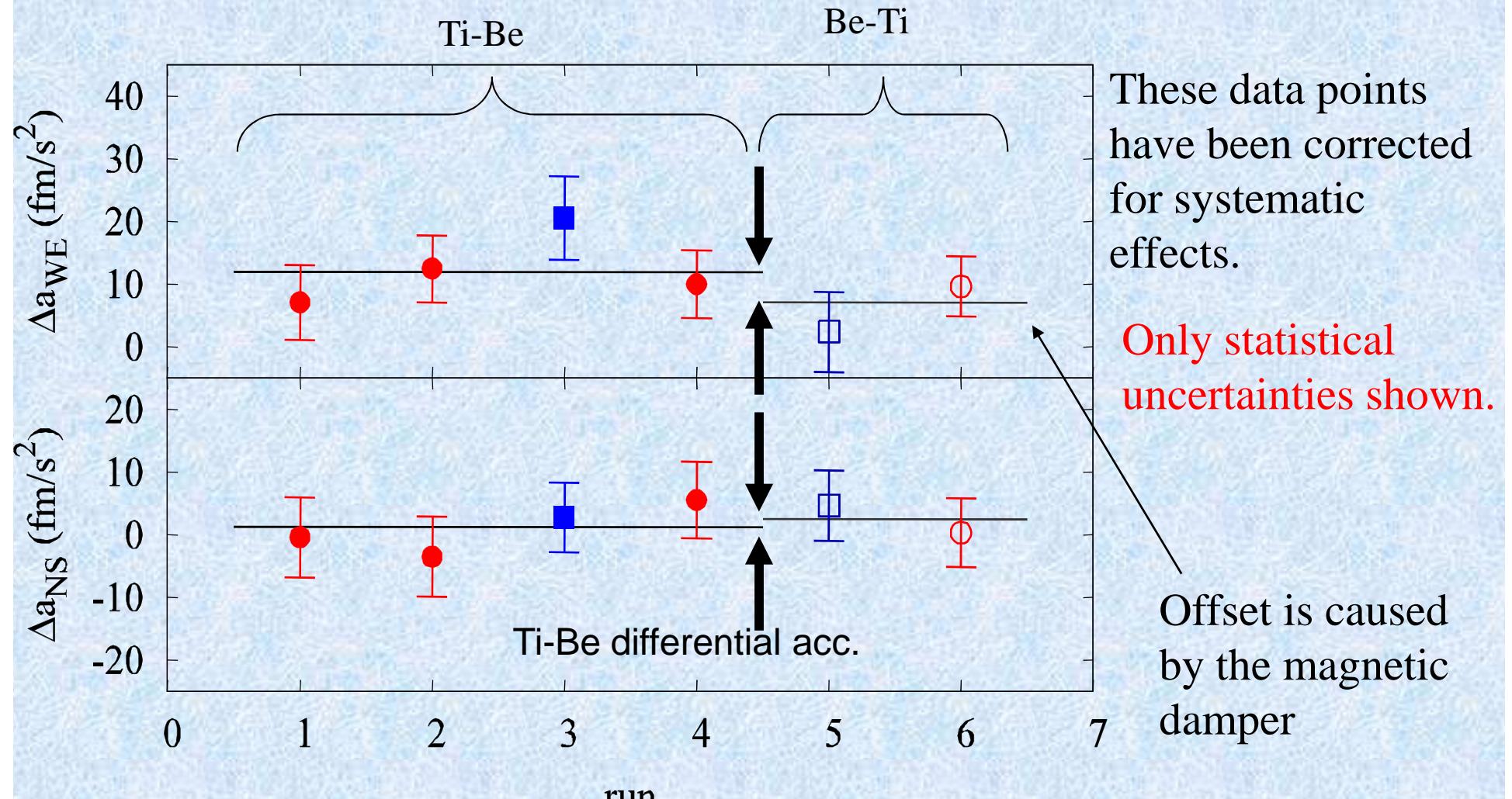


Δa can be measured to
20 fm/s²

κ	$2.36 \times 10^{-9} \text{ Nm}$
m	$4.84 \times 10^{-3} \text{ kg}$
d	$1.9 \times 10^{-2} \text{ m}$

Data taking sequence

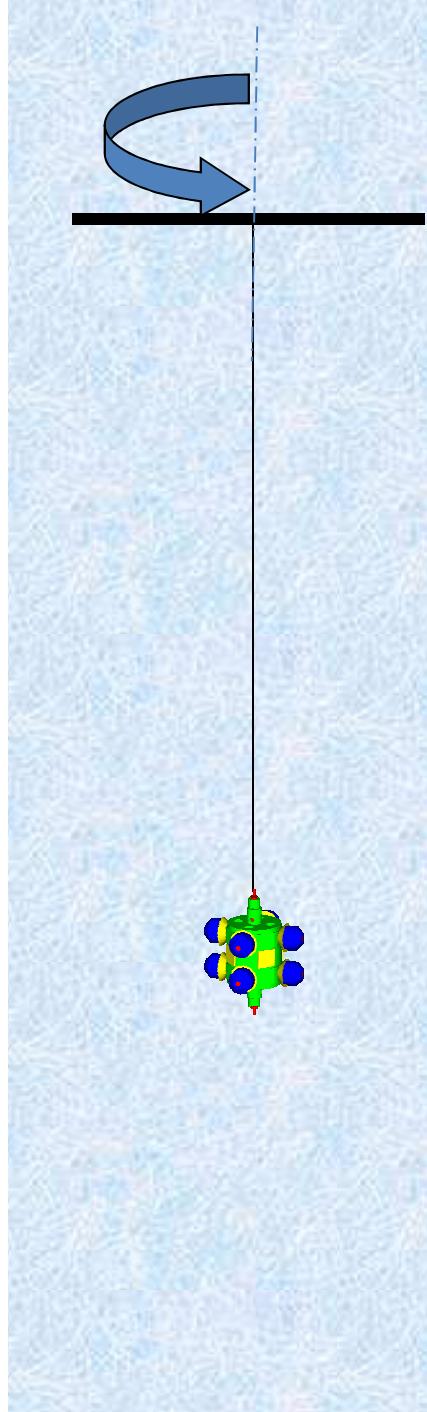
After a 2 months of data taking and systematic checks we physically invert the dipole on the pendulum and put it back into the apparatus.



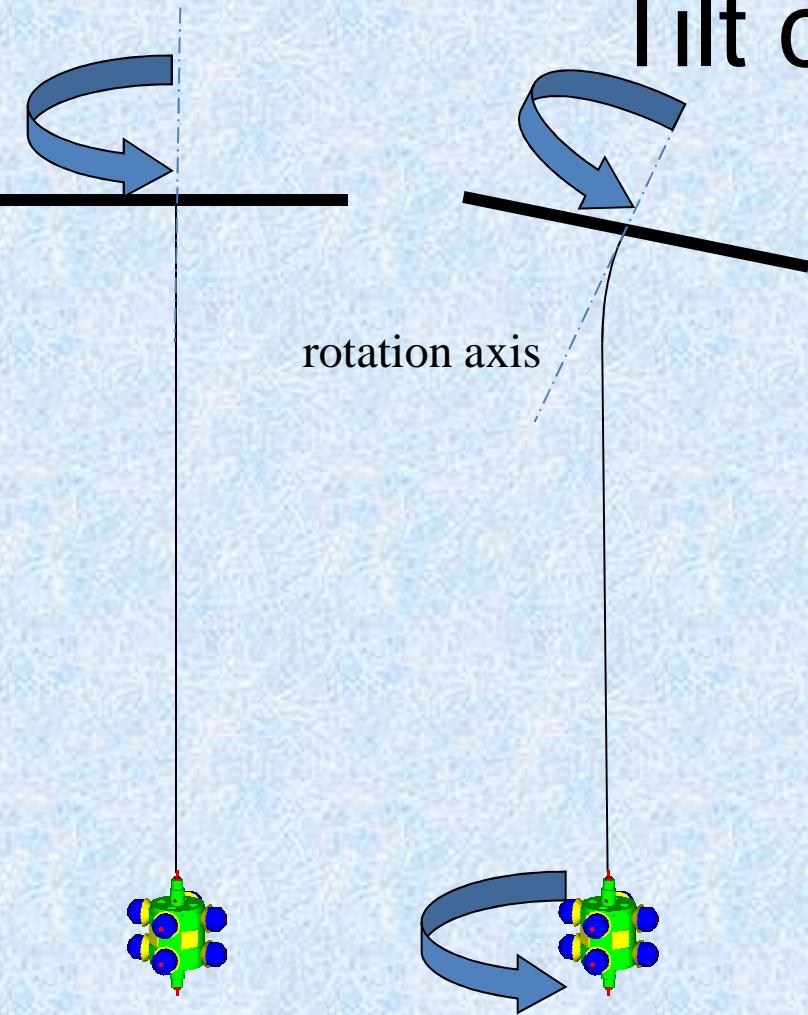
Corrected result

	$\Delta a_{N,Be-Ti}$ (10^{-15} ms^{-2})	$\Delta a_{W,Be-Ti}$ (10^{-15} ms^{-2})
measured	3.3 ± 2.5	-2.4 ± 2.4
gravity gradients	1.6 ± 0.2	0.3 ± 1.7
tilt	1.2 ± 0.6	-0.2 ± 0.7
temperature gradients	0 ± 1.7	0 ± 1.7
magnetic coupling	0 ± 0.3	0 ± 0.3
corrected result	0.6 ± 3.1	-2.5 ± 3.5

Tilt coupling

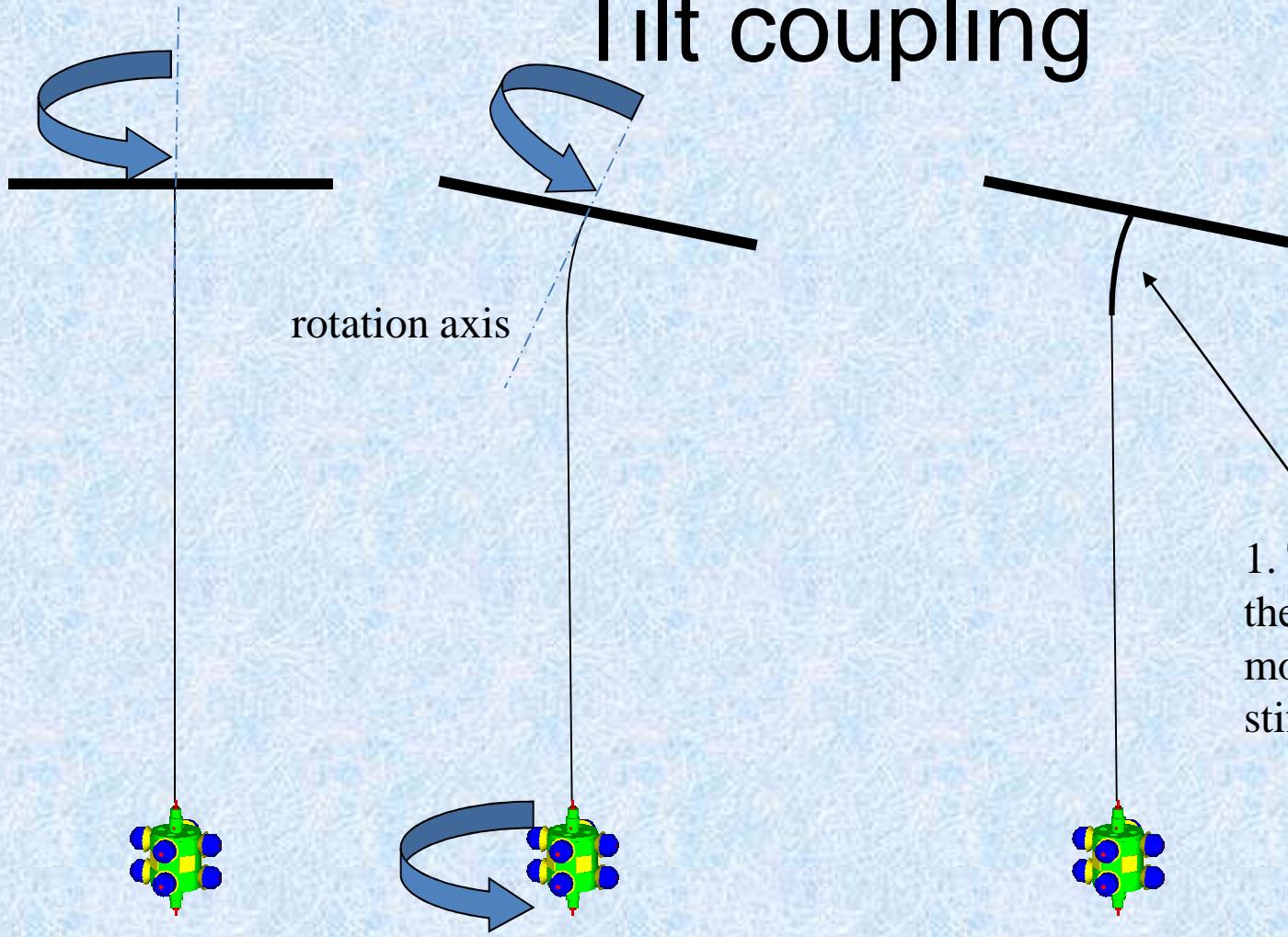


Tilt coupling



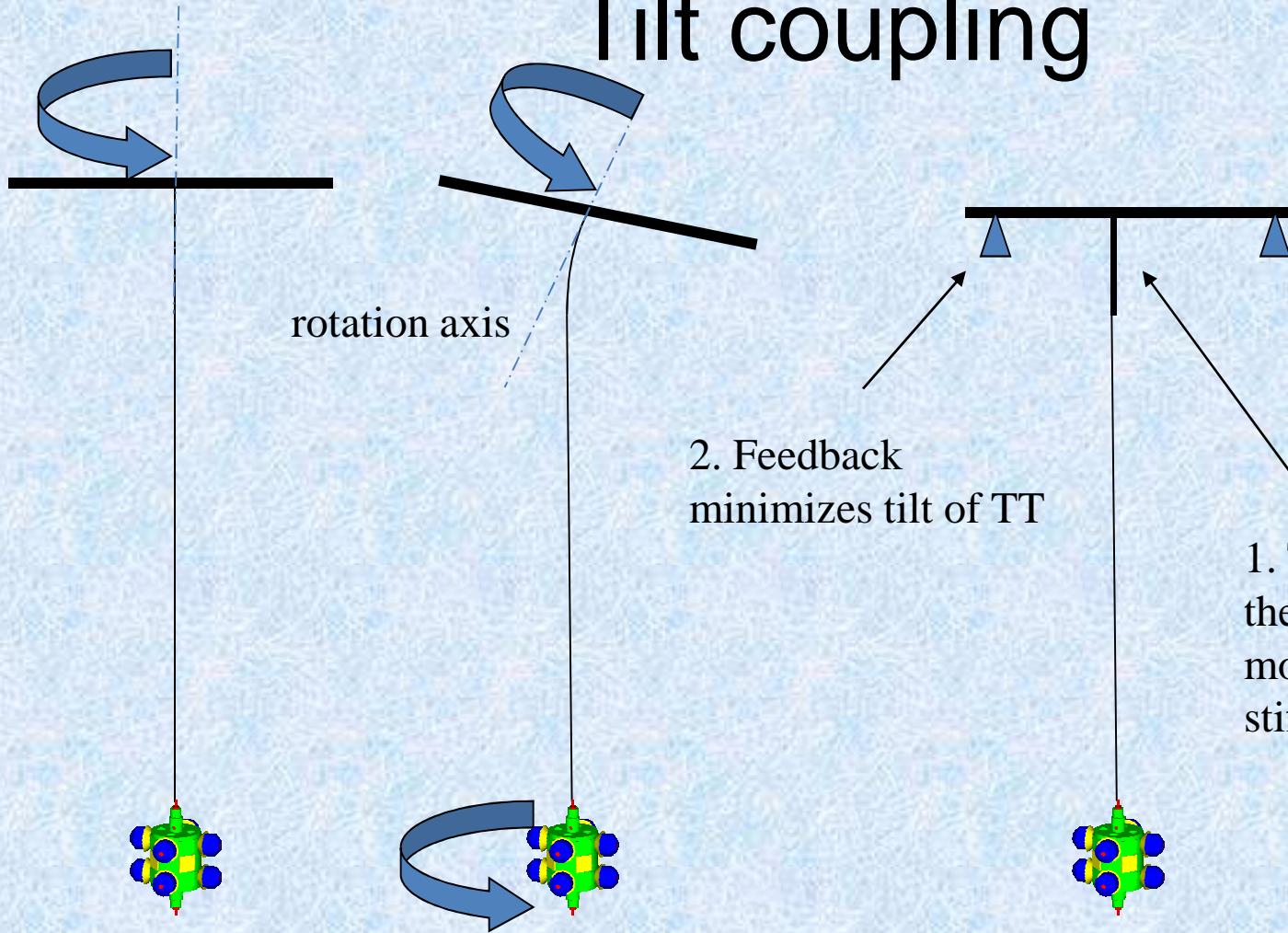
Tilt of the suspension point
+ anisotropies of the fiber
→ will rotate

Tilt coupling



1. Thicker fiber at the top provides more torsional stiffness

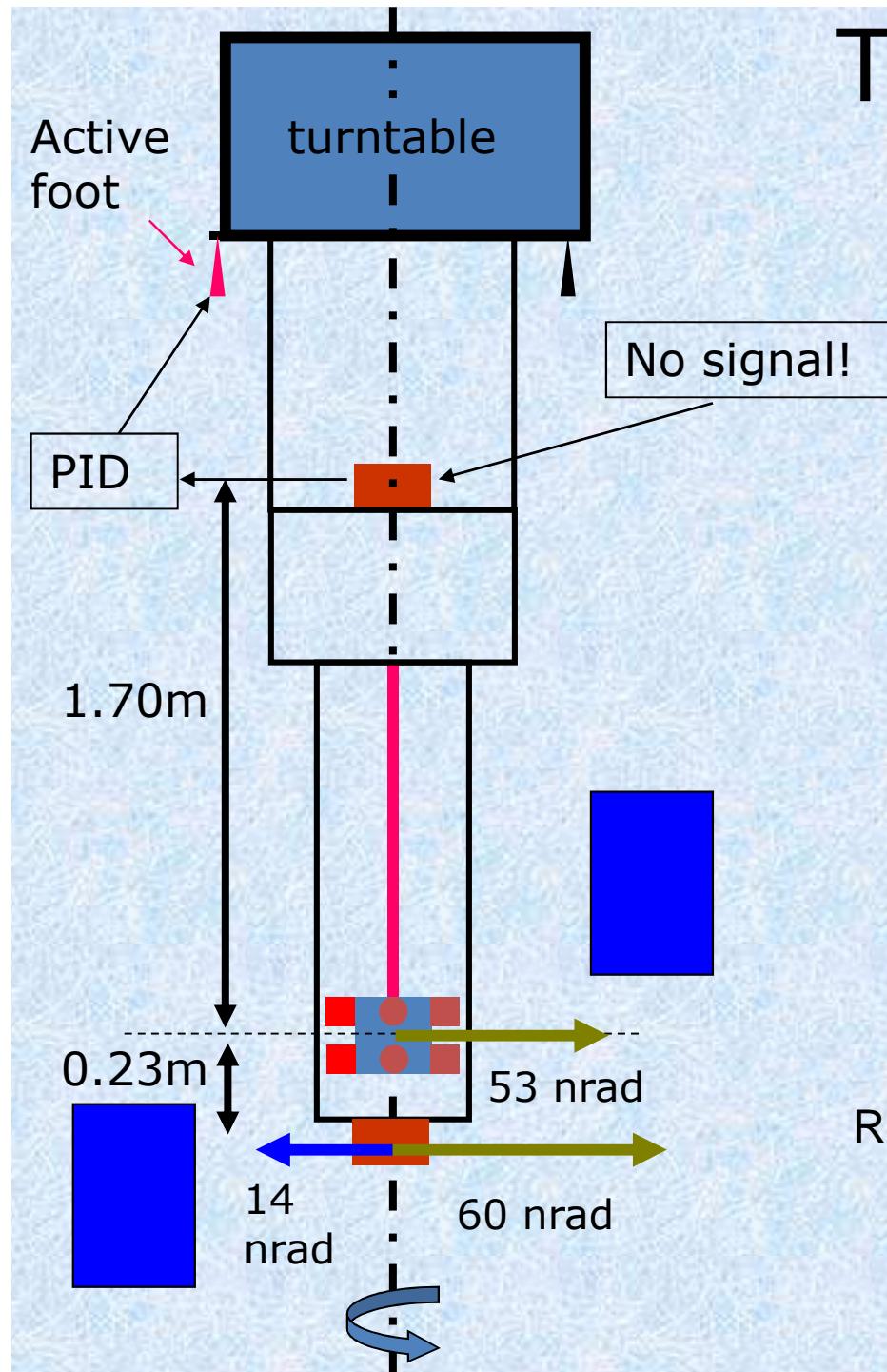
Tilt coupling



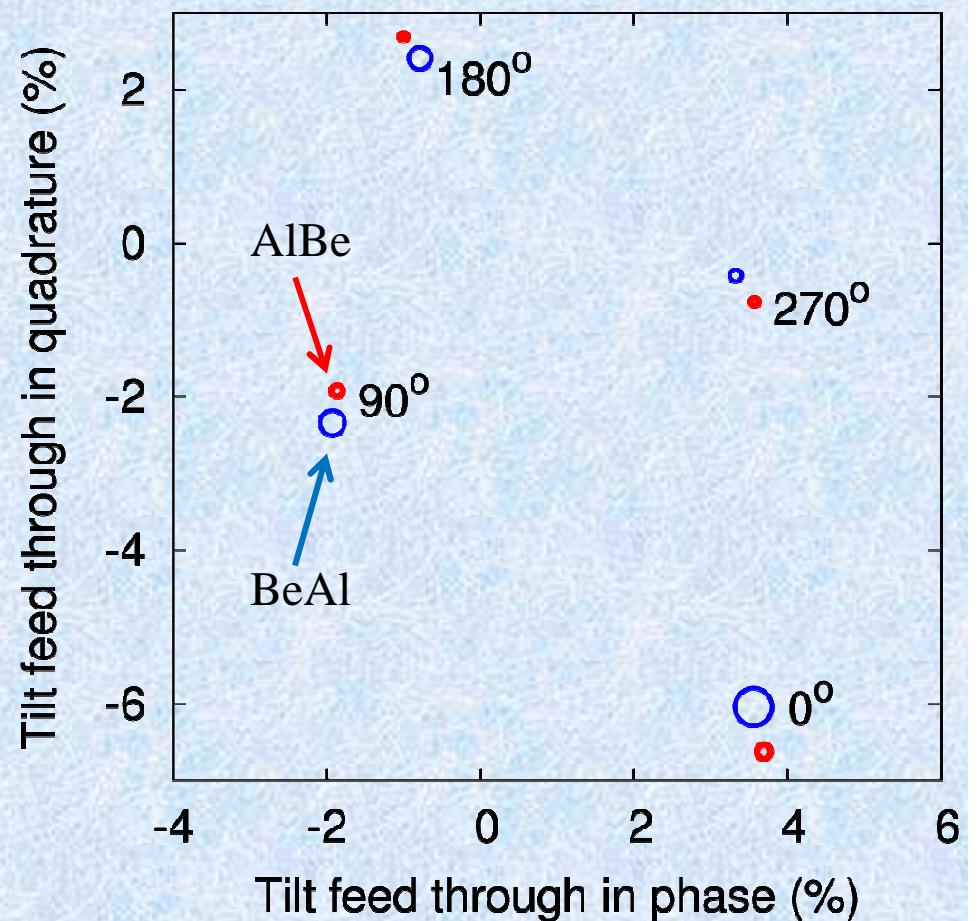
2. Feedback
minimizes tilt of TT

1. Thicker fiber at
the top provides
more torsional
stiffness

Tilt of the suspension point
+ anisotropies of the fiber
→ will rotate



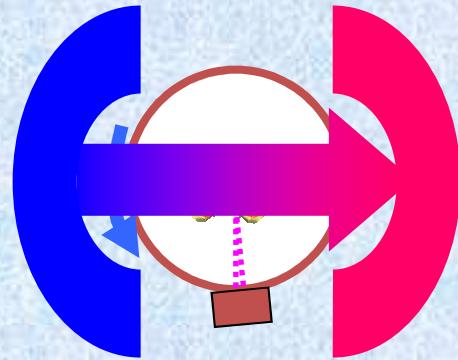
The tilt matrix



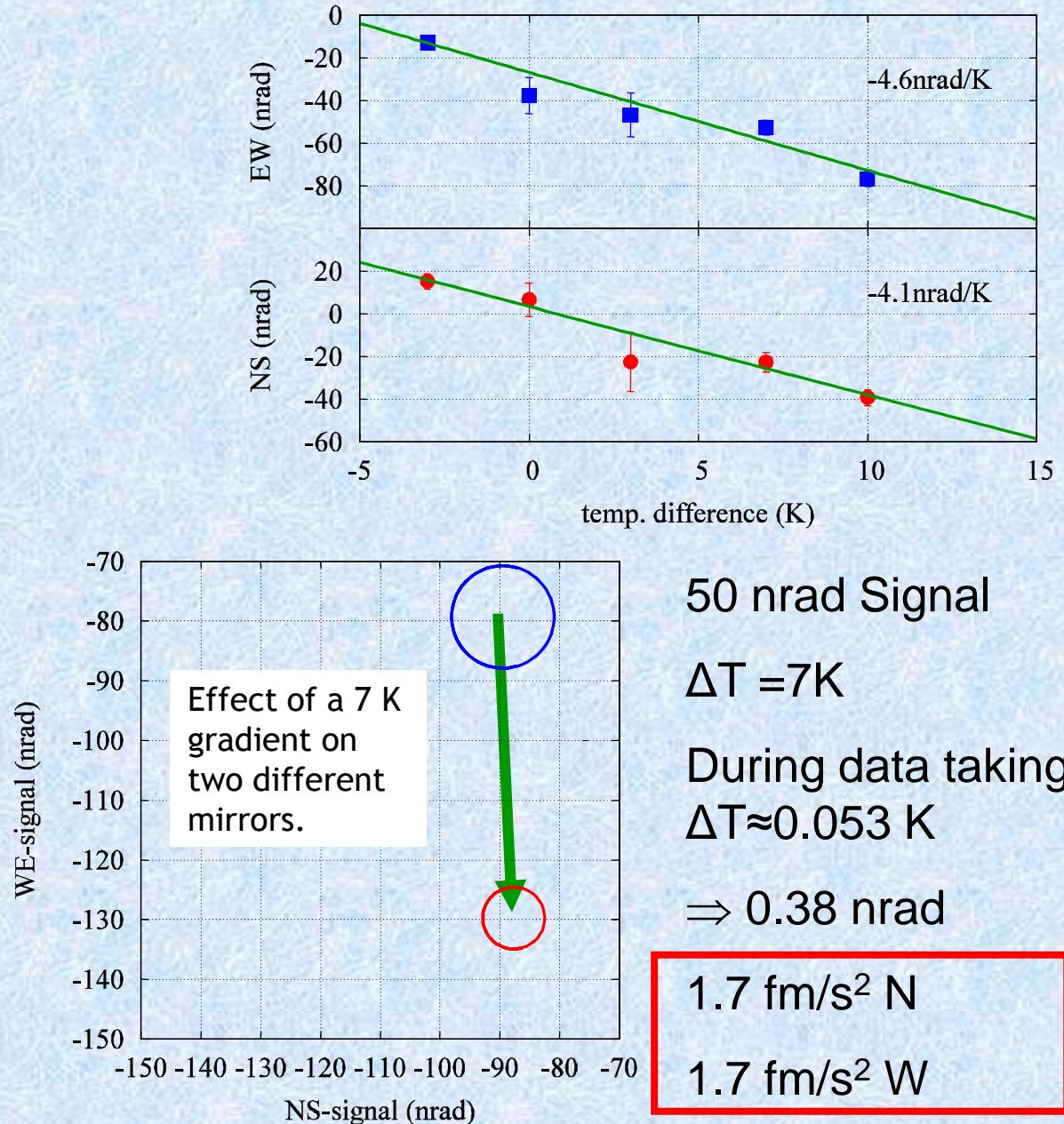
Remaining tilt uncertainty:

0.6 fm/s² N
0.7 fm/s² W

Thermal



Effect on the applied gradient on the signal (measurement was done on one mirror):



Results

		Δa (10^{-15} ms $^{-2}$)	
$a_N(Be)$	-	$a_N(Ti)$	0.6 ± 3.1
$a_W(Be)$	-	$a_W(Ti)$	-2.5 ± 3.5
$a_N(Be)$	-	$a_N(Al)$	-2.6 ± 2.5
$a_W(Be)$	-	$a_W(Al)$	0.7 ± 2.5
$a_{Sun}(Be)$	-	$a_{Sun}(Ti)$	-1.8 ± 2.8
$a_{Sun}(Be)$	-	$a_{Sun}(Al)$	0.0 ± 2.5
$a_{Gal}(Be)$	-	$a_{Gal}(Ti)$	-2.1 ± 3.1
$a_{Gal}(Be)$	-	$a_{Gal}(Al)$	1.6 ± 2.8

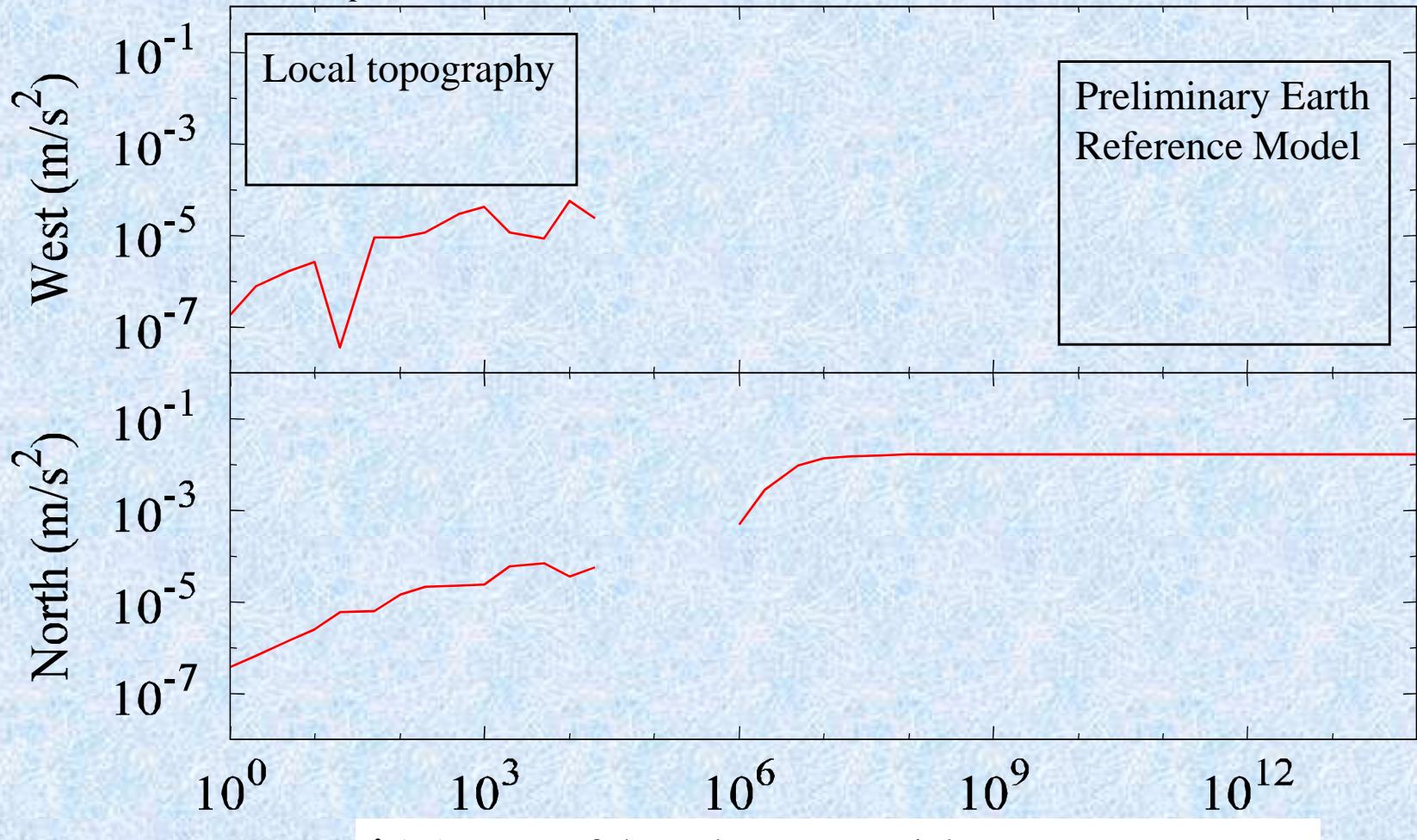
Results

		Δa (10^{-15} ms $^{-2}$)	η
$a_N(Be)$	-	$a_N(Ti)$	0.6 ± 3.1 (0.3 ± 1.8) $\times 10^{-13}$
$a_W(Be)$	-	$a_W(Ti)$	-2.5 ± 3.5
$a_N(Be)$	-	$a_N(Al)$	-2.6 ± 2.5 (-1.5 ± 1.5) $\times 10^{-13}$
$a_W(Be)$	-	$a_W(Al)$	0.7 ± 2.5
$a_{Sun}(Be)$	-	$a_{Sun}(Ti)$	-1.8 ± 2.8 (-3.1 ± 4.7) $\times 10^{-13}$
$a_{Sun}(Be)$	-	$a_{Sun}(Al)$	0.0 ± 2.5 (0.0 ± 4.2) $\times 10^{-13}$
$a_{Gal}(Be)$	-	$a_{Gal}(Ti)$	-2.1 ± 3.1 (-4.4 ± 6.5) $\times 10^{-5}$
$a_{Gal}(Be)$	-	$a_{Gal}(Al)$	1.6 ± 2.8 (3.4 ± 5.8) $\times 10^{-5}$

Source integration

$$\Delta \vec{a} = \alpha \Delta \left(\frac{q}{\mu} \right)_p \vec{I}$$

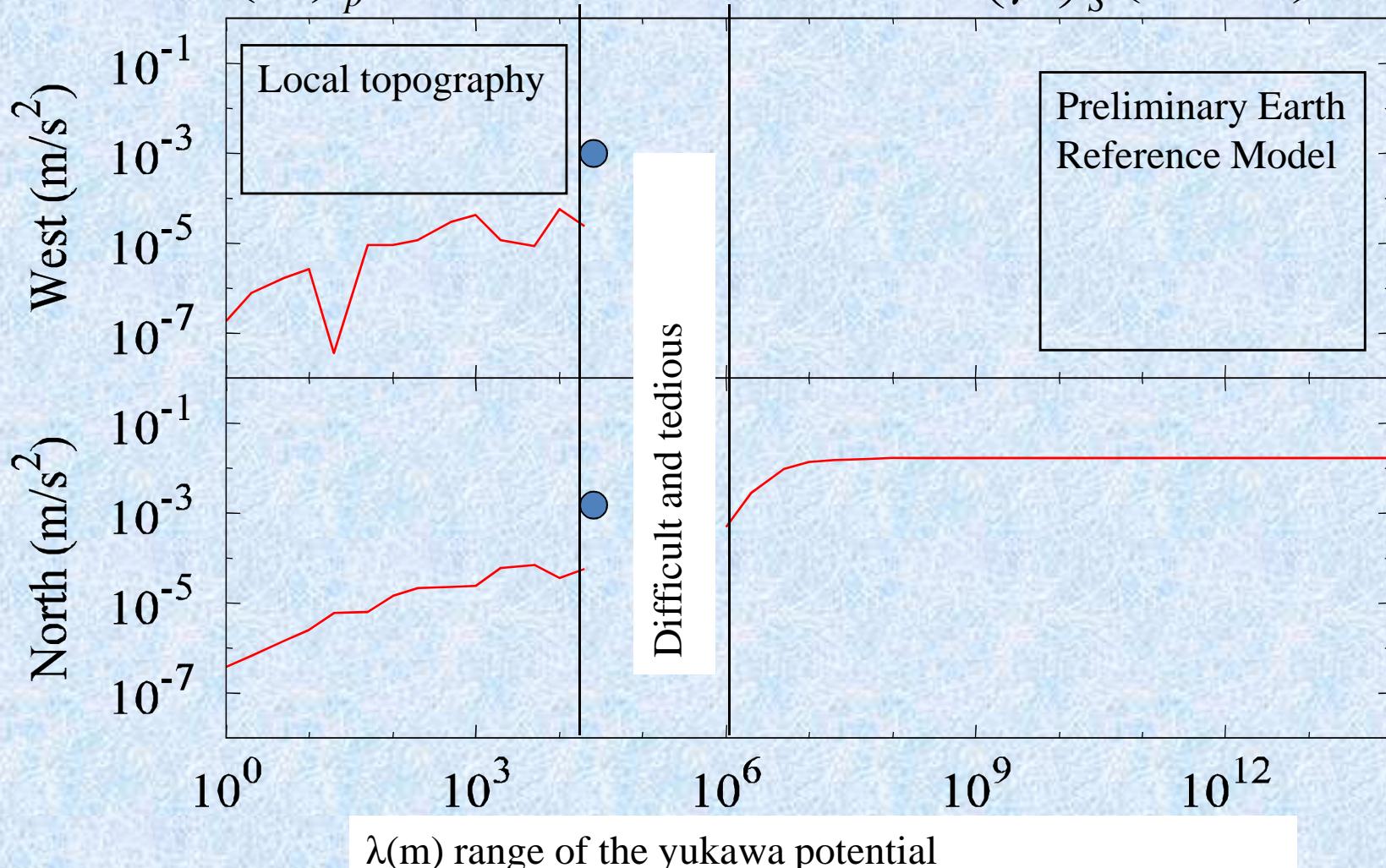
$$\vec{I} = G \int d^3 r' \rho(r') \left(\frac{q}{\mu} \right)_S \left(\frac{1}{r'} + \frac{1}{\lambda} \right) e^{-r'/\lambda} \frac{\hat{r}'}{r'}$$



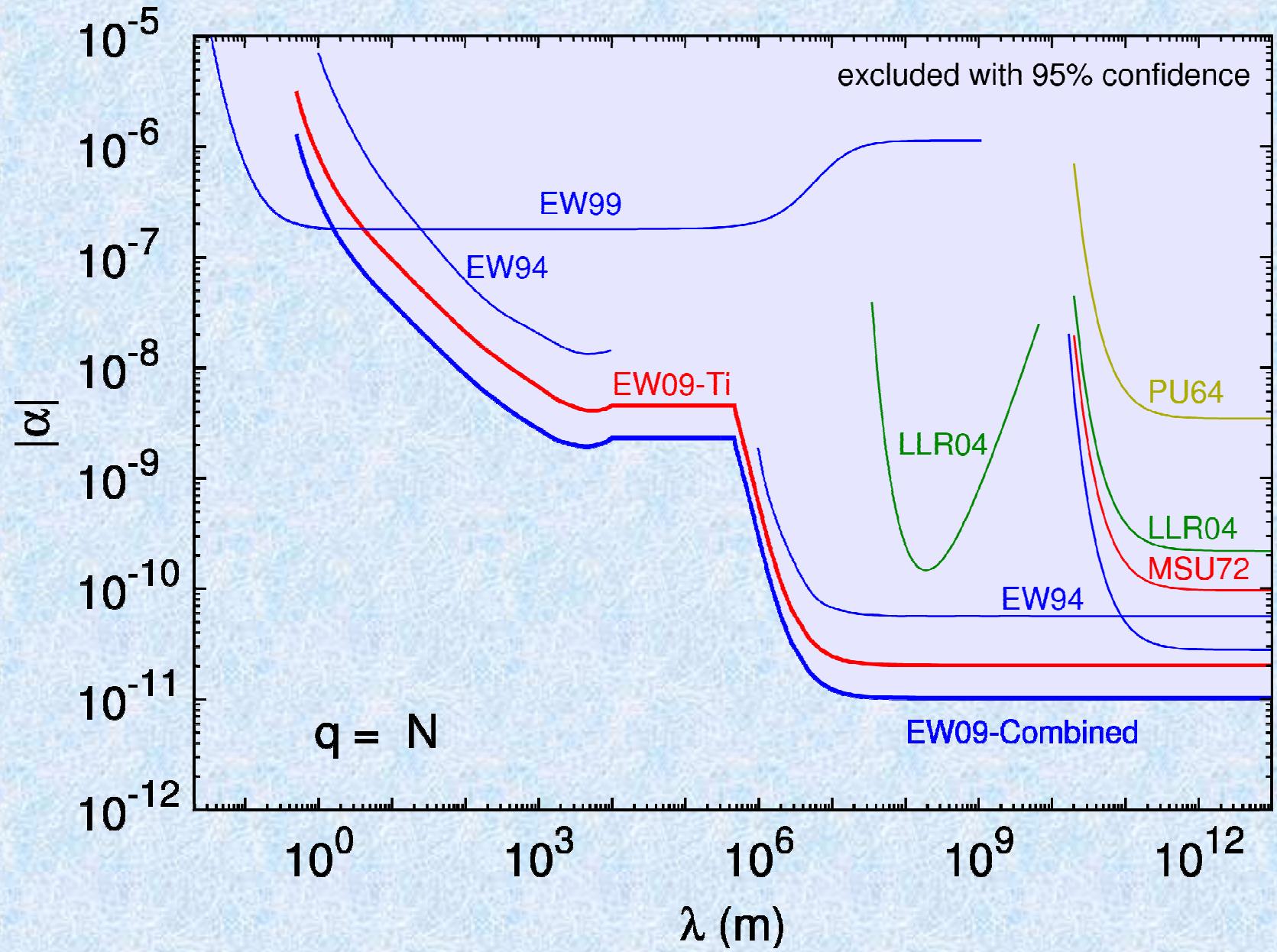
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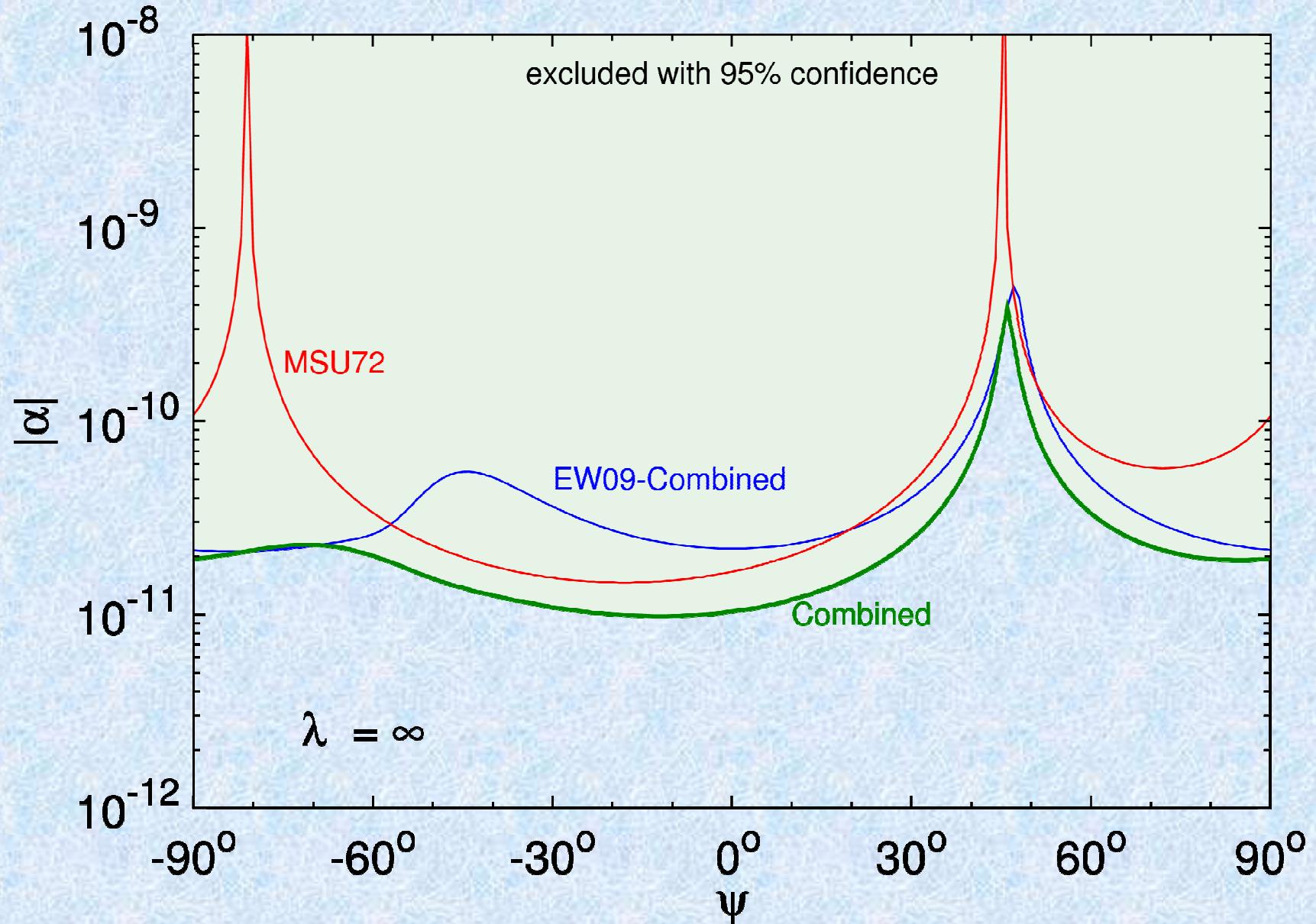
$$\vec{I} = G \int d^3 r' \rho(r') \left(\frac{q}{\mu} \right)_S \left(\frac{1}{r'} + \frac{1}{\lambda} \right) e^{-r'/\lambda} \frac{\hat{r}'}{r'}$$



α - λ plot for $q=N$ ($\psi=\pi/2$)

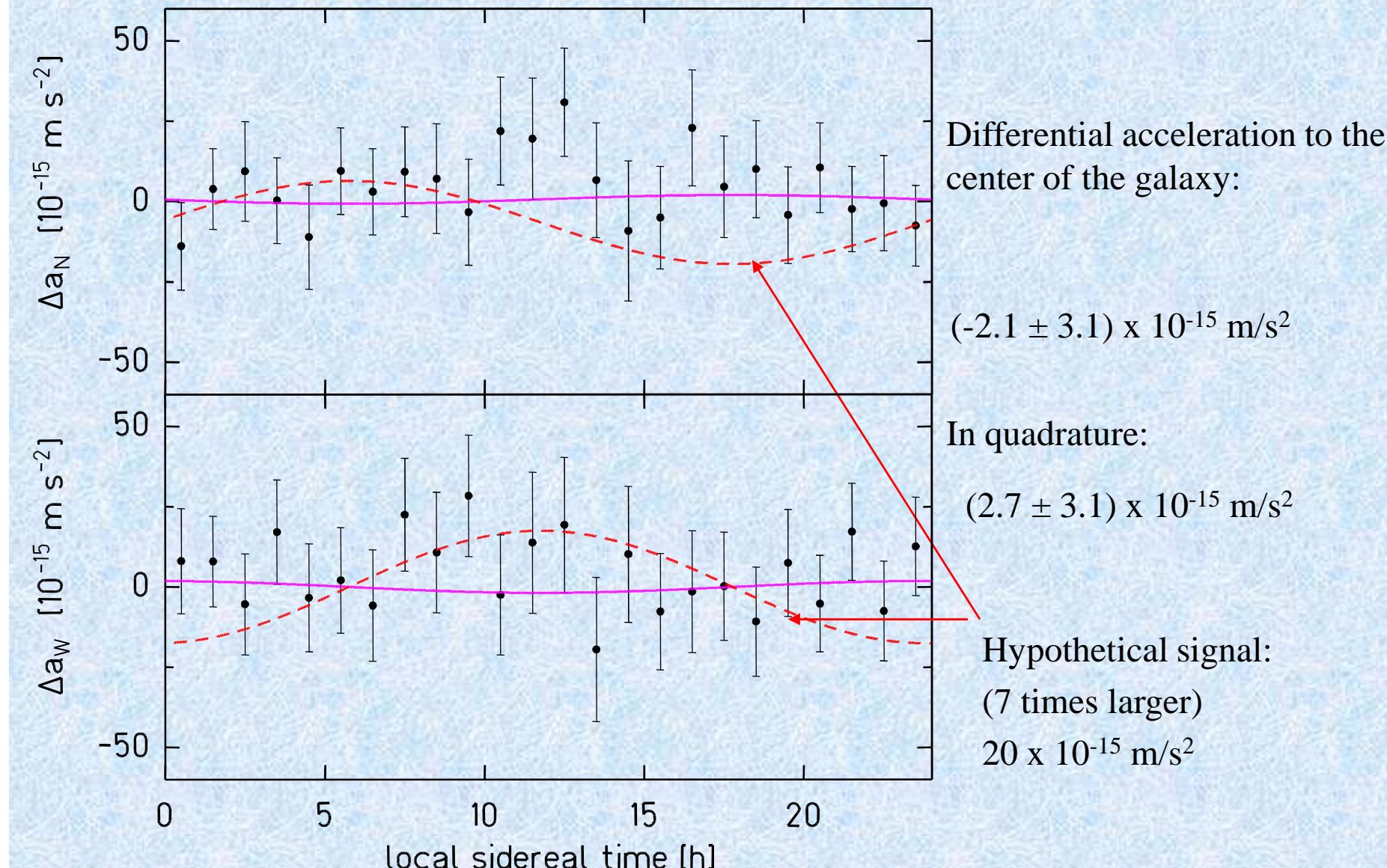


ψ - α plot for q=N (acc. towards the Sun)

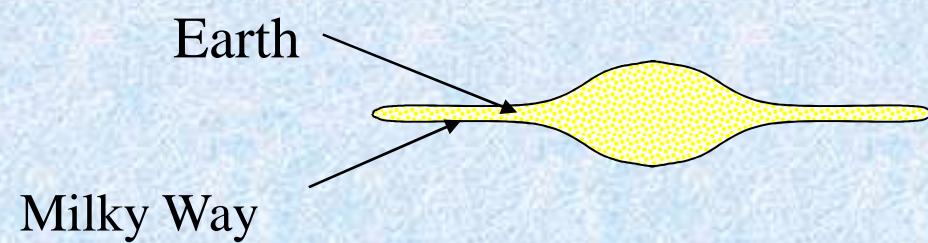


Acceleration to the center of our galaxy

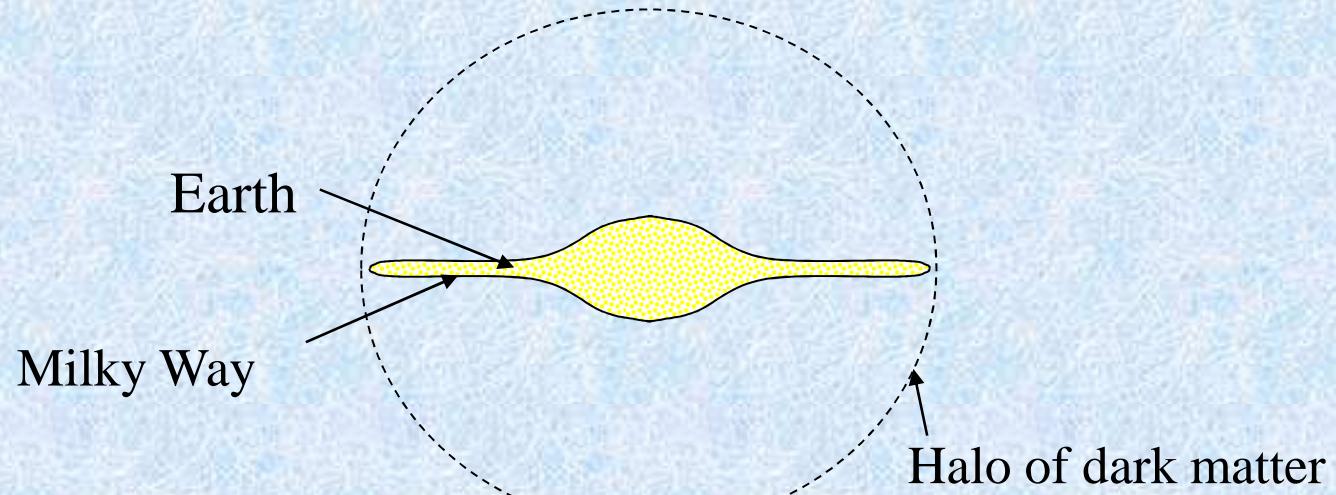
1825 h of data taken over 220 days



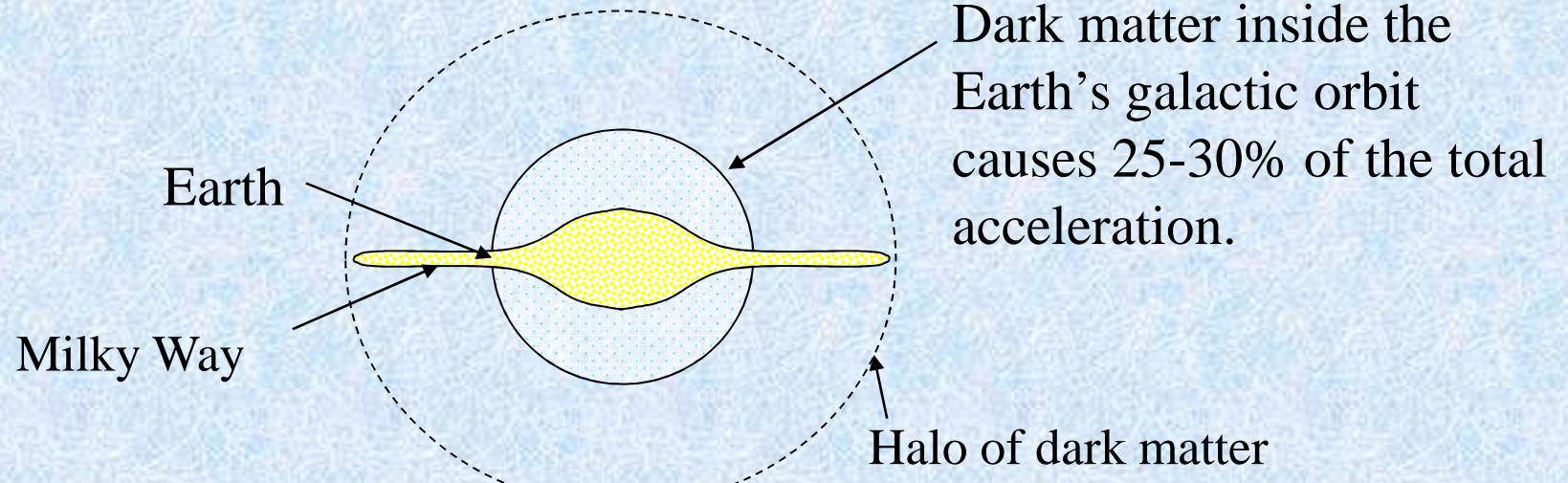
Galactic dark matter



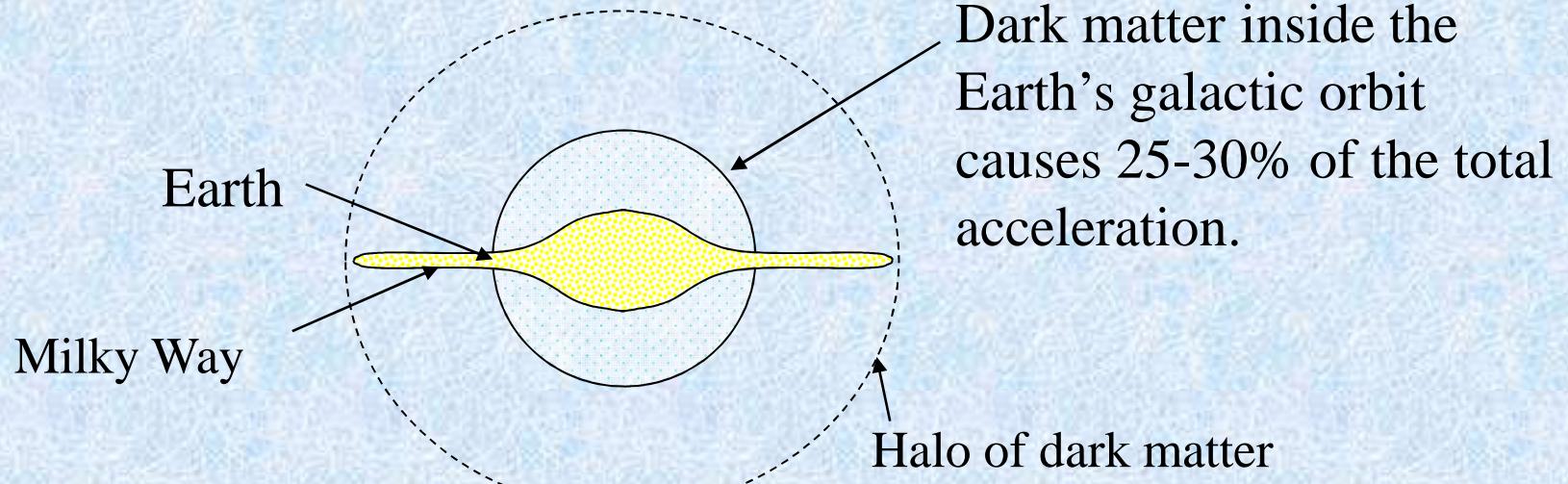
Galactic dark matter



Galactic dark matter



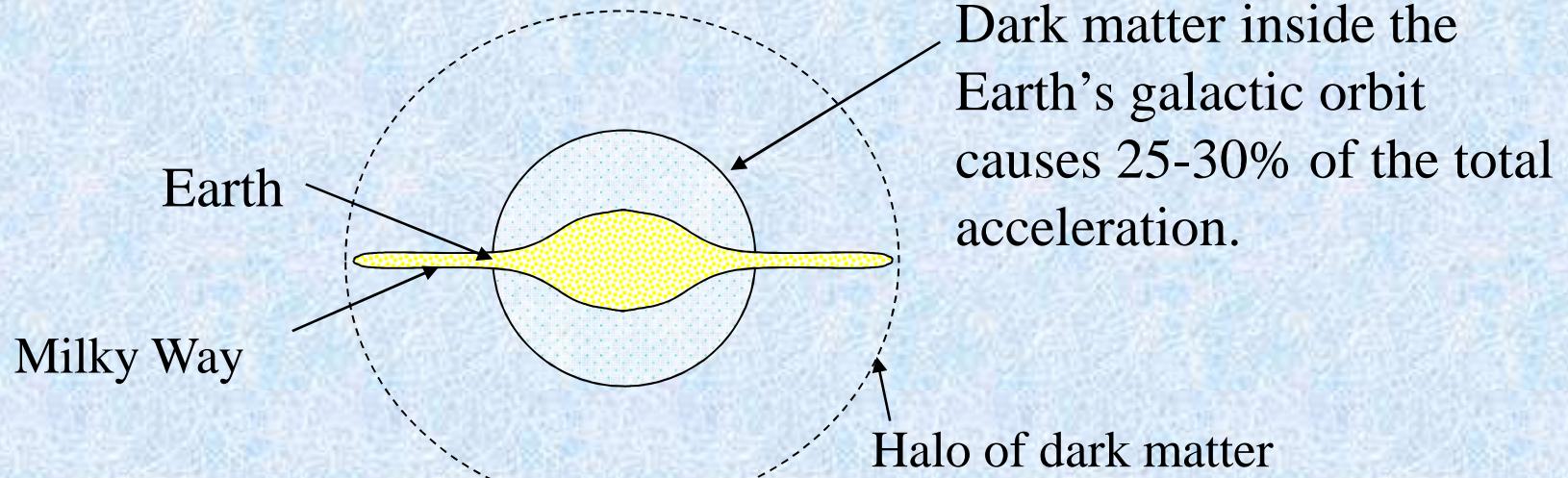
Galactic dark matter



Our acceleration toward the galactic center is:

$$a_{\text{gal}} = a_{\text{dark}} + a_{\text{ordinary}} = 1.9 \times 10^{-10} \text{ m/s}^2 \Rightarrow a_{\text{dark}} = 5 \times 10^{-11} \text{ m/s}^2$$

Galactic dark matter



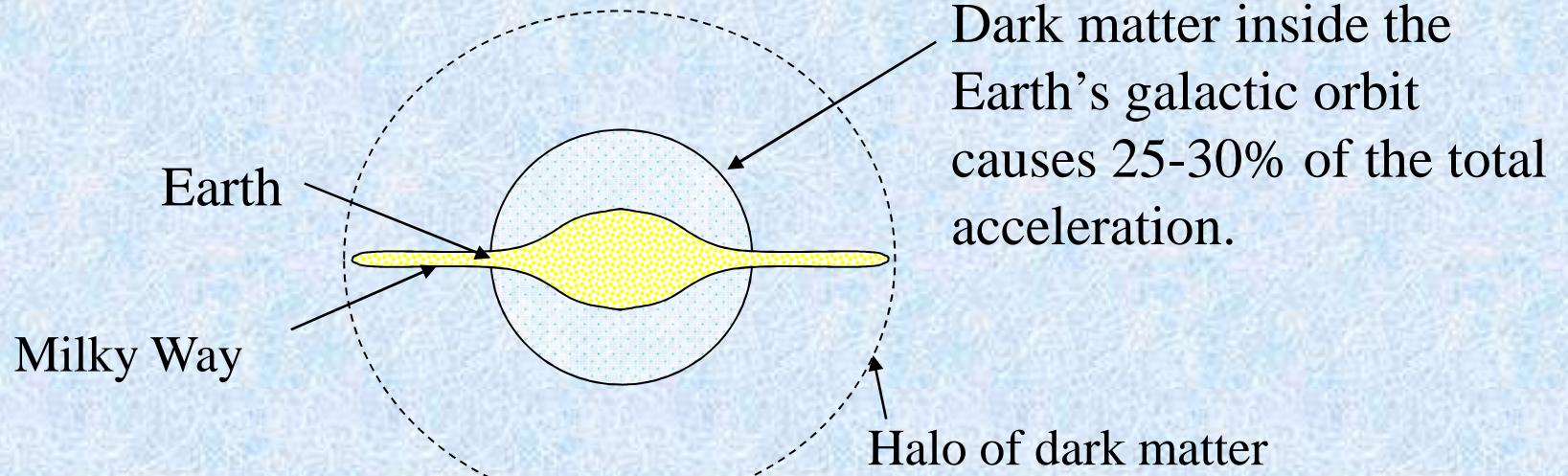
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Measured differential acceleration toward the galactic center:

$$\Delta a_{\text{gal}} = (-2.1 \pm 3.1) \times 10^{-15} \text{ m/s}^2 \Rightarrow \eta_{\text{dark}} = |\Delta a_{\text{gal}}| / a_{\text{dark}} = (-4 \pm 7) \times 10^{-5}$$

Galactic dark matter



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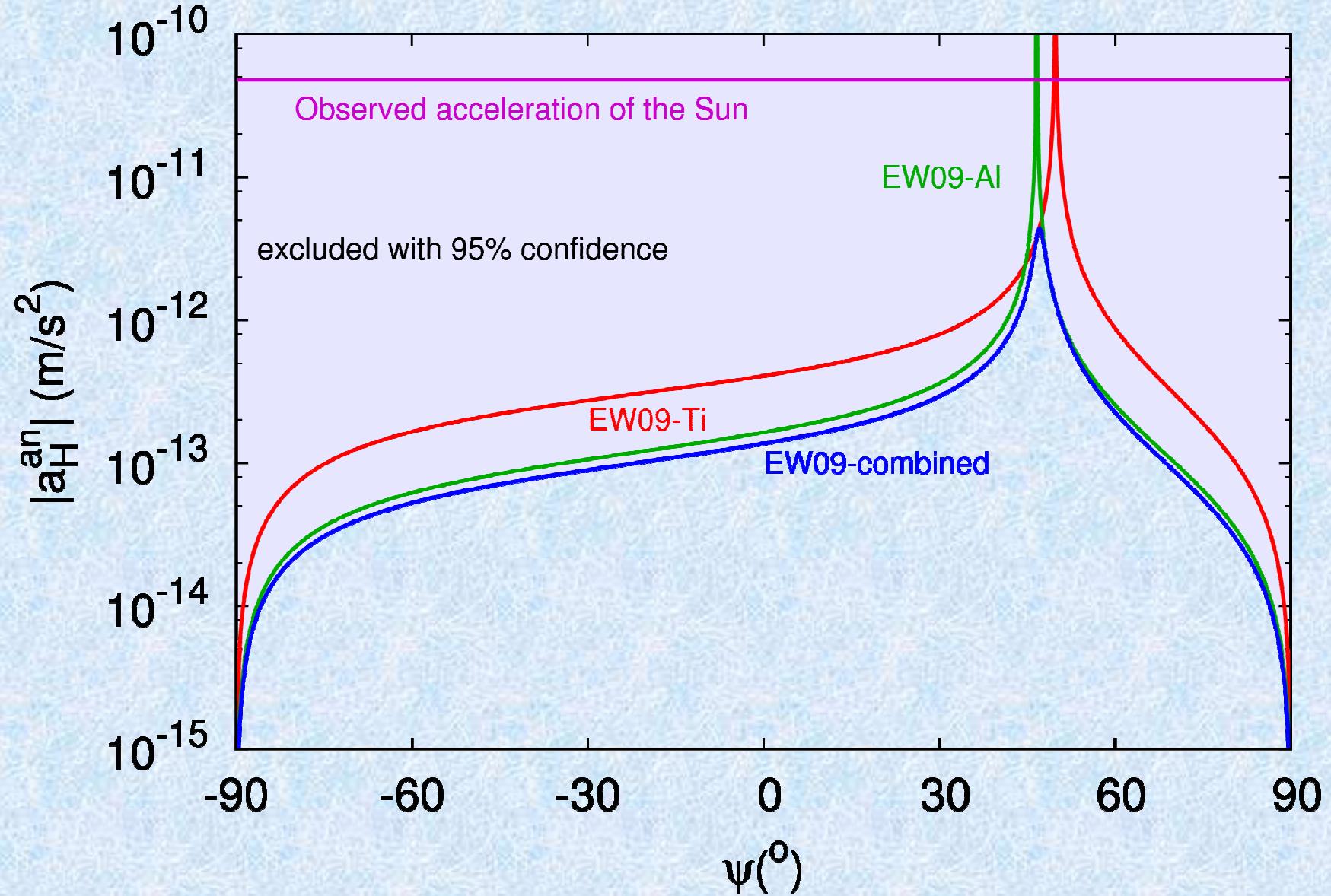
$$a_{\text{gal}} = a_{\text{dark}} + a_{\text{ordinary}} = 1.9 \times 10^{-10} \text{ m/s}^2 \Rightarrow a_{\text{dark}} = 5 \times 10^{-11} \text{ m/s}^2$$

Measured differential acceleration toward the galactic center:

$$\Delta a_{\text{gal}} = (-2.1 \pm 3.1) \times 10^{-15} \text{ m/s}^2 \Rightarrow \eta_{\text{dark}} = |\Delta a_{\text{gal}}| / a_{\text{dark}} = (-4 \pm 7) \times 10^{-5}$$

The acceleration of Be and Ti towards dark matter does not differ by more than 150 ppm (with 95 % confidence).

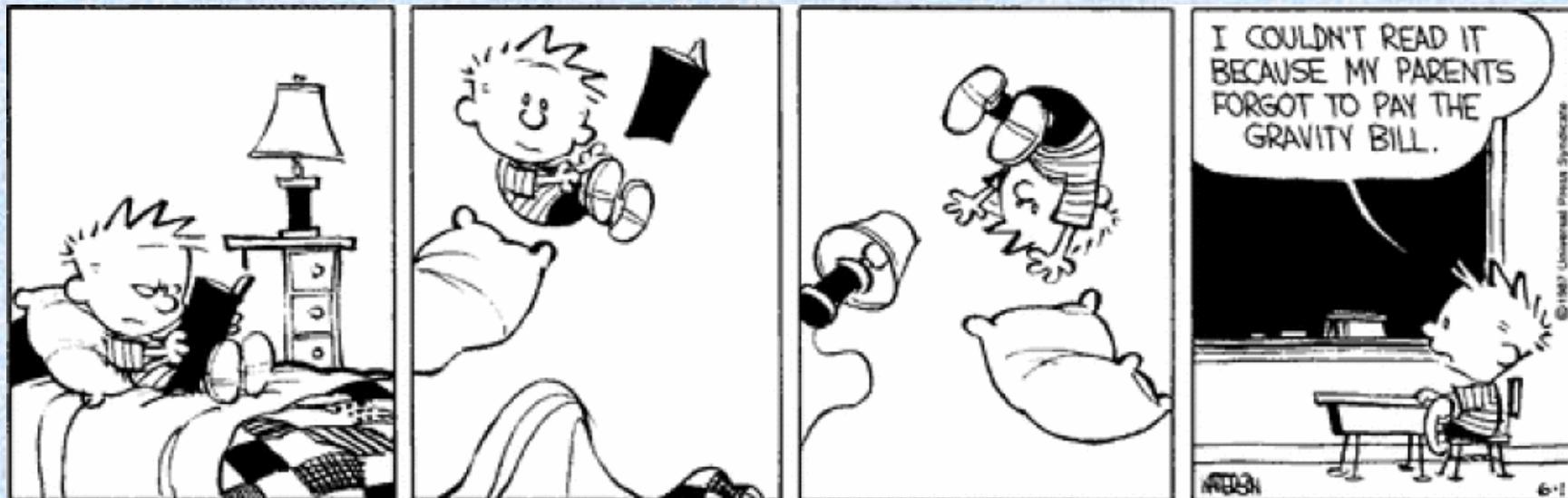
Limits on the acceleration of neutral H towards dark matter



Summary

- The test of the equivalence principle is a sensitive probe for fundamental physics.
- Principle of the measurement.
- Main systematic effects.
- Results
 - Earth (North): $a_{Be} - a_{Ti} = (0.6 \pm 3.1) \times 10^{-15} \text{ m/s}^2$.
 - $\eta = (0.3 \pm 1.8) \times 10^{-13}$.
 - Towards Galaxy: $a_{Be} - a_{Ti} = (-2.1 \pm 3.1) \times 10^{-15} \text{ m/s}^2$.
 - $\eta_{DM} = (-4 \pm 7) \times 10^{-5}$.
 - 10x improved limits on a long range interaction.

Thank you



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